

Primordial Kerr Black Holes

Alexandre Arbey

Lyon University

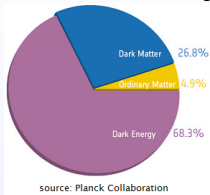
Based on AA, J. Auffinger and J. Silk, arXiv:1906.04196 and 1906.04750

PASCOS 2019

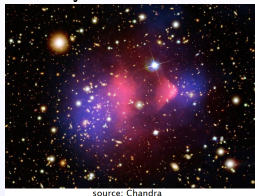
Manchester – July 4th, 2019

Dark Matter

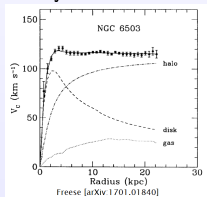
Cosmic Microwave Background



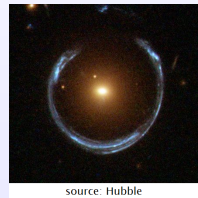
Galaxy clusters collision



Galaxy rotation curves



Gravitational lensing



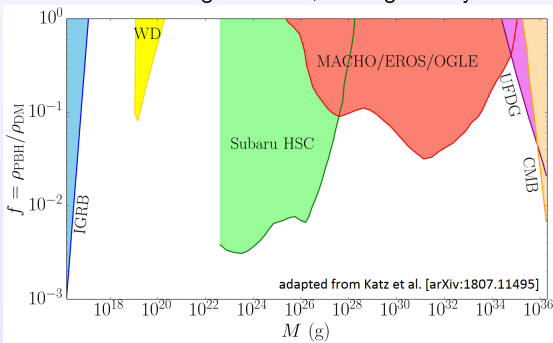
Observations of large scale structures, galaxies and cosmology show that 90% of matter is dark

Primordial Black Holes

Plausible DM candidates

- no Standard Model / General Relativity extension
- dynamically cold
- BH existence (somehow) proven
- mass ranges still available for BHs to represent all of DM

Constraints from PBH Hawking radiation, lensing and dynamics observations



Primordial Black Holes

Multiple inflationary origins

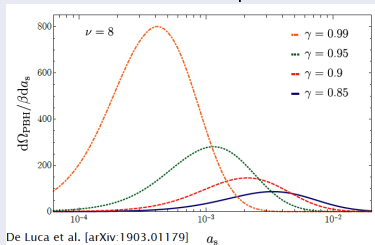
- collapse of large primordial overdensities
- phase transitions
- collapse of cosmic strings, domain walls

Spin predictions

$$a^* \equiv J/M^2$$

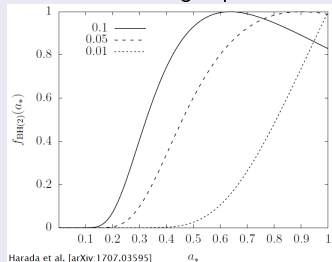
Standard inflationary model

⇒ low spin

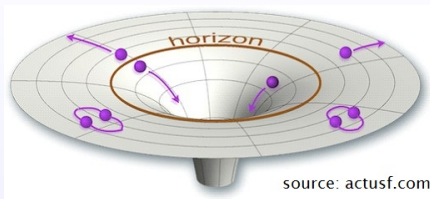


Transient matter domination

⇒ high spin



BH Hawking radiation



Fundamental equation for Kerr BHs

Rate of emission of Standard Model particles i at energy E by a BH of mass M and spin parameter a^* :

$$Q_i = \frac{d^2 N_i}{dt dE} = \frac{1}{2\pi} \sum_{\text{dof.}} \frac{\Gamma_i(M, E, a^*)}{e^{E/T(M, a^*)} \pm 1}$$

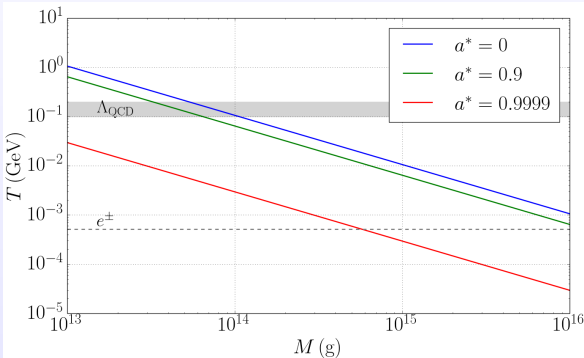
Γ_i is the greybody factor (\sim absorption coefficient in Planck's black-body law)

