

# CLEO-c Measurement of the Pseudoscalar Decay Constant $f_{D_s}$ & the Ratio $f_{D_s}/f_{D^+}$

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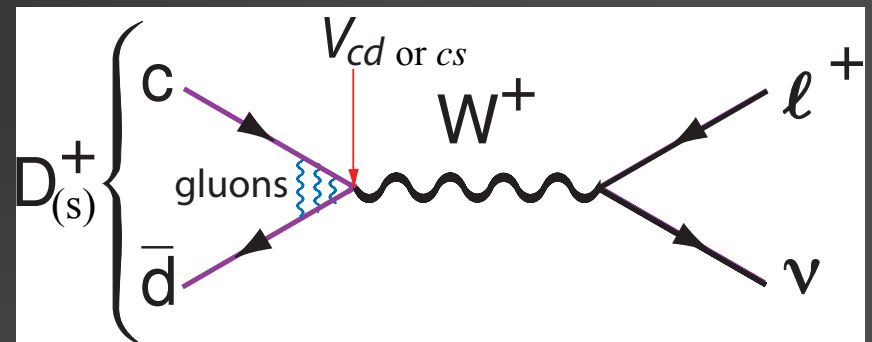


# Leptonic Decays: $D \rightarrow \ell^+ \nu$

Introduction: Pseudoscalar decay constants

$c$  and  $\bar{q}$  can annihilate, probability is  $\propto$  to wave function overlap

Example :



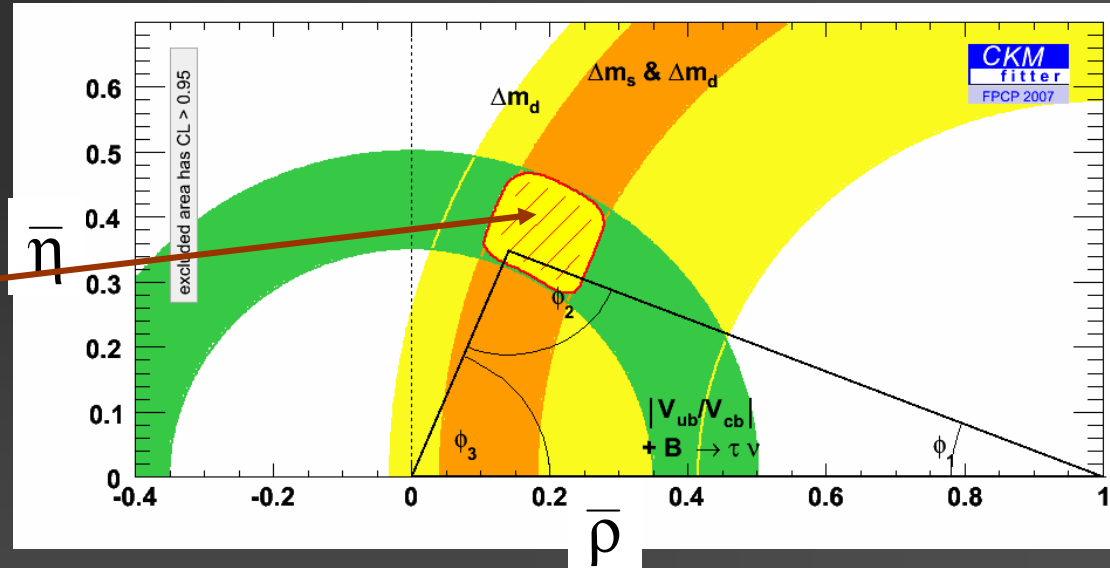
In general for all pseudoscalars:

$$\Gamma(P^+ \rightarrow \ell^+ \nu) = \frac{1}{8\pi} G_F^2 f_P^2 m_\ell^2 M_P \left(1 - \frac{m_\ell^2}{M_P^2}\right)^2 |V_{Qq}|^2$$

Calculate, or measure if  $V_{Qq}$  is known

# Goals in Leptonic Decays

- Test theoretical calculations in strongly coupled theories in non-perturbative regime
- $f_B$  &  $f_{B_s}/f_B$  needed to improve constraints from  $\Delta m_d$  &  $\Delta m_s/\Delta m_d$ . Hard to measure directly (i.e.  $B \rightarrow \tau^+ \nu$  gives  $V_{ub} f_B$ ), but we can determine  $f_D$  &  $f_{D_s}$  using  $D \rightarrow \ell^+ \nu$  and use them to test theoretical models (i.e. Lattice QCD)



Constraints from  $V_{ub}$ ,  $\Delta m_d$ ,  $\Delta m_s$  &  $B \rightarrow \tau^+ \nu$

# New Physics Possibilities

- In Standard Model

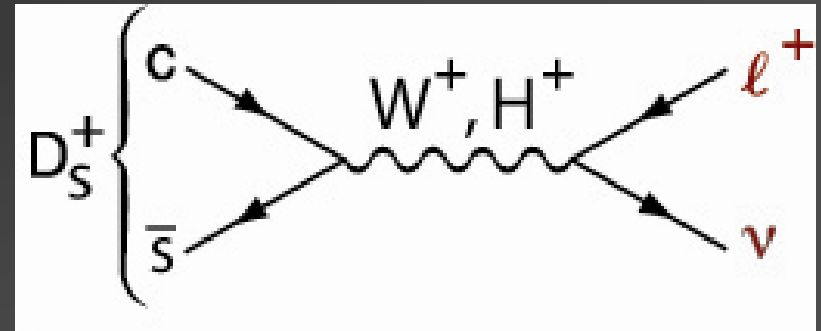
$$\frac{\Gamma(P^+ \rightarrow \tau^+ \nu)}{\Gamma(P^+ \rightarrow \mu^+ \nu)} = m_\tau^2 \left(1 - \frac{m_\tau^2}{M_P^2}\right)^2 / m_\mu^2 \left(1 - \frac{m_\mu^2}{M_P^2}\right)^2$$

