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LLR École polytechnique

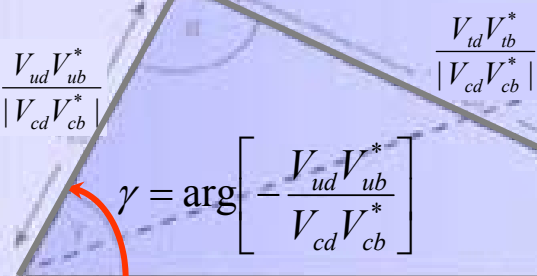
The 2007 Europhysics Conference on High Energy Physics  
July 19<sup>th</sup>-25<sup>th</sup>, 2007 Manchester, England

**BaBar**

Kobayashi-Maskawa matrix

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

# Measurement of the CKM angle $\gamma$ at BaBar



Unitarity triangle

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for the BaBar Collaboration

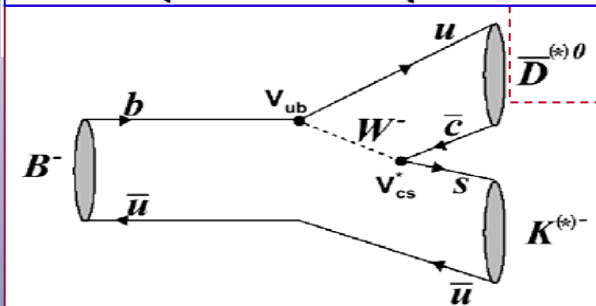
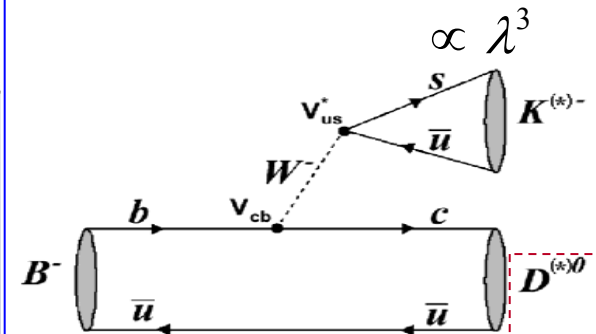




# $\gamma$ with interferences in $B^\pm \rightarrow \tilde{D}^{(*)0} K^{(*)\pm}$

$\tilde{D}^{(*)0}$  = admixture of  $D^{(*)0}$  and  $\bar{D}^{(*)0}$

$$A(B^- \rightarrow D^{(*)0} K^{(*)-}) \propto V_{cb} V_{us}^*$$



$$A(B^- \rightarrow \bar{D}^{(*)0} K^{(*)-}) \propto V_{ub} V_{cs}^*$$

$$\propto \lambda^3 \sqrt{\bar{\rho}^2 + \bar{\eta}^2} e^{i(\delta_B - \gamma)}$$

3 methods

3 methods		
<b>GLW</b>	<b>ADS</b>	<b>GGSZ</b>
<i>CP modes</i>	<i>Doubly Cabbibo Supp.</i>	<i>3 body: Dalitz</i>
$K^+ K^-, \pi^+ \pi^-$ (CP+)	$D^0 \rightarrow K^+ \pi^-$	$K_S \pi^+ \pi^-$
$K_S \phi, K_S \omega, K_S \pi^0$ (CP-)	$\bar{D}^0 \rightarrow K^- \pi^+$	

**Theoretically clean:** no penguin diagram

+ 3 common unknowns:

- $\gamma$ , weak phase difference
- $\delta_B$ , strong phase difference
- $r_B \equiv \left| \frac{A(b \rightarrow u)}{A(b \rightarrow c)} \right| \sim 0.05 - 0.30$

One set for each  $D^0 K^-, D^{*0} K^-, D^0 K^{*-}$ : resp.  $(r_B, \delta_B), (r_B^*, \delta_B^*), (r_{sB}, \delta_{sB})$

**⇔ Possibility and need to combine the methods**

Measuring  $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

Conclusion

Back-up

# GLW method



4 observables measured:

*CP* asymmetries

$$\mathcal{A}_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^{(*)0} K^{(*)-}) - \Gamma(B^+ \rightarrow D_{CP\pm}^{(*)0} K^{(*)+})}{\Gamma(B^- \rightarrow D_{CP\pm}^{(*)0} K^{(*)-}) + \Gamma(B^+ \rightarrow D_{CP\pm}^{(*)0} K^{(*)+})}$$

$$= \frac{\pm 2r_{(s)B}^{(*)} \sin \delta_{(s)B}^{(*)} \sin \gamma}{R_{CP\pm}}$$

Ratio of BFs

$$R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^{(*)0} K^{(*)-}) + \Gamma(B^+ \rightarrow D_{CP\pm}^{(*)0} K^{(*)+})}{[\Gamma(B^- \rightarrow D^{(*)0} K^{(*)-}) + \Gamma(B^- \rightarrow D^{(*)0} K^{(*)-})] / 2}$$

$$= 1 + r_{(s)B}^{(*)2} \pm 2r_{(s)B}^{(*)} \cos \delta_{(s)B}^{(*)} \cos \gamma$$

3 unknowns ( $\gamma$ ,  $\delta_B$ ,  $r_B$ )

1 constraint :  $\mathcal{A}_{CP+} R_{CP+} = -\mathcal{A}_{CP-} R_{CP-}$ .

*Drawbacks of the method*

- 8-fold ambiguity on  $\gamma$
- Small branching fractions  $\sim 10^{-6}$  (including sec. BF)
  - ⇒ Statistically limited
- Main limitation:  $R_{CP+} + R_{CP-} = 2 + r_B^2$  : quadratic dependence in  $r_B$ 
  - ⇒ small sensitivity, small *CP* asymmetries

Measuring  $\gamma$

1. Principle
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Conclusion

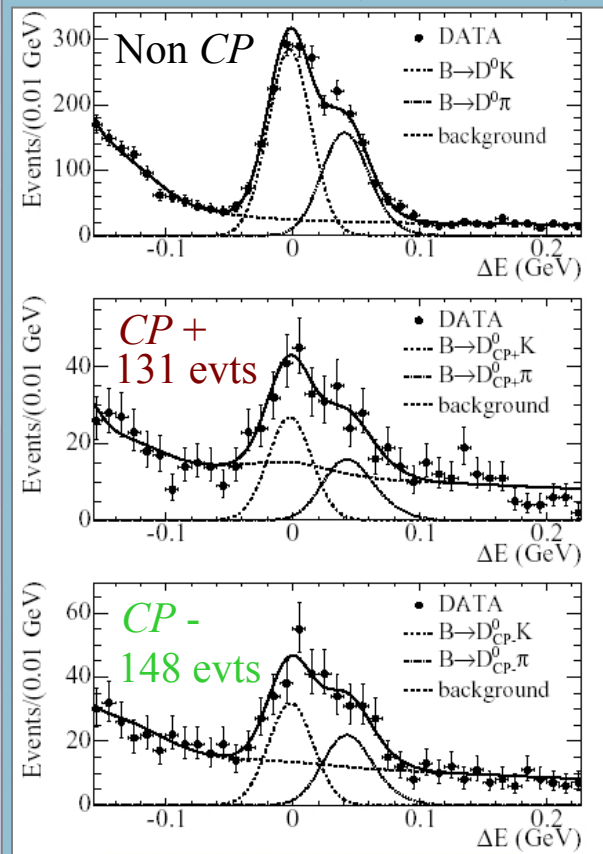
Back-up



PRD 73, 051105 (2006)  
 PRD 72, 071103 (2006)  
 PRD 71, 031102 (2005)

# GLW results

$B^\pm \rightarrow D^0 K^\pm$  ( $232 \times 10^6 B\bar{B}$ )

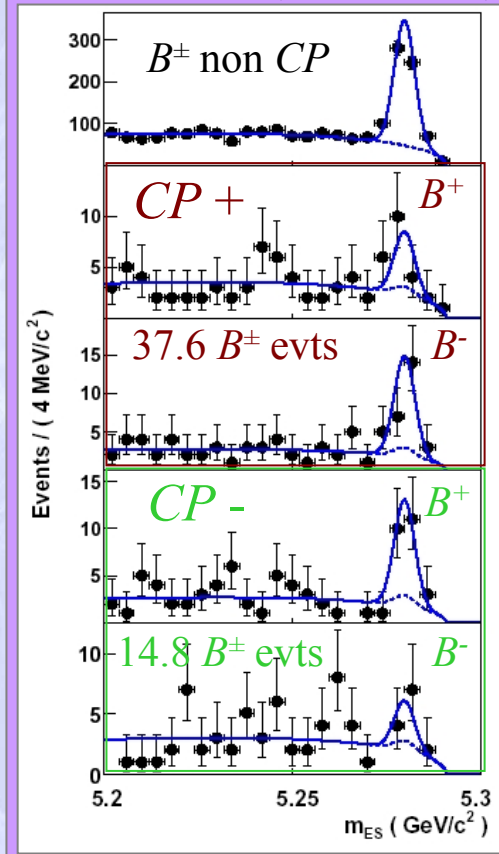


*Non CP:  $K\pi$*

*CP+:  $KK, \pi\pi$*

*CP-:  $K_s \pi^0, K_s \omega, K_s \phi$*

$B^\pm \rightarrow D^0 K^{*\pm}$  ( $232 \times 10^6 B\bar{B}$ )

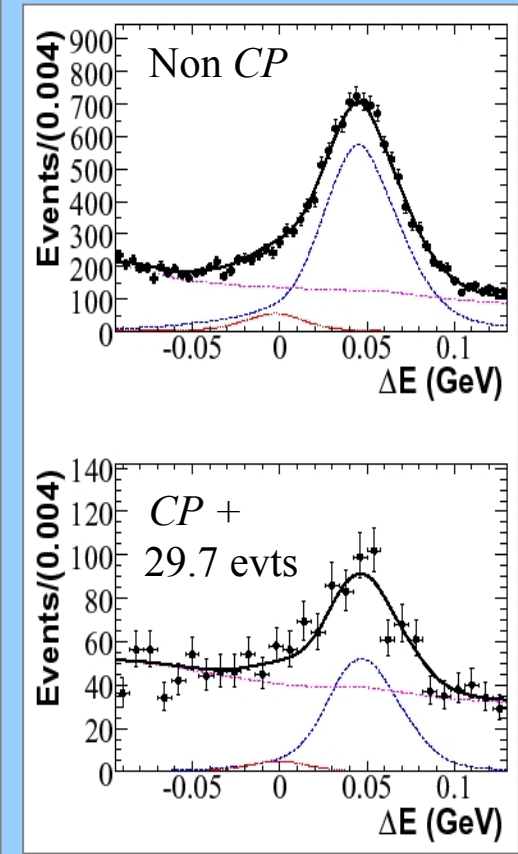


*$K^{*-} \rightarrow K_s \pi^-$*

*Non CP: same as  $D^* K$*

*CP: same as  $DK$*

$B^\pm \rightarrow D^{*0} K^\pm$  ( $124 \times 10^6 B\bar{B}$ )



