



Resonant dark matter annihilation in a gauge-independent manner

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MD, Bohdan Grządkowski, Apostolos Pilaftsis, *Gauge-Independent Approach to Resonant Dark Matter Annihilation,* JHEP 1902 (2019) 141 [1812.11944]

MD, Bohdan Grządkowski, *Resonance enhancement of dark matter interactions,* JHEP 1709 (2017) 159 [1705.10777]

Dark matter – motivation





Convincing evidence on various astrophysical and cosmological scales





leading hypothesis → new, unknown particle

Resonant DM annihilation in a gauge-independent manner

Resonance region



Resonant DM annihilation in a gauge-independent manner

Breit-Wigner resonance

Breit-Wigner resonance $2M_{\rm DM} pprox M_{\rm R}$

enhanced annihilation \rightarrow suppressed coupling

- low sensitivity to direct detection
- velocity dependent cross-section → possibility of enhanced indirect detection signals
- kinetic decoupling $T_{\mathrm{DM}}
 eq T_{\mathrm{SM}}$
- large self-interaction cross-section constrained by indirect detection
- proper description of annihilation amplitudes
 Is Breit-Wigner approximation applicable?



Breit-Wigner resonance



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Resonant cross-section

$$\simeq \frac{1}{s} \sum_{f \neq i} \frac{M_R^2 \Gamma_R^2 B_i B_f}{(s - M_R^2)^2 + M_R^2 \Gamma_R^2}$$

$$\delta = \frac{4M_{DM}^2}{M_R^2} - 1, \qquad \gamma = \frac{\Gamma_R}{M_R}$$
 resonance position , width

- strong temperature dependence
- thermally averaged cross section grows with falling temperature
- enhanced indirect detection signal

Resummed propagator



Abelian vector dark matter

Additional complex scalar field S

• singlet of
$$U(1)_Y \times SU(2)_L \times SU(3)_c$$
, charged under $U(1)_X$
 $\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + (D_\mu S)^* D^\mu S + \tilde{V}(H, S)$
 $V(H, S) = -\mu_H^2 |H|^2 + \lambda_H |H|^4 - \mu_S^2 |S|^2 + \lambda_S |S|^4 + \kappa |S|^2 |H|^2$
Vacuum expectation values: $\langle H \rangle = \frac{v_{SM}}{\sqrt{2}}$, $\langle S \rangle = \frac{v_x}{\sqrt{2}}$

Dark $U(1)_X$ vector gauge boson X_{μ}

• Stability condition - no mixing of $U(1)_X$ with $U(1)_Y = B_{\mu\nu} V^{\mu\nu}$ $\mathcal{Z}_2: V_\mu \to -V_\mu, \qquad S \to S^*, \qquad S = \phi e^{i\sigma}: \phi \to \phi, \ \sigma \to -\sigma$

• Higgs mechanism in the hidden sector $M_X = g_x v_x$

Higgs couplings – mixing angle α , $M_{h_1} = 125 \text{ GeV}$

$$\mathcal{L} \supset \frac{h_1 c_{\alpha} + h_2 s_{\alpha}}{v} \left(2M_W W^+_{\mu} W^{\mu-} + M_Z^2 Z_{\mu} Z^{\mu} - m_f \bar{f} f \right) + \frac{h_1 s_{\alpha} - h_2 c_{\alpha}}{v_x} M_X^2 X_{\mu} X^{\mu}$$

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 $\sqrt{2}$

Problems with resummation in R_ε gauge

$$h_i \longrightarrow h_j$$

Dark vector contribution to the Higgs self-energy in R_{ϵ} gauge

$$\begin{split} \Pi_{ij}^{(XX)}(s) &= \frac{g_x^2 R_{2i} R_{2j}}{32\pi^2 M_X^2} \Big[\left(s^2 - 4M_X^2 s + 12M_X^4 \right) B_0(s, M_X^2, M_X^2) \\ &- \left(s^2 - m_i^2 m_j^2 \right) B_0(s, \xi_X M_X^2, \xi_X M_X^2) \Big] \\ \end{split}$$
Problems with self-energy:
$$\begin{split} \mathrm{Im} B_0(s, M_X^2, M_X^2) &\sim \sqrt{1 - 4M_X^2/s} \end{split}$$

- explicit dependence on gauge fixing parameter
- presence of s² term modification of high-energy behavior
- unphysical threshold at $s=\xi_X M_X^2$

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Pinch Technique

Reorganization of the sub-amplitudes that have the same kinematical properties



We have to look for the propagator-like pieces inside vertex and box diagrams

- PT algorithm: employ Ward identities
- equivalent to calculation in Background Field Method ($\xi_0 = 1$)