- Another Gauge

Boson could also

mediate decay, could

modify ratio or change decay rates

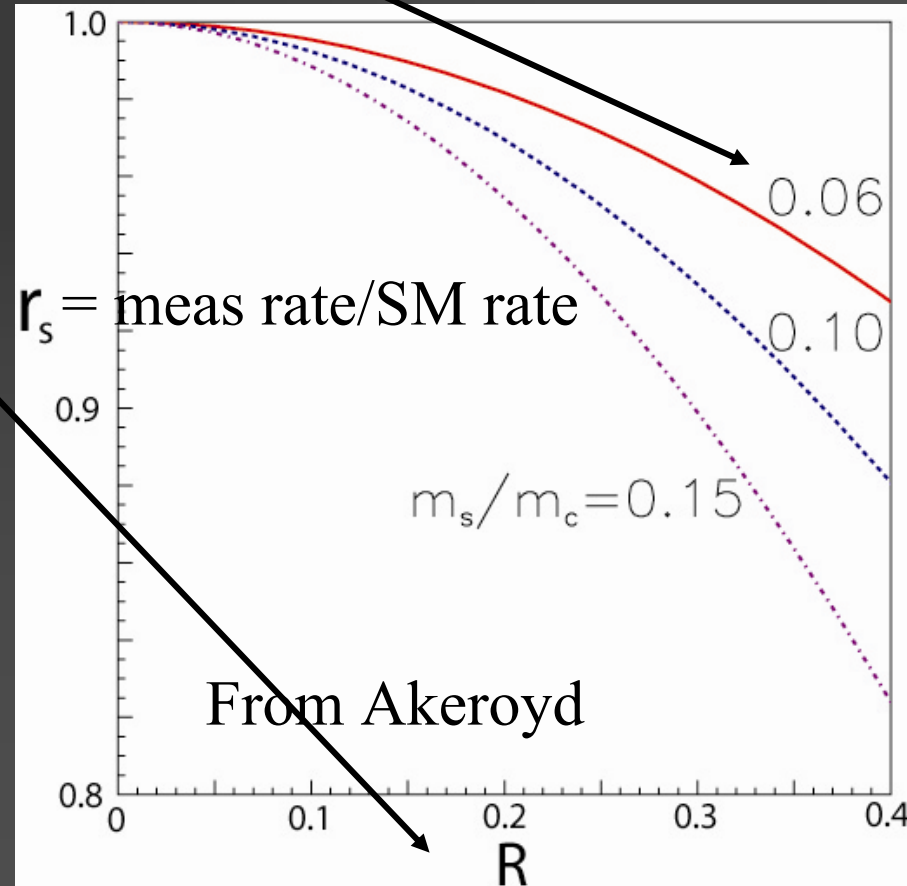


See Hewett [hep-ph/9505246] & Hou, PRD 48, 2342 (1993).

# New Physics Possibilities II

- In SUSY Akeroyd calculated Leptonic decay rate as a function of  $m_s/m_c$ .
- In terms of SUSY parameter  $R = \tan\beta/m_H$

See Akeryod [hep-ph/0308260]



# Experimental methods

- $D\bar{D}$  production at threshold: used by Mark III, and more recently by CLEO-c and BES-II.

- Unique event properties
- Large cross sections:

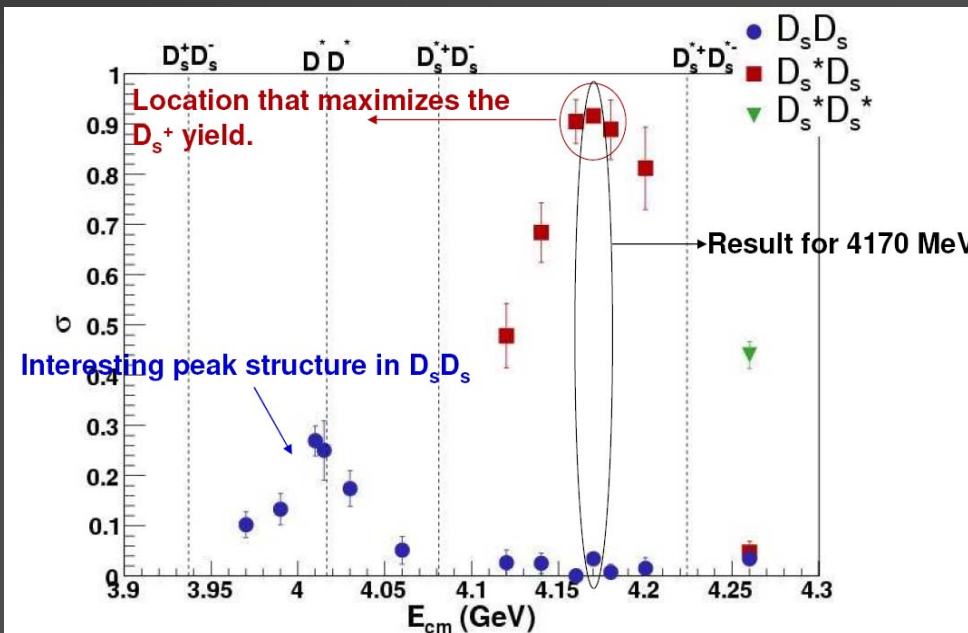
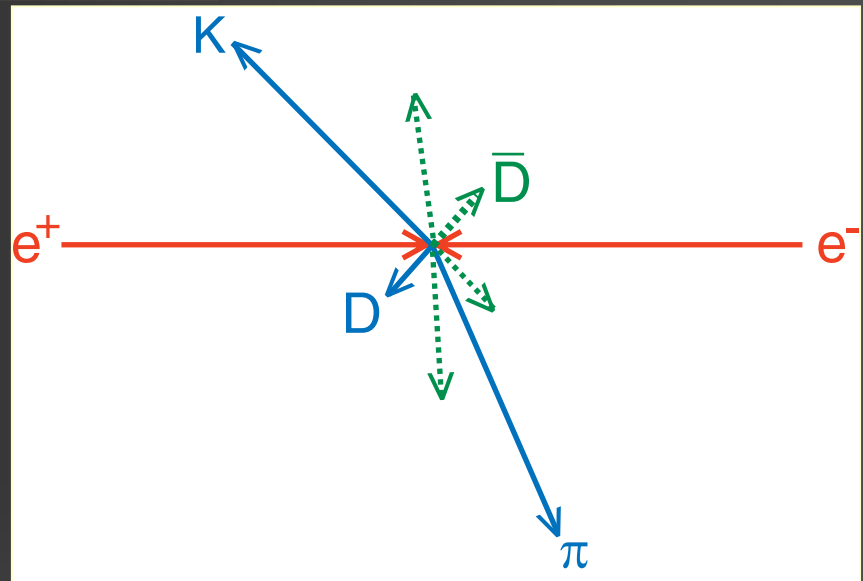
$$\left. \begin{aligned} \sigma(D^0\bar{D}^0) &= 3.72 \pm 0.09 \text{ nb} \\ \sigma(D^+D^-) &= 2.82 \pm 0.09 \text{ nb} \end{aligned} \right\} \text{World Ave}$$

