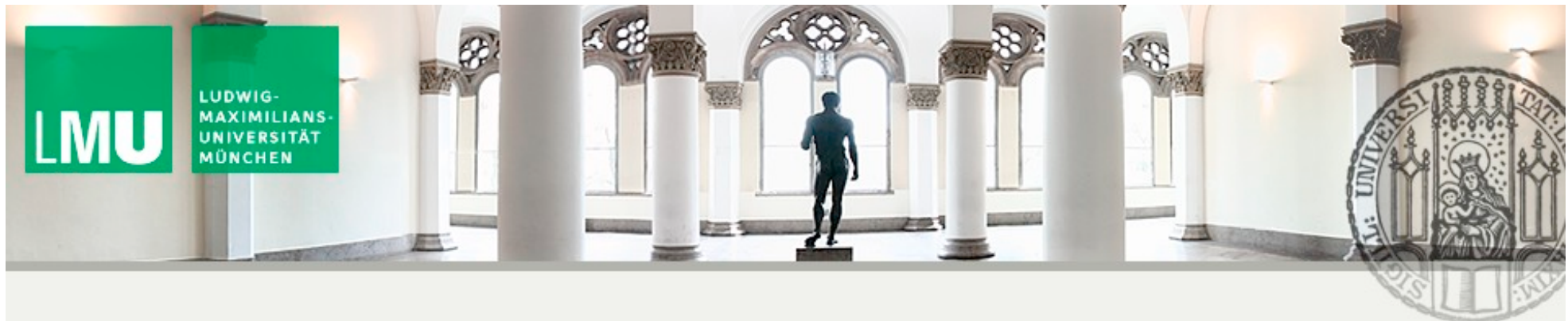


# The Landscape of String theory

Dieter Lüst, LMU (ASC) and MPI München



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in collaboration with

Riccardo Appreda, Ralph Blumenhagen, Gabriel L.

Cardoso, Mirjam Cvetič, Johanna Erdmenger,

Florian Gmeiner, Viviane Grass, Michael Haack,

Daniel Krefl, Gabriele Honecker,

Jan Perz, Susanne Reffert, Robert Richter, Christoph Sieg,

Maren Stein, Stephan Stieberger Antoine van Proeyen,

Timo Weigand and Marco Zagermann

# I) Introduction



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String Theory

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**Geometry:** Calabi-Yau spaces, mirror symmetry, generalized spaces, D-branes (submanifolds), K-theory, Gromov/Witten invariants, ...

**String Theory**

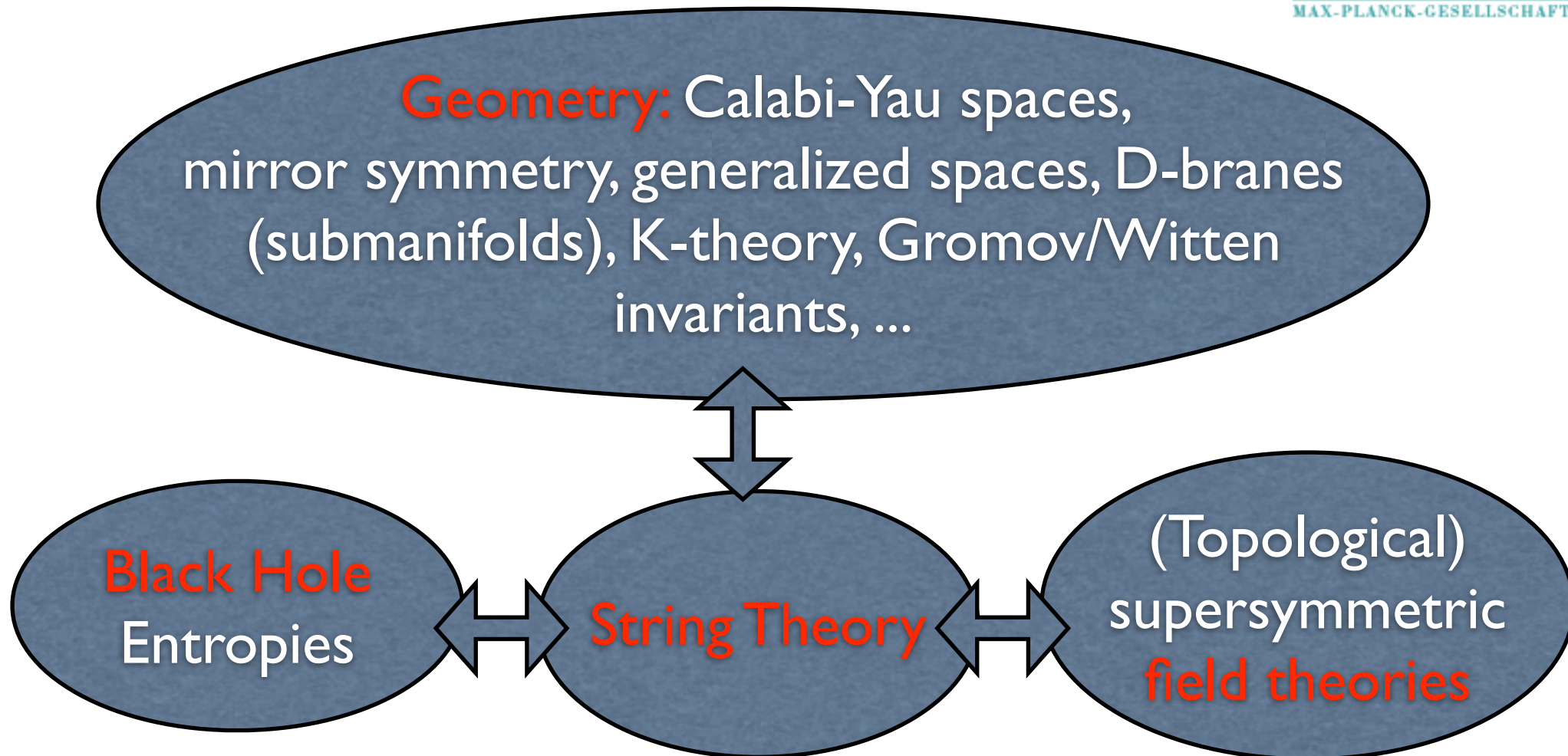
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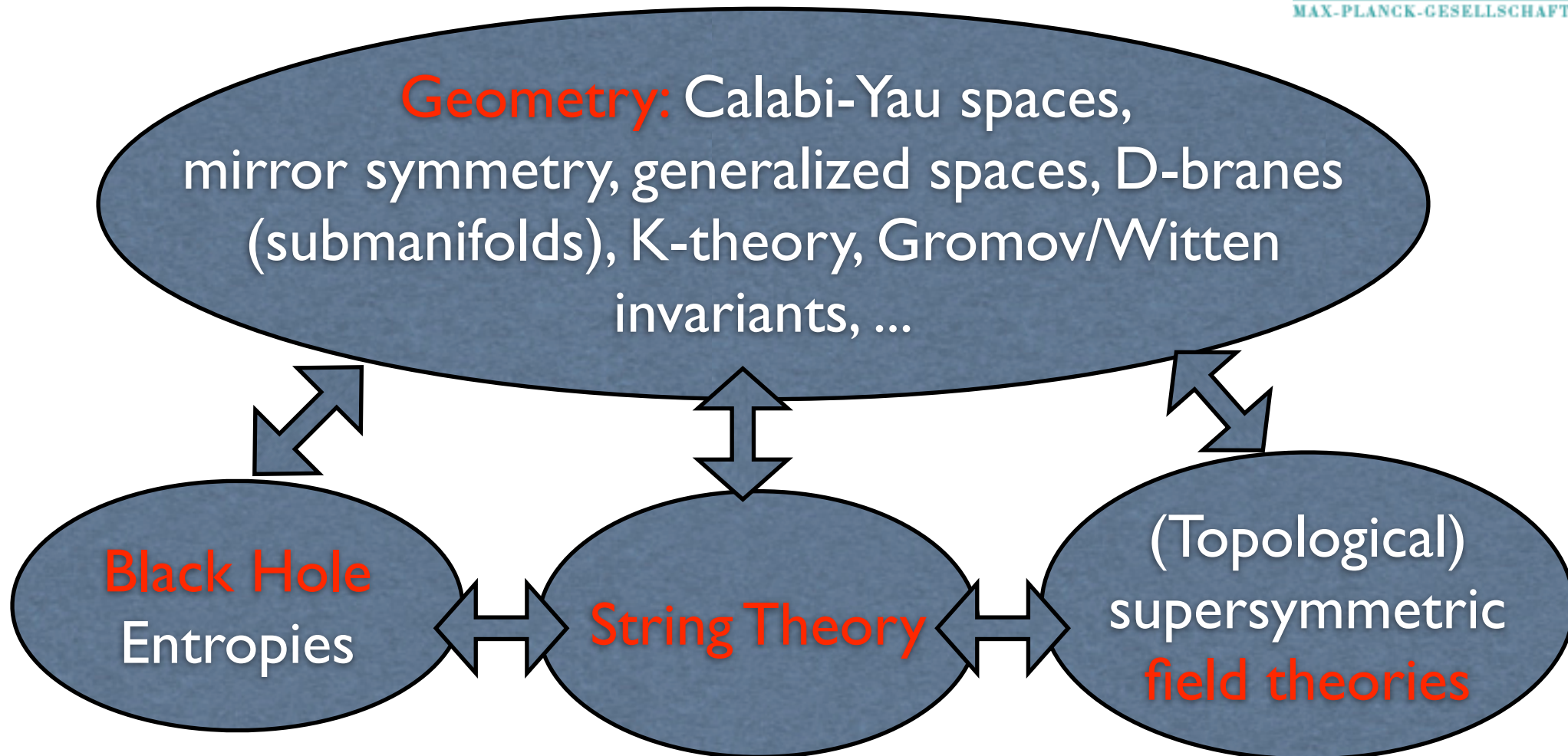