*$D^{*0} \rightarrow D^0 \pi^0$*

*Non CP:  $K\pi, K\pi\pi^0, K\pi\pi\pi$*

*CP+:  $KK, \pi\pi$  (No CP-)*

Measuring  $\gamma$

1. Principle
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Conclusion

Back-up



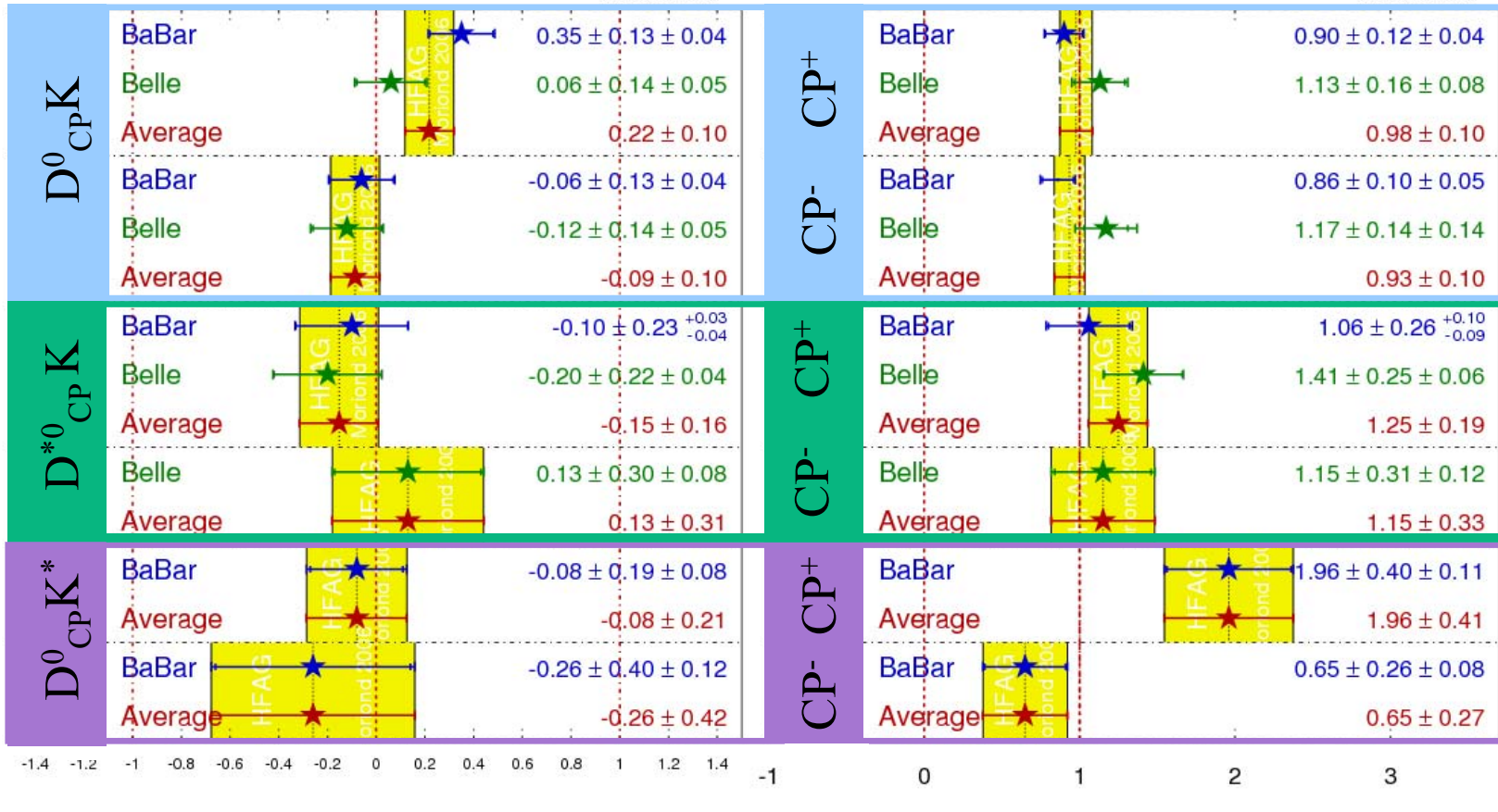
# GLW averages

## $A_{CP}$ Averages

**HFAG**  
Moriond 2006

## $R_{CP}$ Averages

**HFAG**  
Moriond 2006



Measuring  $\gamma$

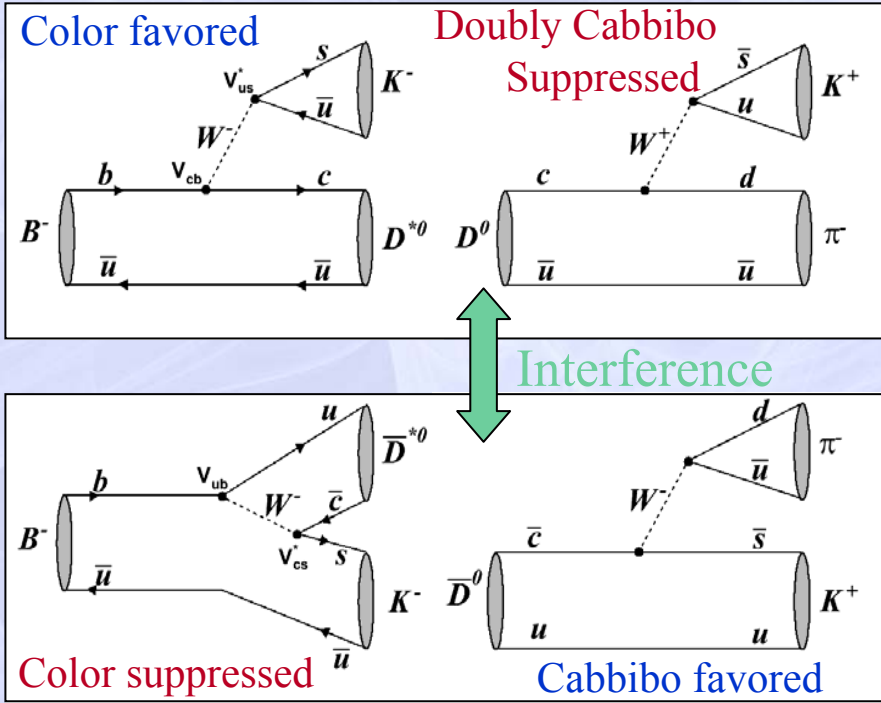
1. Principle
2. GLW
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Conclusion

Back-up

- GLW method alone **cannot constrain  $\gamma$**  alone with current statistics
- But **useful when  $x_{\pm}$  combined** with GGSZ method (see slide 12)

# ADS method



2 observables measured  
(4 with  $D^*K$ , *PRD70,091503(2004)*)

Ratio of BFs

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow D[K^+\pi^-]K^-) + \Gamma(B^+ \rightarrow D[K^-\pi^+]K^+)}{\Gamma(B^- \rightarrow D[K^-\pi^+]K^-) + \Gamma(B^+ \rightarrow D[K^+\pi^-]K^+)}$$

$$= r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos\gamma$$

CP asymmetries

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow D[K^+\pi^-]K^-) - \Gamma(B^+ \rightarrow D[K^-\pi^+]K^+)}{\Gamma(B^- \rightarrow D[K^+\pi^-]K^-) + \Gamma(B^+ \rightarrow D[K^-\pi^+]K^+)}$$

$$= 2r_B r_D \sin(\delta_B + \delta_D) \sin\gamma / R_{ADS}$$

And 5 unknowns:  $r_B, r_D, \delta_B, \delta_D, \gamma$

$$r_D^2 \equiv \left| \frac{A(D \rightarrow K^+\pi^-)}{A(D \rightarrow K^-\pi^+)} \right|^2 = (0.365 \pm 0.021)\%$$

PLB 592,1 (PDG 2004)

$D$  decay strong phase  
Scan all possible values

- Main limitation: small BF  $\sim 10^{-6}$
- Good sensivity to  $r_B^2$  with  $R_{ADS}$
- But amplitudes comparable  $\Rightarrow$  Larger CP violation

Measuring  $\gamma$

1. Principle
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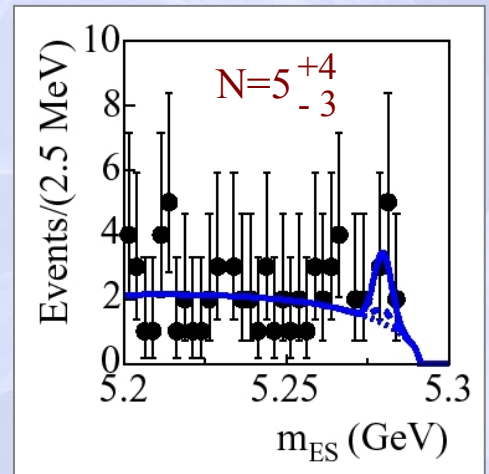
Conclusion

Back-up

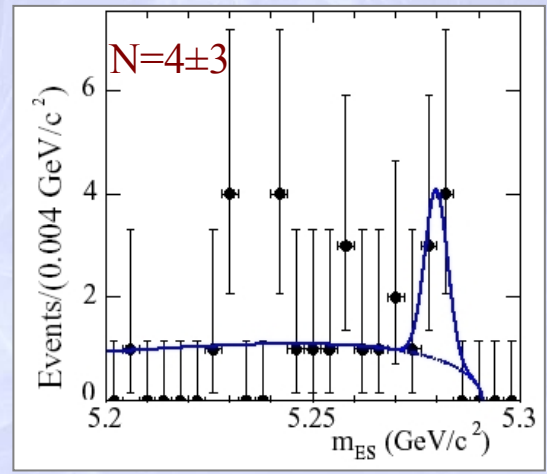


# ADS results

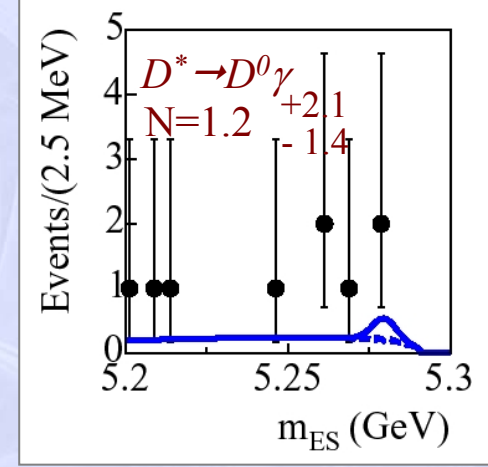
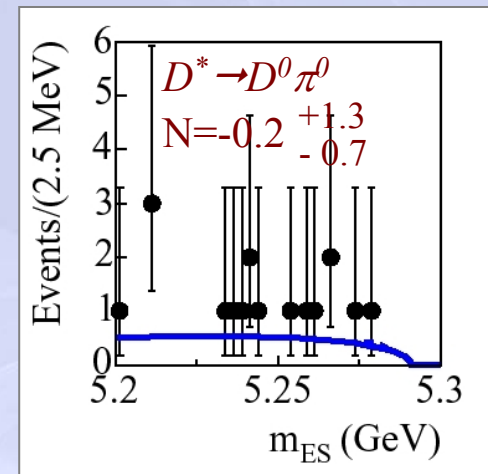
$B^\pm \rightarrow D^0 K^\pm$



$B^\pm \rightarrow D^0 K^{*\pm}$



$B^\pm \rightarrow D^{*0} K^\pm$



**No significant signal**

Only bayesian limits (90% CL) on  $R_{ADS}$  and  $r_{(s)B}^{(*)}$

	$R_{ADS}$	$r_B$
$D^0 K$	$<0.029$	$r_B < 0.23$
$D^{*0} K$	$<0.023 (D^0 \pi^0)$ $<0.045 (D^0 \gamma)$	$(r_B^{*})^2 < (0.16)^2$
$D^0 K^*$	$0.046 \pm 0.032$	$r_{sB} = 0.20 \pm 0.14$

Measuring  $\gamma$

1. Principle
2. GLW
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4. GGSZ

Conclusion

Back-up



# ADS results: $B^- \rightarrow [K^+ \pi^- \pi^0]_D K^-$



- Similar to classic ADS analysis with DCS  $D^0 \rightarrow K^+ \pi^-$ 
  - Complication:  $(|A_D|, \delta_D)$  varying in the Dalitz plane