Reduced temperature

Hawking temperature for Kerr BHs

$$T(M, a^*) = \frac{1}{4\pi M} \left(\frac{\sqrt{1 - (a^*)^2}}{1 + \sqrt{1 - (a^*)^2}} \right) \xrightarrow[a^*=0]{\text{Schwarzschild}} \frac{1}{8\pi M}$$

Comparison with the e^\pm rest mass and QCD scale Λ_{QCD}

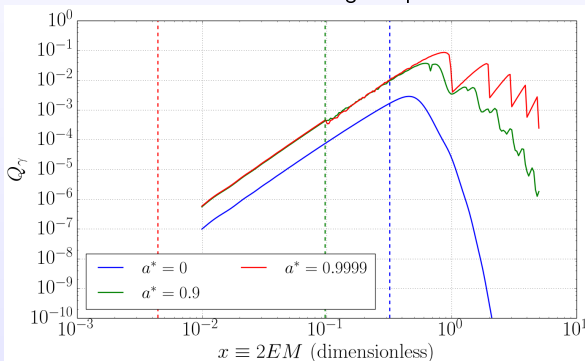


Enhanced emission

BH-particle spin coupling \Rightarrow superradiance effects (see e.g. Chandrasekhar & Detweiler papers in the 1970s)

The Hawking radiation is enhanced for particles of spin 1 or 2.

Example of spin 1 massless emissivity (photon)
Dotted lines = Hawking temperature



Reduced lifetime

Evolution equations

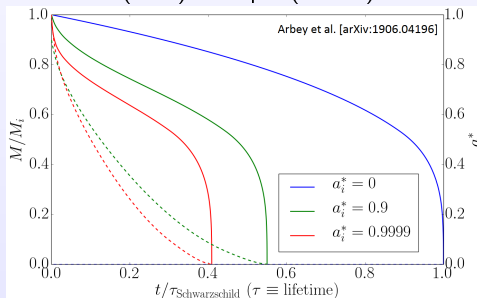
$$\frac{dM}{dt} = -\frac{f(M, a^*)}{M^2}$$

$$\frac{da^*}{dt} = \frac{a^*(2f(M, a^*) - g(M, a^*))}{M^3}$$

$$f \sim \int_E \text{ener.} \times \text{emiss.}$$

$$g \sim \int_E \text{ang. mom.} \times \text{emiss.}$$

BH mass (solid) and spin (dotted) evolution

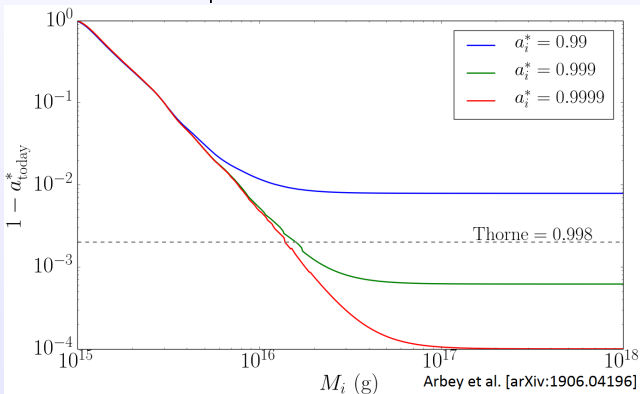


Extremal spin today?

Could high spin BHs exist today? Can we get over Thorne's limit on the spin of rotating BHs from disk accretion?

→ Yes, with sufficiently massive and extremal PBHs

PBH final spin as a function of its initial mass

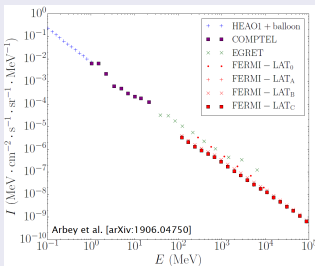


Isotropic gamma ray background (IGRB) constraints

Origin

Diffuse background +

- Active galactic nuclei
- Gamma ray bursts
- DM annihilation/decay?
- Hawking radiation?