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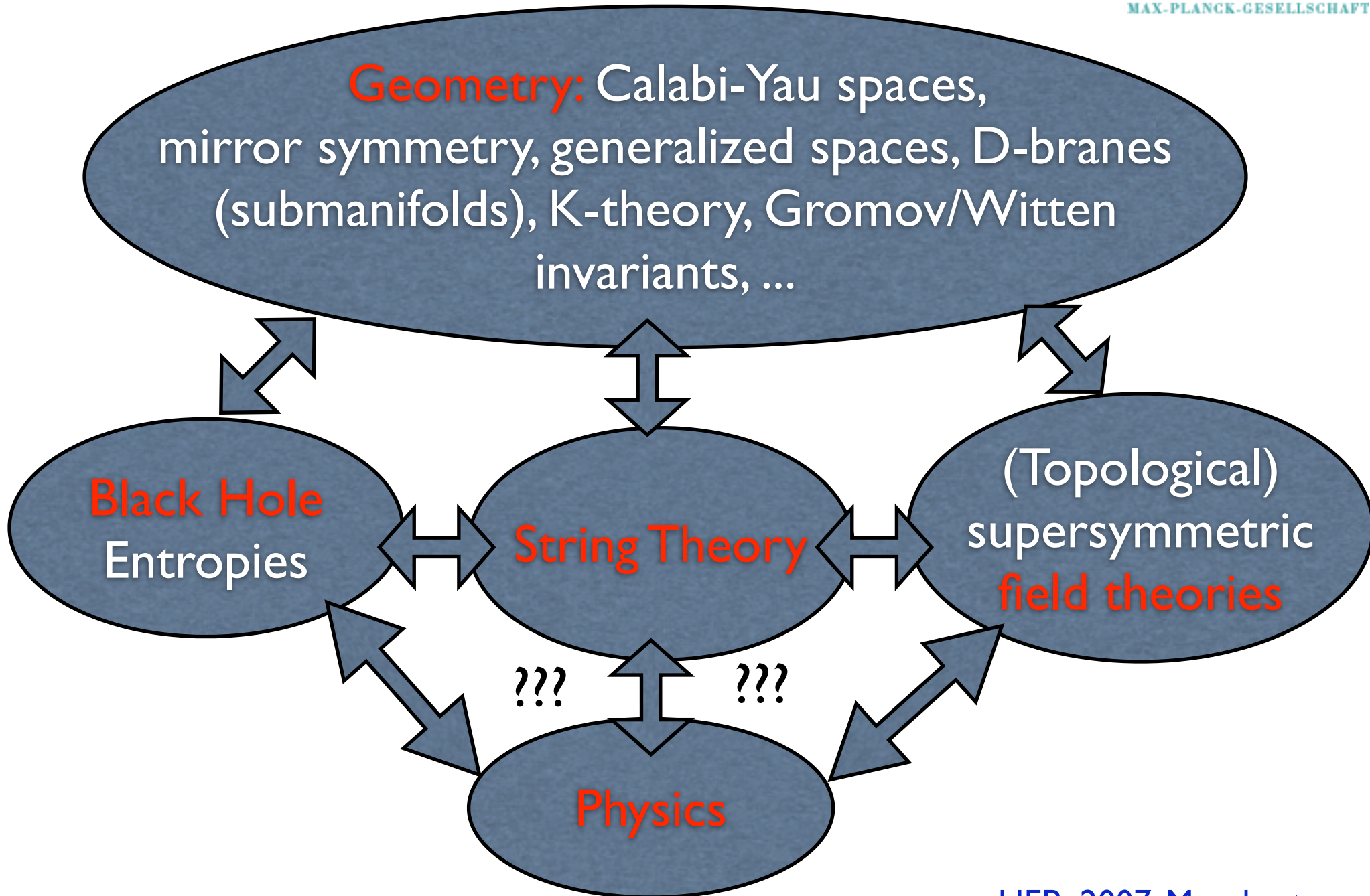
(Topological)  
supersymmetric  
**field theories**







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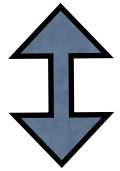
## ☺ Quantum Gravity



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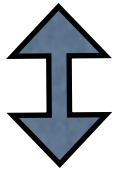
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Gauge (4D) - Gravity (5D) Correspondence

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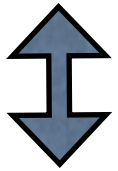


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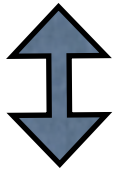
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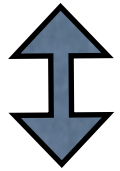
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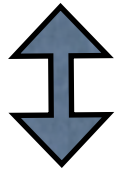
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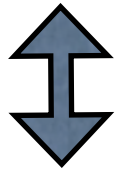


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- ☞ New testable experimental signatures (extra dimensions, black holes)??

Count the number of consistent string solutions



Vast landscape with  $N_{sol} = 10^{500-1500}$  discrete vacua!

(Lerche, Lüst, Schellekens (1986), Douglas (2003))



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Two strategies to find something interesting:

- Explore all mathematically consistent possibilities:  
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(perhaps some anthropic point of view is necessary?)
- Do not look randomly - look for green (promising) spots  
in the landscape  $\Rightarrow$  model building, **bottom up approach.**





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  - ☞ Tests
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(Review: D. Lüst, arXiv:0707:2305)

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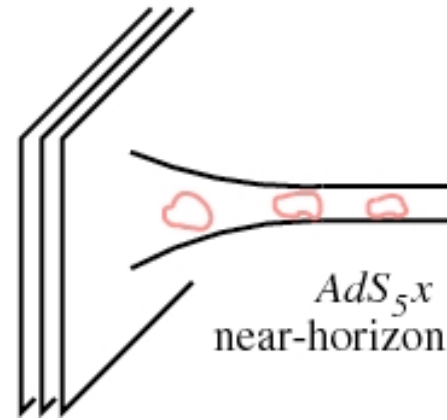
D3 branes in 10d

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open strings



duality



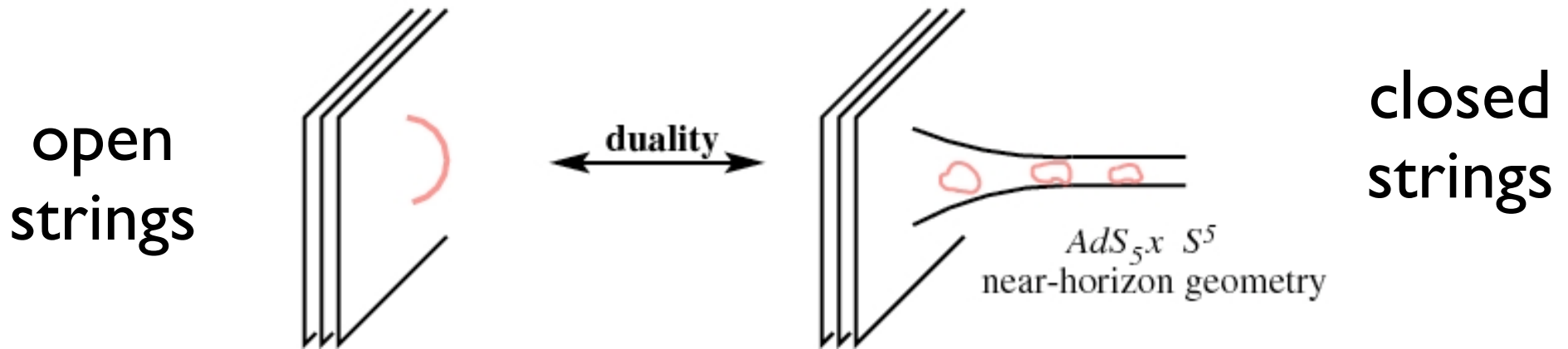
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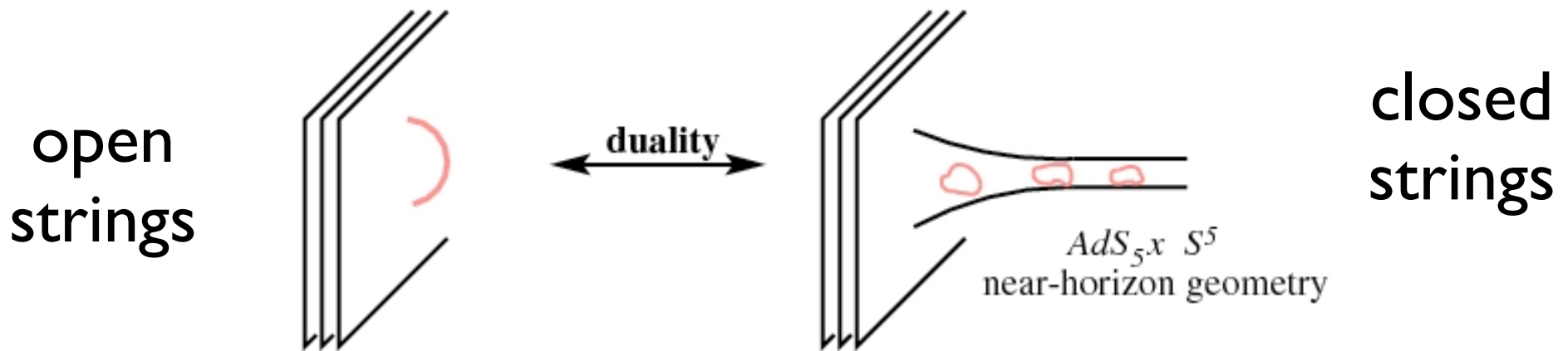