$$\sigma(D_S D_S^*) = \sim 0.9 \text{ nb}$$

Continuum  $\sim 12 \text{ nb}$

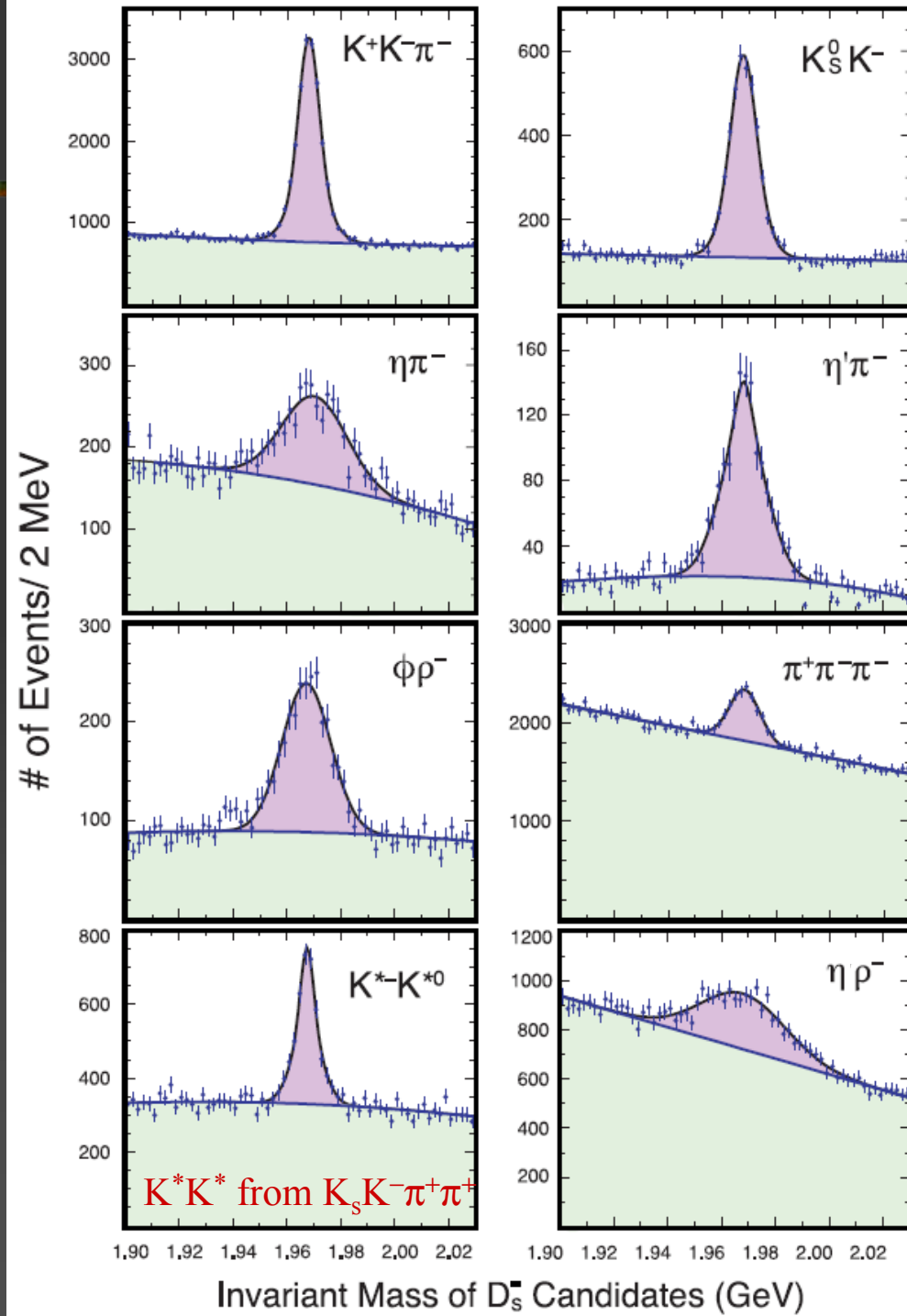
- Ease of B measurements using "double tags"

- $\mathcal{B}_A = \# \text{ of } A / \# \text{ of } D\text{'s}$



# Invariant masses

- $D_s$  studies done at  $E_{\text{cm}} = 4170 \text{ MeV}$
- To choose tag candidates:
  - Fit distributions & determine  $\sigma$
  - Cut at  $\pm 2.5 \sigma$
- Define sidebands to measure backgrounds  $5-7.5 \sigma$
- Total # of Tags  
=  $31,302 \pm 472 \text{ (stat)}$



# Measurements of $f_{D_S}$

- Two separate techniques
- (1) Measure  $D_S^+ \rightarrow \mu^+ \nu$  along with  $D_S \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow \pi^+ \nu$ . This requires finding
  - a  $D_S^-$  tag,
  - a  $\gamma$  from either  $D_S^{*-} \rightarrow \gamma D_S^-$  or  $D_S^{*+} \rightarrow \gamma \mu^+ \nu$ .
  - the muon or pion
  - Then inferring a single missing  $\nu$  using kinematical constraints (use  $314 \text{ pb}^{-1}$ , *results are accepted for publication*)
- (2) Find  $D_S^+ \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow e^+ \nu \nu$  opposite a  $D_S^-$  tag (use  $195 \text{ pb}^{-1}$ , *results are preliminary*)



# Measurement of $D_S^+ \rightarrow \mu^+ \nu$

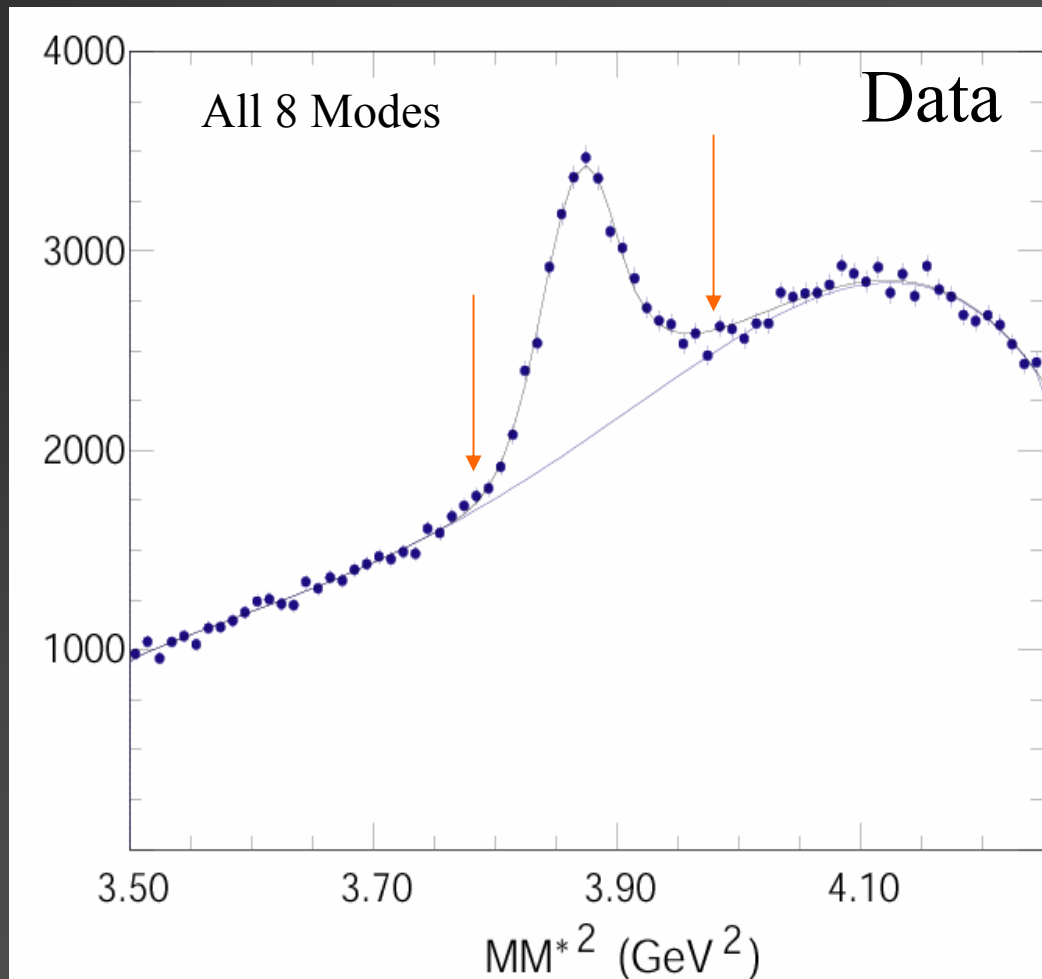
- We see all the particles from  $e^+e^- \rightarrow D_S^* D_S, \gamma, D_S$  (tag) +  $\mu^+$  except for the single  $\nu$
- We use a kinematic fit to (a) improve the resolution & (b) remove ambiguities
  - Constraints include: total p & E, tag  $D_S$  mass,  $\Delta m = M(\gamma D_S) - M(D_S)$  [or  $\Delta m \equiv M(\gamma \mu \nu) - M(\mu \nu)$ ] = 143.6 MeV, E of  $D_S$  (or  $D_S^*$ ) fixed
  - Lowest  $\chi^2$  solution in each event is kept
  - No  $\chi^2$  cut is applied

# Tag Sample using $\gamma$

- First we define the tag sample by computing the  $MM^{*2}$  off of the  $\gamma$  &  $D_s$  tag

$$MM^{*2} = (E_{CM} - E_{D_s} - E_{\gamma})^2 - (-\vec{p}_{D_s} - \vec{p}_{\gamma})^2$$

- Total of  $11880 \pm 399 \pm 504$  tags, after the selection on  $MM^{*2}$ .



