

# Confronting Higgs couplings from D-term Extensions & Natural SUSY at the ILC

**Moritz McGarrie**

with

G.Moortgat-Pick (DESY,Hamburg) & S.Porto (Hamburg)

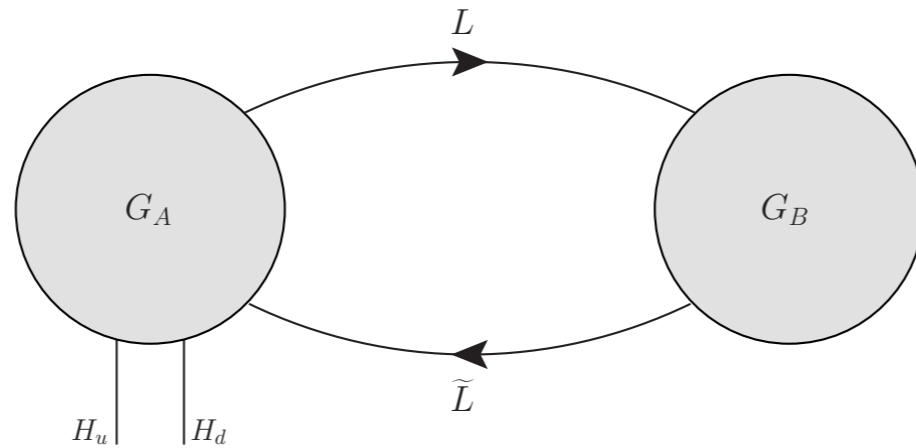
and

A.Bharucha(Marseille) & A.Goudelis(LAPTh) ArXiv:1310.4500



# Non decoupled D-terms

UV  
↓  
IR



$$V = V_{D_A} + V_{D_B} + \dots$$

- Two gauge groups
- Two D-term scalar potentials
- Higgs only charged under one
- Integrate out Linking fields
- An effective action remains
- Works for  $U(1)_Y$  &  $SU(2)_L$

at low energies  
MSSM +

$$\delta\mathcal{L} = -g_1^2 \Delta_1 (H_u^\dagger H_u - H_d^\dagger H_d)^2 - g_2^2 \Delta_2 \sum_a (H_u^\dagger \sigma^a H_u + H_d^\dagger \sigma^a H_d)^2$$

$$U(1)_A \times U(1)_B \rightarrow U(1)_Y$$

$$SU(2)_A \times SU(2)_B \rightarrow SU(2)_L$$

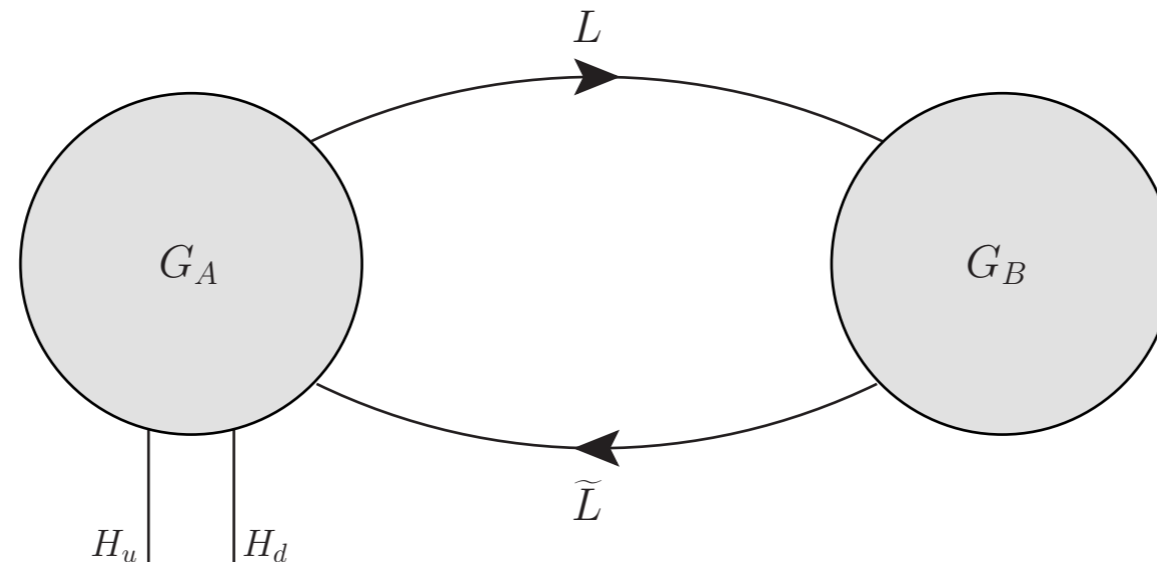
$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

$$\Delta = \left( \frac{g_A^2}{g_B^2} \right) \frac{2m_L^2}{m_v^2 + 2m_L^2}$$

$$m_z^2 \rightarrow m_z^2 + \left( \frac{g_1^2 \Delta_1 + g_2^2 \Delta_2}{2} \right) v_{ew}^2$$