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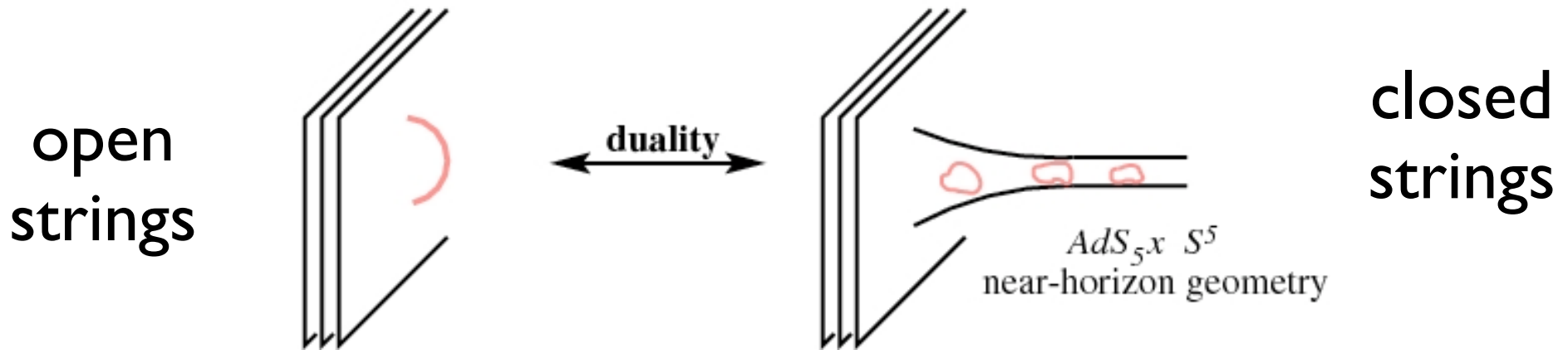
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The correspondence is so far tested for:  $N \rightarrow \infty, \lambda \rightarrow \infty$ .  
HEP 2007, Manchester

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(High temperature QCD)

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Consider the anomalous dimension of twist-2 operators:

$$\mathcal{O} = \text{Tr}[(\Phi^k (D\Phi)^l) + \dots], \quad \langle \mathcal{O}(x) \mathcal{O}(0) \rangle = C |x - y|^{-2\Delta}.$$

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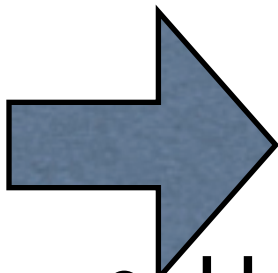
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MAX-PLANCK-GESellschaft



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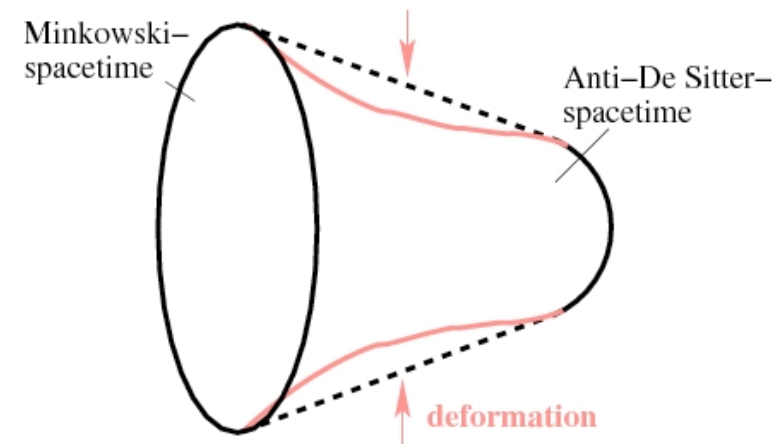
MAX-PLANCK-GESELLSCHAFT

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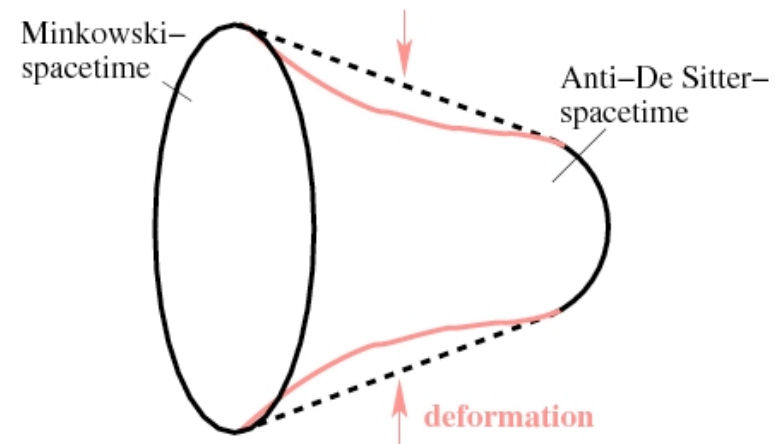
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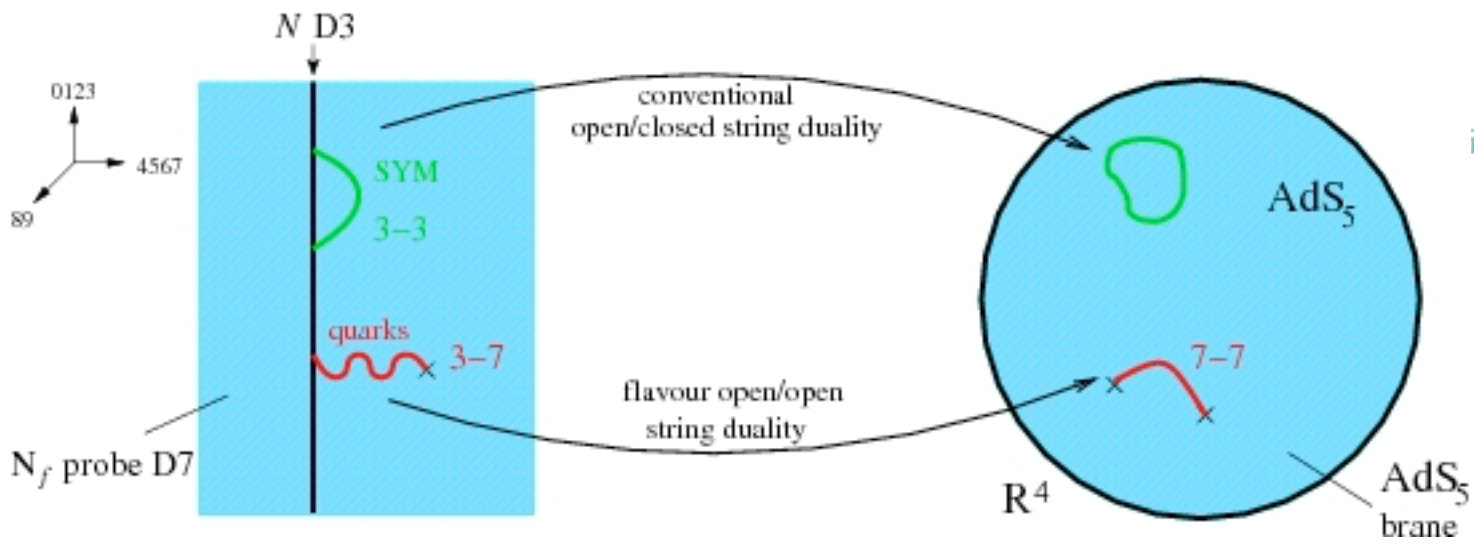
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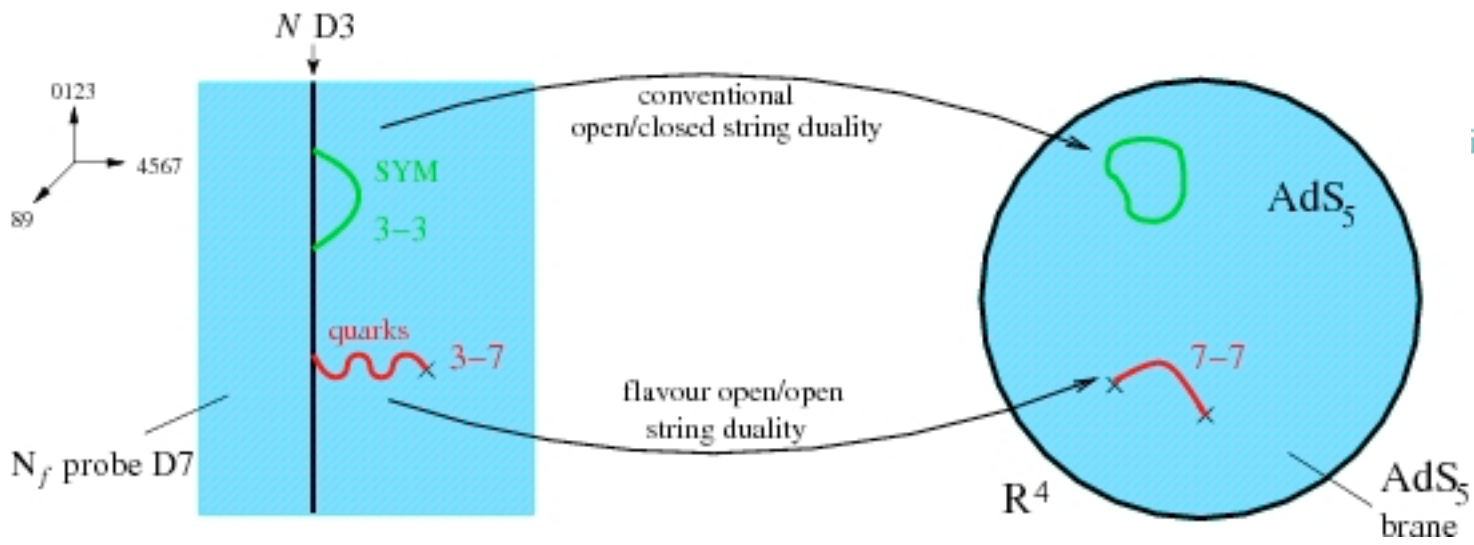
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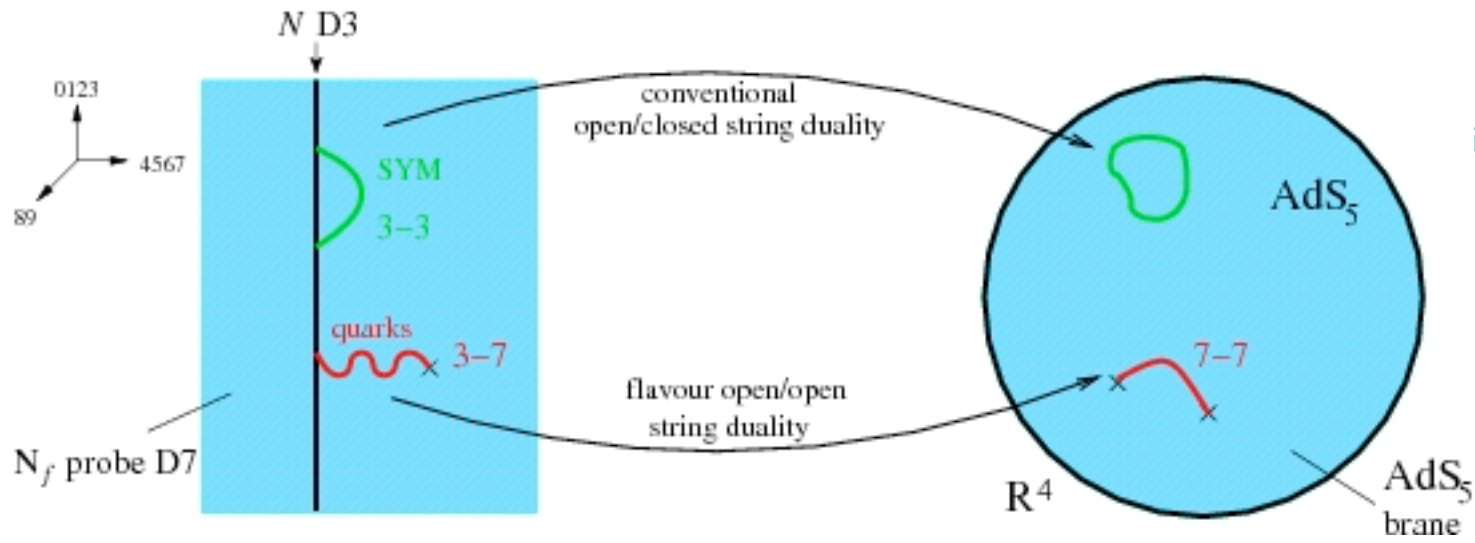
- Add quark flavor fields in fundamental repr. of  $SU(N)$ :