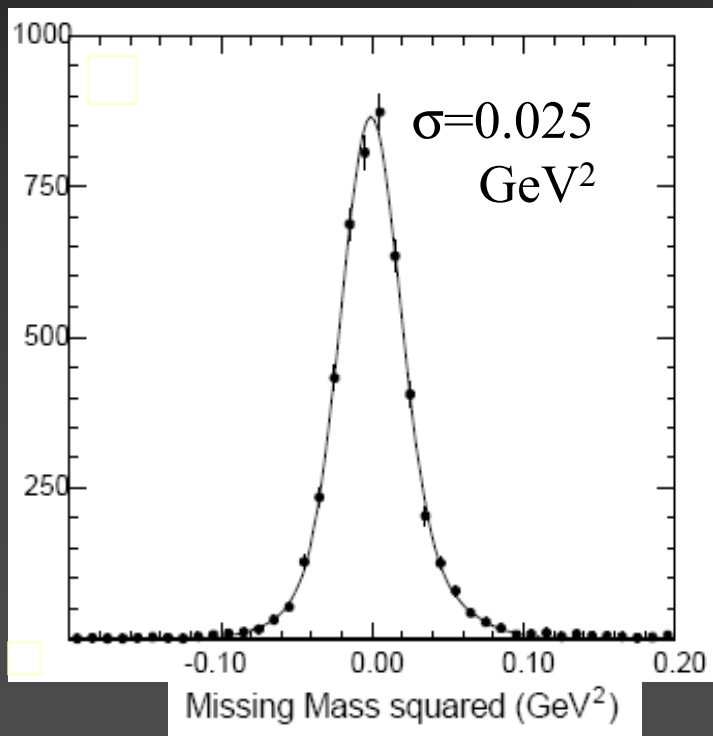
# Define Three Classes

- Class (i), single track deposits  $< 300$  MeV in calorimeter, minimum ionizing (accepts 99% of muons and 60% of kaons & pions)
- Class (ii), single track deposits  $> 300$  MeV in calorimeter (accepts 1% of muons and 40% of kaons & pions)
- Class (iii) single track consistent with electron
- For all 3 cases require no other  $\gamma$  with energy  $> 300$  MeV.

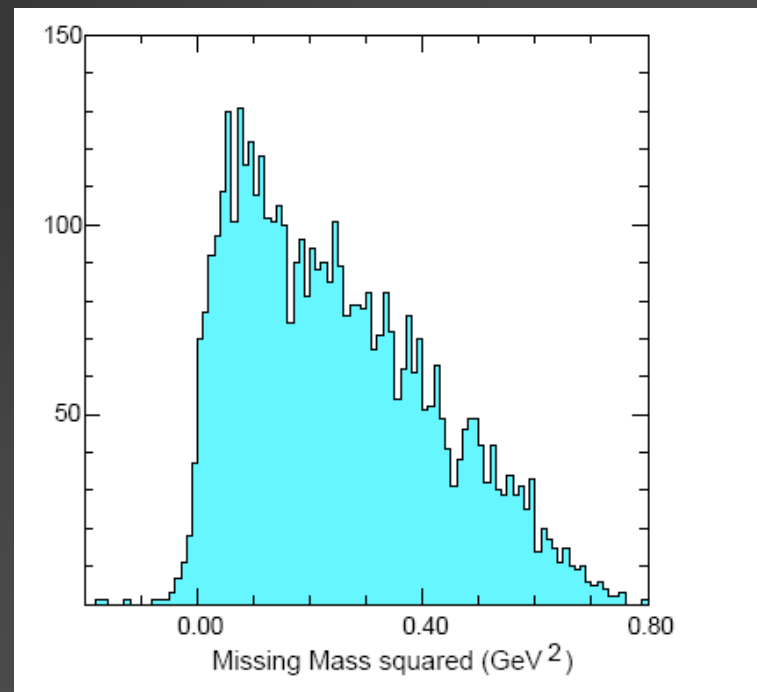
# The $MM^2$

- To find the signal events, we compute

$$MM^2 = (E_{CM} - E_{D_S} - E_{\gamma} - E_{\mu})^2 - (-\vec{p}_{D_S} - \vec{p}_{\gamma} - \vec{p}_{\mu})^2$$