Flux estimation for BHs

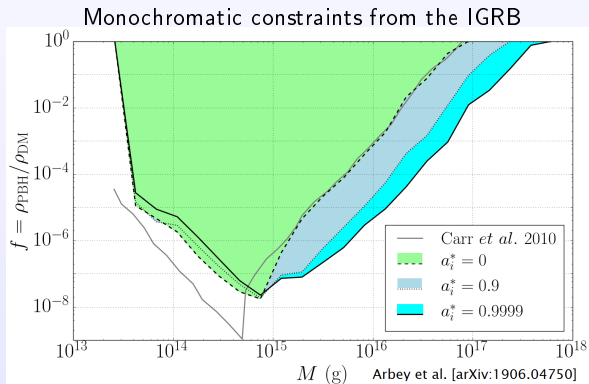
Arbey et al. [arXiv:1906.04750]

$$I \approx \frac{1}{4\pi} E \int_{t_{\text{CMB}}}^{t_{\text{today}}} (1 + z(t)) \times \int_M \left[\frac{dn}{dM} \frac{d^2N}{dt dE} (M, (1 + z(t))E) dM \right] dt$$

IGRB and Kerr PBHs: monochromatic mass distributions

Main spin effects

- enhanced luminosity \Rightarrow stronger constraints
- reduced temperature \Rightarrow reduced emission energy \Rightarrow weaker constraints

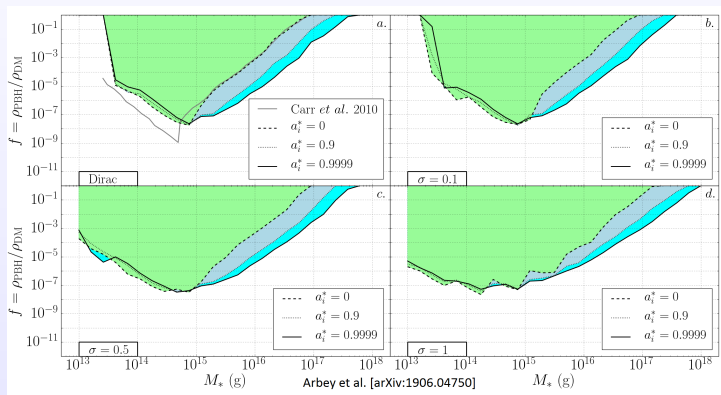


IGRB and Kerr PBHs: Extension to broad mass functions

Main width effects

$$Md_n/dM \propto \exp(-\ln(M/M_*)^2/2\sigma^2)$$

- broadening of the spectrum \Rightarrow stronger constraint
- broadening of the mass distribution \Rightarrow greater DM total density \Rightarrow weaker constraint



Public C code computing Hawking radiation:

- Schwarzschild & Kerr PBHs
- primary spectra of all Standard Model fundamental particles
- secondary spectra of stable particles (hadronization with PYTHIA or HERWIG)
- extended mass functions
- time evolution of the PBHs

Download: <http://blackhawk.hepforge.org>

Manual: [arXiv:1905.04268](https://arxiv.org/abs/1905.04268)

- Home
- Description
- Manual
- Download
- Contact

BlackHawk

By **Alexandre Arbey** and **Jérémy Auffinger**

Calculation of the Hawking evaporation spectra of any black hole distribution

BlackHawk is a public C program for calculating the Hawking evaporation spectra of any black hole distribution. This program enables the users to compute the primary and secondary spectra of stable or long-lived particles generated by Hawking radiation of the distribution of black holes, and to study their evolution in time.

If you use BlackHawk to publish a paper, please cite:

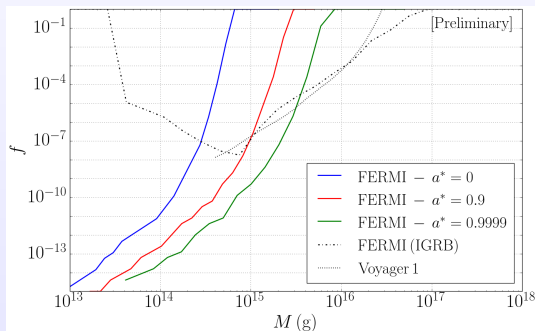
A. Arbey and J. Auffinger, [arXiv:1905.04268 \[gr-qc\]](https://arxiv.org/abs/1905.04268)

For any comment, question or bug report please contact us.

