

Measurements of β in Charmless B Decays at BABAR

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BABAR collaboration

20 July 2007

The 2007 Europhysics Conference on
High Energy Physics



Outline

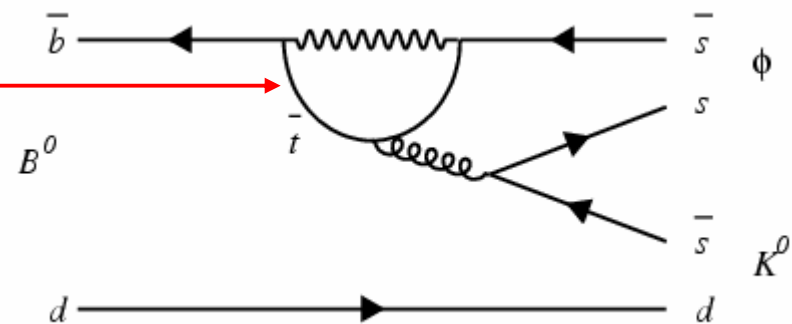
- Intro to time-dependent CP violation
 - Penguin diagrams as a window on New Physics
- $\sin 2\beta$ in charmless decays at BaBar
 - $B^0 \rightarrow \rho^0 K_S$
 - $B^0 \rightarrow \pi^0 K_S$
 - $B^0 \rightarrow K_S K_S K_S$
 - $B^0 \rightarrow \pi^0 \pi^0 K_S$
- Measurements of β using Dalitz analysis
 - $B^0 \rightarrow K^+ K^- K^0$
- Summary

Motivation: Physics Beyond SM

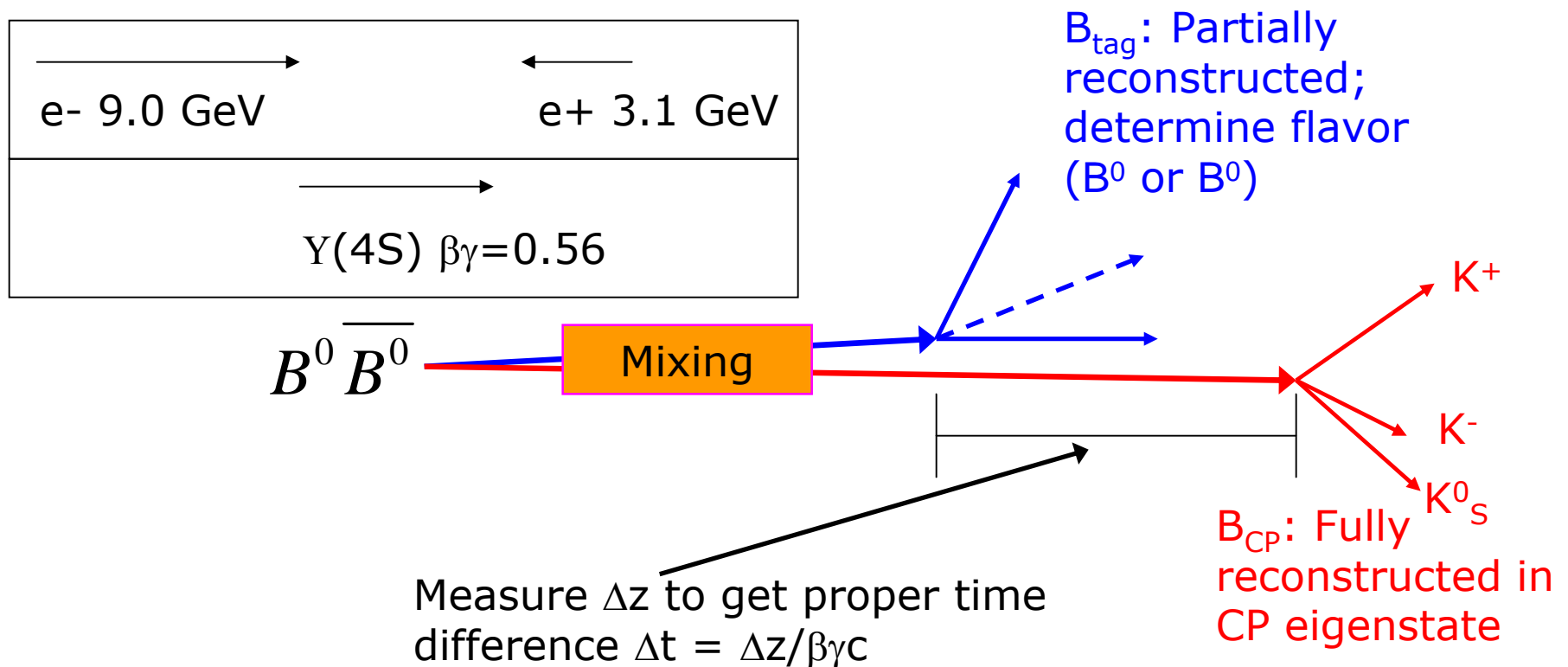


- Charmonium (e.g. $B^0 \rightarrow J/\psi K_S$) decays dominated by tree diagrams \rightarrow good laboratory to measure SM values (see M. Bomben talk, this session):
 - $\sin 2\beta = 0.678 \pm 0.026$ ($\beta = 0.372 \pm 0.017$) (HFAG Moriond 07)
- Charmless $b \rightarrow s$ decays dominated by loop (penguin) diagrams:
 - In the SM, expect $\sin 2\beta_{\text{eff}} \approx \sin 2\beta$

- Massive particles beyond the SM could enter in the loop
- Could yield $\sin 2\beta_{\text{eff}} \neq \sin 2\beta$



BaBar: An Asymmetric B Factory



B_{CP} characterized w/standard kinematic variables: $m_{\text{ES}}, \Delta E$
 $e^+e^- \rightarrow qq$ background rejected using event shape variables

Time Dep. CP Violation Formalism

Decay rate as a function of Δt :

$$\frac{d\Gamma}{d\Delta t} \propto \frac{e^{-|\Delta t|/\tau}}{\tau} \times \left[\begin{aligned} &|A|^2 + |\bar{A}|^2 \pm 2 \operatorname{Im}(\eta_{CP} \bar{A} A^* e^{-2i\beta}) \sin \Delta m \Delta t \\ &\mp \left(|A|^2 - |\bar{A}|^2 \right) \cos \Delta m \Delta t \end{aligned} \right]$$

This is usually simplified to

$$\frac{d\Gamma}{d\Delta t} \propto \frac{e^{-|\Delta t|/\tau}}{\tau} \times \left[1 \pm \left(-\eta S \sin \Delta m \Delta t - C \cos \Delta m \Delta t \right) \right]$$

CP violation parameters:

- in interference between decay w/ and w/o mixing : **S** ($\sim \sin 2\beta$ in SM)
- in decay (direct): **C** (~ 0 in SM)