Cornwall 1989 Denner+ 1994, Papavasilliou, Pilaftsis 1995 Binosi+ 2002

Model with mixed scalars

$$\begin{split} & \text{Contributions to Higgs self-energy X, Z, W, f, h} \\ \widehat{\Pi}_{ij}^{(XX)}(s) \ = \ \frac{g_x^2 R_{2i} R_{2j}}{8\pi^2} \left[\frac{(m_i m_j)^2}{4M_X^2} + \frac{m_i^2 + m_j^2}{2} - (2s - 3M_X^2) \right] B_0(s, M_X^2, M_X^2) \,, \\ \widehat{\Pi}_{ij}^{(ZZ)}(s) \ = \ \frac{g^2 R_{1i} R_{1j} M_Z^2}{32\pi^2 M_W^2} \left[\frac{(m_i m_j)^2}{4M_X^2} + \frac{m_i^2 + m_j^2}{2} - (2s - 3M_Z^2) \right] B_0(s, M_Z^2, M_Z^2) \,, \\ \widehat{\Pi}_{ij}^{(WW)}(s) \ = \ \frac{g^2 R_{1i} R_{1j}}{32\pi^2} \left[\frac{(m_i m_j)^2}{4M_X^2} + \frac{m_i^2 + m_j^2}{2} - (2s - 3M_W^2) \right] B_0(s, M_W^2, M_W^2) \,, \end{split} \quad \text{no fictitious thresholds} \\ \widehat{\Pi}_{ij}^{(tt)}(s) \ = \ \frac{3g^2 R_{1i} R_{1j} m_t^2}{32\pi^2 M_W^2} \left(s - 4m_t^2 \right) B_0(s, m_t^2, m_t^2) \,, \end{aligned}$$

Resummation of the propagator with scalar mixing

$$i\widehat{\Delta} = i\Delta_0 + i\Delta_0 i\widehat{\Pi} i\Delta_0 + i\Delta_0 (i\widehat{\Pi} i\Delta_0)^2 + \dots$$

diagonal tree-level propagator

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$$\widehat{\Delta}(s) = \frac{1}{D(s)} \begin{pmatrix} s - m_2^2 + \widehat{\Pi}_{22}(s) & -\widehat{\Pi}_{12}(s) \\ -\widehat{\Pi}_{21}(s) & s - m_1^2 + \widehat{\Pi}_{11}(s) \end{pmatrix}$$

$$D(s) = \left[s - m_1^2 + \widehat{\Pi}_{11}(s)\right] \left[(s - m_2^2 + \widehat{\Pi}_{22}(s)) - \widehat{\Pi}_{12}(s)\widehat{\Pi}_{21}(s)\right]$$

Born-improved amplitude

Pinch technique self-energy and one-loop corrected vertices:



Tree-level like Ward identities are satisfied by the PT self-energies and vertices

$$\begin{split} p_{2}^{\nu} \widehat{V}_{\mu\nu}^{h_{i}XX}(q,p_{1},p_{2}) &+ iM_{X} \widehat{V}_{\mu}^{h_{i}XG_{X}} = -g_{x} R_{2i} \widehat{\Pi}_{\mu}^{XG_{X}}(p_{1}) \\ p_{1}^{\mu} \widehat{V}_{\mu}^{h_{i}XG_{X}} &+ iM_{X} \widehat{V}^{h_{i}G_{X}G_{X}} = -g_{x} \Big[R_{2j} \widehat{\Pi}_{ji}(q^{2}) + R_{2i} \widehat{\Pi}^{G_{X}G_{X}}(p_{2}) \Big], \\ p_{1}^{\mu} p_{2}^{\nu} \widehat{V}_{\mu\nu}^{h_{i}XX} &+ M_{X}^{2} \widehat{V}^{h_{i}G_{X}G_{X}} = ig_{x} M_{X} \Big[R_{2j} \widehat{\Pi}_{ji}(q^{2}) + R_{2i} \Big(\widehat{\Pi}^{G_{X}G_{X}}(p_{1}) + \widehat{\Pi}^{G_{X}G_{X}}(p_{2}) \Big) \Big] \\ \widehat{\Pi}_{\mu}^{XG_{X}}(p) &= -\frac{iM_{X} p_{\mu}}{p^{2}} \widehat{\Pi}^{G_{X}G_{X}}(p^{2}) \end{split}$$

Generalized equivalence theorem satisfied

Proper high-energy behaviour as required by unitarity

$$p_1^{\mu} p_2^{\nu} \widehat{\Gamma}_{\mu\nu}^{h_i XX}(q, p_1, p_2) = i g_x M_X R_{2j} \widehat{\Delta}_{ji}^{-1}(q^2) + \mathcal{O} \left[\ln(s/M_X^2) \right]$$

Cross-section for XX->bb process

standard Breit-Wigner approximation fails



No SM thresholds near the resonance \rightarrow BW approximation applicable

$$\Gamma_{h_i \to \text{SMSM}} = \text{Im} \Pi_{ii}^{(\text{SMSM})} (m_i^2) / m_i$$

For DM contribution, we cannot be use constant width, but

$$\Gamma_{h_i \to XX} = \sqrt{\frac{1 - 4M_X^2/s}{1 - 4M_X^2/m_i^2}} \frac{\operatorname{Im} \Pi_{ii}^{(XX)}(m_i^2)}{m_i} \theta \left(s - 4M_X^2\right)$$
leading energy-dependent contribution gauge-independent quantity

Relic density calculation



standard Breit-Wigner approximation

effects of early kinetic decoupling included [1705.10777]

standard Breit-Wigner vs. PT resummation

underestimated indirect detection signal

overestimated annihilation rate



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- resonance region is a viable part of many otherwise strongly constraint dark matter model
- the Breit-Wigner approximation fails if mediator couples dominantly to the dark matter state
- relativistic treatment of resonant amplitude requires proper resummation technique
- pinch technique provides a method respecting the gauge invariance and unitarity what results in the proper behavior near the resonance and in the high energy limit
- in the phenomenological analyses one can use properly approximated energy-dependent width