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# **Minimal Lepton Flavour Violation and Leptogenesis with low-energy CP Violation**

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# Outline

- Minimal Flavour Violation in the Lepton Sector (MLFV)
- Radiative Resonant Leptogenesis & Flavoured Leptogenesis
- Leptogenesis with 3 quasi-degenerate heavy Majorana Neutrinos:
  - with CP Violation at low and high Energies
  - with CP Violation exclusively at low Energies

# Minimal Lepton Flavour Violation (MLFV)

**Flavour symmetry**

$$SU(3)_L \times SU(3)_{e_R} \times O(3)_{\nu_R}$$

Lepton Yukawa couplings break  
the Flavour symmetry

Right-handed Majorana particles

included in MFV Hypothesis

$$L_{Mass} = -\frac{1}{2} \bar{\nu}_R^c M_R \nu_R + h.c.$$

Lepton Number Violation

Majorana mass matrix has a trivial structure

$$M_R = M_\nu \mathbf{1}_{3 \times 3}$$

Yukawas only flavour non-diagonal objects

- SM field content
- 3 degenerate heavy right-handed Majorana neutrinos

# Our Setup

Radiative corrections spoil the degeneracy of Majorana Masses:

$$M_R = M_R(\mu)$$

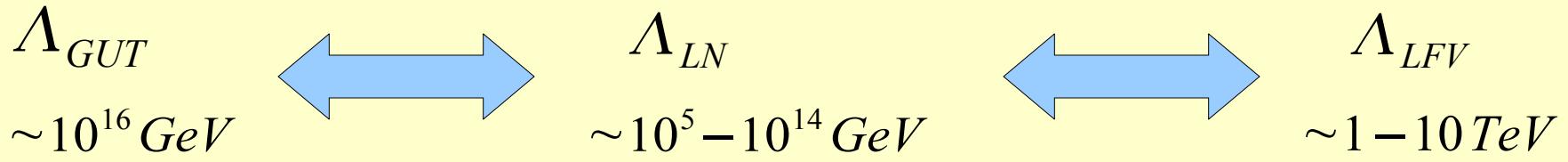
**MLFV Hypothesis + a choice of degeneracy scale (BBJUW)**

$$M_R(\Lambda_{GUT}) = M_\nu \mathbf{1}_{3 \times 3}$$

+ high-energy  
 CP violation  
**GUT scale**

**Lepton number  
 violating scale**  
**Majorana scale**

**Lepton flavour  
 violating scale**  
 $B(\mu \rightarrow e \gamma)$



**Radiative Resonant Leptogenesis**

Felipe, Joaquim, Nobre (2004)  
 Turzynski (2004)

Branco, Felipe, Joaquim, Nobre (2006)  
 Branco, Buras, Jäger, S.U., Weiler (2006)

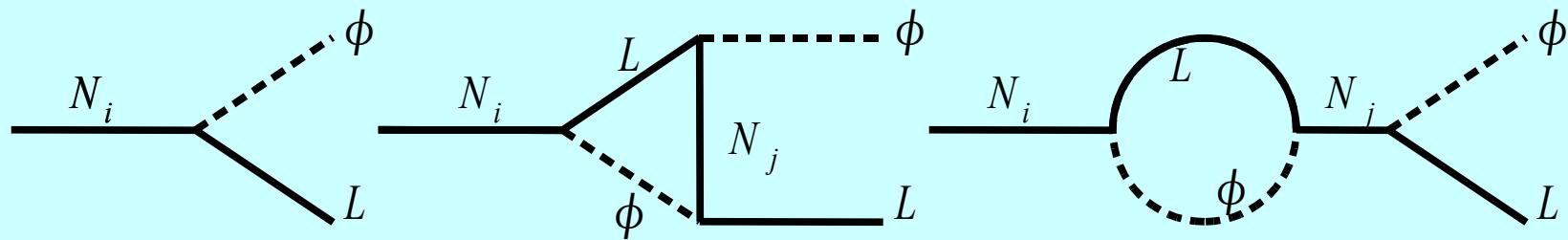
# Radiative Resonant Leptogenesis

## Thermal Leptogenesis

Fukugita, Yanagida (1986)

