

# ***LHC / ILC interplay in SUSY searches***

**Gudrid Moortgat-Pick**

*(K Desch, J Kalinowski, GMP, K Rolbiecki, WJ Stirling, JHEP 0612:007, 2006 )*

## **Outline**

- **SUSY parameter determination and LHC/ILC interplay**
- **Case study: chosen scenario with heavy sfermions**
- **Numerical results: expectations for LHC**
- **Numerical results: ILC strategy and LHC/ILC interplay**
- **Conclusions**

# Supersymmetry

## ● In which range do we expect SUSY?

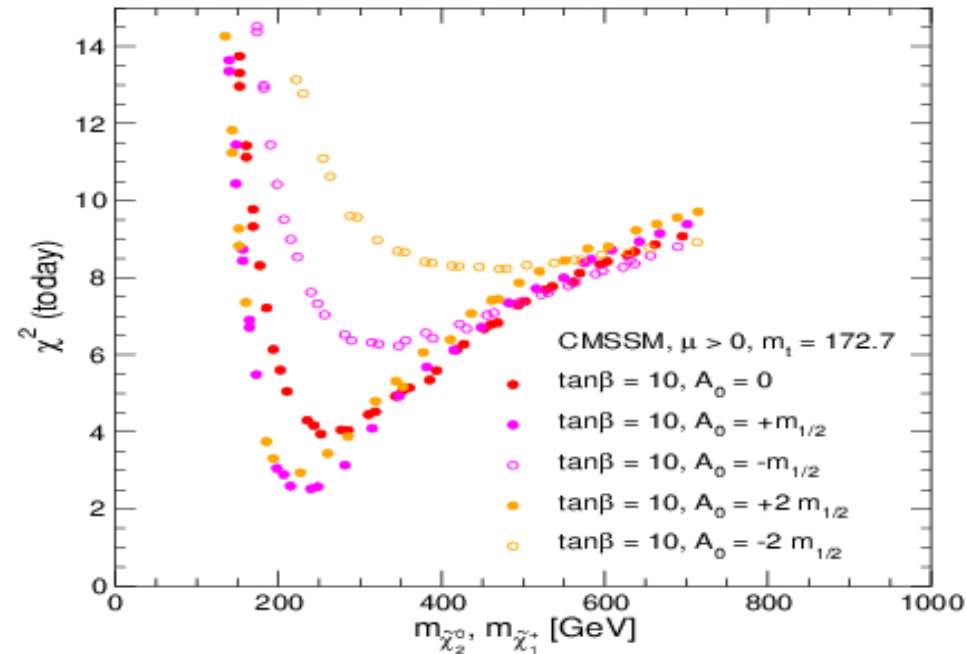
→ at least **some light particles** should **be accessible at 500 GeV**

→ **best possible tools** needed to get **maximal information** out of only **the part of the spectrum**

● **To reveal the structure of the underlying physics, it is important to determine the parameters in a model-independent way and test all model assumptions experimentally**

● **Soon we will have LHC data, but LHC/ILC interplay will be essential and both machines cover a large range of the parameter space !**

*Ellis, Heinemeyer, Olive, Weber, Weiglein '07*



# Discovery of SUSY

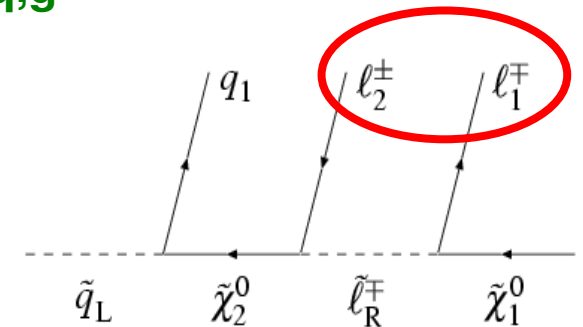
## Expectations at the LHC:

→ Coloured SUSY partners: discovery reach  $m_{\tilde{q},\tilde{g}} < 2\text{-}2.5 \text{ TeV}$

→ Non-coloured partners:

a) via Drell-Yan  $m_\chi < 250 \text{ GeV}$

b) via cascade decay chains



→ Parameter determinations: in specific SUSY breaking models

## At the ILC:

→ direct production of all kind of SUSY particles up to kinematical limit  $\sqrt{s}/2$

→ indirect mass bounds due to high precision

→ precise model-independent parameter determination

● Particularly promising field for LHC/ILC interplay studies !

