

# $\tan(\beta)$ Enhanced Yukawa Couplings for Supersymmetric Higgs Singlets at One-Loop

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# Outline

- 1 SUSY Higgs Singlets
- 2 One Loop Singlet Couplings
- 3 Phenomenology
  - mnSSM Results
  - NMSSM Results
- 4 Conclusions

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# The Minimal Supersymmetric Standard Model

- Before SUSY breaking, models are defined by their gauge symmetries and **Superpotential**
- The MSSM superpotential contains only the Yukawa couplings and a Higgs mass term  $\mu$

$$\mathcal{W}_{\text{MSSM}} = h_l \hat{H}_1^T i\tau_2 \hat{L} \hat{E} + h_d \hat{H}_1^T i\tau_2 \hat{Q} \hat{D} + h_u \hat{Q}^T i\tau_2 \hat{H}_2 \hat{U} - \mu \hat{H}_1^T i\tau_2 \hat{H}_2$$

- $\mu$  should naturally be of the order of the Planck scale, but successful electroweak symmetry breaking requires it to be much smaller, of the order  $M_{\text{SUSY}}$

## Effective $\mu$ Parameter

- Introduce a new Higgs field  $\hat{S}$  and replace the  $\mu$  term in the superpotential with

$$\mathcal{W} = \dots + \lambda \hat{S} \hat{H}_1^T i\tau \hat{H}_2$$

- An effective  $\mu$  term is then generated when  $\hat{S}$  develops a VEV  $v_S$

$$\mu = \frac{\lambda v_S}{\sqrt{2}}$$

- The Singlet Higgs  $\hat{S}$  does not have tree level couplings to **any** SM fermions or gauge bosons

## Breaking the Peccei-Quinn Symmetry

This new superpotential contains a Peccei-Quinn symmetry which must be broken.<sup>1</sup>

- NMSSM: add term  $+\frac{1}{3}\kappa\hat{S}^3$  to  $\mathcal{W}$
- mnSSM: use non-renormalisable supergravity terms + discrete  $Z^5$  or  $Z^7$  R symmetry
- UMSSM: additional  $U(1)'$  gauge symmetry
- ...

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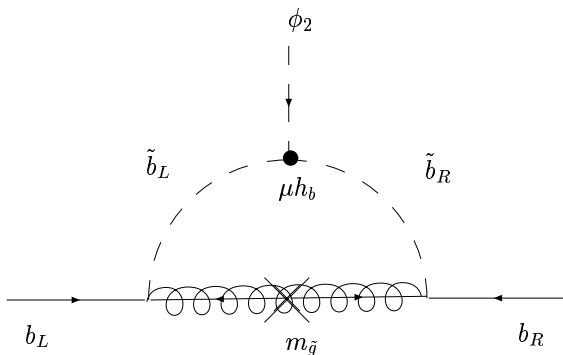
<sup>1</sup>See E. Accomando *et al.*, arXiv: hep-ph/0608079 and references within

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# Dominant 1-loop Graphs

$\tan \beta$  Enhanced MSSM coupling<sup>2</sup>



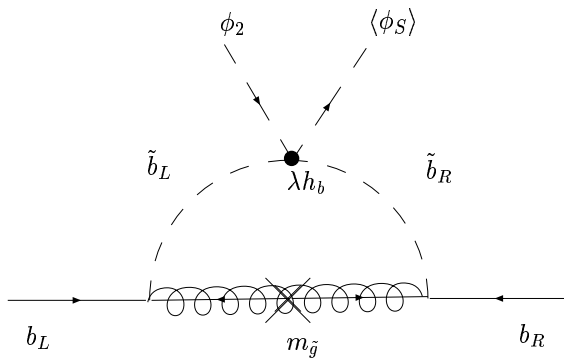
<sup>2</sup>T. Banks, Nucl. Phys. B **303** (1988) 172;

L.J. Hall, R. Rattazzi and U. Sarid, arXiv: hep-ph/9306309



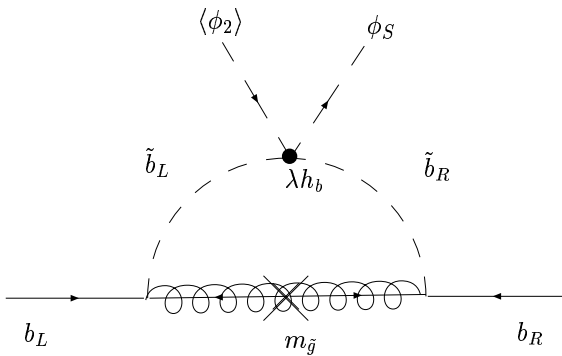
# Dominant 1-loop Graphs

$\tan \beta$  enhanced MSSM+S coupling



# Dominant 1-loop Graphs

$\tan \beta$  enhanced MSSM+S coupling



## $Sb\bar{b}$ Coupling

- This SQCD graph gives the dominant contribution

$$\Delta_b^{\phi_S} \approx \left( \frac{2\alpha_S}{3\pi} \right) \frac{M_3 \mu}{|\text{Max}(M_3, M_{\tilde{Q}})|^2} \frac{v_2}{v_S}$$