CP-violating out-of-equilibrium decays of right-handed heavy Majorana neutrinos:

→ Excess in lepton number → Lepton asymmetry → Baryon asymmetry



## Radiatively induced Mass splittings at Majorana scale

## Resonant Leptogenesis

Pilaftsis (1997)

Pilaftsis, Underwood (2003)

Anisimov, Broncano, Plümacher (2005)

Blanchet, Di Bari (2006)

Resonant enhancement of the CP asymmetries (due to self-energy contribution)  
Automatically fulfilled in our setup

# Flavour Effects and Leptogenesis

Barbieri, Creminelli, Strumia, Tetradiis (1999)

Pilaftsis, Underwood (2005)

Nardi, Nir, Roulet, Racker (2006)

Abada, Davidson, Josse-Michaux, Losada, Riotto (2006)

Blanchet, Di Bari (2006)

$$M_i < (10^9 - 10^{12}) \text{ GeV}$$

...

$\mu$  and  $\tau$  charged lepton Yukawa interactions much faster than expansion  $H$  below some temperature.



$\mu$  and  $\tau$  Yukawa couplings in equilibrium



Solution of flavour-specific Boltzmann equations required

$M_i < 10^{10} \text{ GeV}$  Flavour-specific treatment

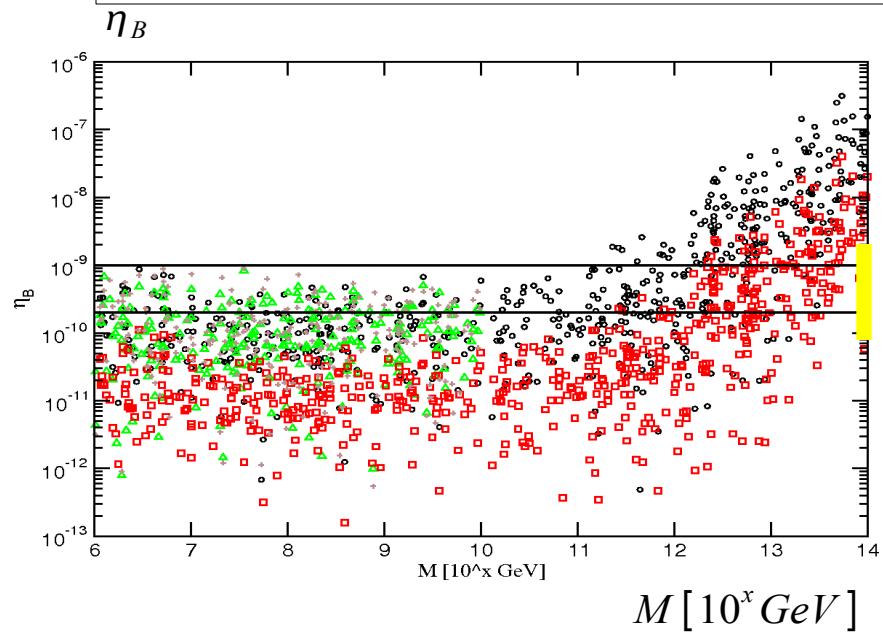
(BBJUW )  
 $M_i > 10^{10} \text{ GeV}$  Single flavour