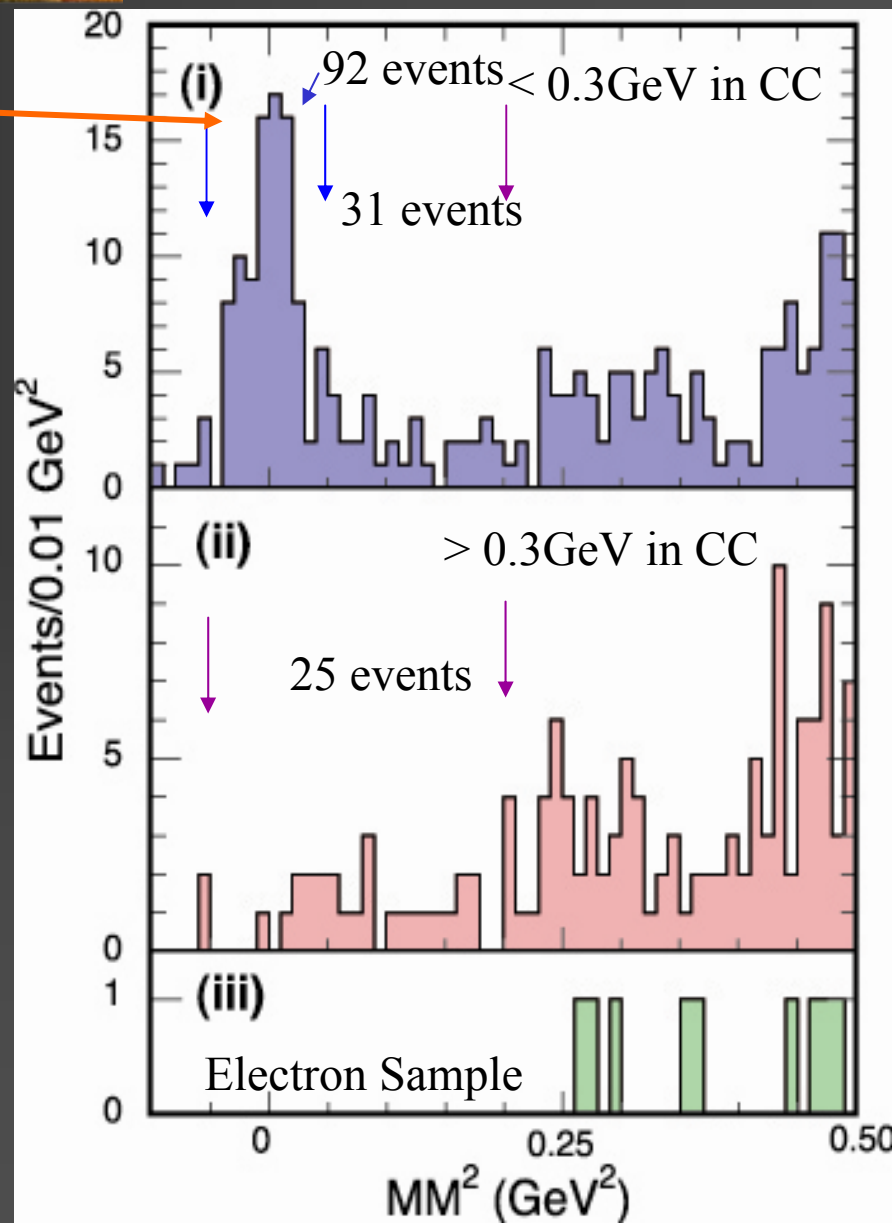
Signal  $\mu\nu$



Signal  $\tau\nu, \tau \rightarrow \pi\nu$

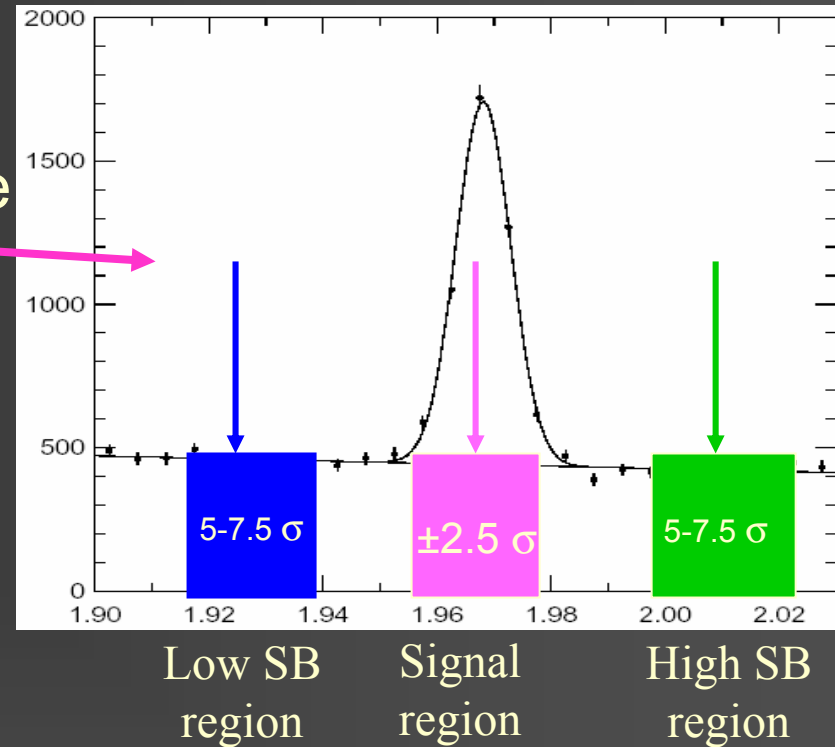
# MM<sup>2</sup> In Data

- Clear  $D_S^+ \rightarrow \mu^+ \nu$  signal for case (i)
- Will show that events  $< 0.2 \text{ GeV}^2$  are mostly  $D_S \rightarrow \tau^+ \nu$ ,  $\tau \rightarrow \pi^+ \nu$  in cases (i) & (ii)
- No  $D_S \rightarrow e^+ \nu$  seen, case (iii)



# Background Samples

- Two sources of background
- 1) Bkgrnd under invariant mass peaks – Use sidebands to estimate
- In  $\mu^+\nu$  signal region, case (i) &  $|MM|^2 < 0.05 \text{ GeV}^2$ , 3.5 bkgrd, out of 92 events
- Bkgrnd for cases (i) & (ii) &  $MM^2 < 0.20 \text{ GeV}^2 = 9.0 \pm 2.3$
- 2) Backgrounds from real  $D_S$  decays, e.g.  $\pi^+\pi^0\pi^0$ , or  $D_S \rightarrow \tau^+\nu$ ,  $\tau \rightarrow \pi^+\pi^0\nu \dots < 0.2 \text{ GeV}^2$ , none in  $\mu\nu$  signal region
- $B(D_S \rightarrow \pi^+\pi^0) < 1.1 \times 10^{-3}$  &  $\gamma$  energy cut yields  $< 0.2$  evts

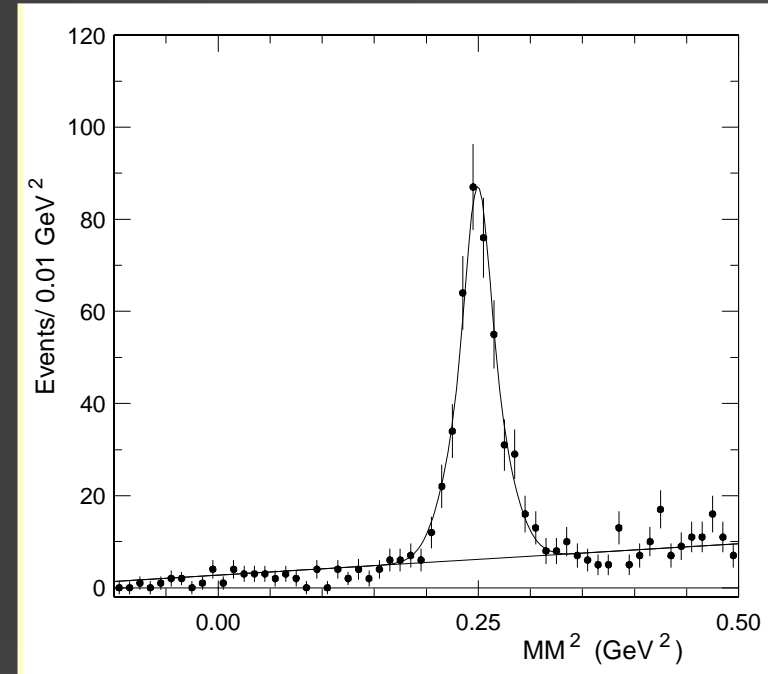


Backgrounds from real  $D_S^+$  in  $\tau \rightarrow \pi\nu$

Source	$B(\%)$	# of events case (i)	# of events case(ii)	Sum
$D_s^+ \rightarrow X\mu^+\nu$	8.2	$0_{-0}^{+1.8}$	0	$0_{-0}^{+1.8}$
$D_s^+ \rightarrow \pi^+\pi^0\pi^0$	1.0	$0.03 \pm 0.04$	$0.08 \pm 0.03$	$0.11 \pm 0.04$
$D_s^+ \rightarrow \tau^+\nu$	6.4			
$\tau^+ \rightarrow \pi^+\pi^0\nu$	1.5	$0.55 \pm 0.22$	$0.64 \pm 0.24$	$1.20 \pm 0.33$
$\tau^+ \rightarrow \mu^+\nu$	1.0	$0.37 \pm 0.15$	0	$0.37 \pm 0.15$
Sum		$1.0_{-0}^{+1.8}$	$0.7 \pm 0.2$	$1.7_{-0.4}^{+1.8}$

# Check: $\mathcal{B}(D_s^+ \rightarrow K^+ K^0)$

- Do almost the same analysis but consider  $MM^2$  off of an identified  $K^+$
- Allow extra charged tracks and showers to not veto  $K^0$  decays or interactions in EM cal
- Signal verifies expected  $MM^2$  resolution
- Find  $(2.90 \pm 0.19 \pm 0.18)\%$ , compared with result from double tags  $(3.00 \pm 0.19 \pm 0.10)\%$