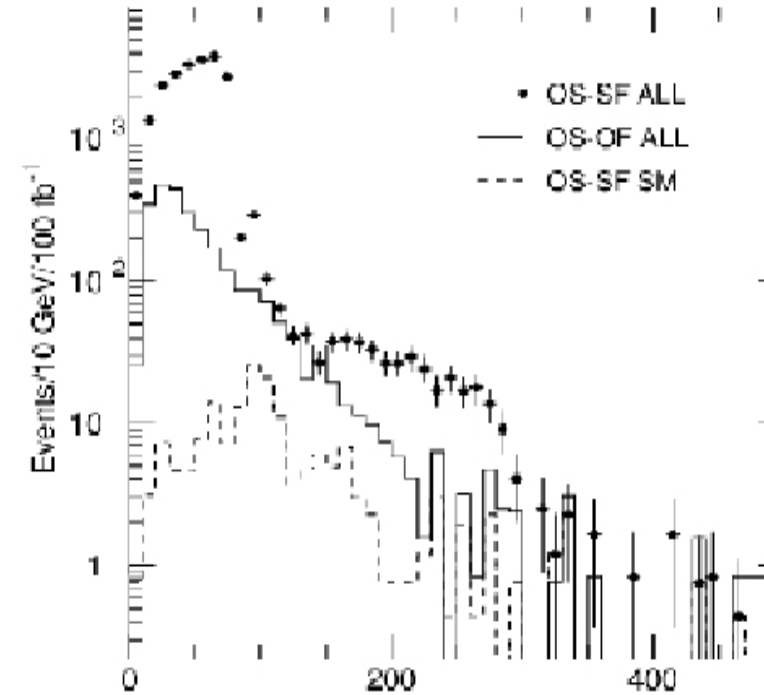
# LHC / ILC interplay

- If fundamental parameters determined: allows mass predictions for heavier particles

→ **significant increase of sensitivity** for searches at the LHC and **unique identification of particles in decay chain**

→ **Powerful test of the model**

*K. Desch, K. Kalinowski, GMP, M. Nojiri,  
G. Polesello, JHEP 2004*



|                       | $M_1$          | $M_2$           | $\mu$           | $\tan \beta$   |
|-----------------------|----------------|-----------------|-----------------|----------------|
| input                 | 99.1           | 192.7           | 352.4           | 10             |
| LC <sub>500</sub>     | $99.1 \pm 0.2$ | $192.7 \pm 0.6$ | $352.8 \pm 8.9$ | $10.3 \pm 1.5$ |
| LHC+LC <sub>500</sub> | $99.1 \pm 0.1$ | $192.7 \pm 0.3$ | $352.4 \pm 2.1$ | $10.2 \pm 0.6$ |

- **strong improvement in parameter determination via interplay!**

# NMSSM versus MSSM

- SUSY scenario in the NMSSM: Higgs and light particle sector (neutralino / chargino ) show no hints for model distinction
- measured at ILC (500 GeV):  $m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_{1,2}^0}, \sigma(e^+e^- \rightarrow \tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^0\tilde{\chi}_2^0)$

→ Consistent within MSSM-analysis

→ Predictions:

$$m_{\tilde{\chi}_3^0} = [352, 555] \text{ GeV} \rightarrow \text{pure higgsino}$$

$$m_{\tilde{\chi}_4^0} = [386, 573] \text{ GeV} \rightarrow \text{larger gaugino comp.}$$

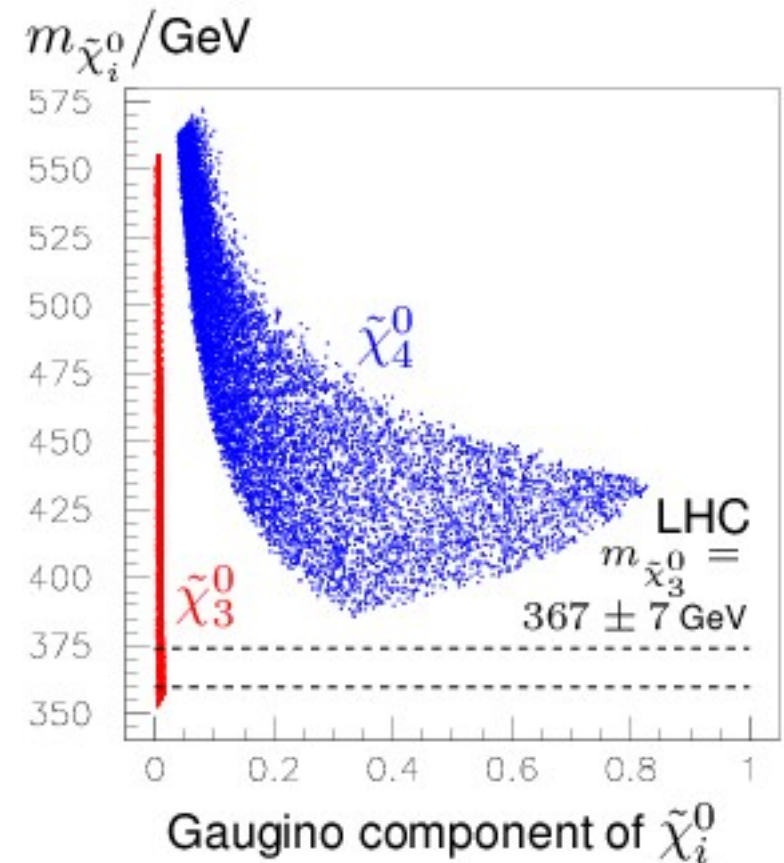
$$m_{\tilde{\chi}_2^\pm} = [450, 600] \text{ GeV}$$