$B^0 \rightarrow \rho^0 K_S$

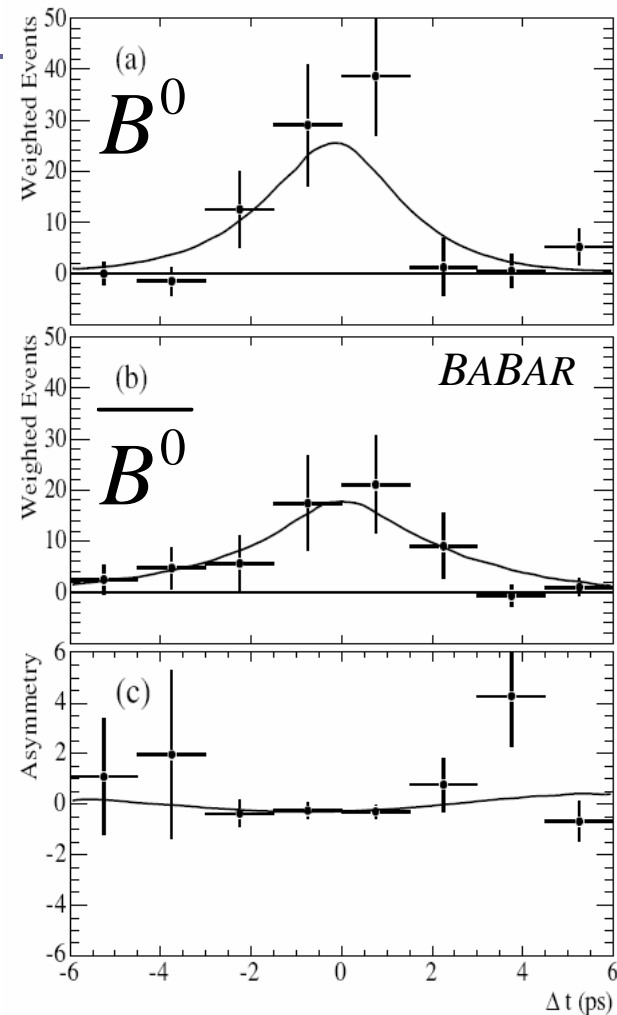
$$\rho^0 \rightarrow \pi^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$$

- Maximum Likelihood fit to:
 - $m_{ES}, \Delta E, NN, \cos \theta_{\pi^+}, m_{\pi\pi}, \Delta t$
 - $N_{\text{signal}} = 111 \pm 19$
 - $B(B^0 \rightarrow \rho^0 K^0) = (4.9 \pm 0.8 \pm 0.9) 10^{-6}$
 - 5.0σ significance incl. syst.
- $S = 0.20 \pm 0.52 \pm 0.24$
- $C = 0.64 \pm 0.41 \pm 0.20$

Largest contribution:
neglect of interference

PRL 98, 051803 (2007)

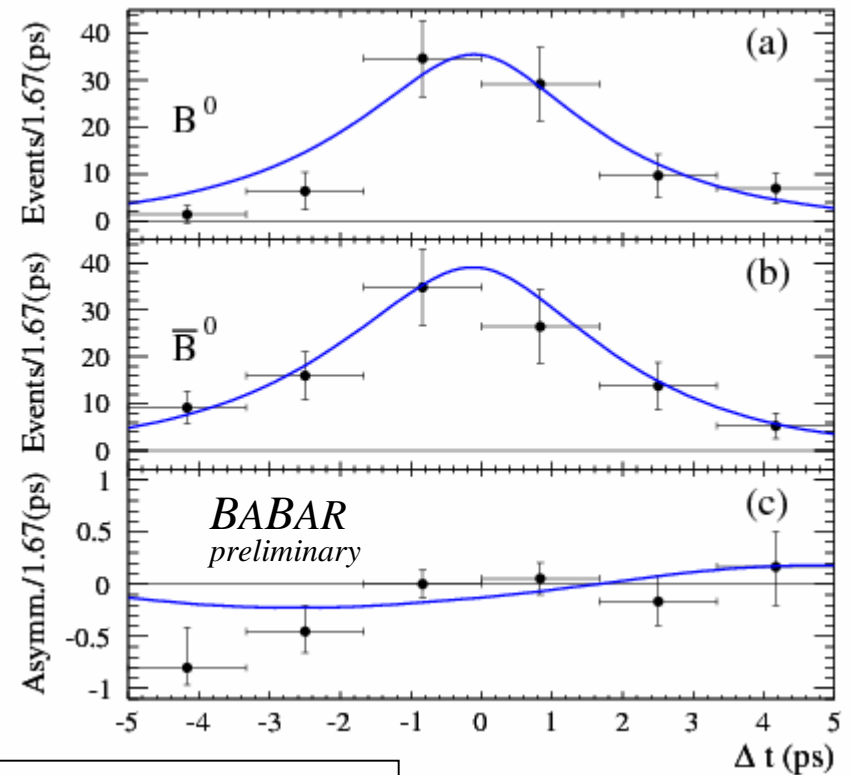
227×10^6 BB pairs



$B^0 \rightarrow \pi^0 K_S$

- Δt computed using technique pioneered by BaBar
 - K_S momentum vector pointed back to the IP
 - B production vertex is constrained to come from the beam axis
- $N_{\text{sig}} = 459 \pm 29$
 - $B(B^0 \rightarrow \pi^0 K^0) = (10.34 \pm 0.66 \pm 0.58) 10^{-6}$
- $S = 0.40 \pm 0.23 \pm 0.03$
- $C = 0.24 \pm 0.15 \pm 0.03$

383 x 10^6 BB pairs

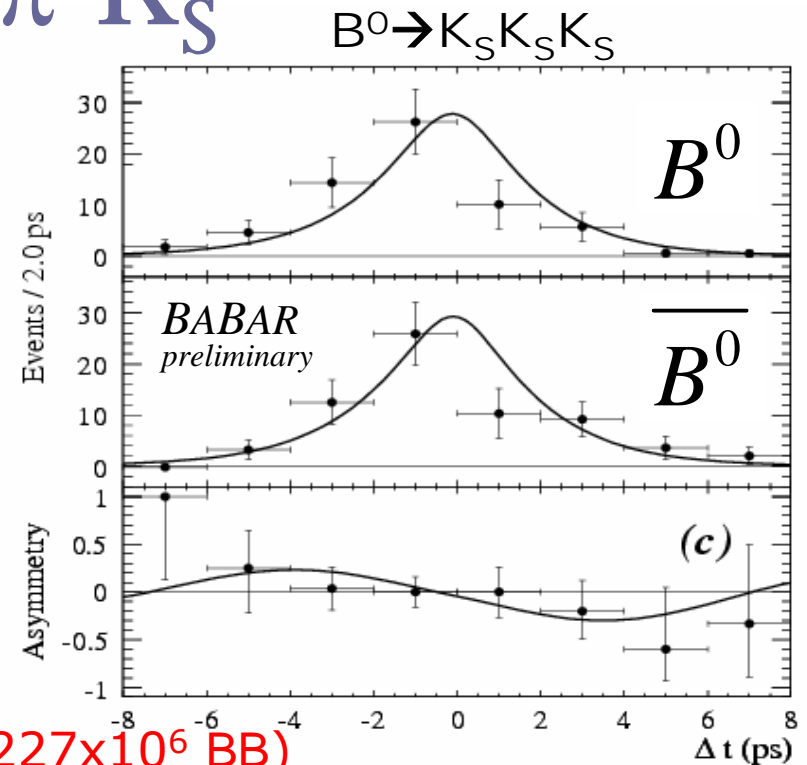


arXiv:0707.2980
Sub. to PRD-RC

New!