# Branching Ratio & Decay Constant

- $D_S^+ \rightarrow \mu^+ \nu$ 
  - 92 signal events, 3.5 background, use SM to calculate  $\tau \nu$  yield near 0  $MM^2$  based on known  $\tau \nu / \mu \nu$  ratio ( $\sim 7$  evnts)
  - $B(D_S^+ \rightarrow \mu^+ \nu) = (0.597 \pm 0.067 \pm 0.039)\%$
- $D_S^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \pi^+ \nu$ 
  - Sum case (i)  $0.05 < MM^2 < 0.2 \text{ GeV}^2$  & case (ii)  $-0.05 < MM^2 < 0.2 \text{ GeV}^2$ . Total of 56 signal and 8.6 background
  - $B(D_S^+ \rightarrow \tau^+ \nu) = (8.0 \pm 1.3 \pm 0.4)\%$
- By summing both cases above, (& use SM ratio) find  
 $B^{\text{eff}}(D_S^+ \rightarrow \mu^+ \nu) = (0.638 \pm 0.059 \pm 0.033)\%$
- $f_{D_S} = 274 \pm 13 \pm 7 \text{ MeV}$
- $B(D_S^+ \rightarrow e^+ \nu) < 1.3 \times 10^{-4}$

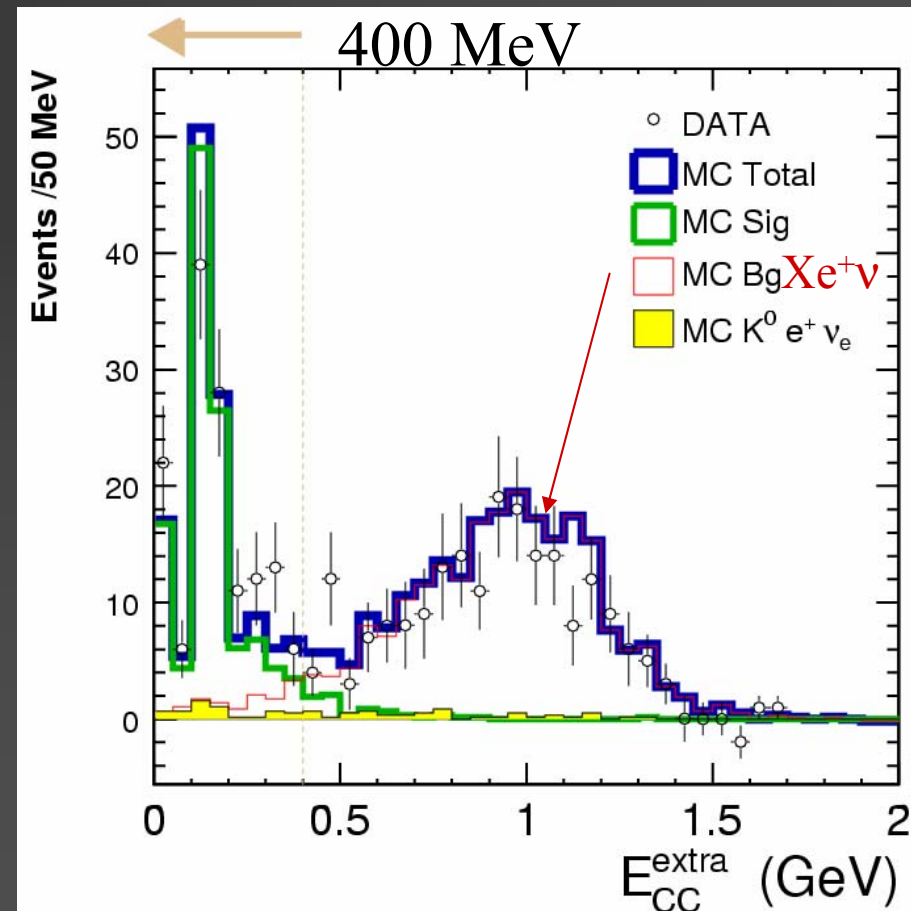


# $\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu)$ Systematic errors

Error Source	Size (%)
Track finding	0.7
Photon veto	1
Minimum ionization <input type="checkbox"/>	1
Number of tags	5
Total	5.2

# Measuring $D_S^+ \rightarrow \tau^+ \nu$ , $\tau^+ \rightarrow e^+ \nu \nu$

- Use  $195 \text{ pb}^{-1}$  for this preliminary analysis
- $B(D_S^+ \rightarrow \tau^+ \nu) \cdot B(\tau^+ \rightarrow e^+ \nu \nu) \sim 1.3\%$  is “large” compared with expected  $B(D_S^+ \rightarrow X e^+ \nu) \sim 8\%$
- Technique is to find events with an  $e^+$  opposite  $D_S^-$  tags & no other tracks, with  $\Sigma$  calorimeter energy  $< 400 \text{ MeV}$
- No need to find  $\gamma$  from  $D_S^*$
- $B(D_S^+ \rightarrow \tau^+ \nu)$   
 $= (6.29 \pm 0.78 \pm 0.52)\%$
- $f_{D_S} = 278 \pm 17 \pm 12 \text{ MeV}$



# $f_{D_s}$ & $f_{D_s} / f_{D^+}$

- **Weighted Average:**  $f_{D_s} = 275 \pm 10 \pm 5$  MeV, the systematic error is mostly uncorrelated between the measurements

- Previously CLEO-c measured

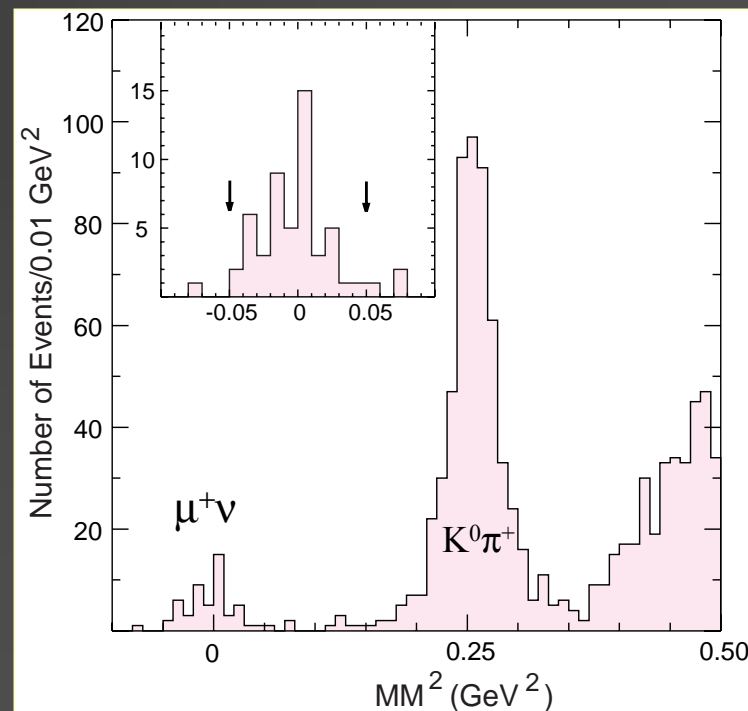
$$f_{D^+} = (222.6 \pm 16.7^{+2.3}_{-3.4}) \text{ MeV}^\dagger$$