⇒  $\tilde{\chi}_3^0$  not accessible at LHC

However:  $\tilde{\chi}_3^0$  in underlying NMSSM scenario has large gaugino component

→ visible at LHC → inconsistency

*S Hesselbach, GMP, F Franke, H Fraas, 2005*



- Model inconsistency determined via LHC/ILC

# ***Tricky case with heavy sfermions***

- **Feature of, for instance, focuspoint - inspired scenarios**
  - features: **very heavy squarks, sleptons, heavy H, A but light SM-like h and light gluino and light charginos / neutralinos**
  - **challenging for the LHC.....but is the ILC then the right machine ?**
  - **some analysis done at LHC, but within mSUGRA and still difficult**
- **Our approach: take a focuspoint-inspired scenario, but **do not impose** any assumption on the SUSY breaking mechanism and apply LHC / ILC analysis**
- **How well is it possible to**
  - **determine the underlying fundamental parameters?**
  - **predict masses of heavier states?**

# Chosen scenario

- MSSM parameters:

$$M_1 = 60 \text{ GeV}, M_2 = 121 \text{ GeV}, M_3 = 322 \text{ GeV}, \mu = 540 \text{ GeV}, \tan\beta = 20$$

- Resulting masses:

| $m_{\tilde{\chi}_1^\pm}$ | $m_{\tilde{\chi}_2^\pm}$ | $m_{\tilde{\chi}_1^0}$ | $m_{\tilde{\chi}_2^0}$ | $m_{\tilde{\chi}_3^0}$ | $m_{\tilde{\chi}_4^0}$ | $m_{\tilde{g}}$ |
|--------------------------|--------------------------|------------------------|------------------------|------------------------|------------------------|-----------------|
| 117                      | 552                      | 59                     | 117                    | 545                    | 550                    | 416             |

| $m_h$ | $m_{H,A}$ | $m_{H^\pm}$ |
|-------|-----------|-------------|
| 119   | 1934      | 1935        |

→ light gauginos/higgsinos, light gluino, light h but heavy H's, A

| $m_{\tilde{\nu}}$ | $m_{\tilde{e}_R}$ | $m_{\tilde{e}_L}$ | $m_{\tilde{\tau}_1}$ | $m_{\tilde{\tau}_2}$ | $m_{\tilde{q}_R}$ | $m_{\tilde{q}_L}$ | $m_{\tilde{t}_1}$ | $m_{\tilde{t}_2}$ |
|-------------------|-------------------|-------------------|----------------------|----------------------|-------------------|-------------------|-------------------|-------------------|
| 1994              | 1996              | 1998              | 1930                 | 1963                 | 2002              | 2008              | 1093              | 1584              |

→ heavy squarks and sleptons in the multi-TeV range

# What is expected that LHC could do ?

- In principle: all squarks should be kinematically accessible

→ stops:  $BR(\tilde{t}_{1,2} \rightarrow \tilde{g}t) \sim 66\%$ ,

**background t large**, no new interesting channels open in decays

→ other quarks: decay mainly via gluino and q, but reconstruction of heavy squarks at 2 TeV difficult

→ assume: **mass resolution of squarks with uncertainty of ~50 GeV**

- Light gluino: perfect for LHC (high rates, several decays)

|      |   |  |   |   |  |   |
|------|---|--|---|---|--|---|
| Mode | $\tilde{g} \rightarrow \tilde{\chi}_2^0 b\bar{b}$ | $\tilde{g} \rightarrow \tilde{\chi}_1^- q_u \bar{q}_d$ | $\tilde{\chi}_1^+ \rightarrow \tilde{\chi}_1^0 \bar{q}_d q_u$ | $\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \ell^+ \ell^-$ | $\tilde{t}_{1,2} \rightarrow \tilde{g}t$ | $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell^- \bar{\nu}_\ell$ |
| BR   | 14.4%   | 10.8%  | 33.5%   | 3.0%  | 66%                                      | 11.0%   |

→ **clear dilepton edge** from neutralino decay  $\delta(m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}) \sim 0.5 \text{ GeV}$