Include D7-branes: Quarks are open strings, stretched between D3- and D7-branes.





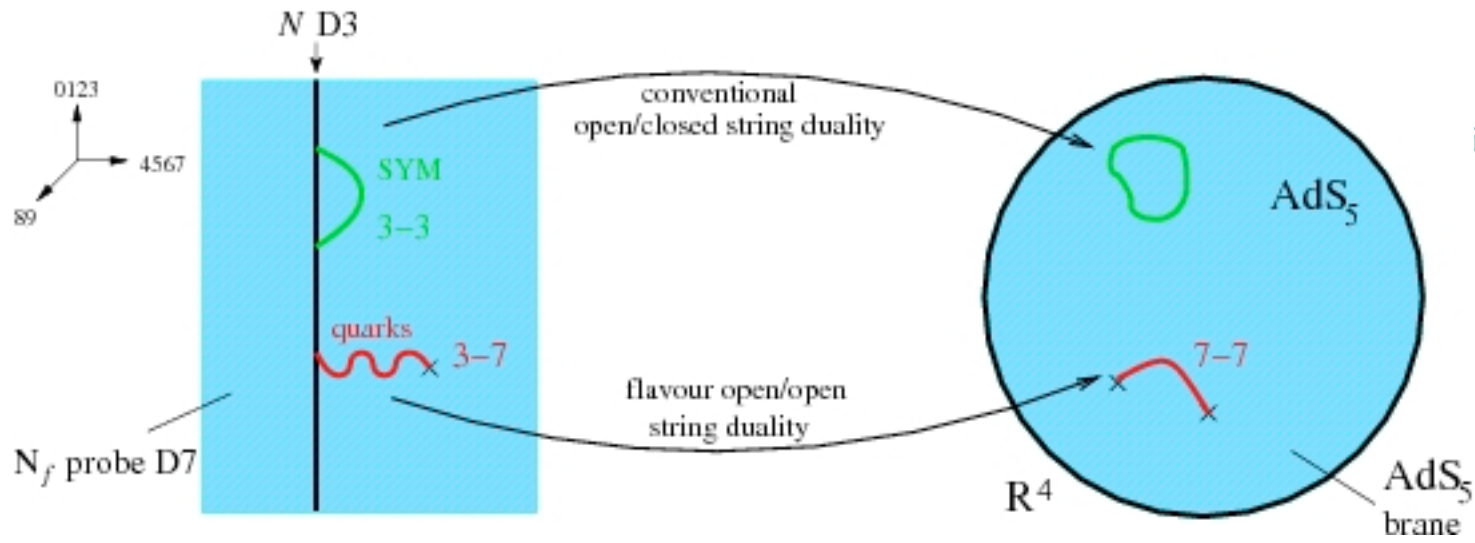
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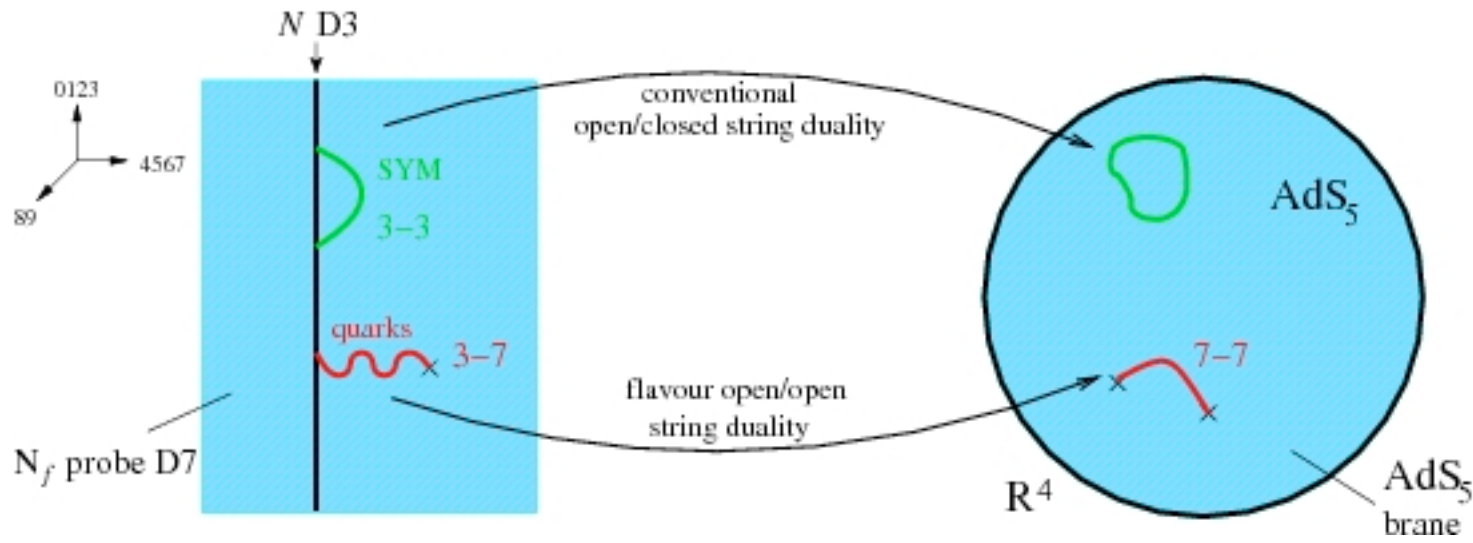




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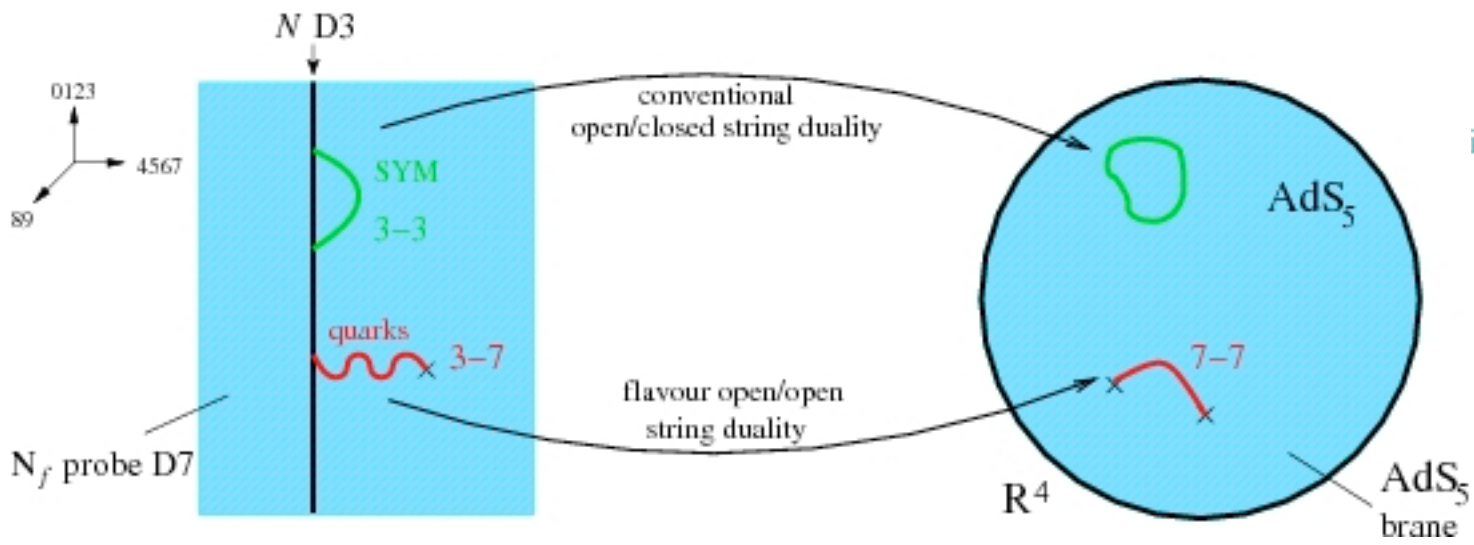
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- ☺ Alternative models: D4/D8-branes

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UNIVERSAL BEHAVIOR?

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(Policastro, Son, Starinets (2001))

UNIVERSAL BEHAVIOR?

More realistic models: Inclusion of quarks via D7-branes.

(Mateos, Myers, Thomson (2006))

HEP 2007, Manchester

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Heterotic string compactifications

- Type II orientifolds models

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- ☹ Moduli stabilization (bundle moduli!) with H-flux is difficult.