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow D[K^+ \pi^-]K^-) + \Gamma(B^+ \rightarrow D[K^- \pi^+]K^+)}{\Gamma(B^- \rightarrow D[K^- \pi^+]K^-) + \Gamma(B^+ \rightarrow D[K^+ \pi^-]K^+)}$$

$$= r_B^2 + r_D^2 + 2r_B r_D C \cos \gamma$$

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow D[K^+ \pi^-]K^-) - \Gamma(B^+ \rightarrow D[K^- \pi^+]K^+)}{\Gamma(B^- \rightarrow D[K^+ \pi^-]K^-) + \Gamma(B^+ \rightarrow D[K^- \pi^+]K^+)}$$

$$= 2r_B r_D S \sin \gamma / R_{ADS}$$

- Smaller  $r_D = (0.214 \pm 0.011)\%$   $\Rightarrow$  better sensitivity on  $r_B$
- C unknown:  $|C| \leq 1$
- More background, but higher BF's

$$C = \frac{\int A_D(\vec{s}) \bar{A}_D(\vec{s}) \cos(\delta_D(\vec{s}) + \delta_B(\vec{s})) d\vec{s}}{\sqrt{\int |A_D(\vec{s})|^2 d\vec{s}} \sqrt{\int |\bar{A}_D(\vec{s})|^2 d\vec{s}}}$$

$$S = \frac{\int A_D(\vec{s}) \bar{A}_D(\vec{s}) \sin(\delta_D(\vec{s}) + \delta_B(\vec{s})) d\vec{s}}{\sqrt{\int |A_D(\vec{s})|^2 d\vec{s}} \sqrt{\int |\bar{A}_D(\vec{s})|^2 d\vec{s}}}$$

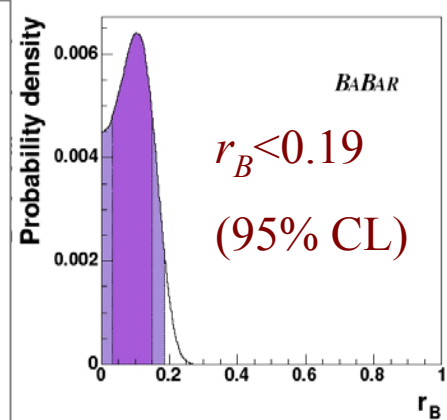
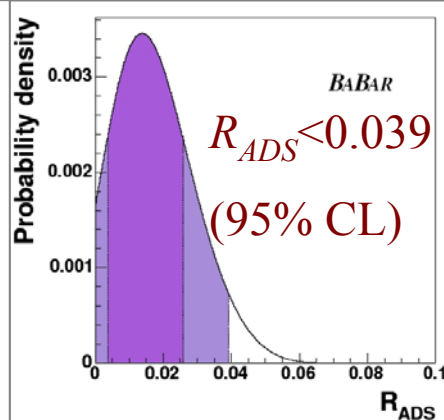
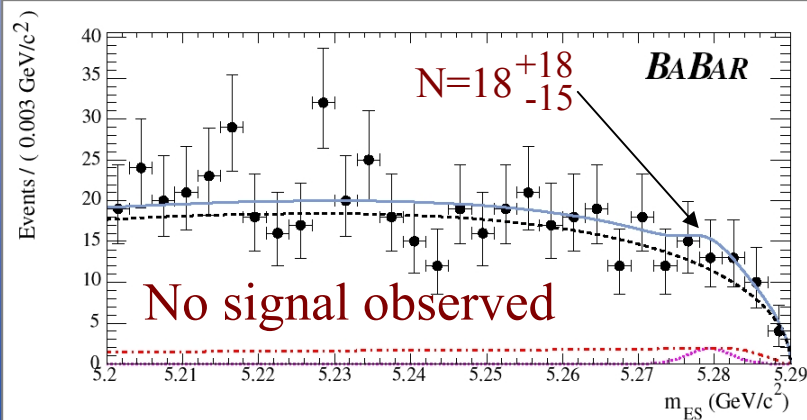
$$\vec{s} = (m_{K\pi}^2, m_{K\pi^0}^2)$$

Measuring  $\gamma$

- Principle
- GLW
- ADS
- GSZ

Conclusion

Back-up



Experimental LH

Bayesian LH

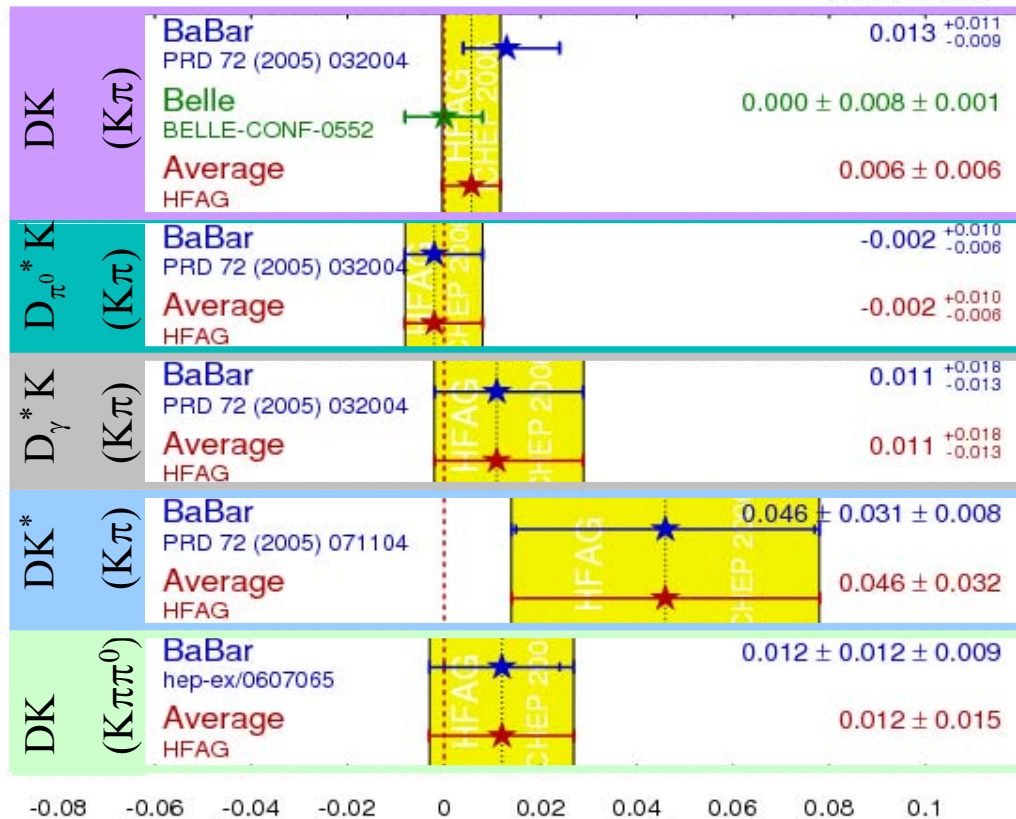




# ADS averages

## $R_{ADS}$ Averages

**HFAG**  
ICHEP 2006  
PRELIMINARY



- Not possible to constrain  $r_{(s)B}^{(*)}$  with  $R_{ADS}$  measurements alone

- $r_{(s)B}^{(*)}$  smaller than expected

- $A_{ADS}$  not measured

Measuring  $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

Conclusion

Back-up



# Dalitz GGSZ: $B^- \rightarrow D^{(*)} K_S \pi^+ \pi^- K^{(*)-}$

- $D^0 \rightarrow K_S \pi^+ \pi^-$  final state accessible through many decays: Dalitz analysis

$$\mathcal{A}_{B^-}(m_{K_S \pi^-}^2, m_{K_S \pi^+}^2) = \mathcal{A}_D(m_{K_S \pi^-}^2, m_{K_S \pi^+}^2) + \kappa r_{(s)B}^{(*)} e^{i(\delta_{(s)B}^{(*)} - \gamma)} \mathcal{A}_D(m_{K_S \pi^+}^2, m_{K_S \pi^-}^2)$$

$$\mathcal{A}_{B^+}(m_{K_S \pi^+}^2, m_{K_S \pi^-}^2) = \mathcal{A}_D(m_{K_S \pi^+}^2, m_{K_S \pi^-}^2) + \kappa r_{(s)B}^{(*)} e^{i(\delta_{(s)B}^{(*)} + \gamma)} \mathcal{A}_D(m_{K_S \pi^-}^2, m_{K_S \pi^+}^2)$$

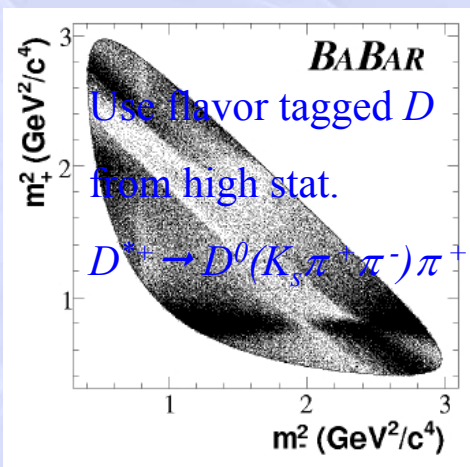
**$DK^-$**   $\kappa=+1$        **$DK^{*-}$**  Interference with  $B^\pm \rightarrow D(K_S \pi^\pm)_{\text{non-K}^*}$   
 $0 \leq \kappa \leq 1$       If interference  $\rightarrow 0$ :  $\kappa \rightarrow 1$   
 **$D^*K^-$**   $\kappa=+1$  for  $D^{*0} \rightarrow D^0 \pi$        $r_{sB} \rightarrow r_B$   
 $\kappa=-1$  for  $D^{*0} \rightarrow D^0 \gamma$        $\delta_{sB} \rightarrow \delta_B$

Measuring  $\gamma$

1. Principle
2. GLW
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Conclusion

Back-up



Purity: 97.7%

Same strategy for all analyses:

- 1- Fit the amplitude  $\mathcal{A}_D$
- 2- Fit of the  $B^- \rightarrow D^{(*)}[K_S \pi^+ \pi^-] K^{(*)-}$  Dalitz plot  
 $\Rightarrow$  **CP parameters**
- 3- Obtain CL on observables  $r_{(s)B}^{(*)}, \delta_{(s)B}^{(*)}, \gamma$

**2-fold ambiguity:**  $(\gamma, \delta_B) \rightarrow (\gamma + \pi, \delta_B + \pi)$



# GGSZ: $[K_S \pi^+ \pi^-]_D$ Dalitz model

Breit-Wigner model:

$$\mathcal{A}_D(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) + a_{NR} e^{i\phi_{NR}}$$

16 Resonances

Non Resonant term

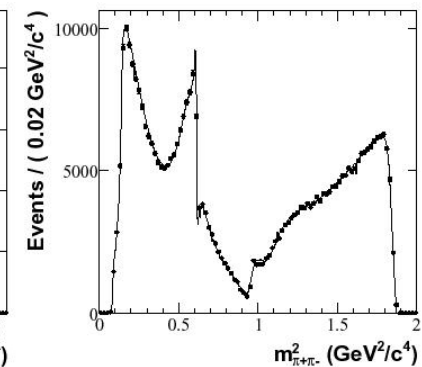
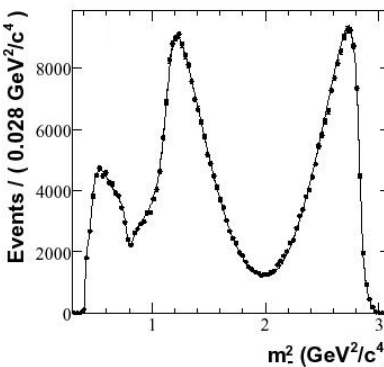
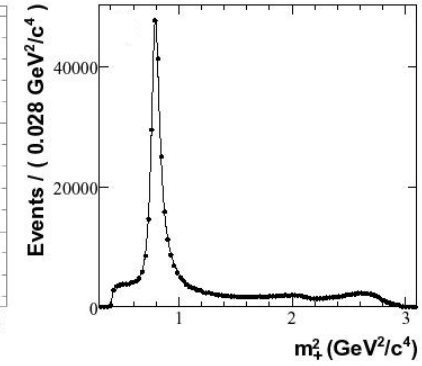
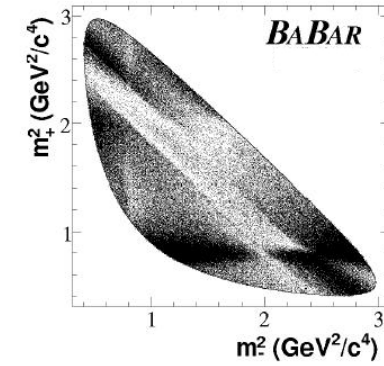
Total=119.5% (due to interferences)