→ decay via chargino less promising (escaping  $\nu$ , 3-body decay)



# What is expected at the ILC (500) ?

- Kinematically only two light neutralinos and light chargino accessible

→ in reality: **light neutralino production below 1 fb** .....

| $\sigma(\tilde{\chi}_i \tilde{\chi}_j)/\text{fb}$ | $\sqrt{s} = 350 \text{ GeV}$ |        | $\sqrt{s} = 500 \text{ GeV}$ |        | $\sqrt{s} = 800 \text{ GeV}$ |        | $\sqrt{s} = 1300 \text{ GeV}$ |         |
|---|------------------------------|--------|------------------------------|--------|------------------------------|--------|-------------------------------|---------|
|   | (-, +)                       | (+, -) | (-, +)                       | (+, -) | (-, +)                       | (+, -) | (-, +)                        | (+, -)  |
| $\tilde{\chi}_1^0 \tilde{\chi}_2^0$               | 0.58                         | 0.08   | 0.93                         | 0.07   | 1.76                         | 0.07   | 3.14                          | 0.08    |
| $\tilde{\chi}_1^0 \tilde{\chi}_3^0$               | -                            | -      | -                            | -      | 0.24                         | 0.27   | 0.13                          | 0.28    |
| $\tilde{\chi}_1^0 \tilde{\chi}_4^0$               | -                            | -      | -                            | -      | 0.05                         | 0.11   | 0.02                          | 0.20    |
| $\tilde{\chi}_2^0 \tilde{\chi}_2^0$               | 0.06                         | 0.05   | 0.49                         | 0.05   | 2.06                         | 0.05   | 4.91                          | 0.07    |
| $\tilde{\chi}_2^0 \tilde{\chi}_3^0$               | -                            | -      | -                            | -      | 1.44                         | 0.79   | 1.18                          | 0.53    |
| $\tilde{\chi}_2^0 \tilde{\chi}_4^0$               | -                            | -      | -                            | -      | 0.23                         | 0.09   | 0.55                          | 0.13    |
| $\tilde{\chi}_3^0 \tilde{\chi}_3^0$               | -                            | -      | -                            | -      | -                            | -      | < 0.001                       | < 0.001 |
| $\tilde{\chi}_3^0 \tilde{\chi}_4^0$               | -                            | -      | -                            | -      | -                            | -      | 38.53                         | 24.97   |
| $\tilde{\chi}_4^0 \tilde{\chi}_4^0$               | -                            | -      | -                            | -      | -                            | -      | 0.002                         | 0.001   |
| $\tilde{\chi}_1^+ \tilde{\chi}_2^-$               | -                            | -      | -                            | -      | 1.36                         | 0.88   | 1.05                          | 0.68    |
| $\tilde{\chi}_2^+ \tilde{\chi}_2^-$               | -                            | -      | -                            | -      | -                            | -      | 143.23                        | 25.95   |

- light pure  $\tilde{\chi}_1^0 \sim \tilde{B}$ ,  $\tilde{\chi}_2^0 \sim \tilde{W}$ : **production suppressed** by heavy  $\tilde{e}_L, \tilde{e}_R$  exchange
- heavier  $\tilde{\chi}_3^0, \tilde{\chi}_4^0 \sim \tilde{H}$  with specific CP-phases: rather **high rates!**
- heavy pair  $\tilde{\chi}_2^+ \tilde{\chi}_2^- \sim \tilde{H}$ : **also high rates!**

# Promising channel: light chargino

- So forget light neutralino production at ILC(500) for today ...
- Use only (light) chargino production, provides high rates
  - subsequent decays:  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 e^- \bar{\nu}_e, \tilde{\chi}_1^0 \mu^- \bar{\nu}_\mu, \tilde{\chi}_1^0 d \bar{u} \tilde{\chi}_1^0 s \bar{c}$
- Due to very limited information, use two energies and polarized beams!

| $\sqrt{s}/\text{GeV}$ | $(P_{e^-}, P_{e^+})$ | $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-)/\text{fb}$ | $\sigma(\tilde{\chi}_1^+ \tilde{\chi}_1^-) B_{slc} e_{slc}/\text{fb}$ |
|-----------------------|----------------------|---|---|
| 350                   | $(-90\%, +60\%)$     | 6195.5  | $1062.5 \pm 4.0$  |
|                       | $(+90\%, -60\%)$     | 85.0  | $14.6 \pm 0.7$  |
| 500                   | $(-90\%, +60\%)$     | 3041.5  | $521.6 \pm 2.3$   |
|                       | $(+90\%, -60\%)$     | 40.3  | $6.9 \pm 0.4$   |

uncertainties: efficiency 50%,  $1\sigma$  stat. uncertainties,  $\Delta P / P = 0.5\%$