Ongoing work on Kerr PBHs

- Big Bang Nucleosynthesis (see e.g. Sedel'nikov 1996, Kohri 2000)
- galactic gamma & X-rays (see e.g. Ballestros *et al.* [arXiv:1906.10113])
- galactic positrons (see e.g. Boudaud & Cirelli [arXiv:1807.03075], DeRocco & Graham [arXiv:1906.07740], Laha [arXiv:1906.09994])
- ...

Dwarf spheroidal (dSph) gamma ray constraints from FERMI-LAT



Conclusions

Main results

- New public code `BlackHawk` to compute the Hawking radiation
- Study of the evolution of Kerr PBHs and constraints from IGRB
- Extension to more realistic broad PBH mass functions

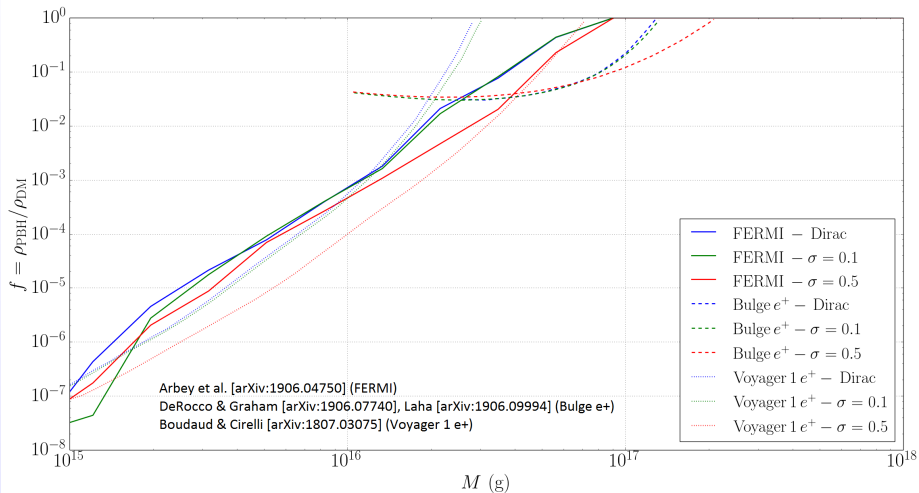
Perspectives

- Closing the remaining PBH mass windows for all DM into PBHs?
- Primordial BH / Astrophysical BH discrimination using GW events?
- Other constraints...

Publications

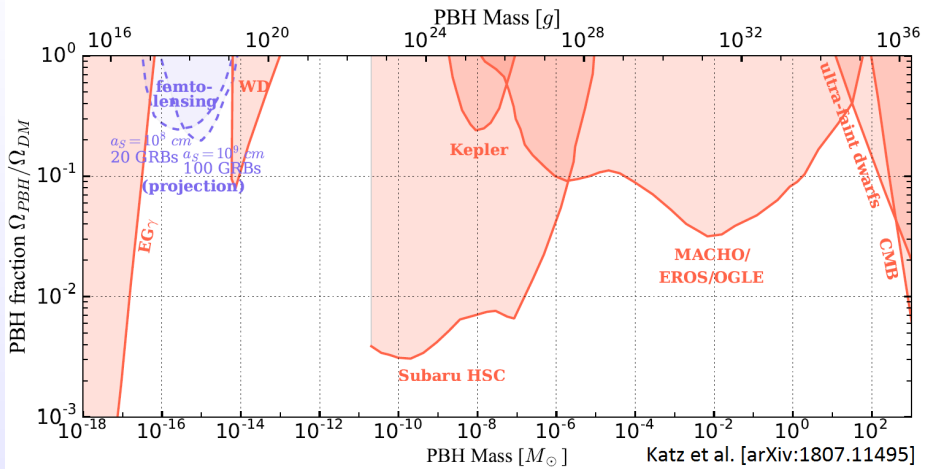
- `BlackHawk`: <http://blackhawk.hepforge.org> [1905.04268]
- Any extremal black holes are primordial [1906.04196]
- Constraining primordial black hole masses with the isotropic gamma ray background [1906.04750]

Backup

Comparison with recent e^+ constraints

Other constraints

Monochromatic constraints with femtolensing prospects



Katz et al. [arXiv:1807.11495]