(Strominger (1985), Becker, Becker, Dasguta, Green (2003); Curio, Cardoso, Dall'Agata, Lüst, Krause (2003/04/05); Braun, He, Ovrut (2006))

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- Can be combined with background fluxes  $\Rightarrow$  **moduli stabilization (GKP) and dS-vacua (KKLT)**



(Review: Blumenhagen, Körs, Lüst, Stieberger, hep-th/0610327)





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- Closed string 6-dimensional background geometry:
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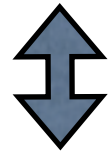
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- (diophantic equations with finite no. of solutions!)



Geometrical, large radius regime:

IIA: special lagrangian submanifolds: D6 on 3-cycles **at angles**



Mirror symmetry (SYZ)

IIB: points, (complex lines), divisors, (CY) **with gauge bundles:**

D3

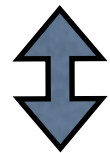
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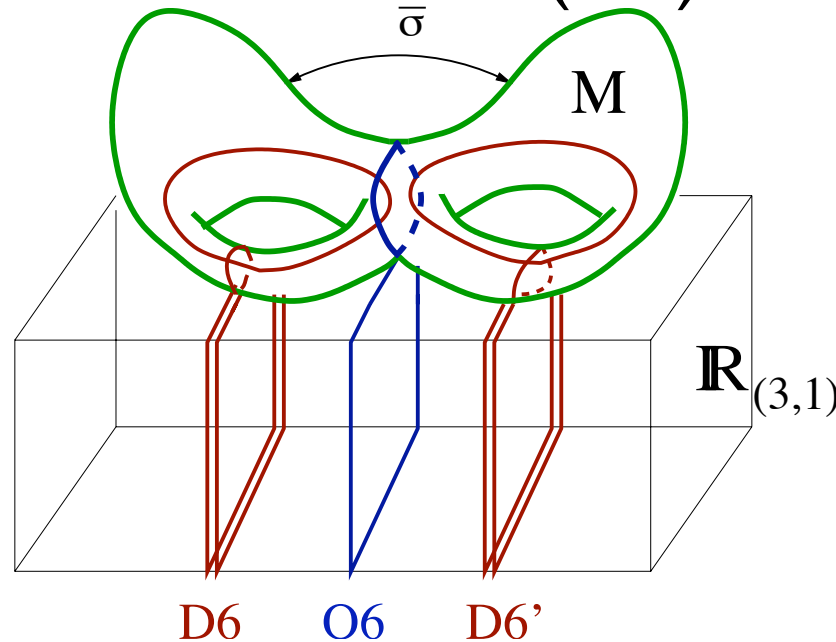
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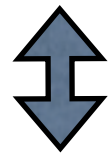
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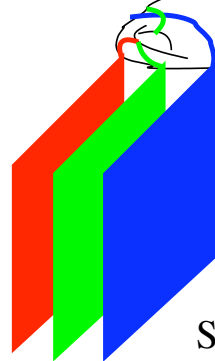
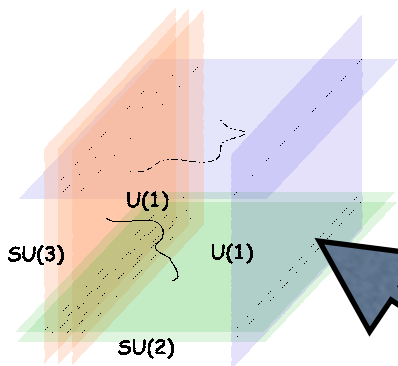
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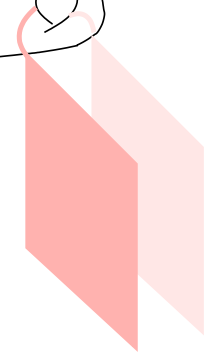
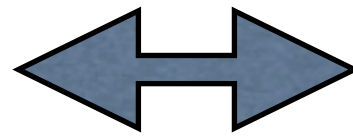
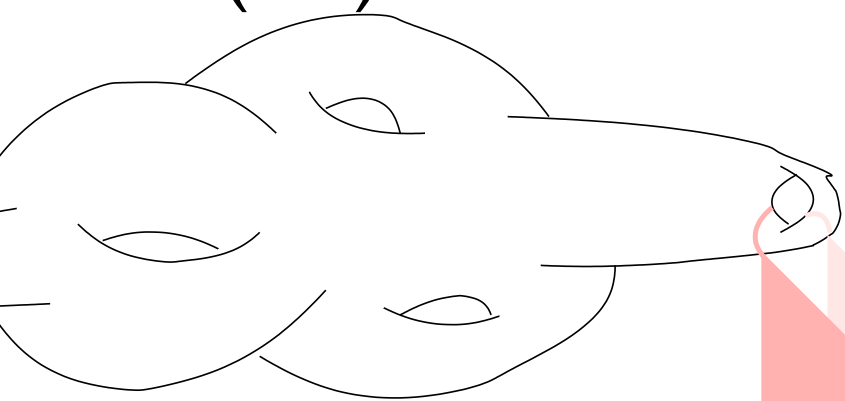
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SM



HS

Soft SUSY breaking



# How many orientifold models exist which come close to the (spectrum of the) MSSM?

(Blumenhagen, Gmeiner, Honecker, Lüst, Stein, Weigand, [hep-th/0411173](#), [hep-th/0510170](#), [hep-th/0703011](#);  
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(Finiteness of models was recently proven by D.T.)



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No symmetric representations	0.839
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**Only one in a billion models gives  
rise to a MSSM like vacuum!**





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- **Explicit D-brane constructions:**

there exist many models that come close to the MSSM.

Problem of exotic particles!

(Chen, Li, Mayes, Nanopoulos, hep-th/0703280; Chen, Li, Nanopoulos, hep-th/0604107; Blumenhagen, Plauschinn, hep-th/0604033; Bailin, Love, hep-th/0603172; Blumenhagen, Cvetic, Marchesano, Shiu, hep-th/0502095; Marchesano, Shiu, hep-th/0409132; Honecker, Ott, hep-th/0407181; .....

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Take into account non-perturbative instanton corrections to the effective action!





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- Can generate new matter couplings (Majorana masses, Yukawa couplings) → see in a moment.

# Two kinds of string instantons:





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- E2 is wrapping a 3-cycle different from the gauge group:  
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MAX-PLANCK-GESELLSCHAFT

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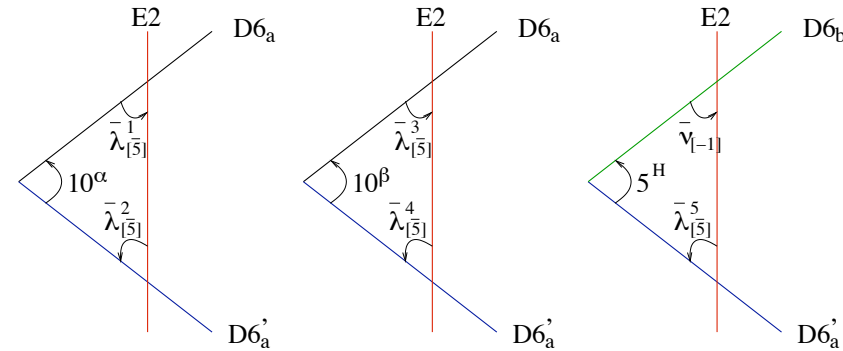
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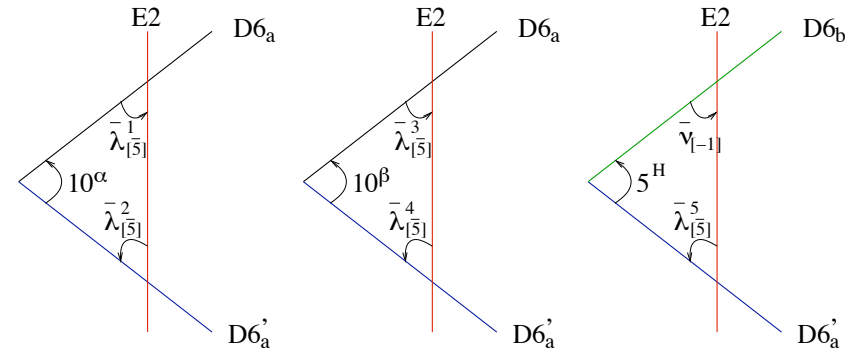


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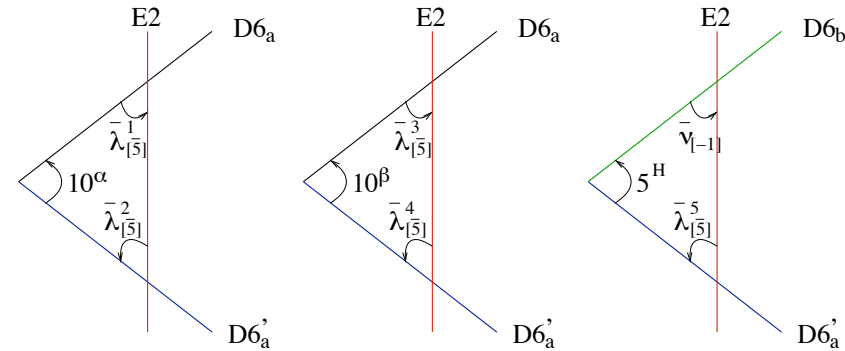
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E2-instantons also relevant for doublet-triplet splitting, Majorana masses, masses for exotic states, ...

(Ibanez, Uranga, hep-th/0609213; Cvetič, Richter, Weigand, hep-th/0703028; Ibanez, Schellekens, Uranga, arXiv:0704.1079; Antusch, Ibanez, Macri, arXiv:07062132;

Bianchi, Kiritsis, arXiv:0702015; Bianchi, Fucito, Morales, arXiv:0704.0784) HEP 2007, Manchester

# Prospects for the next years:







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(How good is the chain between fundamental theory and the data?)

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- Entropy of string vacua (**Entropic answer**): determine a probability function in moduli space,

$$|\psi_{\text{land}}(\phi)|^2 = e^{\mathcal{S}_{\text{land}}(\phi)}$$

and see if  $|\psi_{\text{land}}(\phi)|^2$  is peaked, i.e. has maxima with good phenomenological properties.