Lifts the Higgs mass at tree level

# Non decoupled D-terms



## Related works:

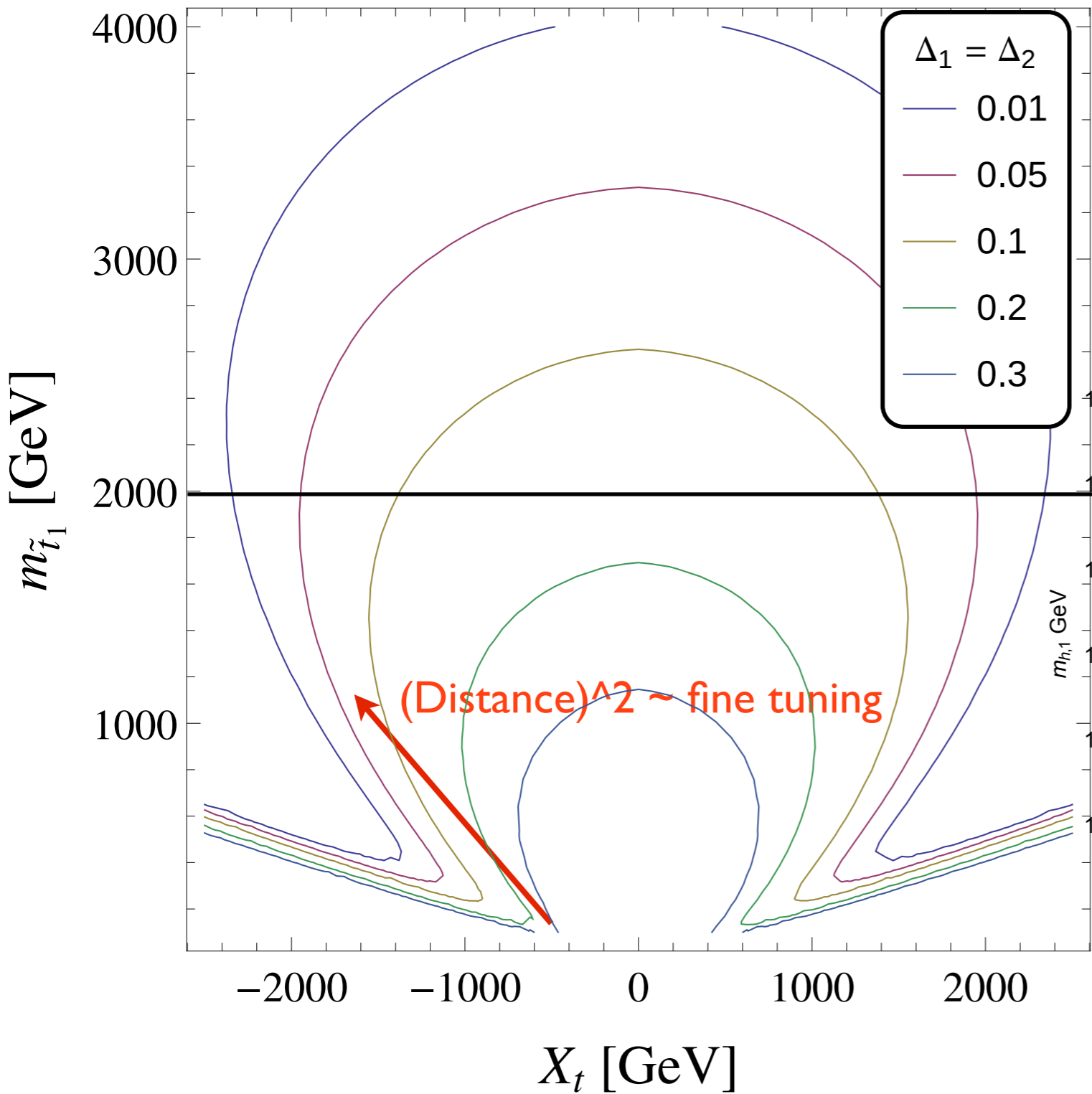
- Csaki, Erlich, Grojean, Kribs 0106044
- Batra, Delgado, Kaplan, Tait 0309149/0404251/0409073
- Medina, Shah, Wagner 0904.1625
- M.M. 1009.0012/1101.5158
- Auzzi, Giveon, Gudnason, Shacham 1009.1714/1011.1664
- Huo, Lee, Thalapillil, Wagner 1212.0560
- Craig, Katz 1212.2635
- Bharucha, Goudelis, M.M. 1310.4500
- and more .....