Component	$Re\{a_r e^{i\phi_r}\}$	$Im\{a_r e^{i\phi_r}\}$	Fit fraction (%)
$K^*(892)^-$	$-1.223 \pm 0.011$	$1.3461 \pm 0.0096$	58.1
$K_0^*(1430)^-$	$-1.698 \pm 0.022$	$-0.576 \pm 0.024$	6.7
$K_2^*(1430)^-$	$-0.834 \pm 0.021$	$0.931 \pm 0.022$	3.6
$K^*(1410)^-$	$-0.248 \pm 0.038$	$-0.108 \pm 0.031$	0.1
$K^*(1680)^-$	$-1.285 \pm 0.014$	$0.205 \pm 0.013$	0.6
$K^*(892)^+$	$0.0997 \pm 0.0036$	$-0.1271 \pm 0.0034$	0.5
$K_0^*(1430)^+$	$-0.027 \pm 0.016$	$-0.076 \pm 0.017$	0.0
$K_2^*(1430)^+$	$0.019 \pm 0.017$	$0.177 \pm 0.018$	0.1
$\rho(770)$	1	0	21.6
$\omega(782)$	$-0.02194 \pm 0.00099$	$0.03942 \pm 0.00066$	0.7
$f_2(1270)$	$-0.699 \pm 0.018$	$0.387 \pm 0.018$	2.1
$\rho(1450)$	$0.253 \pm 0.038$	$0.036 \pm 0.055$	0.1
Non-resonant	$-0.99 \pm 0.19$	$3.82 \pm 0.13$	8.5
$f_0(980)$	$0.4465 \pm 0.0057$	$0.2572 \pm 0.0081$	6.4
$f_0(1370)$	$0.95 \pm 0.11$	$-1.619 \pm 0.011$	2.0
$\sigma$	$1.28 \pm 0.02$	$0.273 \pm 0.024$	7.6
$\sigma'$	$0.290 \pm 0.010$	$-0.0655 \pm 0.0098$	0.9

Kπ

ππ P, D

ππ S



Not well-established:

- mass and width fitted
- give better description of data

Model systematic uncertainty: comparison with alternative model ( $\pi\pi$  S-wave K-matrix)



# GGSZ results: $(x_{\pm}, y_{\pm})$

- At low statistics and low  $r_B$  values, **use of cartesian coordinates:**

- Unbiased and Gaussian
- Not the case for  $(\gamma, \delta_{(S)B}^{(*)}, r_{(S)B}^{(*)})$

$$x_{(s)\pm}^{(*)} = \text{Re}\left(r_{(s)B}^{(*)} e^{i(\delta_{(s)B}^{(*)} \pm \gamma)}\right)$$

$$y_{(s)\pm}^{(*)} = \text{Im}\left(r_{(s)B}^{(*)} e^{i(\delta_{(s)B}^{(*)} \pm \gamma)}\right)$$

$$\Rightarrow x_{(s)\pm}^{(*)2} + y_{(s)\pm}^{(*)2} = r_{(s)B}^{(*)2}$$

hep-ex/0607104

$347 \times 10^6 \bar{B}B$



hep-ex/0507101

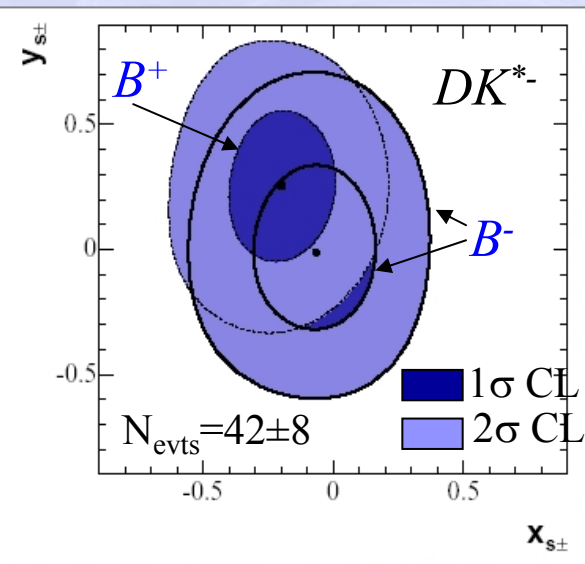
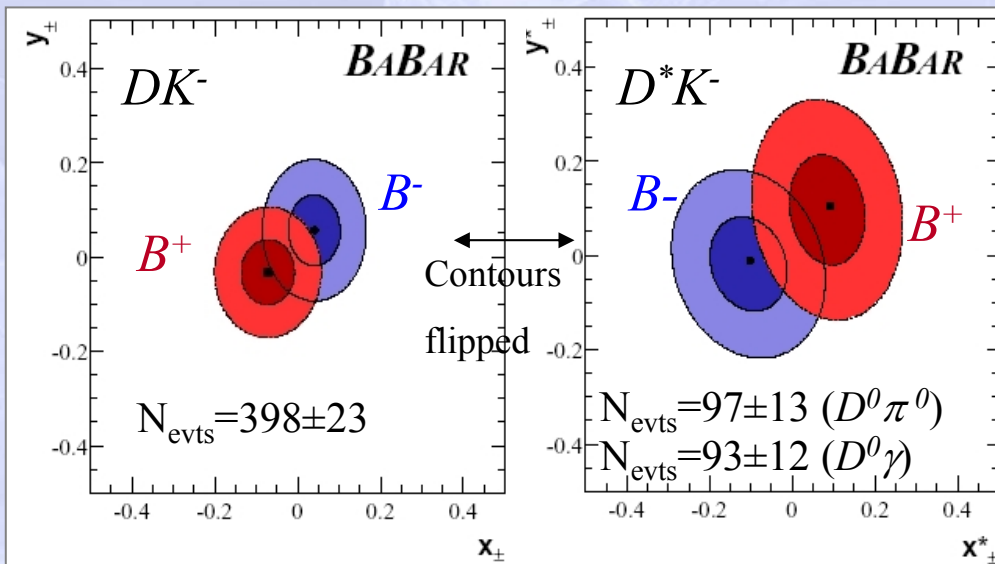
$227 \times 10^6 \bar{B}B$

Measuring  $\gamma$

- Principle
- GLW
- ADS
- GGSZ

Conclusion

Back-up



GLW DK	DK*
$x_+ : 0.102 \pm 0.062 \pm 0.022$	$x_+ : 0.32 \pm 0.18 \pm 0.07$
$x_- : -0.12 \pm 0.08 \pm 0.03$	$x_- : -0.33 \pm 0.16 \pm 0.06$

**GLW Competitive!**



# GGSZ results: $\gamma$

- From fitted  $CP$  parameters  $(x_{\pm}, y_{\pm}), (x_{\pm}^*, y_{\pm}^*), (x_{S\pm}, y_{S\pm})$ :
  - use a nD Neyman Confidence Region approach (frequentist)
  - Extract  $(r_B, r_B, \kappa.r_{SB}^*), (\delta_B, \delta_B^*, \delta_{SB}), \gamma$

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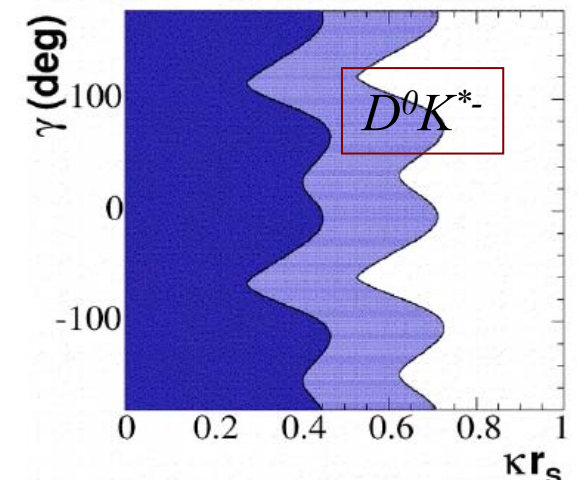
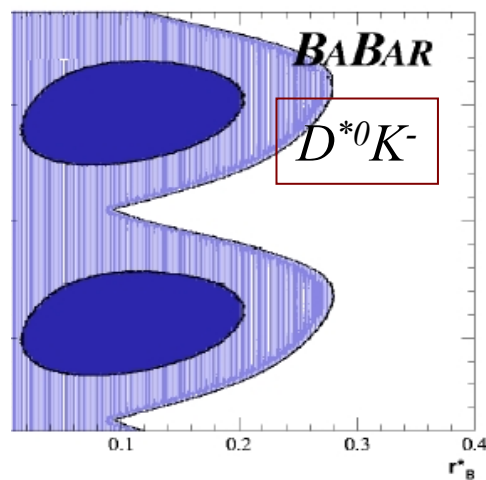
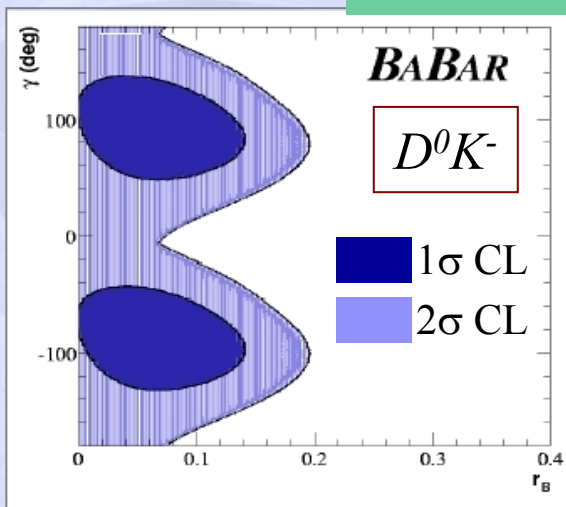
$347 \times 10^6 \bar{B}B$

5D CR

hep-ex/0507101

$227 \times 10^6 \bar{B}B$

3D CR



$\gamma \pmod{\pi} = (92 \pm 41 \pm 11 \pm 12)^\circ$  (2-fold ambiguity)

No  $1\sigma$  limit on  $\gamma$  with  $DK^*$  alone

$$r_B < 0.142$$

$$\kappa.r_{SB} < 0.5$$

$$r_B^* \in [0.016; 0.206] \text{ Smaller than 2005 analysis}$$

Measuring  $\gamma$

- Principle
- GLW
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Conclusion

Back-up

# Dalitz GGSZ: $B^- \rightarrow D \pi^+ \pi^- \pi^0 K^-$

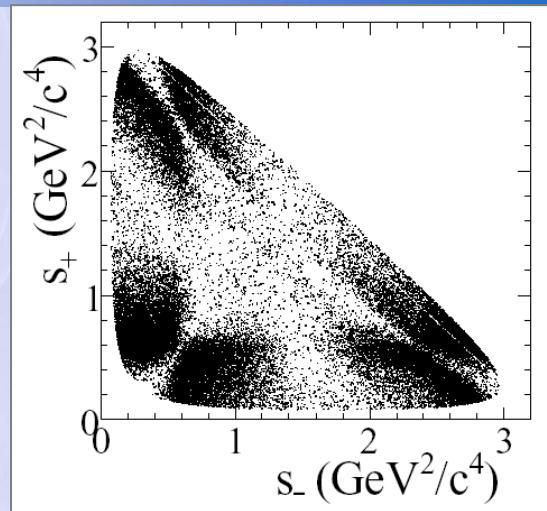


- Compared to  $B^\pm \rightarrow [K_S \pi^+ \pi^-]_D K^\pm$ :
  - Different Dalitz structure (15 resonances)
  - Larger backgrounds
- Non linear correlations with  $(r_B, \delta_B, \gamma)$  and cartesian coordinates