→ to separate background WW: use semileptonic chargino decay channel, since mass constraints applicable

# Mass measurements at LHC+ILC

- Expected chargino mass resolution:

- in the continuum: up to 0.5 GeV

- threshold scan:

$$m_{\tilde{\chi}_1^\pm} = 117.1 \pm 0.1 \text{ GeV}$$

- Neutralino mass resolution:

- use either energy  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \ell^- \bar{\nu}_\ell$  or invariant mass distribution  
 $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 q_d \bar{q}_u$

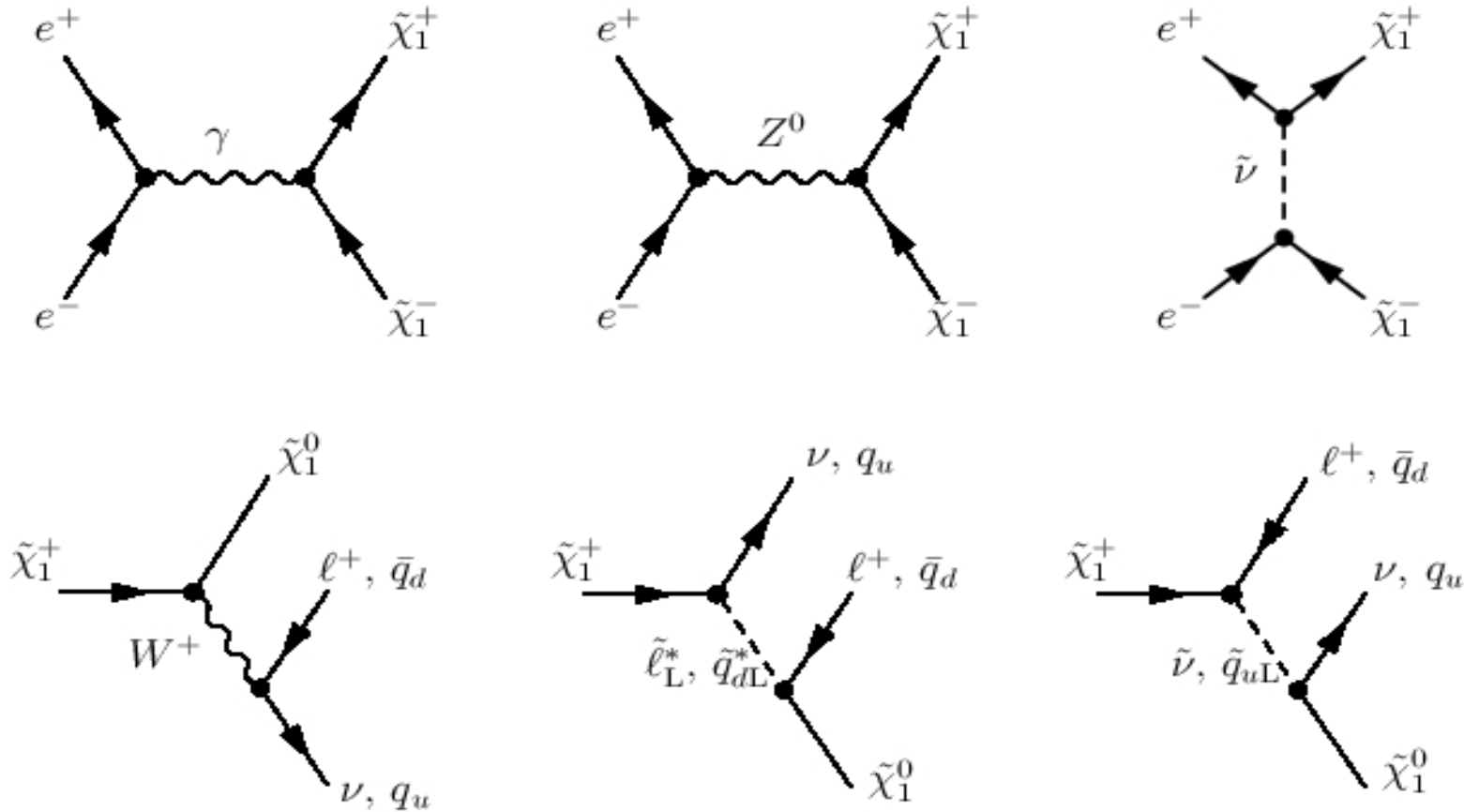
$$m_{\tilde{\chi}_1^0} = 59.2 \pm 0.2 \text{ GeV}$$

- together with LHC mass information ( $\delta(m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}) \sim 0.5 \text{ GeV}$ ):

$$m_{\tilde{\chi}_2^0} = 117.1 \pm 0.5 \text{ GeV}$$

# Determine fundamental parameters

- On which parameters depend the process?