Kerr Hawking radiation equations

Kerr metric

$$ds^2 = \left(1 - \frac{2Mr}{\Sigma^2}\right) dt^2 + \frac{4a^* M^2 r \sin(\theta)^2}{\Sigma^2} dt d\phi - \frac{\Sigma^2}{\Delta} dr^2 \\ - \Sigma^2 d\theta^2 - \left(r^2 + (a^*)^2 M^2 + \frac{2(a^*)^2 M^3 r \sin(\theta)^2}{\Sigma^2}\right) \sin(\theta)^2 d\phi^2$$

$$\Sigma \equiv r^2 + (a^*)^2 M^2 \cos(\theta)^2 \text{ and } \Delta \equiv r^2 - 2Mr + (a^*)^2 M^2$$

Equations of motion in free space

$$\text{Dirac: } (i\cancel{\partial} - \mu)\psi = 0 \text{ (fermions)}$$

$$\text{Proca: } (\square + \mu^2)\phi = 0 \text{ (bosons)}$$

$$\mu = \text{rest mass}$$

Kerr Hawking radiation equations

Teukolsky radial equation

$$\frac{1}{\Delta^s} \frac{d}{dr} \left(\Delta^{s+1} \frac{dR}{dr} \right) + \left(\frac{K^2 + 2i s(r-M)K}{\Delta} - 4i sEr - \lambda_{slm} - \mu^2 r^2 \right) R = 0$$

R radial component of ψ/ϕ

$K \equiv (r^2 + a^2)E + a m$, $s = \text{spin}$, $l = \text{angular momentum}$ and $m = \text{projection}$

Transformation into a Schrödinger equation

Change $\psi/\phi \rightarrow Z$ and $r \rightarrow r^*$ (generalized Eddington - Finkelstein coordinate)
(Chandrasekhar & Detweiler 1970s)

$$\frac{d^2 Z}{dr^{*2}} + (E^2 - V(r^*))Z = 0 \quad (1)$$

Solved with purely outgoing solution $Z \xrightarrow{r^* \rightarrow -\infty} e^{-iEr^*}$

Transmission coefficient $\Gamma \equiv |Z_{\text{out}}^{+\infty} / Z_{\text{out}}^{\text{horizon}}|^2$

Chandrasekhar potentials

$$V_0(r) = \frac{\Delta}{\rho^4} \left(\lambda_{0lm} + \frac{\Delta + 2r(r-M)}{\rho^2} - \frac{3r^2\Delta}{\rho^4} \right)$$

$$V_{1/2,\pm}(r) = (\lambda_{1/2lm} + 1) \frac{\Delta}{\rho^4} \mp \frac{\sqrt{(\lambda_{1/2,l,m} + 1)\Delta}}{\rho^4} \left((r-M) - \frac{2r\Delta}{\rho^2} \right)$$

$$V_{1,\pm}(r) = \frac{\Delta}{\rho^4} \left((\lambda_{1lm} + 2) - \alpha^2 \frac{\Delta}{\rho^4} \mp i\alpha\rho^2 \frac{d}{dr} \left(\frac{\Delta}{\rho^4} \right) \right)$$

$$V_2(r) = \frac{\Delta}{\rho^8} \left(q - \frac{\rho^2}{(q - \beta\Delta)^2} \left((q - \beta\Delta) (\rho^2\Delta q'' - 2\rho^2q - 2r(q'\Delta - q\Delta')) \right) \right. \\ \left. + \rho^2(\kappa\rho^2 - q' + \beta\Delta')(q'\Delta - q\Delta') \right)$$