M. Artuso et al., Phys. Rev. Lett. 95 (2005) 251801

- $\dagger$  Thus  $f_{D_s} / f_{D^+} = 1.24 \pm 0.10 \pm 0.03$

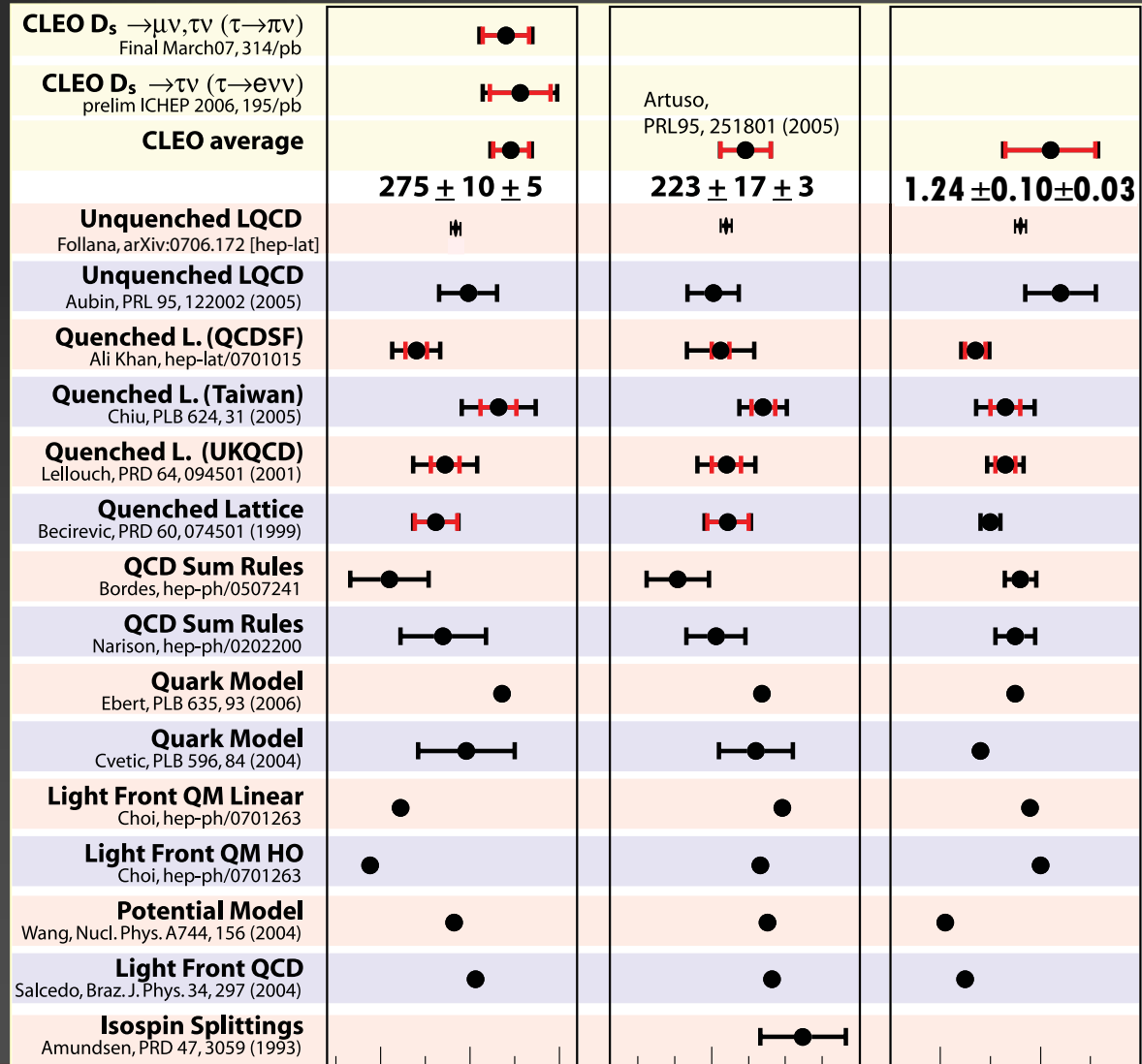
- $\Gamma(D_s^+ \rightarrow \tau^+ \nu) / \Gamma(D_s^+ \rightarrow \mu^+ \nu) = 11.5 \pm 2.0$ , SM = 9.72, consistent with lepton universality

$D^+ \rightarrow \mu^+ \nu$



# Comparisons with Theory

- We are consistent with most models, more precision needed
- Using Lattice ratio find  $|V_{cd}/V_{cs}| = 0.2166 \pm 0.020$  (exp)  $\pm 0.0017$  (theory)



200 250 300

200 300

1 1.2 1.4

# Comparison with Previous Experiments

TABLE VI: These results compared with previous measurements. Results have been updated for new values of the  $D_s$  lifetime. ALEPH uses both measurements to derive a value for the decay constant.

Exp.	Mode	$\mathcal{B}$	$\mathcal{B}_{\phi\pi}$ (%)	$f_{D_s^+}$ (MeV)
CLEO-c	combined	-		$275 \pm 10 \pm 5$
CLEO	$\mu^+\nu$	$(6.2 \pm 0.8 \pm 1.3 \pm 1.6)10^{-3}$	$3.6 \pm 0.9$	$273 \pm 19 \pm 27 \pm 33$
BEATRICE	$\mu^+\nu$	$(8.3 \pm 2.3 \pm 0.6 \pm 2.1)10^{-3}$	$3.6 \pm 0.9$	$315 \pm 43 \pm 12 \pm 39$
ALEPH	$\mu^+\nu$	$(6.8 \pm 1.1 \pm 1.8)10^{-3}$	$3.6 \pm 0.9$	$285 \pm 19 \pm 40$
ALEPH	$\tau^+\nu$	$(5.8 \pm 0.8 \pm 1.8)10^{-2}$		
OPAL	$\tau^+\nu$	$(7.0 \pm 2.1 \pm 2.0)10^{-2}$	?	$286 \pm 44 \pm 41$
L3	$\tau^+\nu$	$(7.4 \pm 2.8 \pm 1.6 \pm 1.8)10^{-2}$	?	$302 \pm 57 \pm 32 \pm 37$
BaBar	$\mu^+\nu$	$(6.5 \pm 0.8 \pm 0.3 \pm 0.9)10^{-3}$	$4.8 \pm 0.5 \pm 0.4$	$279 \pm 17 \pm 6 \pm 19$

- CLEO-c is most precise result to date for both  $f_{D_s}$  &  $f_{D^+}$



*The End*

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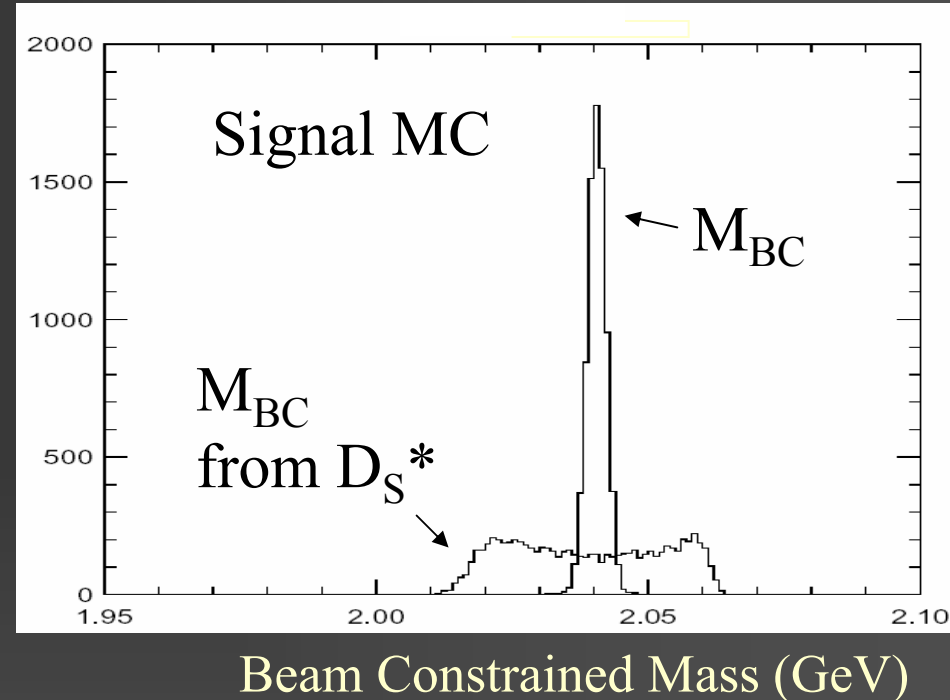
# CLEO $D_S^+$ Results at 4170 MeV

- Since  $e^+e^- \rightarrow D_S^* D_S$ , the  $D_S$  from the  $D_S^*$  will be smeared in beam-constrained mass.