## Features:

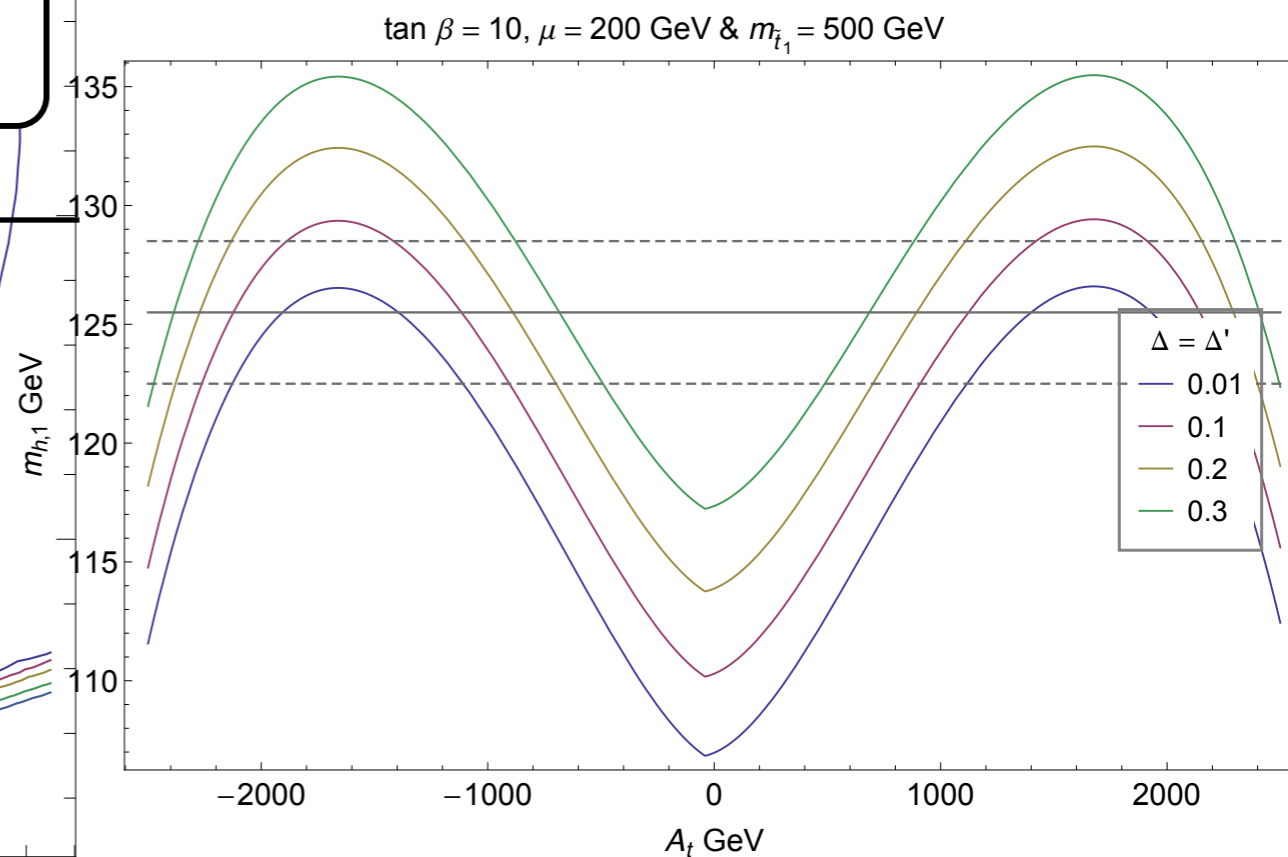
- ✓ Lifts the Higgs at **tree level**
- ✓ Allows for light stops
- ✓ More natural than NMSSM?
- ✓ embeds into magnetic SQCD
- ✓ Deconstructs an extra dimension
- ✓ “**Split families**”: Batra, Kaplan, Tait, Delgado