➔ Parameters in the gaugino/higgsino:  $M_1, M_2, \mu, \tan \beta$

➔ But heavy virtual particles:  $\tilde{m}_\nu, \tilde{m}_\ell, m_{qL}, m_{qR}$

# Strategy, 1<sup>st</sup> step

- Use measured masses and polarized cross sections
- Analytical conversion and derive / fit parameters
  - do  $\chi^2$  test for  $M_1$ ,  $M_2$ ,  $\mu$  and  $m_{\tilde{\nu}}$
  - BR not sensitive to heavy slepton masses
  - was necessary to fix  $\tan\beta$  (took several values) to get convergence of fit ! (strong correlations among parameters)

## Results:

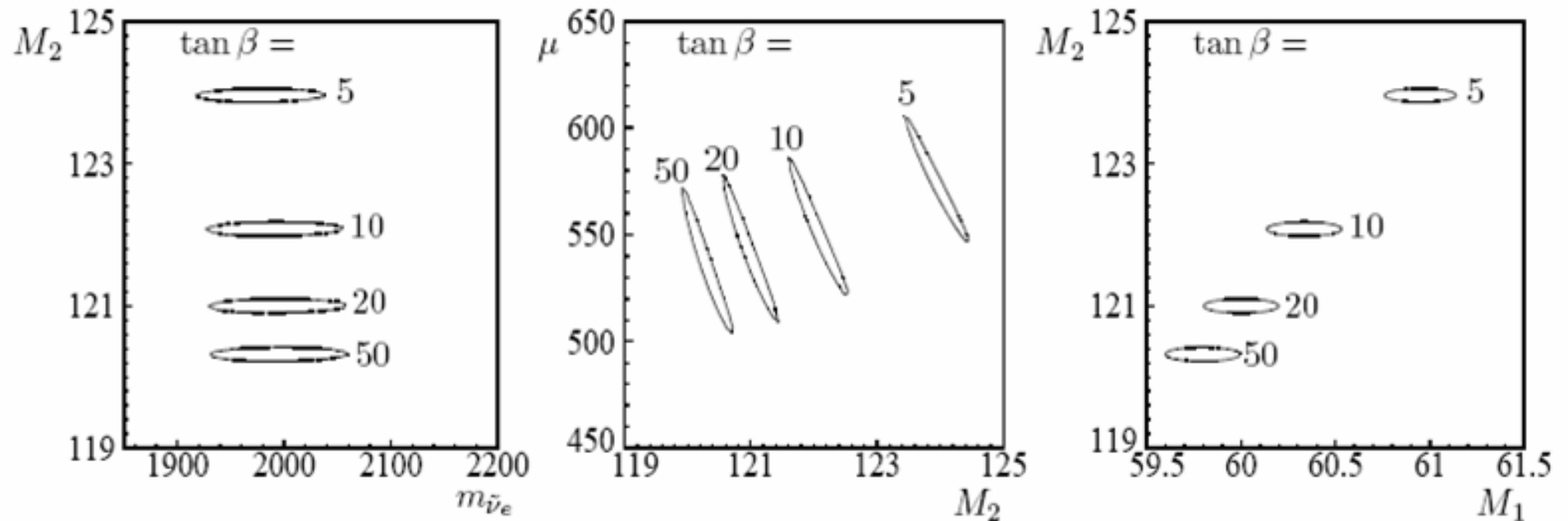
→ contradiction to theory for  $\tan\beta < 1.7$

$$450 \leq \mu \leq 750 \text{ GeV}, \quad 1800 \leq m_{\tilde{\nu}_e} \leq 2210 \text{ GeV}$$
$$59.4 \leq M_1 \leq 62.2 \text{ GeV}, \quad 118.7 \leq M_2 \leq 127.5 \text{ GeV},$$

$M_1$ ,  $M_2$  good (~5%), but  $\mu$  and  $m_{\tilde{\nu}}$  rather weak (~16%) (limited info)

# Strategy, 1<sup>st</sup> step

- Masses and cross sections are not enough to constrain five parameter space due to strong correlations
- Allowed ranges migrate with change of  $\tan \beta$



- Need another observable to get better constraints

# Strategy, 2<sup>nd</sup> step -- spin correlations

- Which further observable could be used?