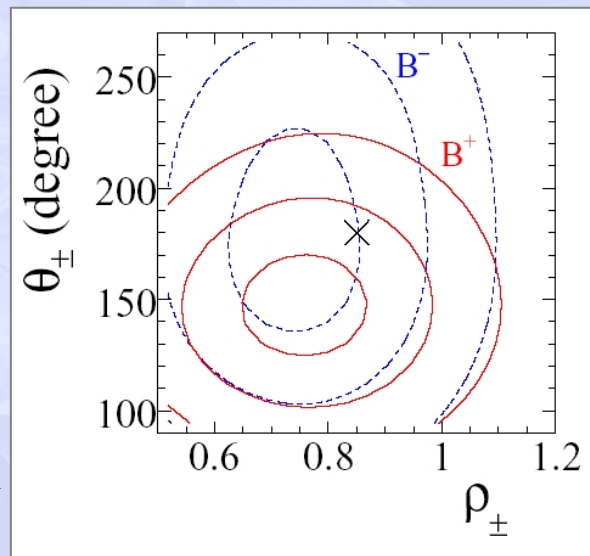
⇒ use of polar coordinates

$$\rho_\pm \equiv \sqrt{(x_\pm - x^0)^2 + y_\pm^2} \quad \theta_\pm \equiv \arctan\left(\frac{y_\pm}{x_\pm - x^0}\right)$$

$$x^0 \equiv \int A_D(m_-, m_+) \bar{A}_D(m_-, m_+) dm^- dm^+ = 0.85$$



Contours of constant  $\mathcal{L}$  :  $1\sigma, 2\sigma, 3\sigma$



## Measuring $\gamma$

1. Principle
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4. GGSZ

## Conclusion

## Back-up

**$N = 170 \pm 29$  events**

$$\rho_+ = 0.75 \pm 0.11 \pm 0.06$$

$$\rho_- = 0.72 \pm 0.11 \pm 0.06$$

$$\theta_+ = (147 \pm 23 \pm 13)^\circ$$

$$\theta_- = (173 \pm 42 \pm 19)^\circ$$

$\rho_+/\rho_-$  corr. = 14%

other corr. < 1%

Systematics mostly from Dalitz model

Errors on:

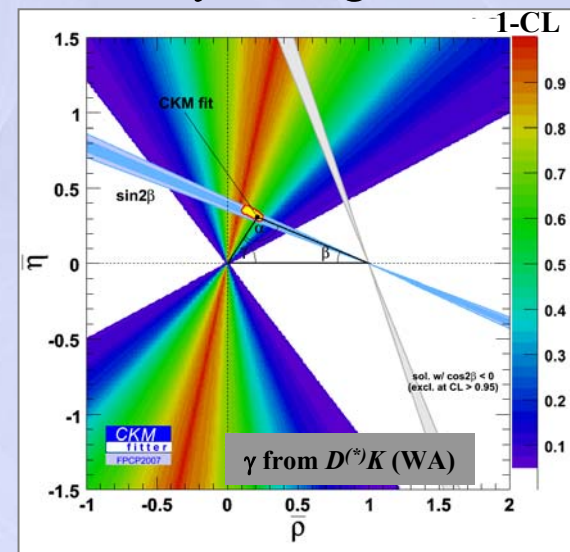
-  $\theta_\pm$ : too large to determine  $\gamma$

-  $\rho_\pm$ : small enough to be useful



# Conclusion and perspectives

- $\gamma$  is a difficult measurement: deemed impossible a few years ago
- The direct path to  $\gamma$  : charged  $B$  decays
  - 3 theoretically clean methods
  - Dalitz method is the most powerful so far
  - GLW has competitive errors on  $x_{\pm}$ : improves constraints when combined
  - Only part of the statistics available used: need to update analyses
  - At high stat.: will need a model independent Dalitz to avoid model syst.



Courtesy of V. Tisserand

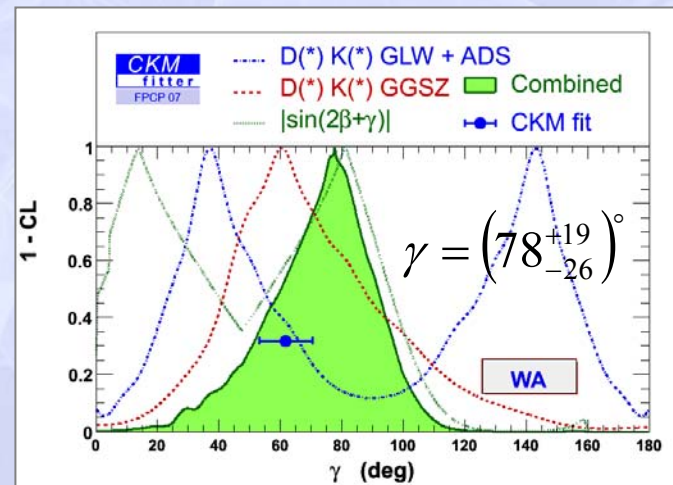
## Measuring $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

## Conclusion

## Back-up

- The indirect path to  $\gamma$ : neutral  $B$  decays
  - Helps in constraining
  - But need input for  $r^{(*)}$ , and stat. limited
- A long way ahead



Courtesy of V. Tisserand

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# *Back-up slides*

*Back-up slides*

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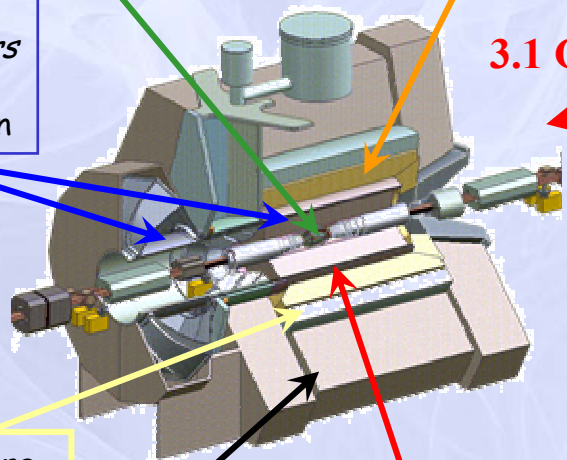


# The BaBar experiment

**SVT**  
**Silicon Vertex Tracker**  
 5 layers, double sided  
 Precise  $\Delta z$  measurement p

**EMC**  
**EM Calorimeter**  
 6580 CsI(Tl) crystals  
 Good E resolution  $\pi^0, \gamma$   
 ( $E_\gamma > 30\text{MeV}$ )

**DIRC**  
 144 quartz bars  
 11000 PMs  
 K/ $\pi$  Separation



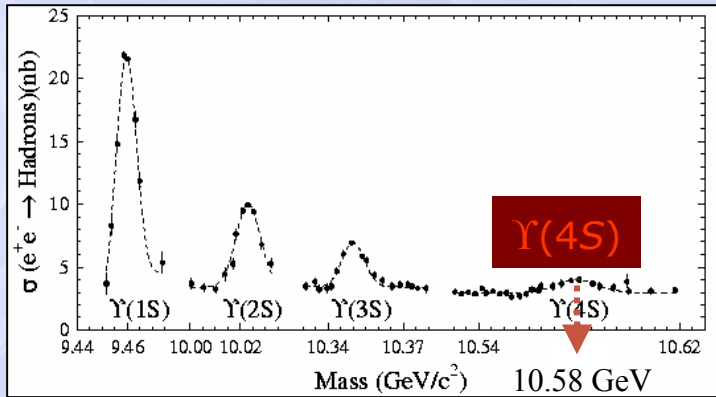
3.1 GeV  $e^+$

9 GeV  $e^-$

**Solenoid Supra**  
 1.5 T

**DCH**  
**Drift Chamber**  
 40 layers  
 Good p resolution  
 K/ $\pi$  Separation(dE/dx)

**IFR**  
**Instrumented Flux Return**  
 Iron / Resistive Plate Chambers  
 / Limited Streamer Tubes  
 muon / neutral hadrons id



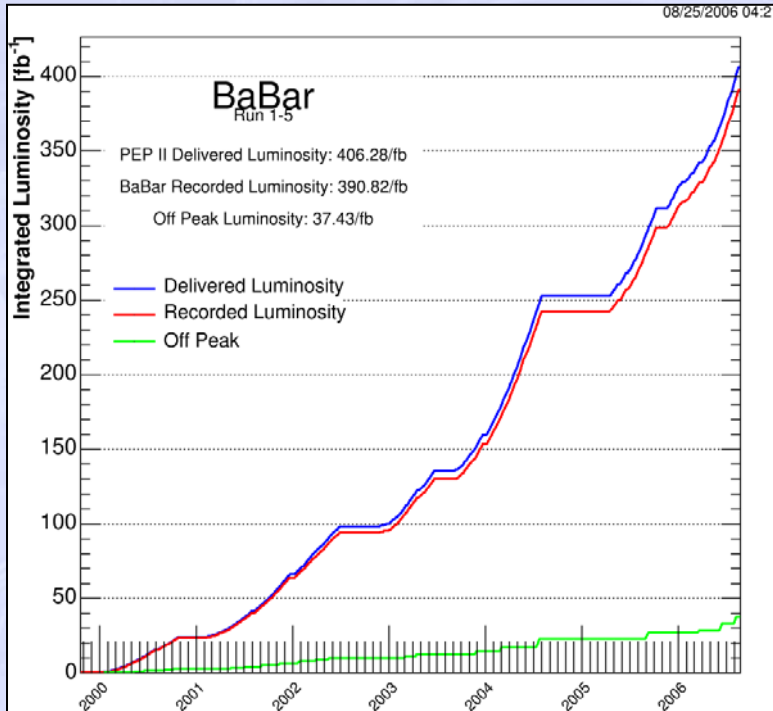
$B\bar{B}$  threshold

Measuring  $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

Conclusion

Back-up

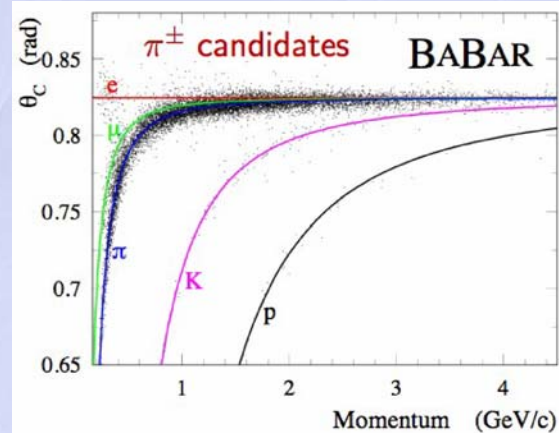




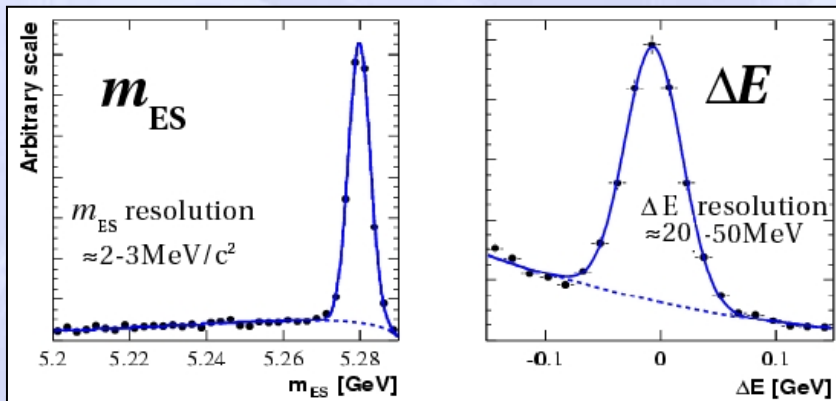
# Common analysis techniques

## Reconstruction

- Cut on geometric variable (polar angles)
  - *Reduce combinatorics from low momentum  $\pi$*
  - *Eliminate quickly varying acceptance region*
- PID requirements
  - *Combine info from SVT, DCH, DIRC*
  - *Provide  $K/\pi$  separation*
- **Best  $B$  candidate** selected with  $\chi^2$  on different variables



## Signal identification



Beam energy substituted mass

$$m_{ES} = \sqrt{\left(\frac{s}{2} + \vec{p}_0 \cdot \vec{p}_B\right)^2 / E_0^{*2} - \vec{p}_B^2}$$

B energy in CM frame

$$\Delta E = E_B^* - \frac{\sqrt{s}}{2}$$

Requires mass hyp.