$B^0 \rightarrow K_S K_S K_S$ and $\pi^0 \pi^0 K_S$

- CP-even three body final states
- $K_S K_S K_S$: SM theory uncertainty small
- Δt computed using same technique as $\pi^0 K_S$
- In $K_S K_S K_S$, one K_S may decay to $\pi^0 \pi^0$



$K_S K_S K_S$: (383×10^6 BB)

$\pi^0 \pi^0 K_S$: (227×10^6 BB)

$N_{\text{sig}} = 125 \pm 13, 64 \pm 12$

$N_{\text{sig}} = 117 \pm 27$

$S = -0.71 \pm 0.24 \pm 0.04$

$S = 0.72 \pm 0.71 \pm 0.08$

$C = 0.02 \pm 0.21 \pm 0.05$

$C = 0.23 \pm 0.52 \pm 0.13$

hep-ex/0702046

hep-ex/0702010

Both sub. to
PRD-RC

K⁺K⁻K⁰: Time-Dependent Dalitz Analysis

- Challenges in B⁰→K⁺K⁻K⁰:
 - Mixture of CP-odd and CP-even
 - Potential for interference among different decay amplitudes
- Answer: Incorporate amplitude structure as a function of phase space into the fit

Plug into top expression on pg. 5:

$$\begin{aligned} \overline{\mathcal{A}}(m_{K^+K^-}, \cos \theta_H) &= \sum_r \overline{\mathcal{A}}_r \\ &= \sum_r \underline{c}_r (1 \mp \underline{b}_r) e^{i(\underline{\varphi}_r \mp \underline{\delta}_r)} \cdot f_r(m_{K^+K^-}, \cos \theta_H), \end{aligned}$$

f_r describes the decay dynamics:
e.g. Breit-Wigner

“Isobar” coefficients: c_r, φ_r

Allow for direct asymmetries: b_r, δ_r

$$A_{CP,r} = -C = -2b_r/(1+b_r^2); \beta_{\text{eff},r} = \beta + \delta_r$$

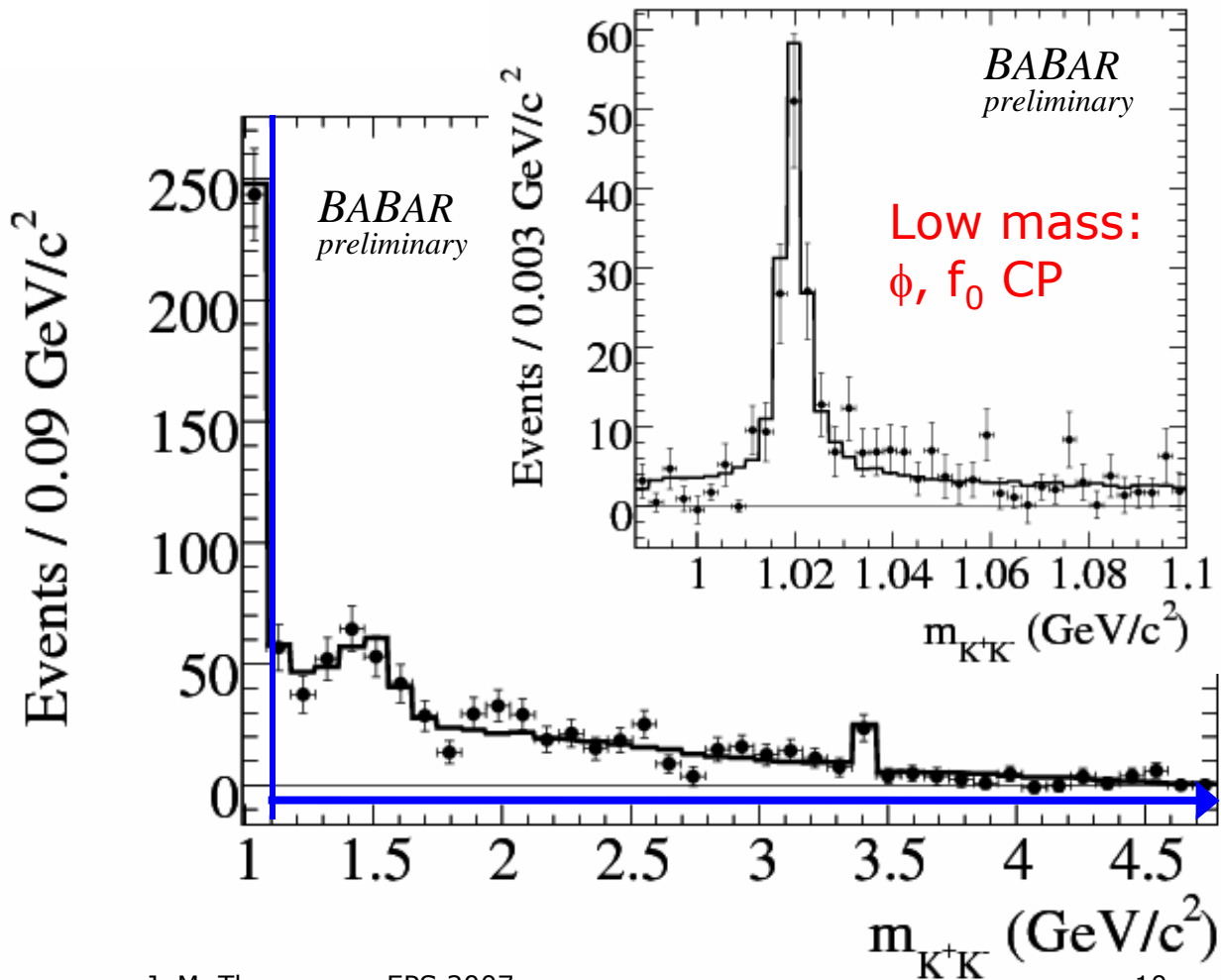
K⁺K⁻K⁰: Analysis Strategy

Combine:

- K_S → π⁺π⁻
- K_S → π⁰π⁰
- K_L

3 steps:

- Whole DP:
 - Average CP
- "Low mass"
- "High mass":
 - Average CP



Amplitude model in $K^+K^-K^0$

- Motivated by DP analysis of $B^+ \rightarrow K^+K^-K^0$
 - BaBar: PRD 74 032003 (2006); Belle: PRD 71 092003 (2005)
- Also BaBar angular moments analysis
 - PRD 71 091102 (2005)