→ **Forward-backward asymmetry of the final lepton / quark**

( angle between incoming beam and final lepton or quark )

- Dependent on spin correlations of decaying chargino:

→ **amplitude squared:**  $e^- + e^+ \rightarrow \tilde{\chi}_1^+ + \tilde{\chi}_1^-$  and  $\tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 + \ell^- + \bar{\nu}$

$$|T|^2 = |\Delta_{f_1}|^2 |\Delta_{f_2}|^2 \sum_{fin.sp.} \overbrace{(P^{\lambda_{f_1} \lambda_{f_2}} P^{*\lambda'_{f_1} \lambda'_{f_2}})}^{\text{spin-density matrix}} \times \overbrace{(Z_{\lambda_{f_1}} Z_{\lambda'_{f_1}}^*)}^{\text{decay matrix}} \times \overbrace{(Z_{\lambda_{f_2}} Z_{\lambda'_{f_2}}^*)}^{\text{decay matrix}}$$

$$\longrightarrow |T|^2 \sim PD_i D_j + \sum_a^P \sum_a^D D_j + \sum_b^P \sum_b^D D_i + \sum_{ab}^P \sum_a^D \sum_b^D$$

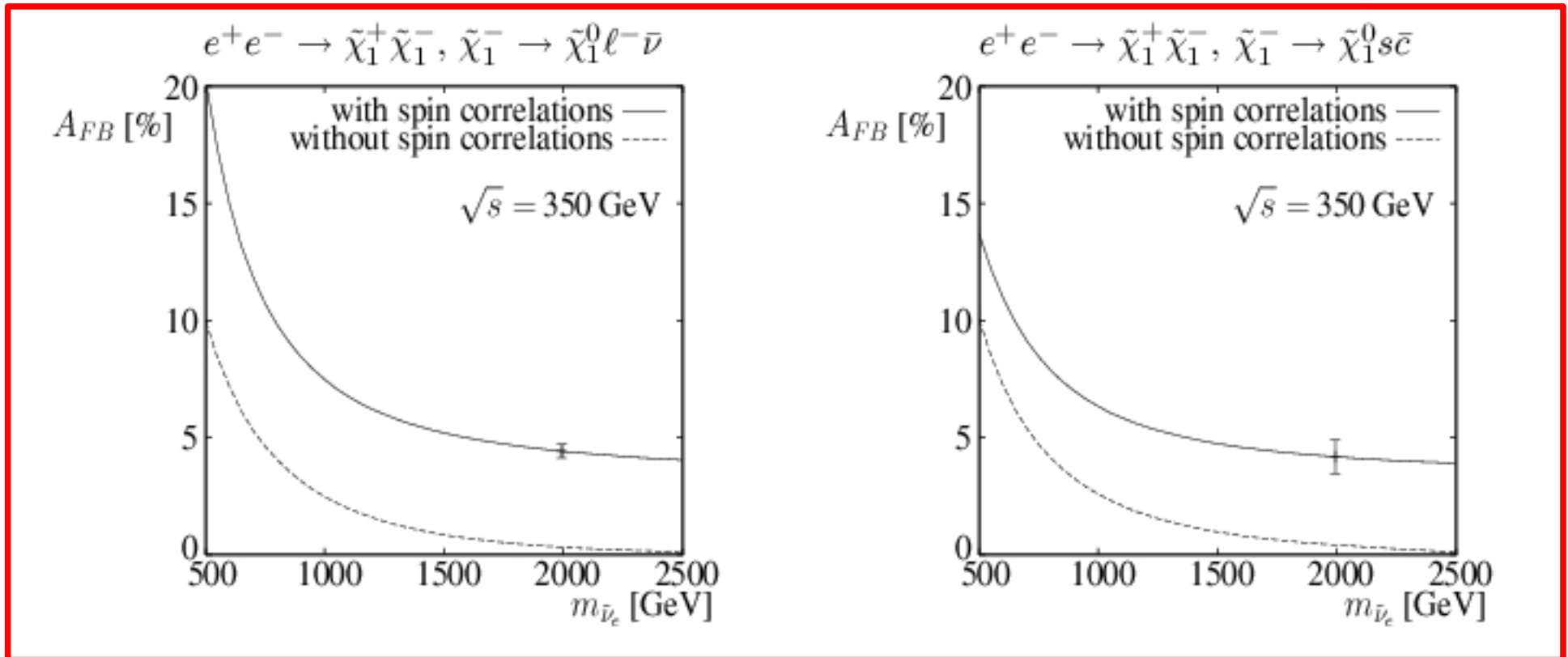
↓
↓
↓
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**cross section**
**A<sub>fb</sub>(I<sup>-</sup>)**
**A<sub>fb</sub>(I<sup>+</sup>)**
**not needed here**

'new contributions'

# How important are spin correlations?

## Impact of the 'new contributions' on $A_{fb}$ :



→ strong influence of spin correlations:  $A_{fb}$  within [5%, 20%]

→ and also sensitivity to heavy sneutrino mass !