We know several (perturbative) vacua of string theory.



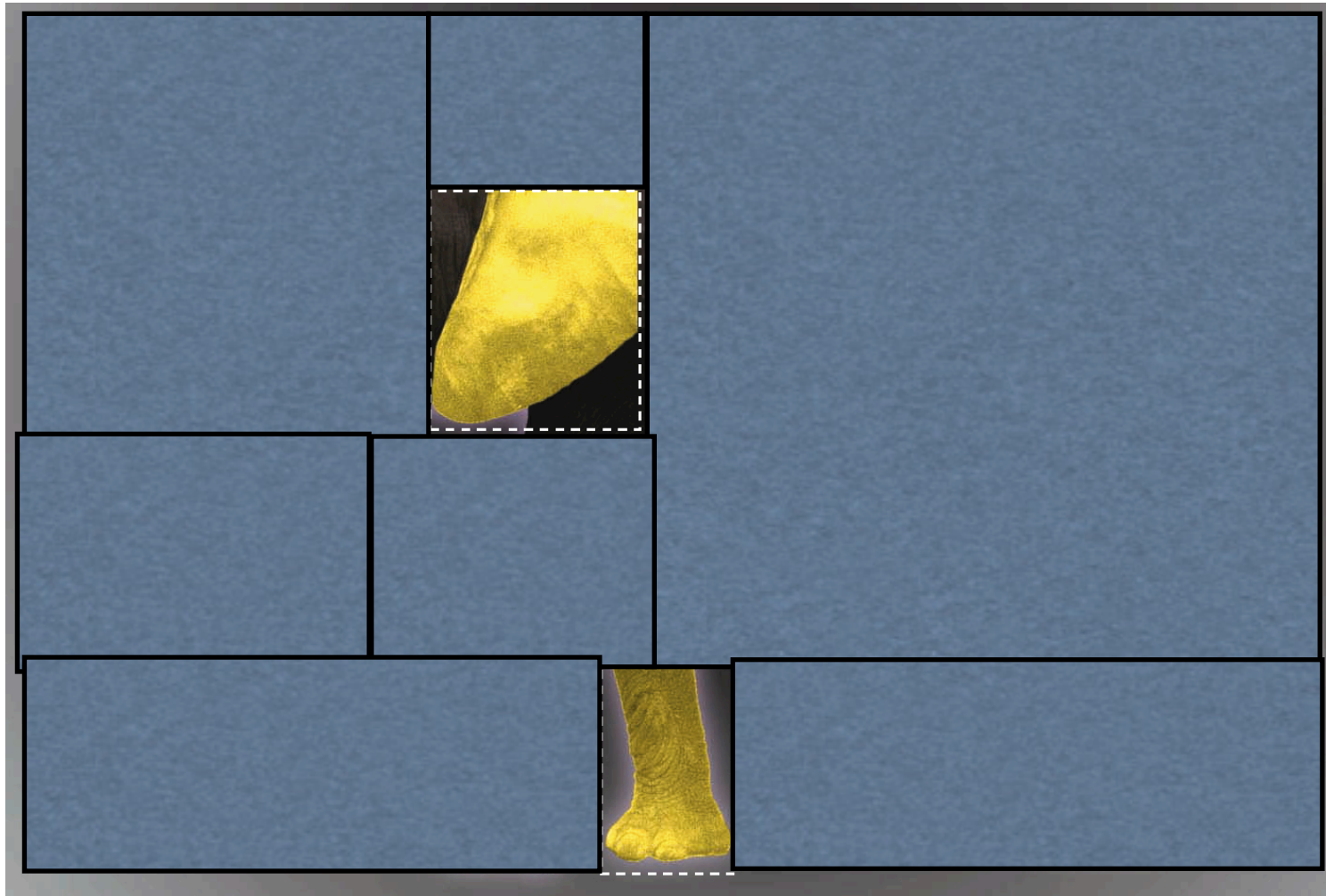
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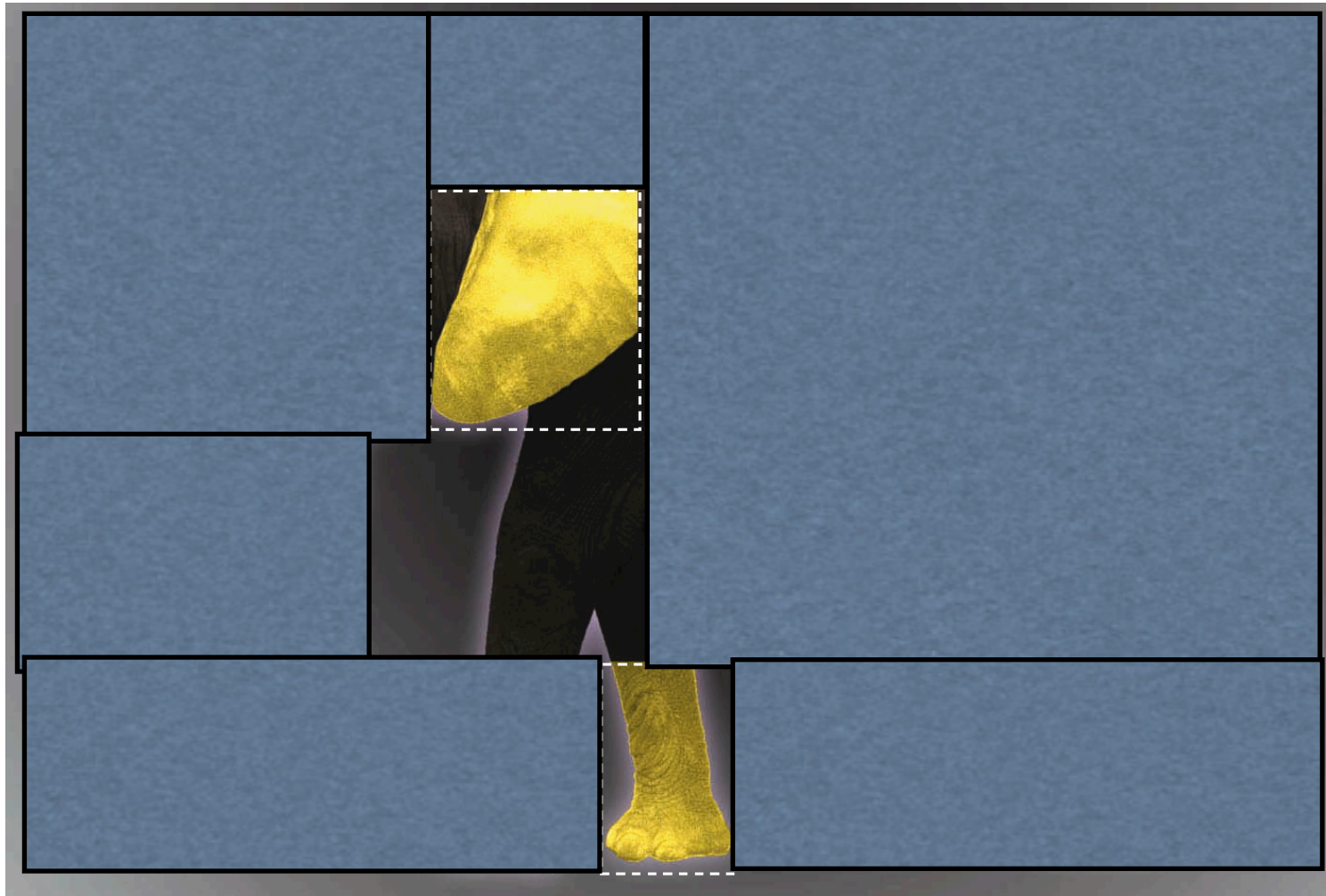
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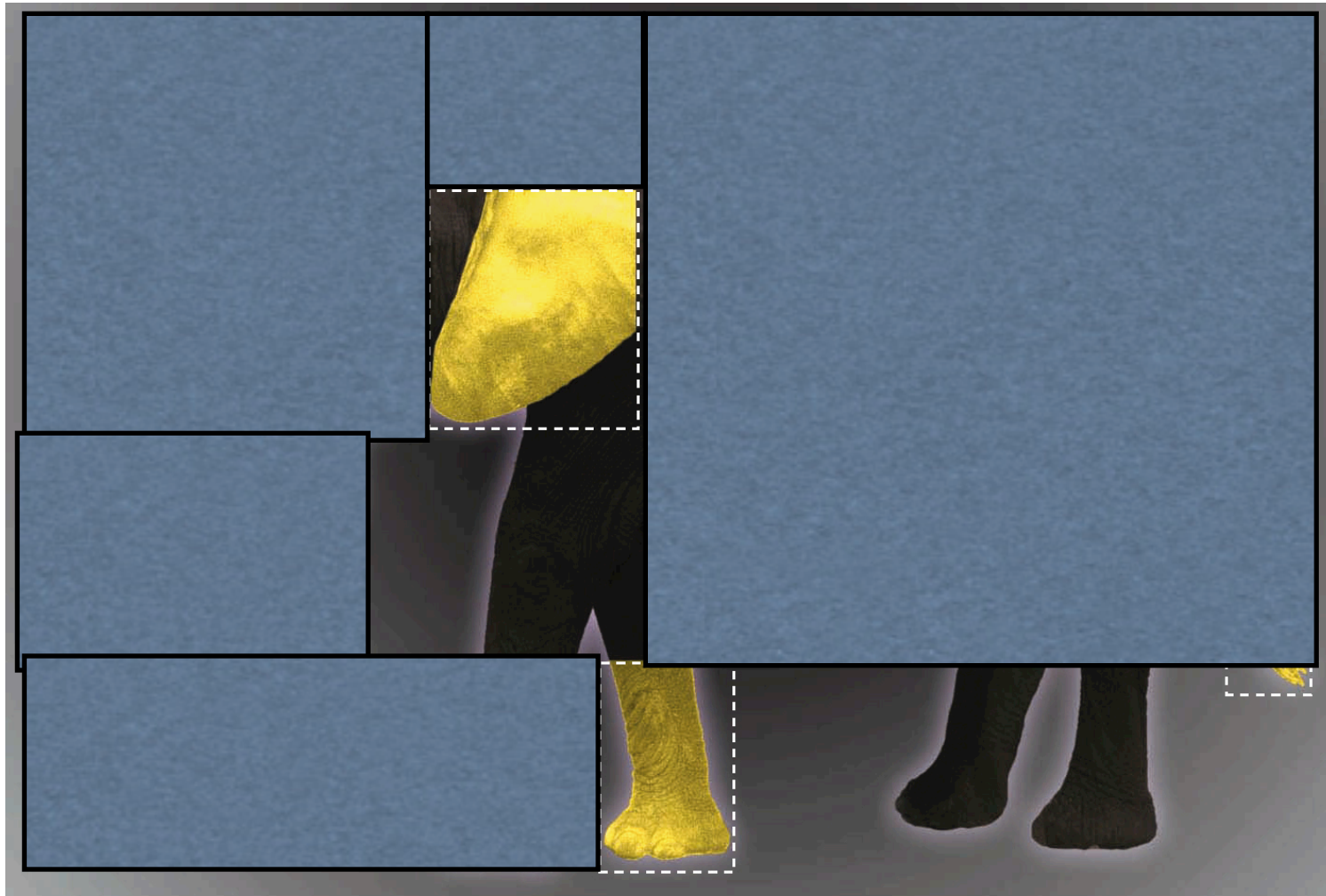