Results: Fit to Whole DP

Fit fraction

Components of
our Isobar Model

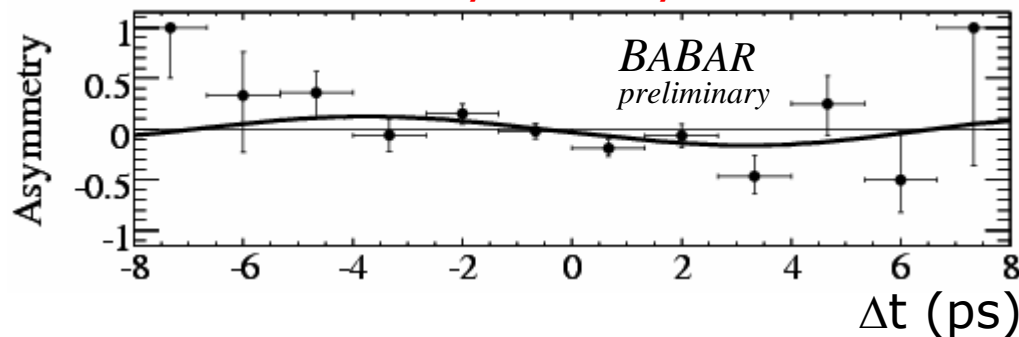
Isobar Mode	Amplitude c_r	Phase φ_r (rad)	\mathcal{F}_r (%)
ϕK^0	0.0085 ± 0.0010	-0.016 ± 0.234	12.5 ± 1.3
$f_0 K^0$	0.622 ± 0.046	-0.14 ± 0.14	40.2 ± 9.6
$X_0(1550)K^0$	0.114 ± 0.018	-0.47 ± 0.20	4.1 ± 1.3
$(K^+K^-)_{NR}K^0$	1 (fixed)	0 (fixed)	
$(K^+K^0)_{NR}K^-$	0.33 ± 0.07	1.95 ± 0.27	112.0 ± 14.9
$(K^-K^0)_{NR}K^+$	0.31 ± 0.08	-1.34 ± 0.37	
$\chi_{c0}(1P)K^0$	0.0306 ± 0.0049	$^{0.81}_{-2.33} \pm 0.54$	3.0 ± 1.2
$D^- K^+$	1.11 ± 0.17		3.6 ± 1.5
$D_s^- K^+$	0.76 ± 0.14		1.8 ± 0.6

K⁺K⁻K⁰: CP Results – Whole DP

	A_{CP}	β_{eff} (rad)
Whole DP	$-0.015 \pm 0.077 \pm 0.053$	$0.352 \pm 0.076 \pm 0.026$

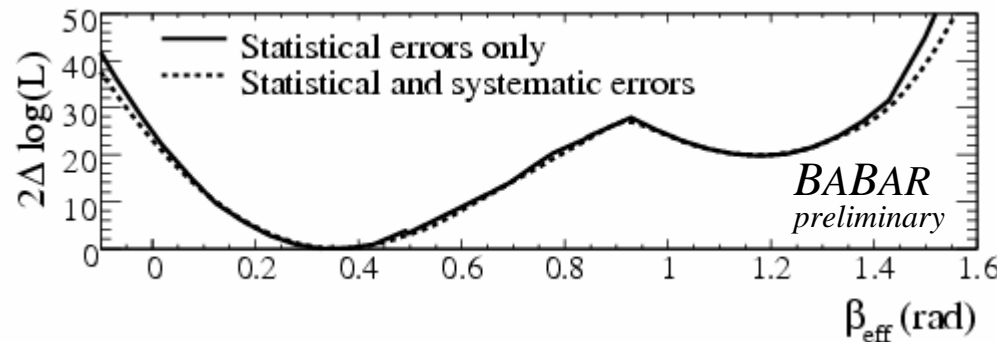
$$(\sin 2\beta_{eff} = 0.647 \pm 0.116 \pm 0.040)$$

Asymmetry



Recall: charmonium
 $\beta = 0.372 \pm 0.017$

Likelihood scan



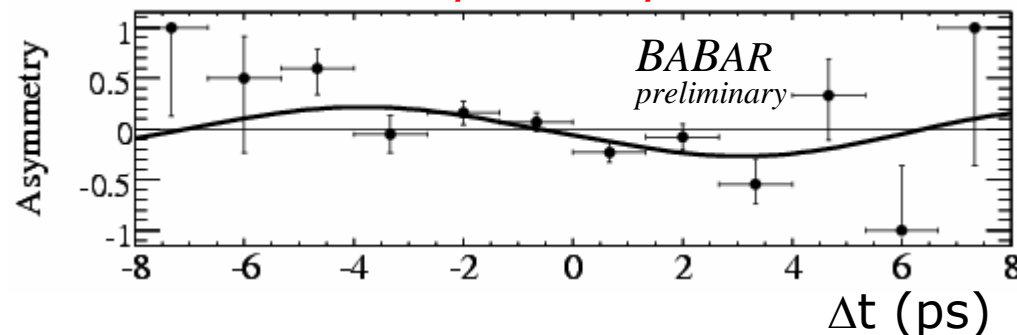
- $\beta_{eff}=0$ excluded at 4.8σ
- Interference between S- and P-waves leads to terms proportional to $\cos 2\beta \rightarrow$ solution near $\pi/2 - \beta$ excluded at 4.5σ
- Note: $\beta \rightarrow \beta + \pi$ ambiguity remains

K⁺K⁻K⁰: CP Results – High Mass

	A_{CP}	β_{eff} (rad)
High-mass	$-0.054 \pm 0.102 \pm 0.060$	$0.436 \pm 0.087 \begin{smallmatrix} +0.055 \\ -0.031 \end{smallmatrix}$

$$(\sin 2\beta_{eff} = 0.764 \pm 0.111 \begin{smallmatrix} +0.071 \\ -0.040 \end{smallmatrix})$$

Asymmetry



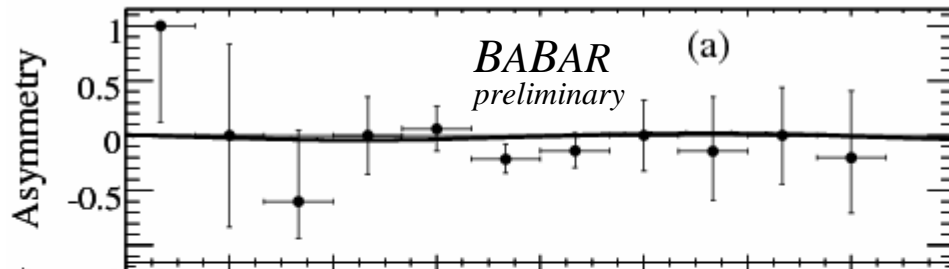
- High-mass result intended to replace “K⁺K⁻K⁰ excluding ϕ ” result
- Using likelihood difference, $\beta_{eff}=0$ excluded at 5.1σ
 - First observation of CP violation in $B^0 \rightarrow K^+K^-K^0$!
 - Second observation in penguin decays after $B^0 \rightarrow \eta'K^0$;
BaBar: PRL 98 031801 (2007), Belle: PRL 98 031802 (2007)

K⁺K⁻K⁰: CP Results – Low Mass

	A_{CP}	β_{eff} (rad)
(1) ϕK^0	$-0.08 \pm 0.18 \pm 0.04$	$0.11 \pm 0.14 \pm 0.06$
(1) $f_0 K^0$	$0.41 \pm 0.23 \pm 0.07$	$0.14 \pm 0.15 \pm 0.05$

(ϕK^0 : $-\eta S = 0.21 \pm 0.26 \pm 0.11$)
 ($f_0 K^0$: $-\eta S = 0.25 \pm 0.26 \pm 0.10$)