$$\rho^2 \equiv r^2 + \alpha^2 \text{ and } \alpha^2 \equiv a^2 + am/E$$

$$q(r) = \nu\rho^4 + 3\rho^2(r^2 - a^2) - 3r^2\Delta$$

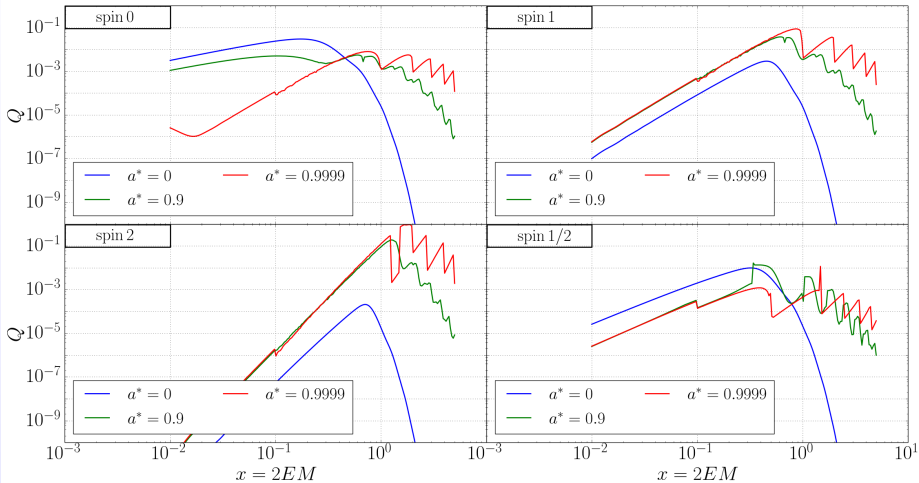
$$q'(r) = r \left((4\nu + 6)\rho^2 - 6(r^2 - 3Mr + 2a^2) \right)$$

$$q''(r) = (4\nu + 6)\rho^2 + 8\nu r^2 - 6r^2 + 36Mr - 12a^2$$

$$\beta_{\pm} = \pm 3\alpha^2$$

$$\kappa_{\pm} = \pm \sqrt{36M^2 - 2\nu(\alpha^2(5\nu + 6) - 12a^2) + 2\beta\nu(\nu + 2)}$$

Luminosities for all spins



Evolution parameters

Page parameters (Page 1976)

$$f(M, a^*) \equiv -M^2 \frac{dM}{dt} = M^2 \int_0^{+\infty} \sum_{\text{dof.}} \frac{E}{2\pi} \frac{\Gamma(E, M, a^*)}{e^{E'/T} \pm 1} dE$$

$$g(M, a^*) \equiv -\frac{M}{a^*} \frac{dJ}{dt} = \frac{M}{a^*} \int_0^{+\infty} \sum_{\text{dof.}} \frac{m}{2\pi} \frac{\Gamma(E, M, a^*)}{e^{E'/T} \pm 1} dE$$

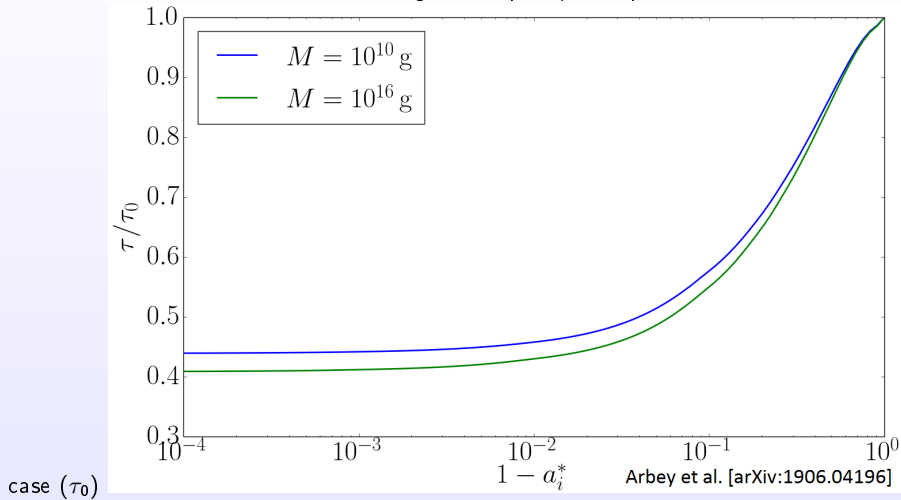
Evolution equations (Page 1976)

$$\frac{dM}{dt} = -\frac{f(M, a^*)}{M^2}$$

$$\frac{da^*}{dt} = \frac{a^*(2f(M, a^*) - g(M, a^*))}{M^3}$$

Reduced lifetime

Decrease of BH lifetime τ for increasing initial spin a_i^* , compared to the Schwarzschild



Log-normal distributions

Definition

$$\frac{dn}{dM} = \frac{A}{\sqrt{2\pi}\sigma M} \exp\left(-\frac{(\log(M/M_*))^2}{2\sigma^2}\right)$$

M^* = central mass, σ = width (dimensionless)

Log-normal distributions (normalized to unity, $M^* = 3 \times 10^{15}$ g)