Measuring  $\gamma$

1. Principle
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Conclusion

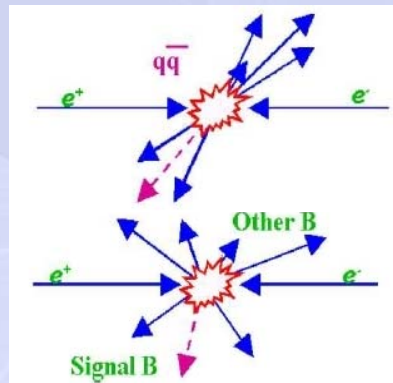
Back-up



# Common analysis techniques

## Background fighting

- $q\bar{q}$  rejection:** uses difference of topology between *spherical B decays* and *jet-like continuum*
  - Cuts on  $|\cos\theta_T|$  ( $< 0.9$  typically)
  - Fisher, NN:  $L_0, L_2, \cos\theta_{Bmom}, \cos\theta_{Bthrust}$
- $\bar{B}B$  rejection:** accounted for in the fit



## Fit: Extended unbinned maximum Likelihood fit

$$L = \frac{\exp(-\sum_j n_j)}{N!} \prod_{i=1}^N \left( \sum_j n_i P_j^i \right)$$

Poisson term

$$P_j^i = \prod_{k=1}^{N_{\text{var}}} P_j(\theta_k^i)$$

Fit variable:  $m_{ES}, \Delta E, \mathcal{F}, \dots$

$$\Rightarrow BF = \frac{n_{\text{meas.}} - n_{\text{bias}}}{n_B \mathcal{E}}$$

$$\mathcal{A}_{CP} = \frac{BF(B \rightarrow X) - BF(\bar{B} \rightarrow \bar{X})}{BF(B \rightarrow X) + BF(\bar{B} \rightarrow \bar{X})}$$

Measuring  $\gamma$

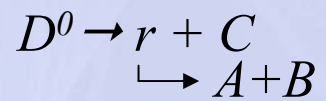
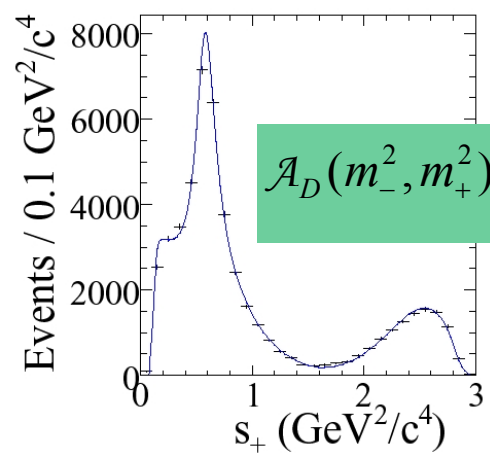
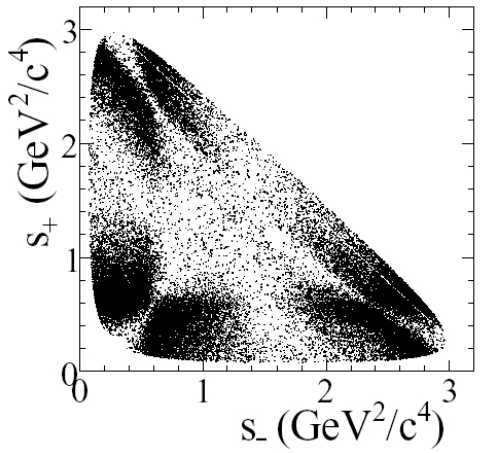
1. Principle
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Conclusion

Back-up

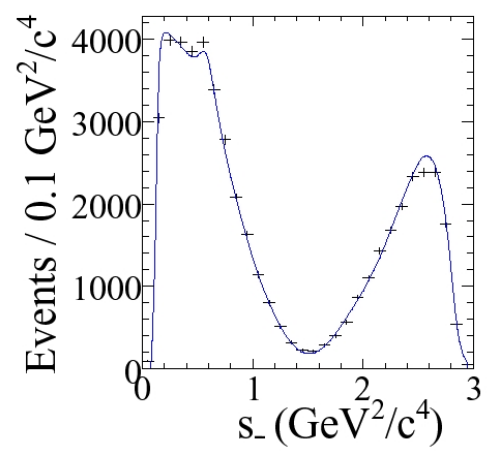


# GGSZ: $[\pi\pi\pi^0]_D$ Dalitz model



$$\mathcal{A}_D(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) + a_{NR} e^{i\phi_{NR}}$$

$$\mathcal{A}_r = \frac{\boxed{F_r F_s} \text{ Spin dep. Form Factors}}{m_r - M_{AB} - im_r \Gamma(M_{AB})}$$



State	$R_r$ (%)	$\Delta\phi_r$ ( $^\circ$ )	$f_r$ (%)
$\rho^+(770)$	100	0	$67.8 \pm 0.0 \pm 0.6$
$\rho^0(770)$	$58.8 \pm 0.6 \pm 0.2$	$16.2 \pm 0.6 \pm 0.4$	$26.2 \pm 0.5 \pm 1.1$
$\rho^-(770)$	$71.4 \pm 0.8 \pm 0.3$	$-2.0 \pm 0.6 \pm 0.6$	$34.6 \pm 0.8 \pm 0.3$
$\rho^+(1450)$	$21 \pm 6 \pm 13$	$-146 \pm 18 \pm 24$	$0.11 \pm 0.07 \pm 0.12$
$\rho^0(1450)$	$33 \pm 6 \pm 4$	$10 \pm 8 \pm 13$	$0.30 \pm 0.11 \pm 0.07$
$\rho^-(1450)$	$82 \pm 5 \pm 4$	$16 \pm 3 \pm 3$	$1.79 \pm 0.22 \pm 0.12$
$\rho^+(1700)$	$225 \pm 18 \pm 14$	$-17 \pm 2 \pm 3$	$4.1 \pm 0.7 \pm 0.7$
$\rho^0(1700)$	$251 \pm 15 \pm 13$	$-17 \pm 2 \pm 2$	$5.0 \pm 0.6 \pm 1.0$
$\rho^-(1700)$	$200 \pm 11 \pm 7$	$-50 \pm 3 \pm 3$	$3.2 \pm 0.4 \pm 0.6$
$f_0(980)$	$1.50 \pm 0.12 \pm 0.17$	$-59 \pm 5 \pm 4$	$0.25 \pm 0.04 \pm 0.04$
$f_0(1370)$	$6.3 \pm 0.9 \pm 0.9$	$156 \pm 9 \pm 6$	$0.37 \pm 0.11 \pm 0.09$
$f_0(1500)$	$5.8 \pm 0.6 \pm 0.6$	$12 \pm 9 \pm 4$	$0.39 \pm 0.08 \pm 0.07$
$f_0(1710)$	$11.2 \pm 1.4 \pm 1.7$	$51 \pm 8 \pm 7$	$0.31 \pm 0.07 \pm 0.08$
$f_2(1270)$	$104 \pm 3 \pm 21$	$-171 \pm 3 \pm 4$	$1.32 \pm 0.08 \pm 0.10$
$\sigma(400)$	$6.9 \pm 0.6 \pm 1.2$	$8 \pm 4 \pm 8$	$0.82 \pm 0.10 \pm 0.10$
Non-Res	$57 \pm 7 \pm 8$	$-11 \pm 4 \pm 2$	$0.84 \pm 0.21 \pm 0.12$

## Measuring $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

## Conclusion

## Back-up



# $\pi\pi$ S-wave K-matrix model

- Purpose: describe  $\pi\pi$  S-wave
- Motivation: **better description of dynamics than BW model** in the presence of overlapping resonances
- No improvement in the  $\chi^2$  test, since dominated by P-wave components, identical in the two models

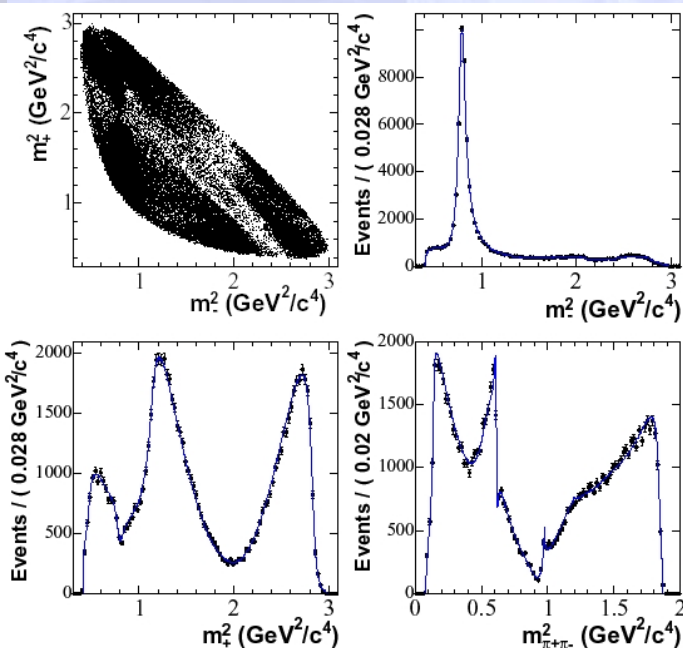
$$\chi^2/n_{\text{DOF}}=1.27$$

Measuring  $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

Conclusion

Back-up

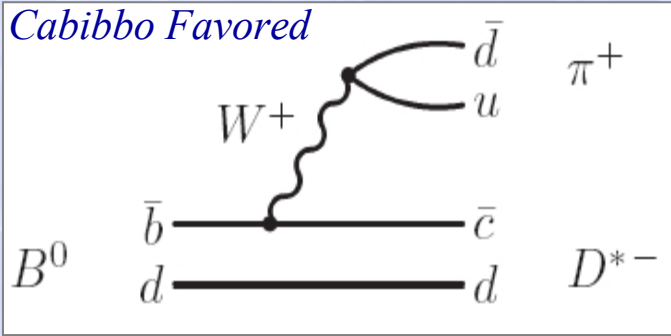


Component	$\text{Re}\{a_r e^{i\phi_r}\}$	$\text{Im}\{a_r e^{i\phi_r}\}$	Fit fraction (%)
$K^*(892)^-$	$-1.159 \pm 0.022$	$1.361 \pm 0.020$	58.9
$K_0^*(1430)^-$	$2.482 \pm 0.075$	$-0.653 \pm 0.073$	9.1
$K_2^*(1430)^-$	$0.852 \pm 0.042$	$-0.729 \pm 0.051$	3.1
$K^*(1410)^-$	$-0.402 \pm 0.076$	$0.050 \pm 0.072$	0.2
$K^*(1680)^-$	$-1.00 \pm 0.29$	$1.69 \pm 0.28$	1.4
$K^*(892)^+$	$0.133 \pm 0.008$	$-0.132 \pm 0.007$	0.7
$K_0^*(1430)^+$	$0.375 \pm 0.060$	$-0.143 \pm 0.066$	0.2
$K_2^*(1430)^+$	$0.088 \pm 0.037$	$-0.057 \pm 0.038$	0.0
$\rho(770)$	1 (fixed)	0 (fixed)	22.3
$\omega(782)$	$-0.0182 \pm 0.0019$	$0.0367 \pm 0.0014$	0.6
$f_2(1270)$	$0.787 \pm 0.039$	$-0.397 \pm 0.049$	2.7
$\rho(1450)$	$0.405 \pm 0.079$	$-0.458 \pm 0.116$	0.3
$\beta_1$	$-3.78 \pm 0.13$	$1.23 \pm 0.16$	—
$\beta_2$	$9.55 \pm 0.20$	$3.43 \pm 0.40$	—
$\beta_4$	$12.97 \pm 0.67$	$1.27 \pm 0.66$	—
$f_{11}^{\text{prod}}$	$-10.22 \pm 0.32$	$-6.35 \pm 0.39$	—
sum of $\pi^+\pi^-$ S-wave			16.2