Asymmetry

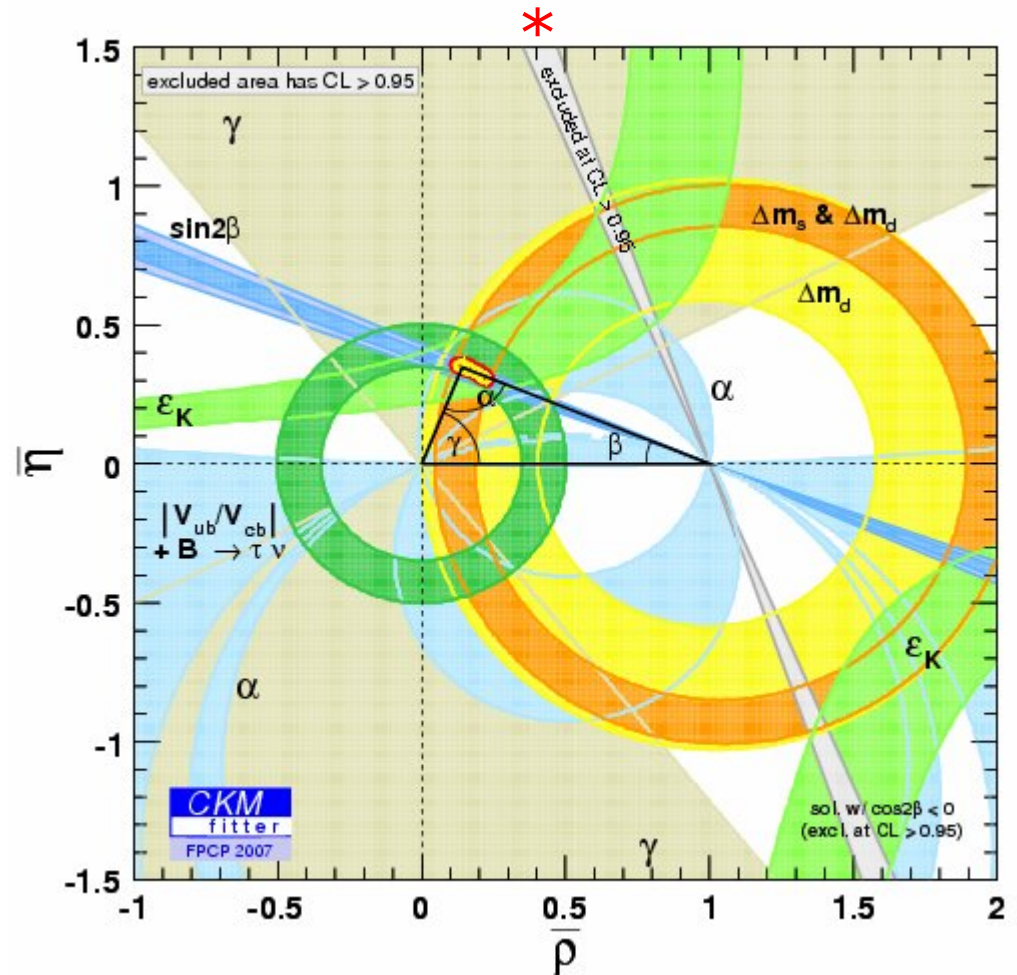


- Fit finds 2 solutions w/ $\Delta \log L = 0.1$
- We choose sol'n compatible with the Standard Model

K⁺K⁻K⁰ Summary



- Results on 383×10^6 BB pairs, submitted to PRL (arXiv:0706.3885)
- Exclude $\pi/2 - \beta$ sol'n at 4.5σ (*)
- Observe CP violation in high-mass $K^+K^-K^0$
- $\phi, f_0 > 1.5\sigma$ from SM

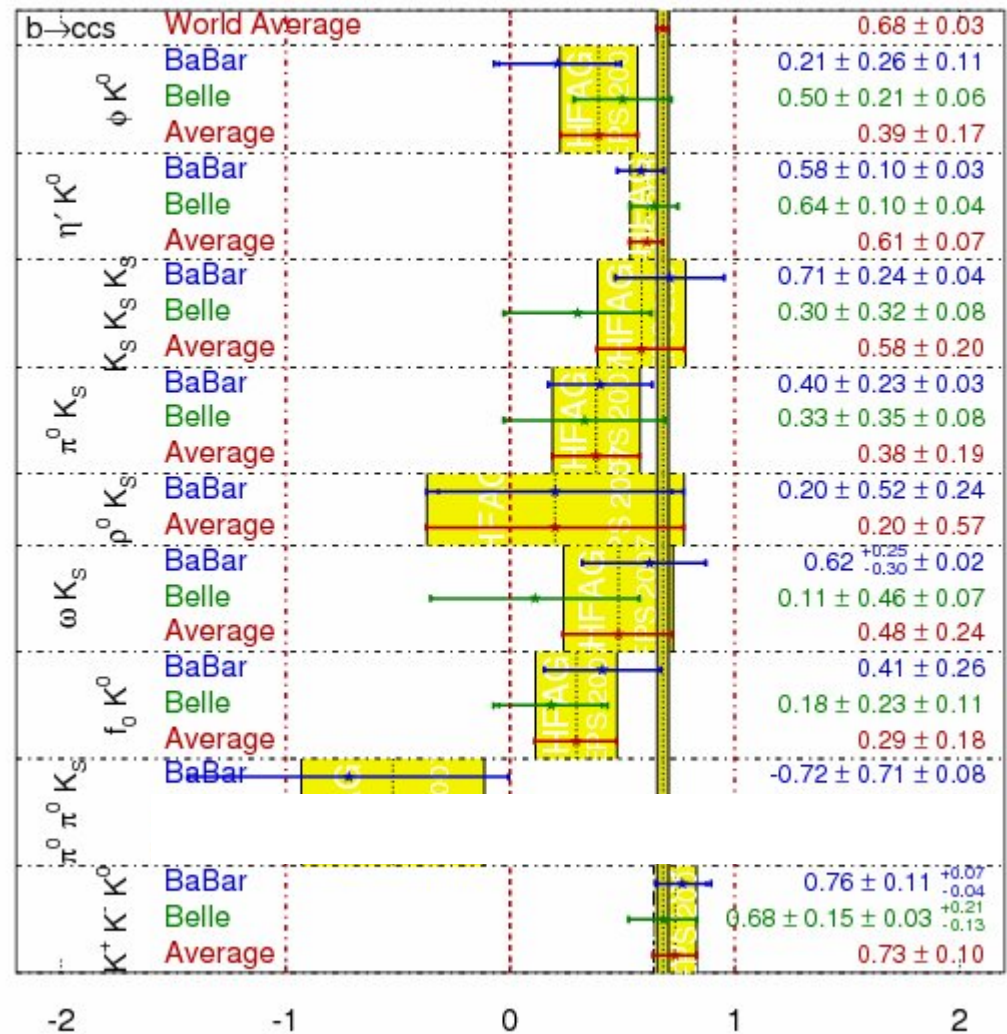


Summary

- Moriond 2007:
HFAG average = 0.53 ± 0.05
 - 2.6σ from $b \rightarrow ccs$
- w/new $\pi^0 K_S, K^+ K^- K^0$:
HFAG average = 0.56 ± 0.05
 - 2.1σ from $b \rightarrow ccs$
- * = BaBar results recently submitted or published