# Strategy, 2<sup>nd</sup> step -- leptonic $A_{fb}$

- use measured masses, cross sections and leptonic  $A_{fb}$
- since decay also depends on unknown left slepton mass, use SU(2) relation:

$$m_{\tilde{e}_L}^2 = m_{\tilde{\nu}_e}^2 + m_Z^2 \cos(2\beta)(-1 + \sin^2 \theta_W)$$

- include also statistical and polarization uncertainty for  $A_{fb}$  :

| $\sqrt{s}/\text{GeV}$ | $(P_{e^-}, P_{e^+})$ | $A_{\text{FB}}(\ell^-)/\%$ | $A_{\text{FB}}(\bar{c})/\%$ |
|-----------------------|----------------------|----------------------------|-----------------------------|
| 350                   | (-90%, +60%)         | $4.42 \pm 0.29$            | $4.18 \pm 0.74$             |
|                       | (+90%, -60%)         | -                          | -                           |
| 500                   | (-90%, +60%)         | $4.62 \pm 0.41$            | $4.48 \pm 1.05$             |
|                       | (+90%, -60%)         | -                          | -                           |

- use only (- +) values due to statistical uncertainty

# Strategy, 2<sup>nd</sup> step -- results

## Results:

→ do  $\chi^2$  test:

$$\chi_{A_{\text{FB}}}^2 = \chi^2 + \sum_i \left( \frac{A_{\text{FB}}(i) - A_{\text{FB}}(i)^{\text{th}}}{\Delta A_{\text{FB}}(i)} \right)^2$$

→ not necessary to fix  $\tan\beta$  any more !!!

$$\begin{aligned} \rightarrow & 59.7 \leq M_1 \leq 60.35 \text{ GeV}, \quad 119.9 \leq M_2 \leq 122.0 \text{ GeV}, \\ & 500 \leq \mu \leq 610 \text{ GeV}, \quad 14 \leq \tan\beta \leq 31 \\ & 1900 \leq m_{\tilde{\nu}_e} \leq 2100 \text{ GeV} \end{aligned}$$

## Improvements:

→ constraints for **multi-TeV sneutrino mass by factor 2, up to 5% accuracy !**

→ accuracy of  **$M_1, M_2$  by factor 5**

→ accuracy of  **$\mu$  by factor 1.6 and  $\tan\beta$  now included!**

# Strategy, 2<sup>nd</sup> step -- mass predictions

- Due to rather precise parameter determination:

→ use these allowed parameters and predict, for instance, the possible ranges for **the masses of the heavier chargino and neutralino states**

→

$$506 < m_{\tilde{\chi}_3^0} < 615 \text{ GeV}$$

$$512 < m_{\tilde{\chi}_4^0} < 619 \text{ GeV}$$

$$514 < m_{\tilde{\chi}_2^\pm} < 621 \text{ GeV}$$

→ Obviously 1.3 TeV as 2<sup>nd</sup> ILC energy stage would be sufficient

- Rather precise parameter determination important and possible at 500 GeV (even in such tricky scenarios with limited information only)

→ **important input for future upgrade strategies**

# **Strategy, 3<sup>rd</sup> step -- also hadronic $A_{fb}$**

- Redo analysis without assuming SU(2) relation between slepton masses
  - squark masses constrained from LHC
  - strategy as before: use masses, cross sections, leptonic  $A_{fb}$
- Include also  $A_{fb}$  from hadronic distribution:
  - charm identification needed : assume c-tag efficiency of 40% for selection efficiency of 50%
- Results (without using SU(2) relation) :

$$59.45 \leq M_1 \leq 60.80 \text{ GeV}, \quad 118.6 \leq M_2 \leq 124.2 \text{ GeV}, \quad 420 \leq \mu \leq 770 \text{ GeV}$$
$$1900 \leq m_{\tilde{\nu}_e} \leq 2120 \text{ GeV}, \quad m_{\tilde{e}_L} \geq 1500 \text{ GeV}, \quad 11 \leq \tan \beta \leq 60.$$

  - again precise parameter determination and constraints for msn
  - no upper bound for msel, but consistent with SU(2) relation !

# Conclusions

- **Tricky case of SUSY: multi-TeV sleptons and squarks**
  - only few particles kinematically accessible at ILC with 500 GeV
- **Study done without assuming a SUSY breaking scheme!**
- **Forward-backward asymmetries of the final leptons/quarks: sensitivity to heavy virtual particles**
  - get tight constraints even for masses in the **multi-TeV range!**
- **Rather accurate parameter determination possible with  $A_{fb}$** 
  - allows to **predict masses of heavier charginos/neutralinos**
- **LHC / ILC(500): neither of these colliders alone can resolve such a challenging scenario with multi-TeV squarks and sleptons --> both LHC and ILC required !**