Sum of fractions: 1.16

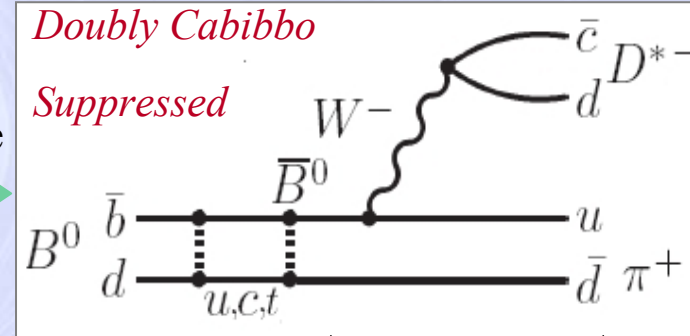


# $\sin(2\beta + \gamma)$ with neutral $B$ decays



$$A \propto V_{cb} V_{ud}^*$$

Interference  $\longleftrightarrow$



$$A \propto V_{ub} V_{cd}^* e^{i\delta} \propto A r^{(*)} e^{i\delta} e^{-i\gamma}$$

strong phase diff.      weak phase diff.

Time-dependent decay rate distribution:

$$P(B^0 \rightarrow D^{(*)\mp} \pi^\pm, \Delta t) \propto 1 \pm C^{(*)} \cos(\Delta m_d \Delta t) + S^{(*)\mp} \sin(\Delta m_d \Delta t)$$

$$P(\bar{B}^0 \rightarrow D^{(*)\mp} \pi^\pm, \Delta t) \propto 1 \mp C^{(*)} \cos(\Delta m_d \Delta t) - S^{(*)\pm} \sin(\Delta m_d \Delta t)$$

$$r^{(*)} = \frac{|A_{DCS}|}{|A_{CF}|} \sim 2\% \quad C^{(*)} = \frac{1 - r^{(*)2}}{1 + r^{(*)2}} \approx 1 \quad S^{(*)\pm} = \frac{2r^{(*)2}}{1 + r^{(*)2}} \sin(2\beta + \gamma \pm \delta^{(*)})$$

- $\Rightarrow$  Small  $CP$  asymmetries
- $\Rightarrow$   $r^{(*)}$  cannot be measured with current stat.
- $\Rightarrow$  Measurements of  $S^+$  and  $S^-$  determine  $(2\beta + \gamma)$  and  $\delta$  if  $r$  is an external input

Measuring  $\gamma$

1. Principle
2. GLW
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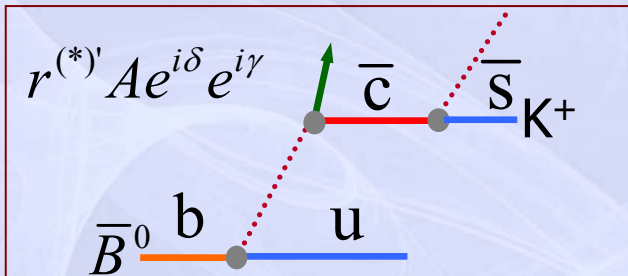
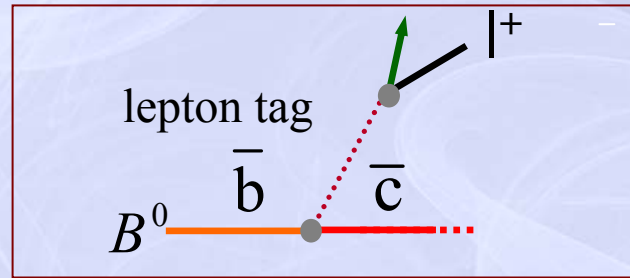
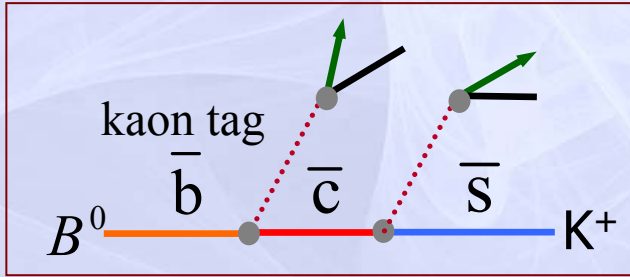
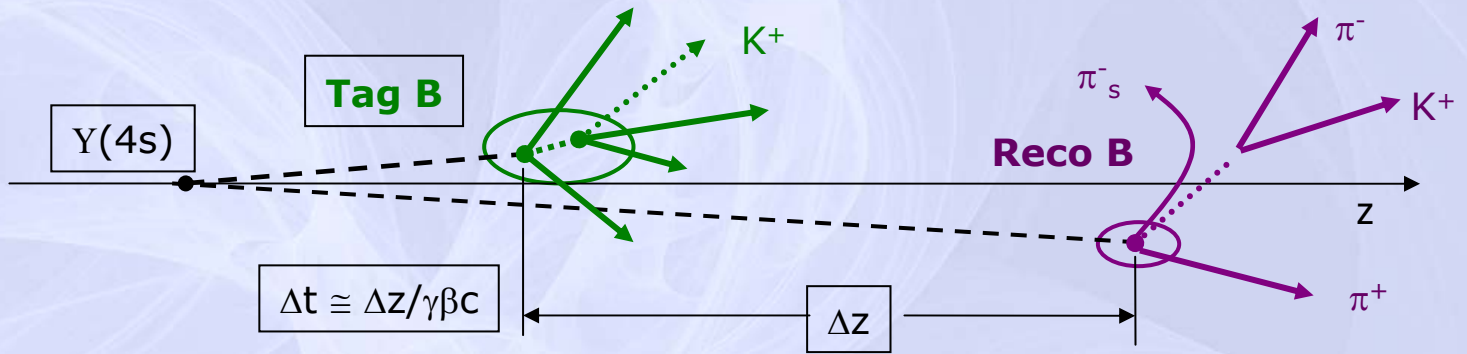
Conclusion

Back-up

- $\triangleright$  Large BF for favored decays ( $\sim 10^{-3}$ )
- $\triangleright$  Small BF for suppressed decays



# $\sin(2\beta + \gamma)$ with neutral $B$ decays



Kaon tag: Potential competing  $CP$  violating effects in  $B_{tag}$  decays (additional  $r'$  and  $\delta'$ ). [hep-ex/0504035](https://arxiv.org/abs/hep-ex/0504035)  
 Comparable to signal  $\rightarrow$  Modified time distributions

$\Leftrightarrow$  Alternative parameterization:

$$a^{(*)} = 2r^{(*)} \sin(2\beta + \gamma) \cos(\delta^{(*)})$$

$$b = 2r' \sin(2\beta + \gamma) \cos(\delta^{(*)})$$

$$c^{(*)} = 2 \cos(2\beta + \gamma) (r^{(*)} \sin \delta^{(*)} - r' \sin \delta')$$

0 for

lepton tag

## Measuring $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

## Conclusion

## Back-up

$$S^{(*)\pm} = (a^{(*)} \pm c^{(*)}) + b$$



$$B \rightarrow D^{(*)\mp} h^\pm, h^\pm = \rho^\pm, \pi^\pm$$

$232 \times 10^6 \bar{B}B$

**Full reconstruction**

Phys.Rev.D73:111101,2006

$D\rho, D\pi, D^*\pi$

- Excellent purity (80-90%)
- Limited tagging efficiency
- Limited event yields

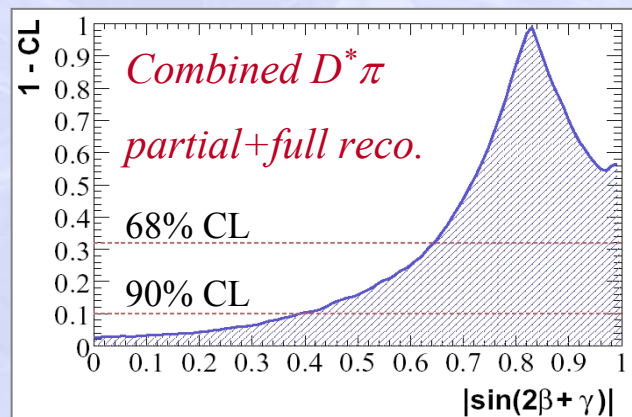
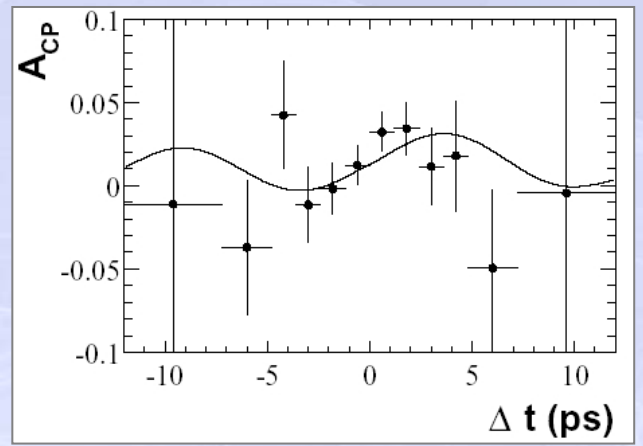
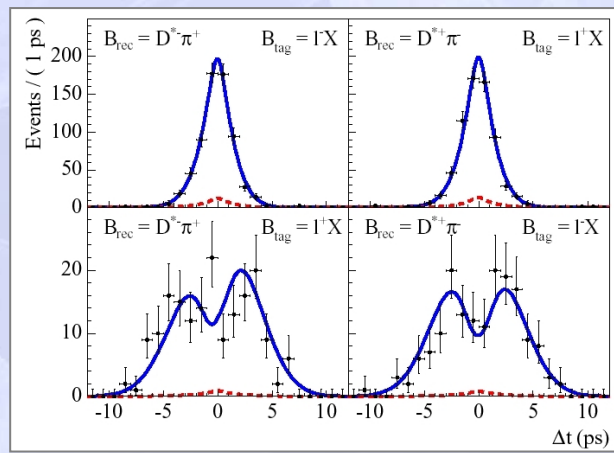
**Partial reconstruction**

$232 \times 10^6 \bar{B}B$

$D^*\pi$  only

Phys.Rev.D71:112003,2005

- Only prompt  $\pi$  and soft  $\pi$  from  $D^*$
- Lower purity (30-55%)
- Higher stat (5-6 times fully reco.)