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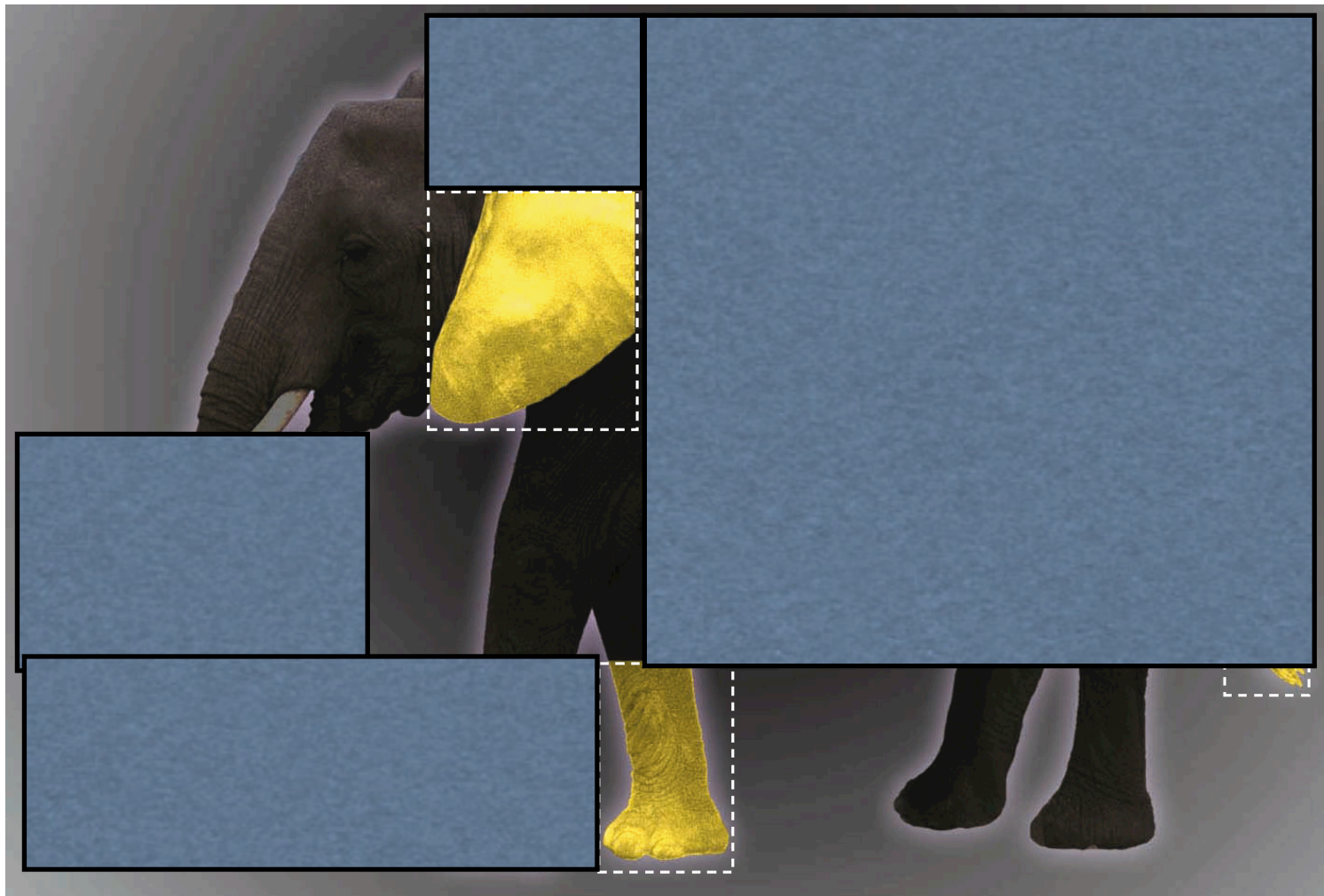
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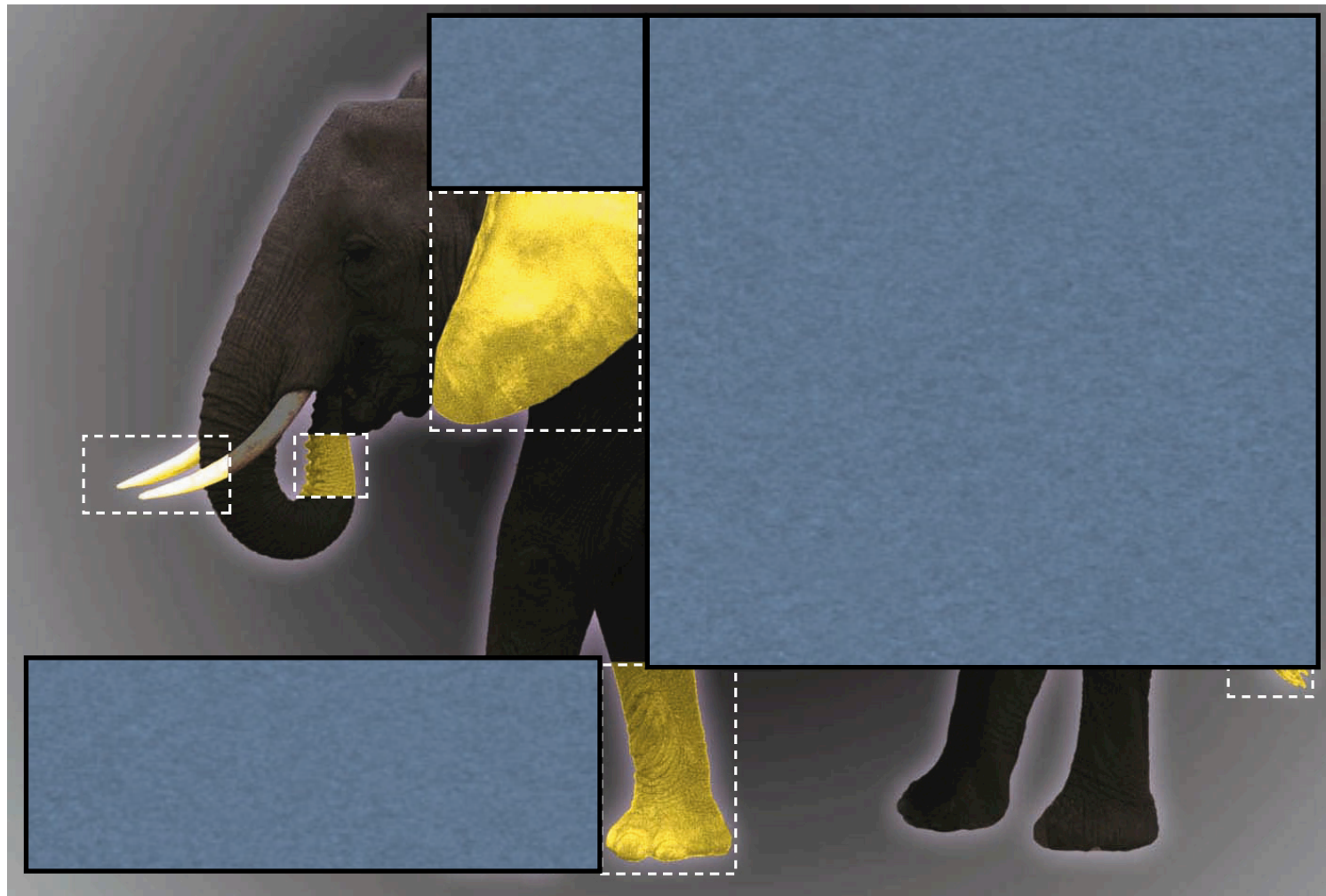
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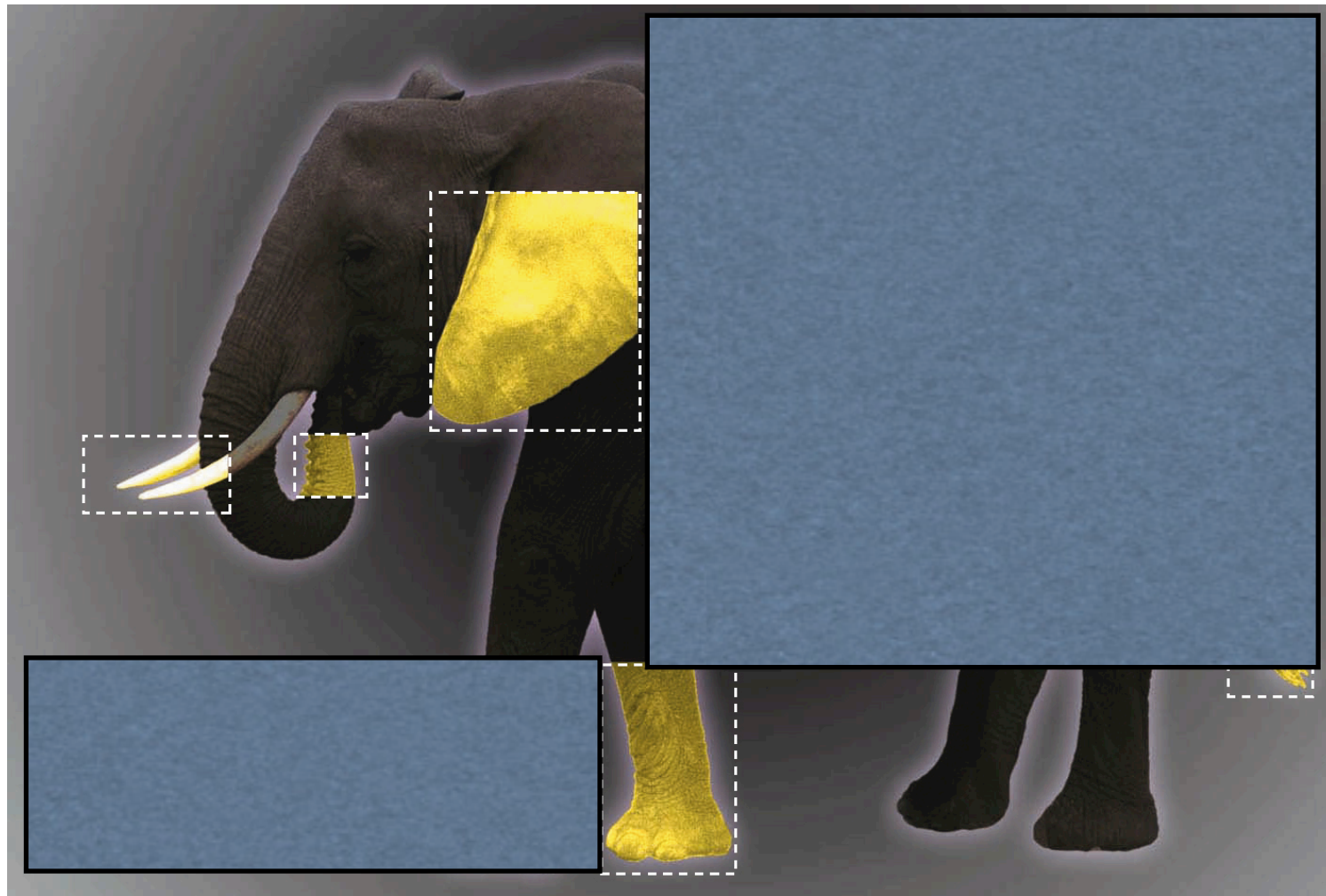