$$M_\nu \approx 10^{10} \text{ GeV}$$

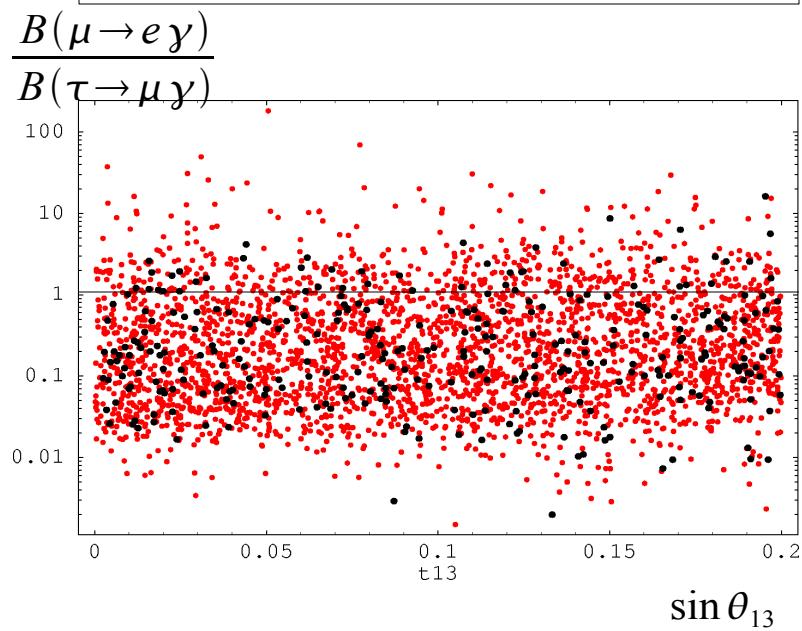
# Leptogenesis with low- and high-energy CP Violation for 3 quasi-degenerate heavy Majorana Neutrinos

Branco, Buras, Jäger, S.U., Weiler (2006)

## Baryon Asymmetry of the Universe



## Ratios of LFV Decays



Successful Leptogenesis  
independent from Majorana scale

Flavour effects enhance the BAU

Leptogenesis constraint does  
not significantly reduce range  
of ratio

No testable relation

# Leptogenesis with low-Energy CP Violation

Nardi, Nir, Roulet, Racker (2006)

Branco, Felipe, Joaquim (2006)

Pascoli, Petcov, Riotto (2006)

Branco, Buras, Jäger, S.U., Weiler (2006)

S.U. (2006)

(hierarchical)

(hierarchical and 2 quasi-degenerate)

(3 quasi-degenerate)

$$\varepsilon_i^l = \frac{1}{(Y_\nu Y_\nu^+)_ii} \sum_j \Im((Y_\nu Y_\nu^+)_ij \cdot (Y_\nu)_{il} (Y_\nu^+)_lj) \cdot g(M_i^2, M_j^2, \Gamma_j^2)$$

un-summed term relevant in flavour specific region

$$Y_\nu = \frac{i}{\nu} \sqrt{M_\nu} R \sqrt{m_\nu} U_{PMNS}^+$$

Casas, Ibarra (2001)

$R$  encodes high-energy CP violation  
(3 physically relevant complex parameters)

$$R(\Lambda_{GUT}) = \mathbf{1}_{3 \times 3}$$

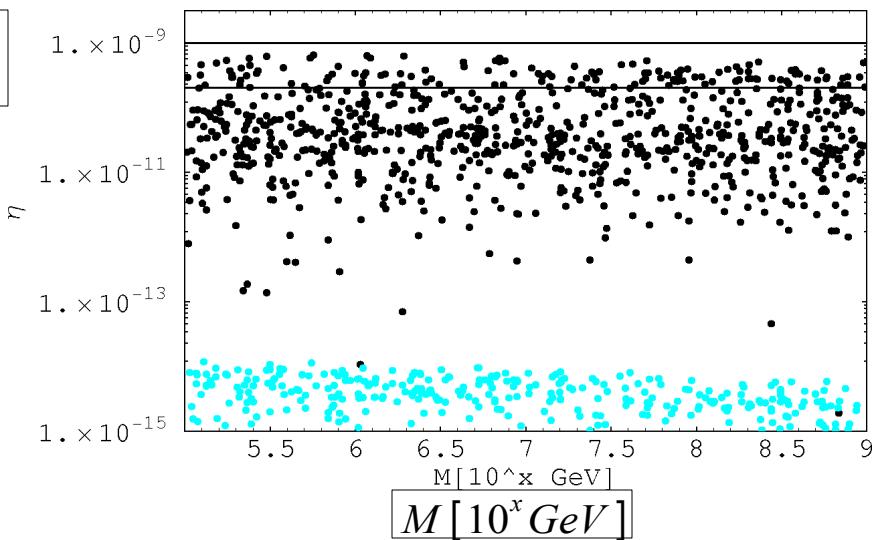
→ only low-energy CP violation via PMNS phases