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

HFAG
 EPS 2007
 PRELIMINARY

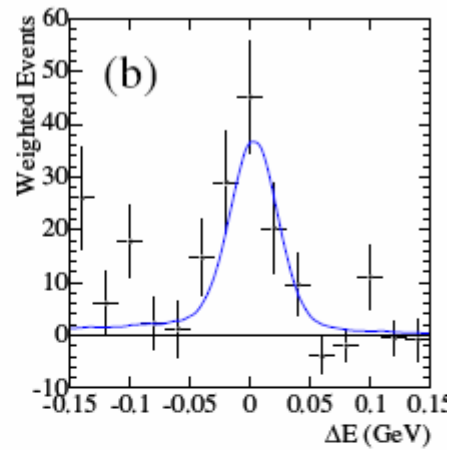
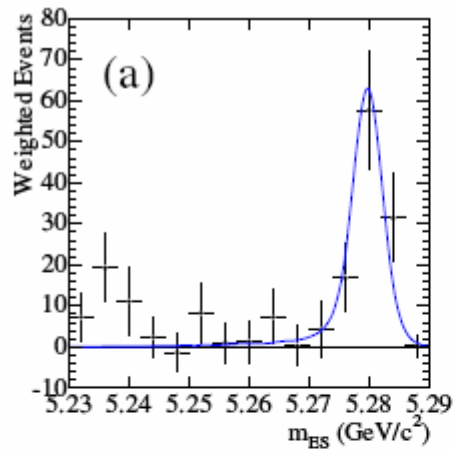


Plot thanks to T. Gershon

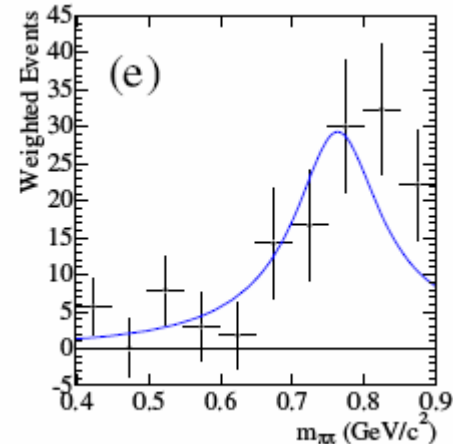
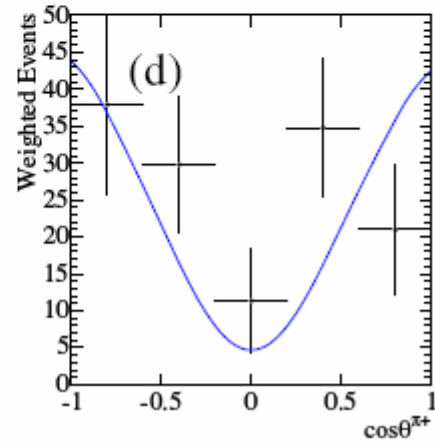
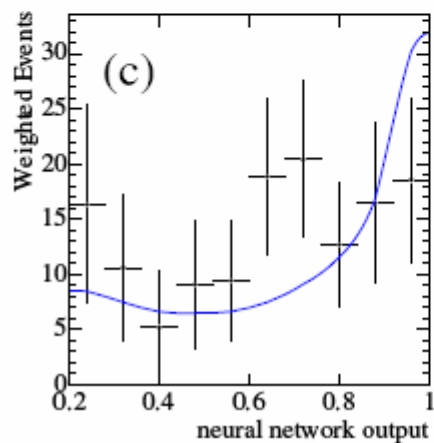


Extra Slides

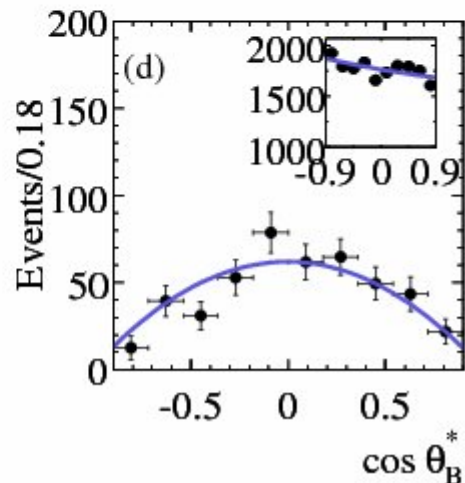
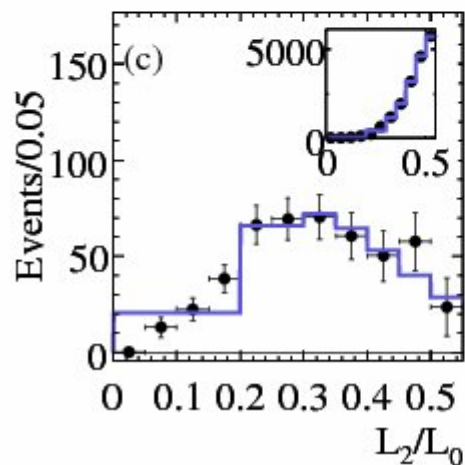
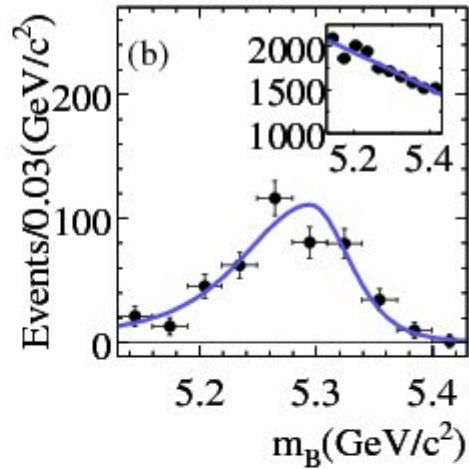
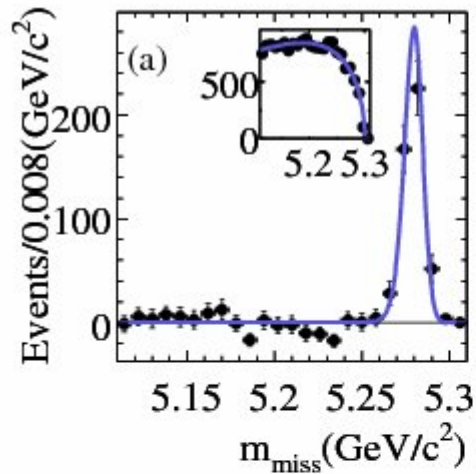
$B^0 \rightarrow \rho^0 K_S$: Likelihood Variables