$|\sin(2\beta+\gamma)| > 0.64$  (68%CL)  
 $> 0.40$  (90%CL)

Measuring  $\gamma$

1. Principle
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Conclusion

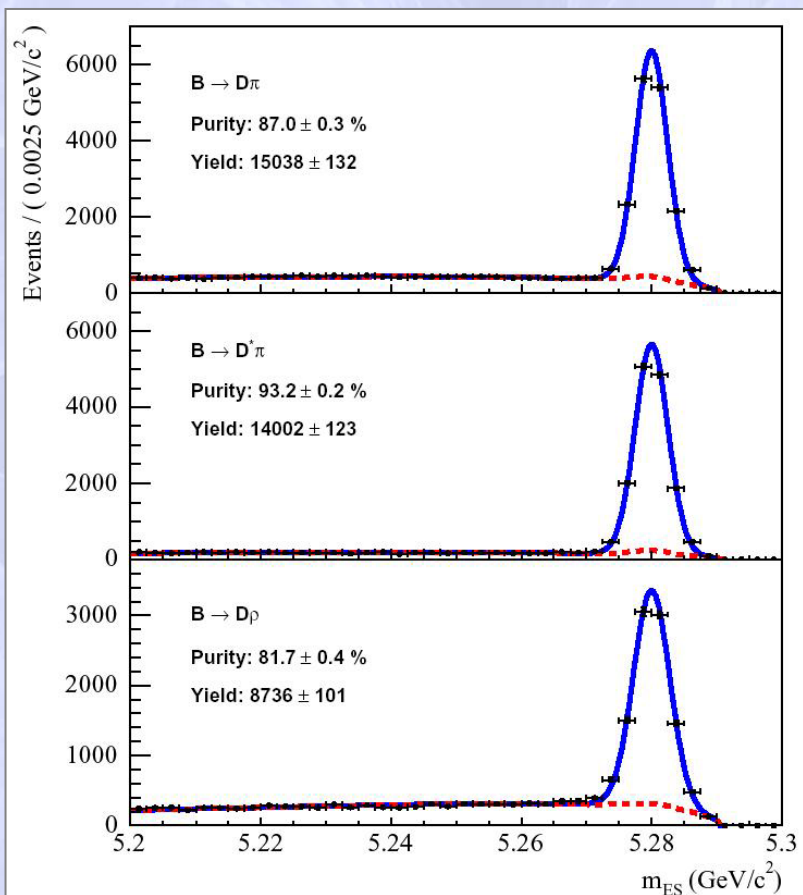
Back-up



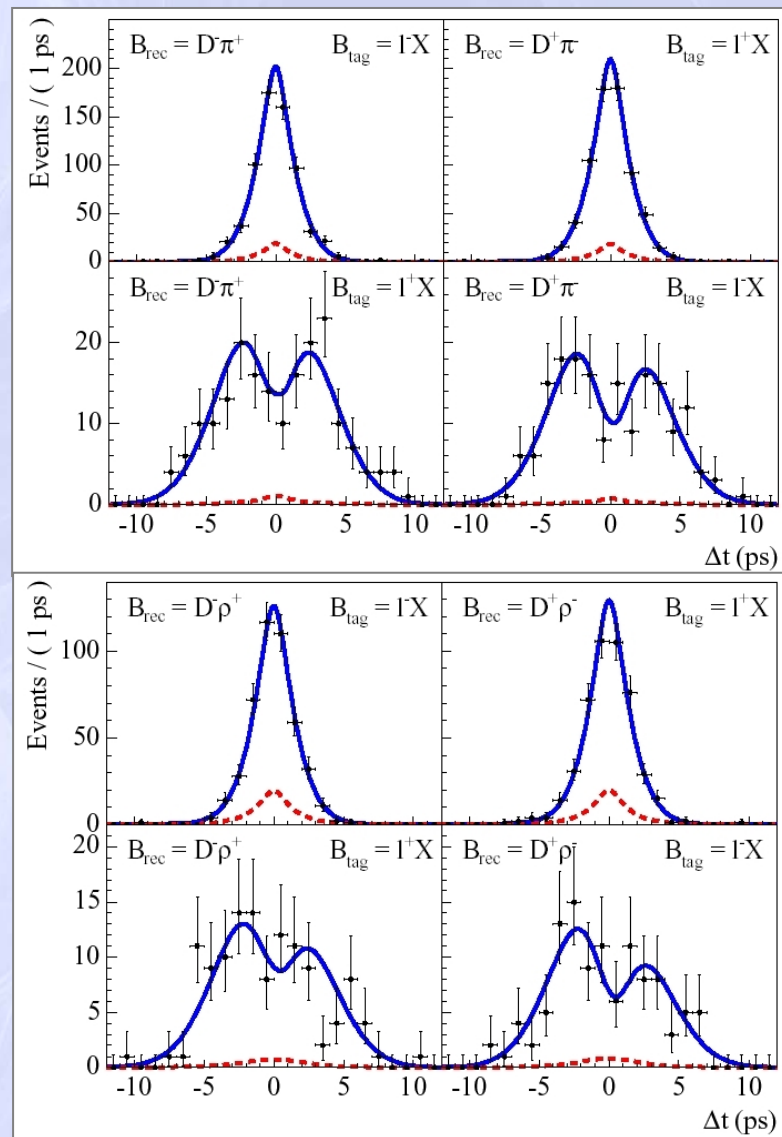


$$\sin(2\beta + \gamma)$$

Purity obtained with full reconstruction



Fitted  $\Delta t$  distributions



Measuring  $\gamma$

1. Principle
2. GLW
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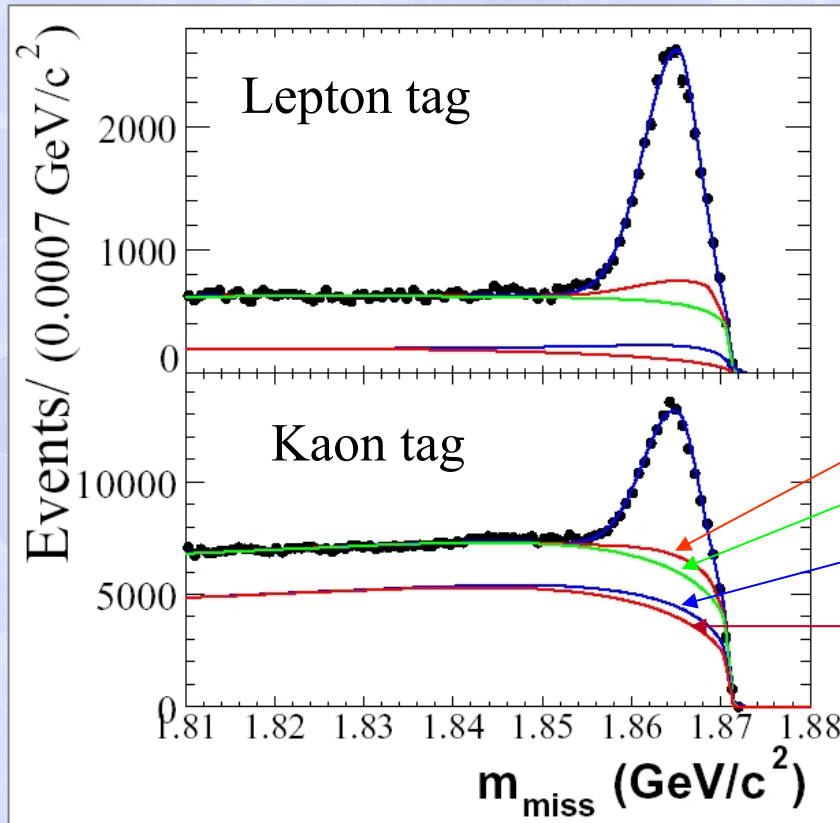
Conclusion

Back-up



$$\sin(2\beta + \gamma)$$

Partial  $B \rightarrow D^* \pi^\pm$  reco.



$D^* \rho$

Combinatoric  $BB$

Peaking  $BB$

continuum

Measuring  $\gamma$

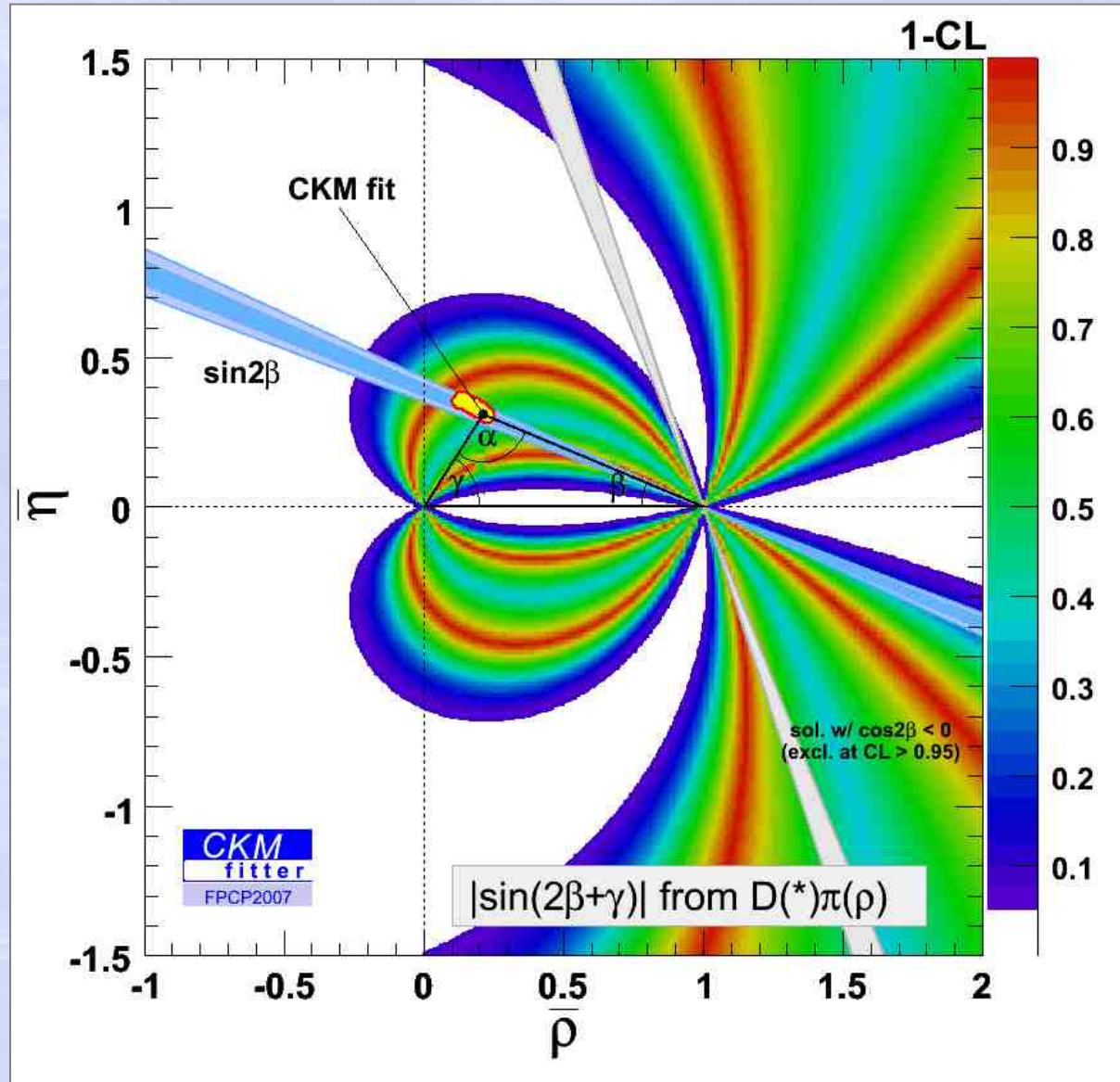
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Conclusion

Back-up



$$\sin(2\beta + \gamma)$$



### Measuring $\gamma$

1. Principle
2. GLW
3. ADS
4. GGSZ

### Conclusion

### Back-up