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta} & -s_{23}c_{12}-s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} e^{i\alpha/2} & 0 & 0 \\ 0 & e^{i\beta/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

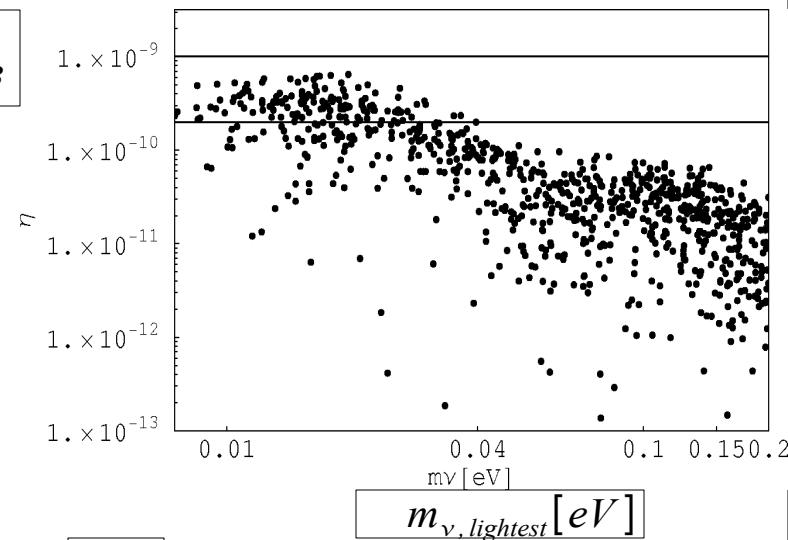
# Leptogenesis with low-Energy CP Violation

S.U. (2006)

$\eta_B$



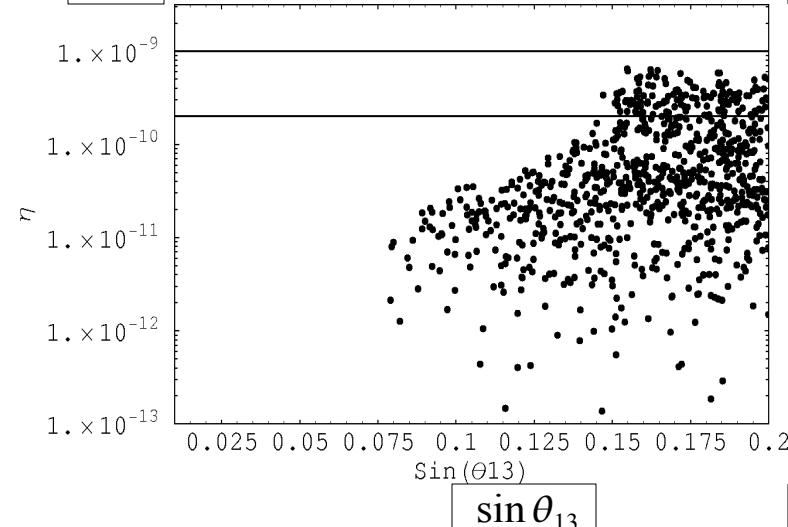
$\eta_B$



Clear constraints for successful leptogenesis

- Consideration of Flavour effects (BBJUW)
- Normal hierarchy of light neutrino masses
- A single non-vanishing Majorana phase
- $\sin \theta_{13} > 0.13$
- $m_{\nu, \text{lightest}} < 0.04 \text{ eV}$