Signal-weighted events



$B^0 \rightarrow \pi^0 K_S$: Likelihood Variables



Weighted events
Main: Signal
Insets: Background

$B^0 \rightarrow K_S K_S K_S$: Kinematic Variables

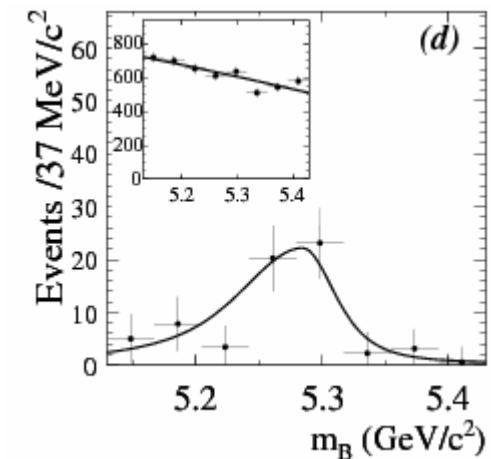
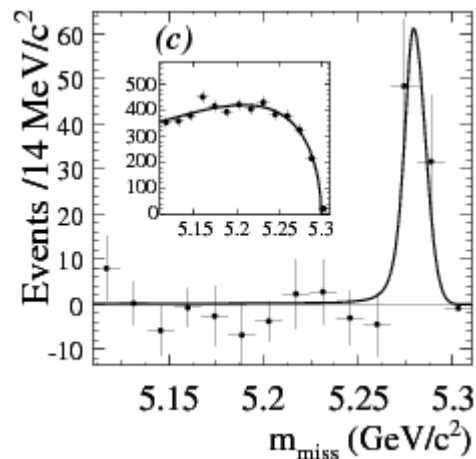
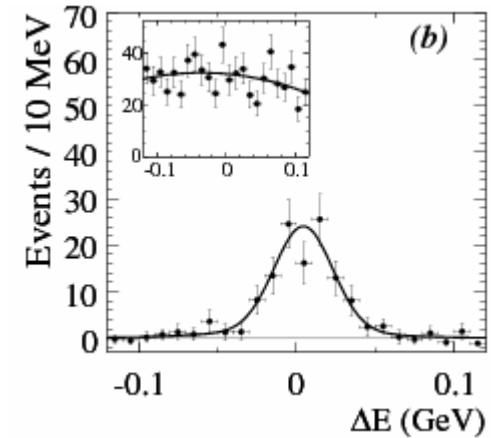
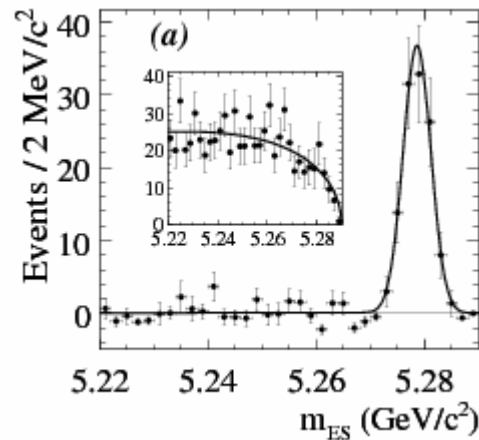
All $K_S \rightarrow \pi^+ \pi^-$

Weighted events

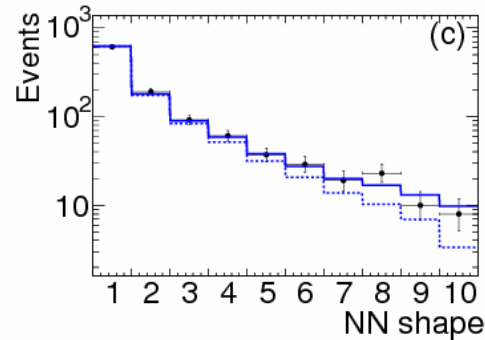
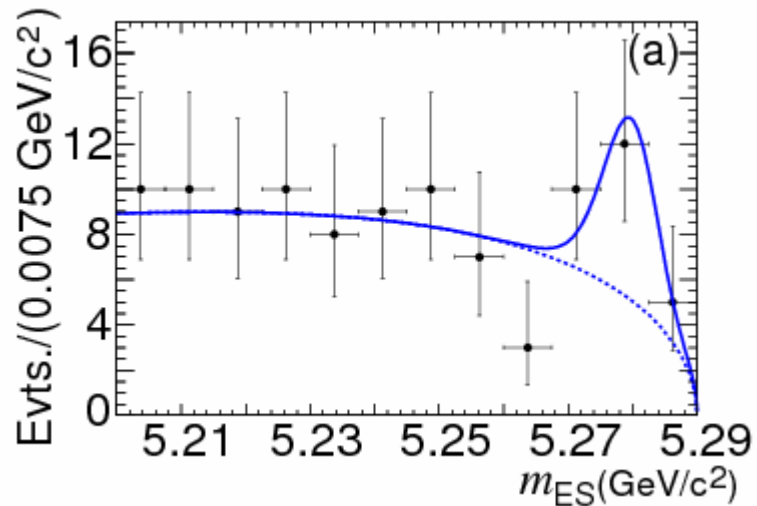
Main: Signal

Insets: Background

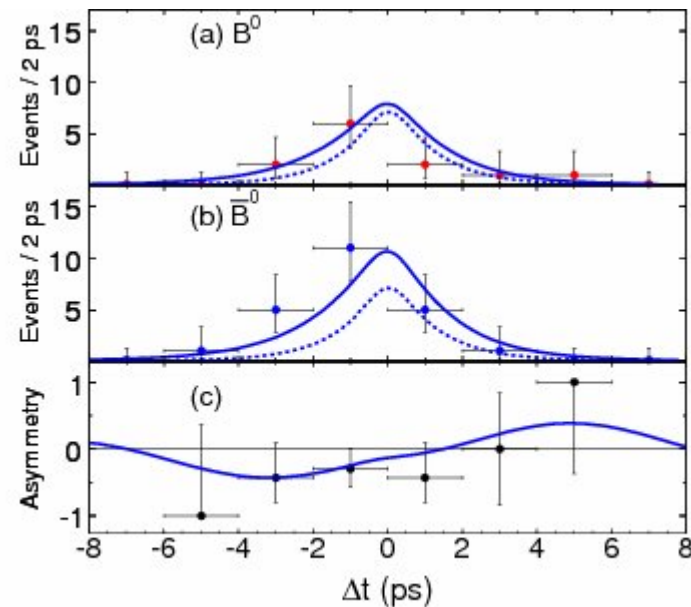
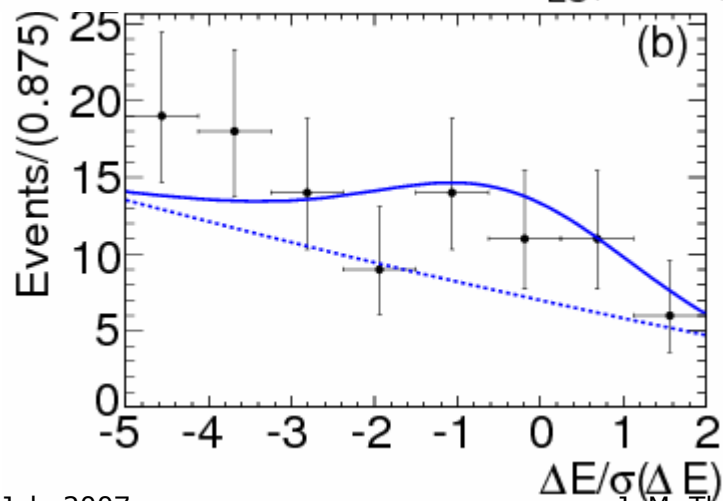
One $K_S \rightarrow \pi^0 \pi^0$