- $$M_{BC}^2 = E_{\text{beam}}^2 - \sum_i \vec{p}_i^2$$

- $\therefore$  cut on  $M_{BC}$  & plot invariant mass (equivalent to a p cut)

- We use  $314 \text{ pb}^{-1}$  of data



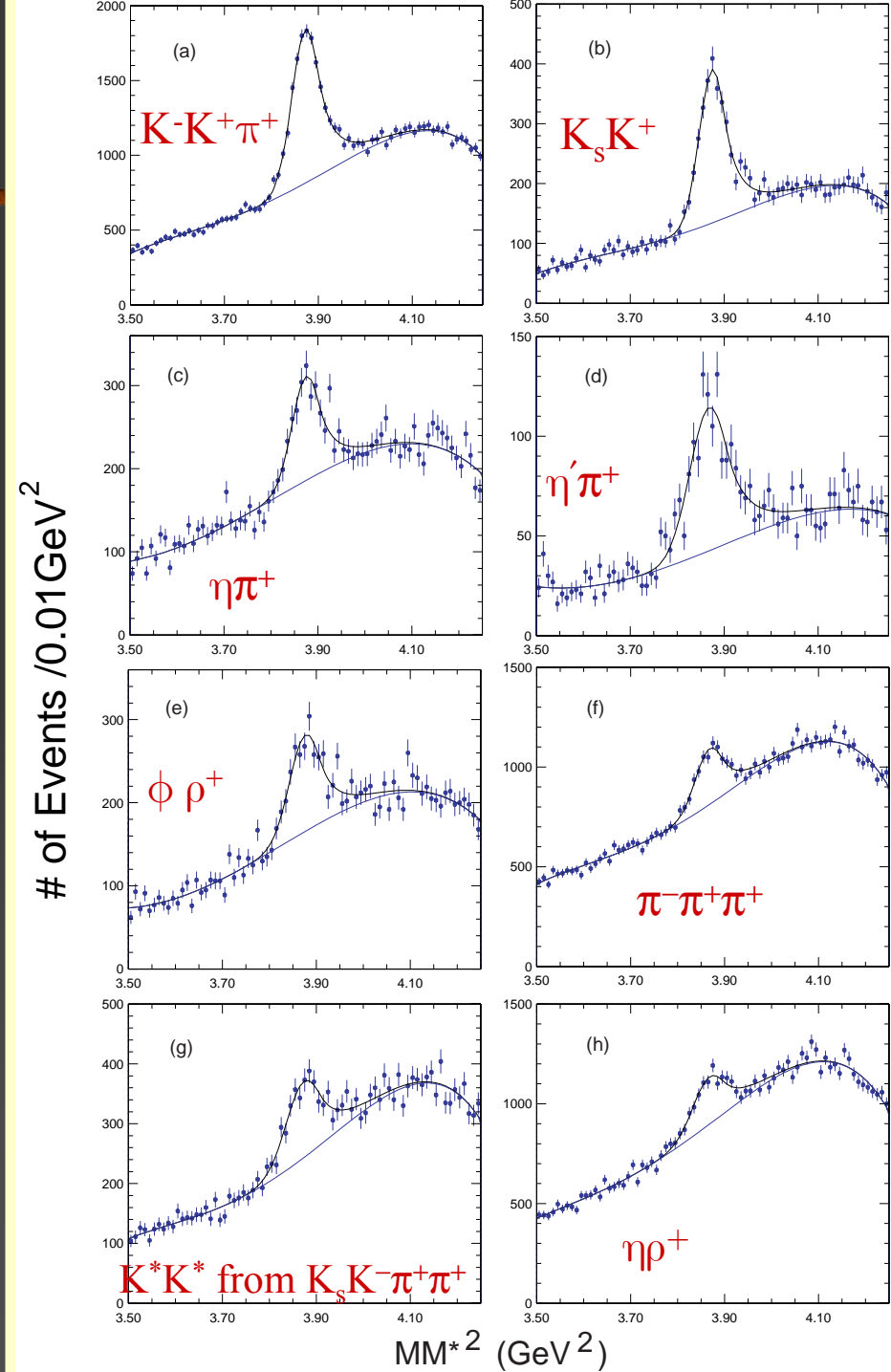
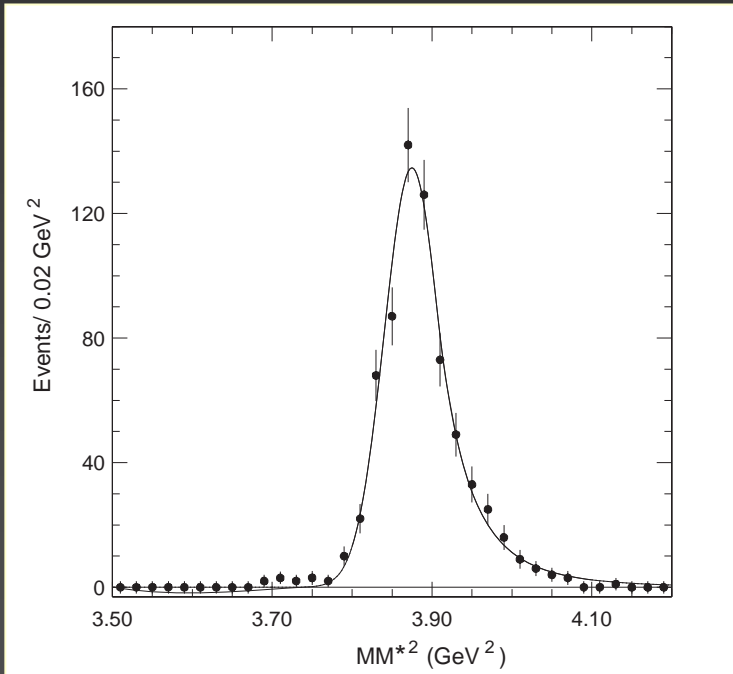
# #Tags: $D_s + \gamma$

- Compute  $MM^{*2}$

$$MM^{*2} = (E_{CM} - E_{D_s} - E_{\gamma})^2 - (-\vec{p}_{D_s} - \vec{p}_{\gamma})^2$$

in each individual mode

- Use  $D_s^* D_s$  sample to measure shape of tail





# Sum of $D_S^+ \rightarrow \mu^+ \nu + \tau^+ \nu$ , $\tau \rightarrow \pi^+ \nu$

- As we will see, there is very little background present in any sub-sample for  $MM^2 < 0.2 \text{ GeV}^2$