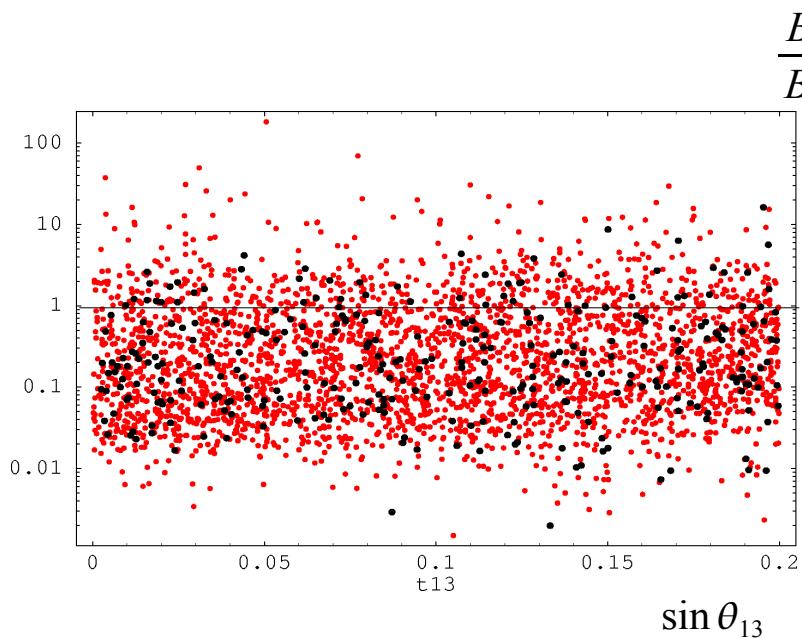
$\eta_B$



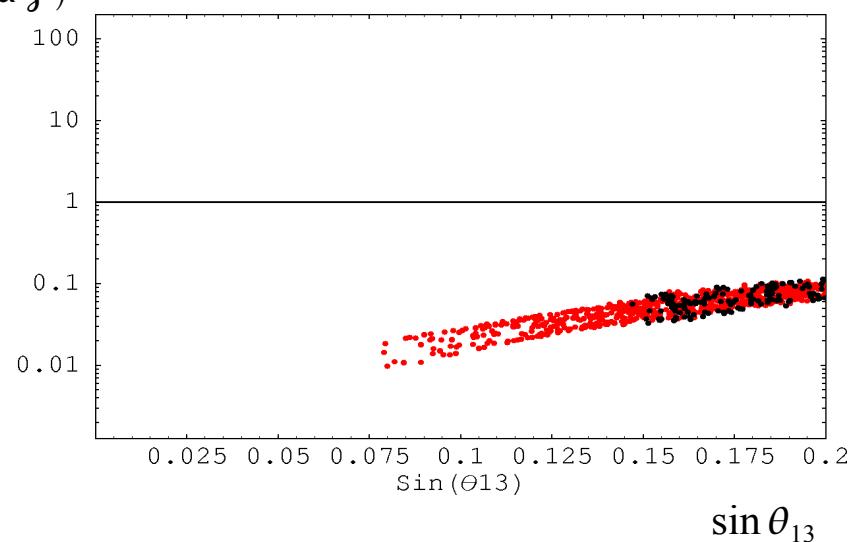
# Story of Predictivity

S.U. (2006)

Low- and high-energy CPV



Low-energy CPV



wide range

< 1

# Conclusions

In the framework of MLFV & RRL the BAU can successfully be generated with CP Violation at low and high Energies.  
Correlation to low-energy Observables is weak.

With the Flavour Effects it is possible to generate the BAU with low-energy CP Violation alone.

This special Case requires clear Relations and Properties of Neutrino Parameters that can be falsified.  
Correlations to low-energy Observables exist.