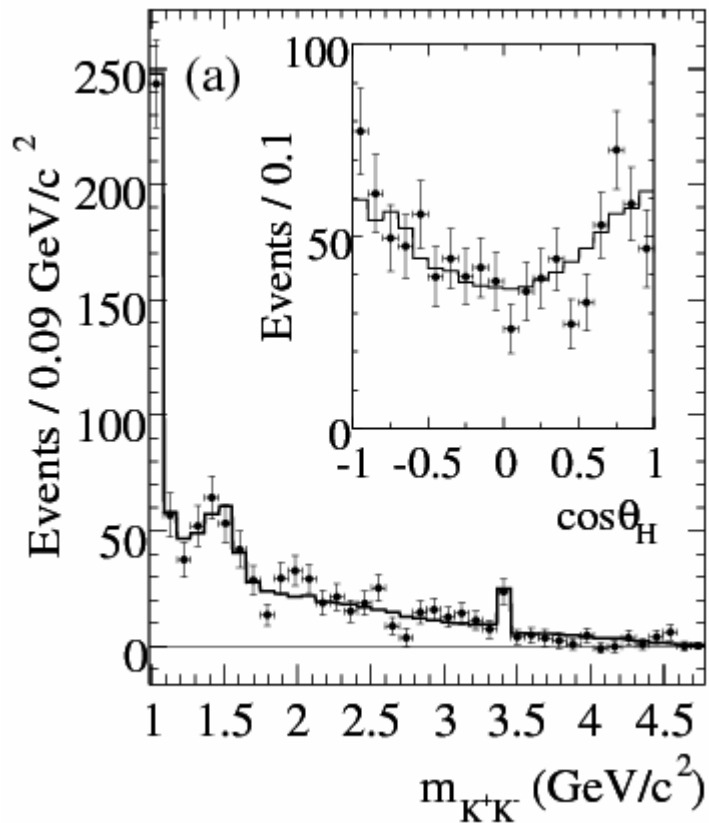
$B^0 \rightarrow \pi^0 \pi^0 K_S$: Likelihood Variables



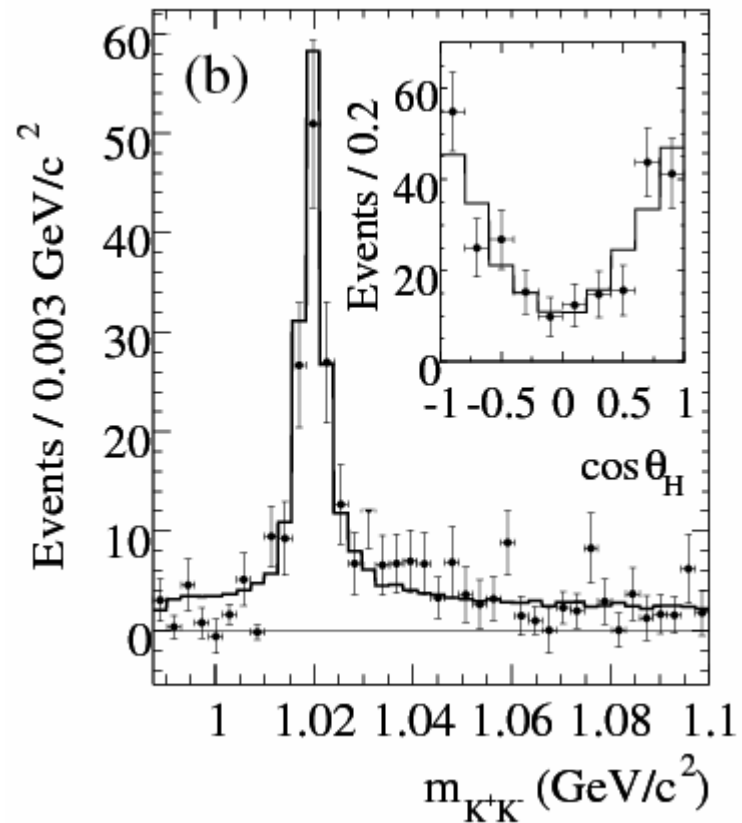
Fit projections
w/cut on
likelihood ratio



$K^+K^-K^0$: DP Fit Projections



Whole DP Fit (signal)



Low-mass Fit (signal)

K⁺K⁻K⁰: Low-mass fit solutions

	A_{CP}	β_{eff} (rad)
(1) ϕK^0	$-0.08 \pm 0.18 \pm 0.04$	$0.11 \pm 0.14 \pm 0.06$
(1) $f_0 K^0$	$0.41 \pm 0.23 \pm 0.07$	$0.14 \pm 0.15 \pm 0.05$
(2) ϕK^0	-0.11 ± 0.18	0.10 ± 0.13
(2) $f_0 K^0$	-0.20 ± 0.31	3.09 ± 0.19

2 solutions w/ $\Delta \log L = 0.1$ – Multiple sol'ns common in DP analyses

- ϕ isobar coefficients significantly different
- Solution (2) is completely inconsistent w/the SM due to β_{eff} in $f_0 K^0$
 - Wrong quadrant of ρ - η plane!
 - We choose (1), as it is consistent w/SM
- For both sol'ns, there is a mathematical ambiguity of $\pm\pi$ in $\beta_{eff, \phi'}$ correlated with a $\pm\pi$ shift in φ_ϕ

K⁺K⁻K⁰: Systematic Errors

Source	Whole DP		High-mass		ϕK^0		$f_0 K^0$	
	A_{CP}	β_{eff}	A_{CP}	β_{eff}	A_{CP}	β_{eff}	A_{CP}	β_{eff}
Fit Bias	0.003	0.001	0.014	0.008	0.03	0.06	0.06	0.03
Isobar model	0.004	0.009	0.025	$^{+0.051}_{-0.024}$	0.00	0.01	0.01	0.03
Other	0.052	0.024	0.053	0.018	0.02	0.01	0.03	0.02
Total	0.053	0.026	0.060	$^{+0.055}_{-0.031}$	0.04	0.06	0.07	0.05

- Fit Bias: negligible in pure toy MC
 - Use values from fits to signal MC + toy background
 - Low-mass bias due to (unmodeled) resolution in KL
- Isobar model: vary model parameters by errors; replace BaBar's $X_0(1550)$ w/Belle's $f_x(1500)$
 - Motivation for low-mass fit: keep uncertainty in scalar sector from introducing a large systematic
- Other: Standard uncertainties in time-dependent analysis; largest contribution: conservative allowance for CP in background

$K^+K^-K^0$: Q2B Parameters

Results of DP fit translated to C and S using:

$$C \equiv -A_{CP}, \text{ and}$$

$$-\eta S \equiv \frac{1 - b^2}{1 + b^2} \sin(2\beta_{\text{eff}}),$$

	C	$-\eta S$
Whole DP	$0.015 \pm 0.077 \pm 0.053$	$0.647 \pm 0.116 \pm 0.040$
High-mass	$0.054 \pm 0.102 \pm 0.060$	$0.764 \pm 0.111 \begin{smallmatrix} +0.071 \\ -0.040 \end{smallmatrix}$
(1) ϕK^0	$0.08 \pm 0.18 \pm 0.04$	$0.21 \pm 0.26 \pm 0.11$
(1) $f_0 K^0$	$-0.41 \pm 0.23 \pm 0.07$	$0.25 \pm 0.26 \pm 0.10$

$B^0 \rightarrow \rho^0 K_S$: Systematic Errors

	S	C	N
Mis-reco'd events and fit bias	0.12	0.09	10
PDF uncertainties	0.13	0.18	2
Tagging parameters	0.02	0.01	-
Neglect of interference	0.14	0.09	7
ρ^0 mass shape	0.07	0.05	3
B Background BF	0.02	0.10	13
CP of background	0.04	0.00	-
Tracking efficiency & B counting	-	-	6
Total	0.24	0.20	19

TABLE II: Summary of contributions to the systematic error.