- Shows expected  $v/v_S$  scaling behaviour, though this is broken by subdominant terms
- A similar mechanism gives a coupling to  $\tau^+\tau^-$
- This is dominated by a chargino exchange graph, giving a dominant contribution

$$\Delta_\tau^{\phi_S} \approx \left( \frac{\alpha_W}{4\pi} \right) \frac{\mu}{M_2} \frac{v_2}{v_S}$$

## Effective Lagrangian

General interaction Lagrangian for down-type quarks and leptons

$$-\mathcal{L}_{\phi\bar{b}b} = \bar{f}_R h_f \left\{ \Phi_1^{0*} + \frac{v_1}{\sqrt{2}} \Delta_f [\Phi_1, \Phi_2, S] \right\} f_L + \text{h.c.}$$

- $\Delta_f [\Phi_1, \Phi_2, S]$  encodes all quantum corrections
- Taking the VEV gives  $m_f$ , in terms of which we express the yukawa couplings

$$h_f = \frac{g_w m_f}{\sqrt{2} M_w (1 + \langle \Delta_f \rangle)} \frac{1}{c_\beta}$$

- A Higgs Low-Energy Theorem allows us to calculate the couplings at zero momentum by taking derivatives of  $\Delta_f$

## Interaction Lagrangian

In terms of the Higgs mass eigenstates,

$$-\mathcal{L}_{\phi\bar{f}f}^{\text{eff}} = \left( \frac{g_w m_f}{\sqrt{2} M_w} \right) \sum_{i=1}^3 g_{H_i f f}^S H_i \bar{f} f + \left( \frac{g_w m_f}{\sqrt{2} M_w} \right) \sum_{j=1}^2 g_{A_j f f}^P A_j (\bar{f} i \gamma^5 f)$$

with

$$g_{H_i f f}^S = \frac{1}{(1 + \langle \Delta_f \rangle)} \left[ \frac{O_{1i}^H}{c_\beta} + \Delta_f^{\phi_2} \frac{O_{2i}^H}{c_\beta} + \Delta_f^{\phi_s} \frac{O_{3i}^H}{c_\beta} \right]$$

$$g_{A_j f f}^P = \frac{1}{(1 + \langle \Delta_f \rangle)} \left[ - (t_\beta + \Delta_f^{a_2}) O_{1j}^A + \Delta_f^{a_s} \frac{O_{2j}^A}{c_\beta} \right]$$

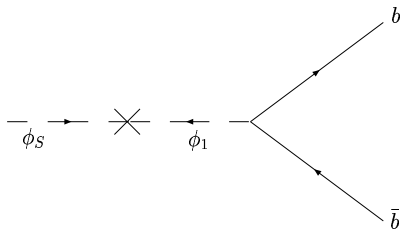
- SM-normalised effective couplings

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# Higgs Scalar Mixing

- The one-loop couplings are  $\tan \beta$  enhanced
- Can be comparable to SM yukawa couplings
- Tree-level couplings are also enhanced
- Mixing effects through  $\phi_1(a_1)$  tend to dominate unless suppressed



## General Strategy

- Difficult to suppress  $\phi_1 \leftrightarrow \phi_S$  and  $\phi_2 \leftrightarrow \phi_S$  mixing simultaneously
- Mixing effects between the pseudoscalars **can** be easily suppressed
- Concentrate on regions of parameter space where the  $A_1 \sim a_S$
- Assume  $\phi_1$  heavy so that it approximately decouples