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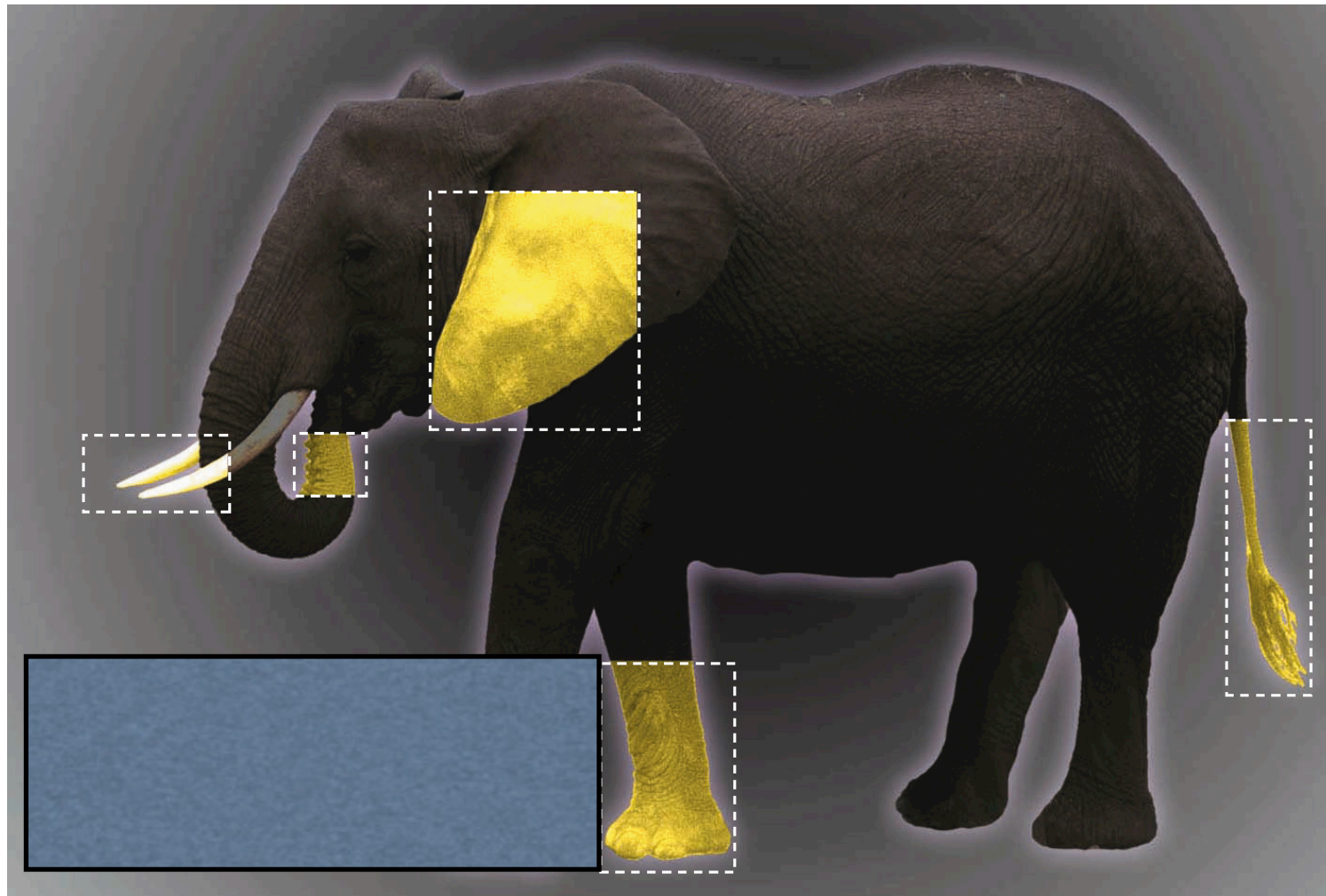
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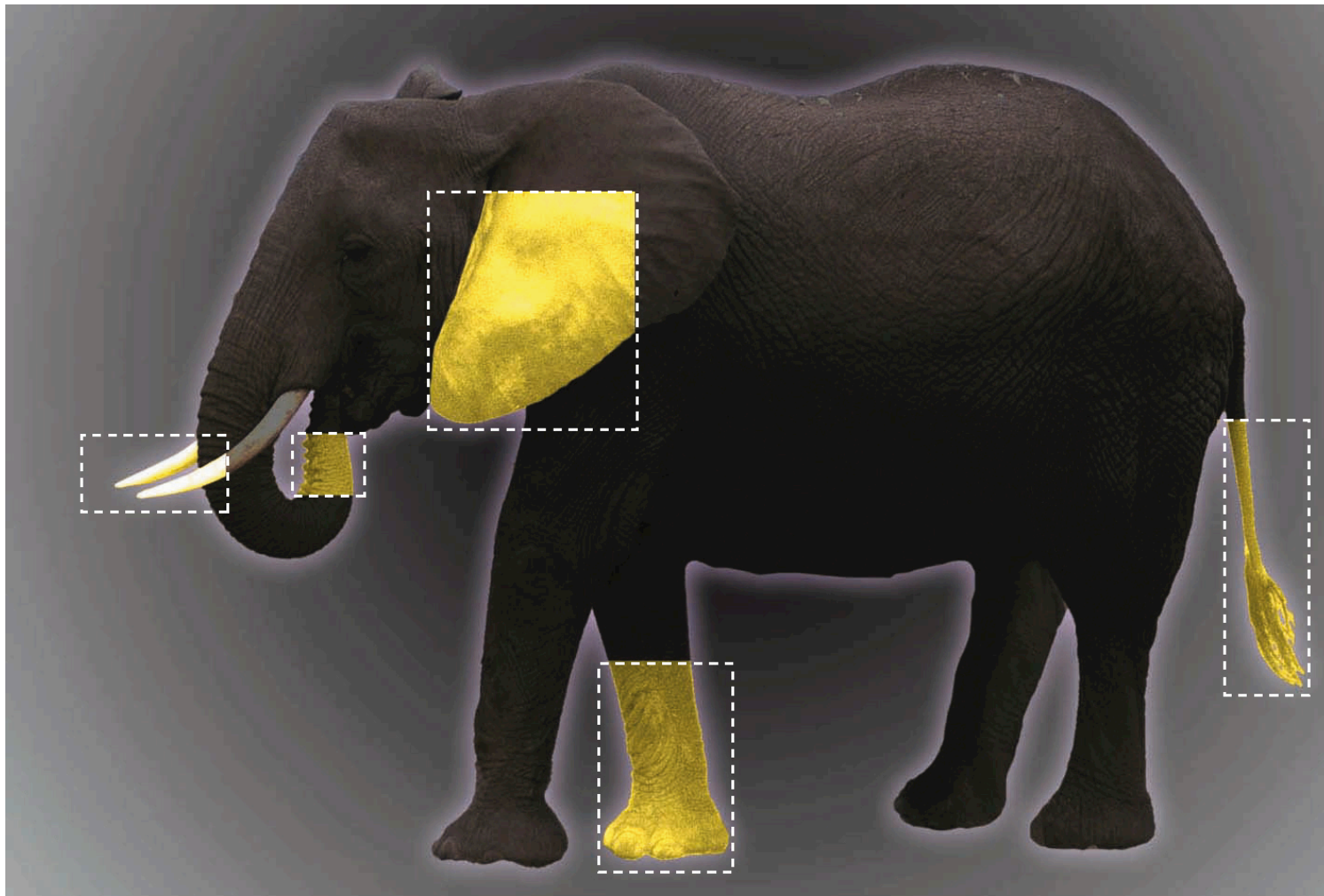
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