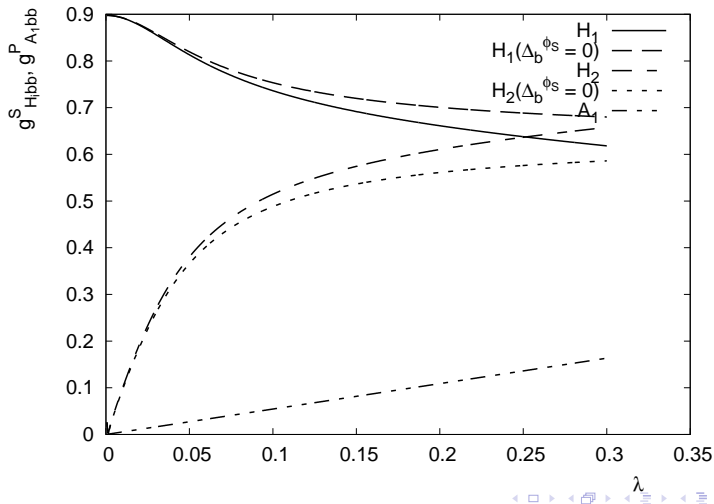


## Benchmark Parameters

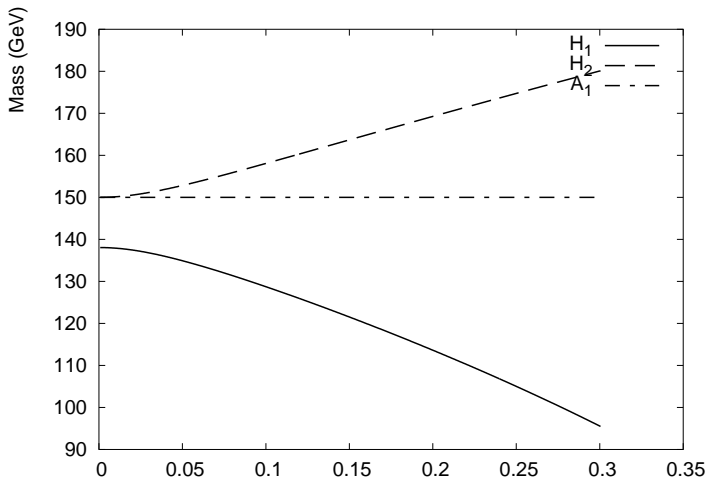
$$\begin{aligned}
 \mu &= 110 \text{ GeV}, & t_\beta &= 50, \\
 M_{\tilde{Q}} &= 300 \text{ GeV}, & M_{\tilde{L}} &= 90 \text{ GeV}, \\
 M_{\tilde{t}} &= 600 \text{ GeV}, & M_{\tilde{b}} &= 110 \text{ GeV}, & M_{\tilde{\tau}} &= 200 \text{ GeV}, \\
 A_t &= 1 \text{ TeV}, & A_b &= 1 \text{ TeV}, & A_\tau &= 1 \text{ TeV}, \\
 M_1 &= 400 \text{ GeV}, & M_2 &= 600 \text{ GeV}, & M_3 &= 400 \text{ GeV} .
 \end{aligned}$$

- Light sparticles in the loops
- $S$  enters through squark mixing, take soft trilinear couplings large
- $\mu$  small to avoid  $v/v_S$  suppression

# Light Higgs Couplings in the mnSSM



# Light Higgs Masses in the mnSSM



# mnSSM Summary

- Mixing between the scalar bosons rules out this scenario for  $\lambda \gtrsim 0.3$
- Singlet contribution suppresses the light  $H_1$  decay rate
- Can provide the dominant decay mechanism for a light singlet pseudoscalar

## NMSSM mass spectrum

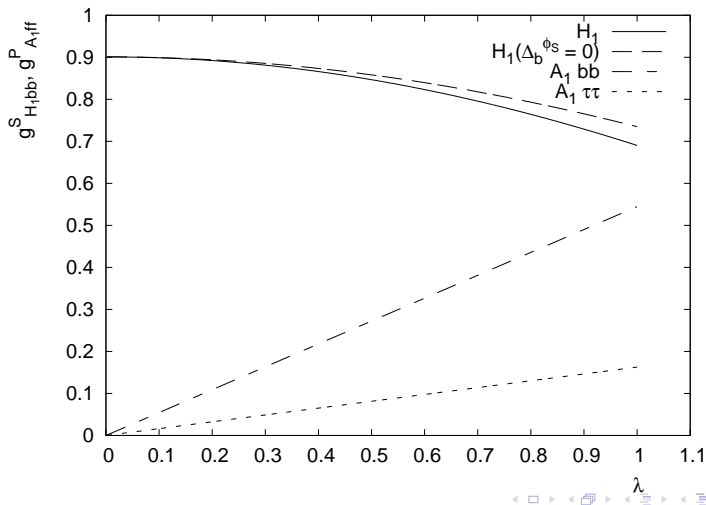
- The NMSSM allows a light pseudoscalar in the spectrum
- This *NMSSM close to the R-symmetry limit* scenario <sup>3</sup> has attracted interest as a low fine-tuning model
- A light  $H_1$  decays to  $A_1 A_1$  pairs
- $A_1$  is singlet dominated (>98%) for minimum fine tuning

Requires  $A_\lambda \sim O(100\text{GeV})$ ,  $A_{\kappa} \sim O(5\text{GeV})$ , which can be naturally arranged in gauge/gaugino mediated SUSY breaking.

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<sup>3</sup>R. Dermisek and J.F. Gunion, arXiv:hep-ph/0510322

# Light Higgs Couplings in the NMSSM



## NMSSM summary

- In the minimally fine tuned scenario decays to  $b\bar{b}$  are kinematically disallowed
- Loop corrections can provide a significant contribution to the  $\tau^+\tau^-$  coupling
- Heavier pseudoscalars  $m_{A_1} \sim 10\text{GeV}$  are not excluded if  $m_{H_1} > 110\text{GeV}$
- Corrections to the  $A_1 \rightarrow b\bar{b}$  coupling can then be comparable to the tree level (mixing) contribution previously considered

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## Summary and Outlook

- The one loop singlet couplings to down-type quarks and leptons are  $\tan \beta$  enhanced, which compensates for their loop suppression
- Mixing can be small between the pseudoscalars and one loop couplings can dominate  $a_S$  decay in some regions of parameter space
- In particular, this effect should be included in studies of the *NMSSM close to the R-symmetry limit*
- Analogous singlet contributions to FCNCs may also be significant as there is no tree-level competition