0404251/0409073

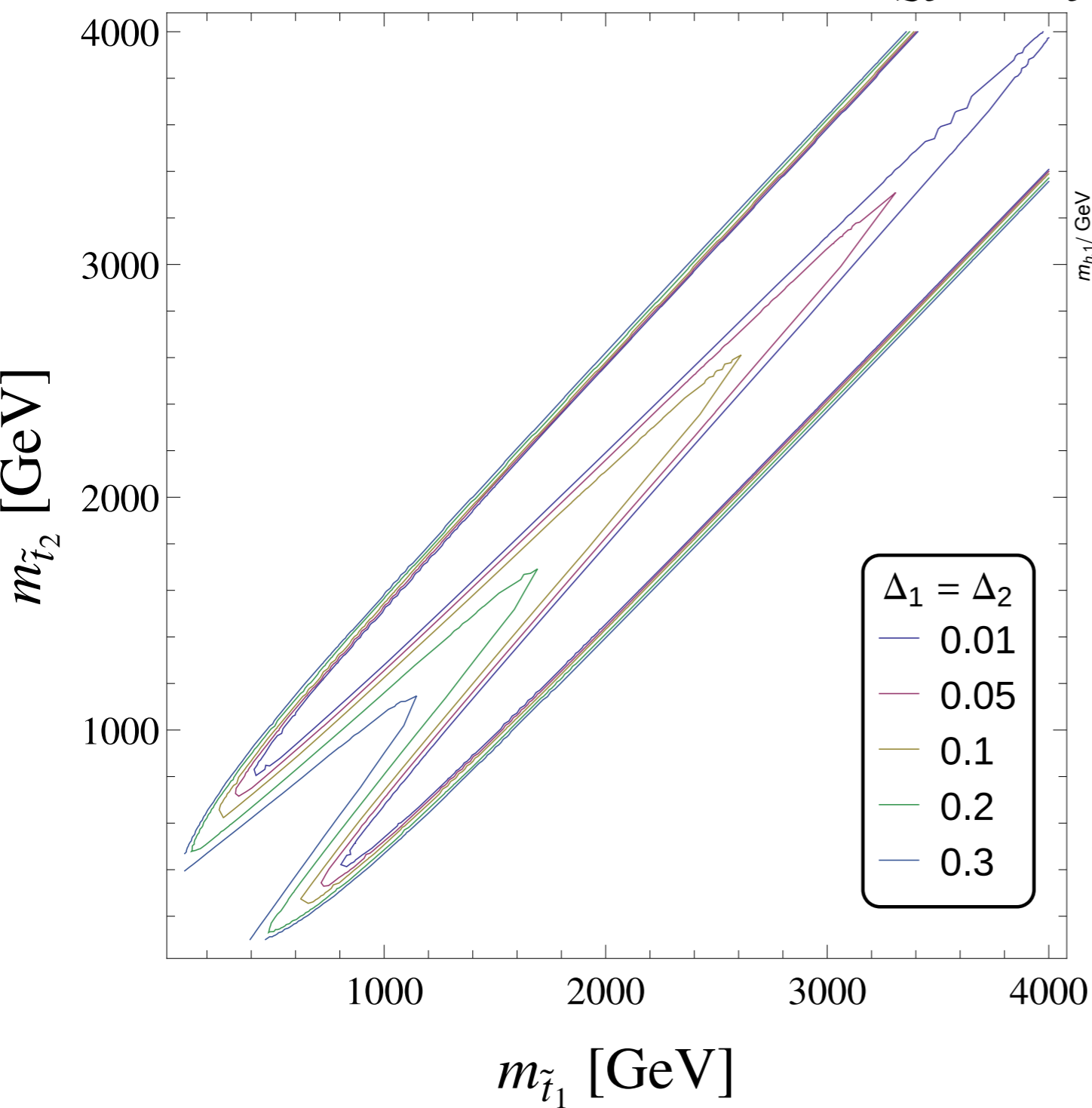
$m_h = 125.5 \text{ GeV}$ ,  $\tan \beta = 10$ ,  $m_{Q_3} = m_{U_3}$



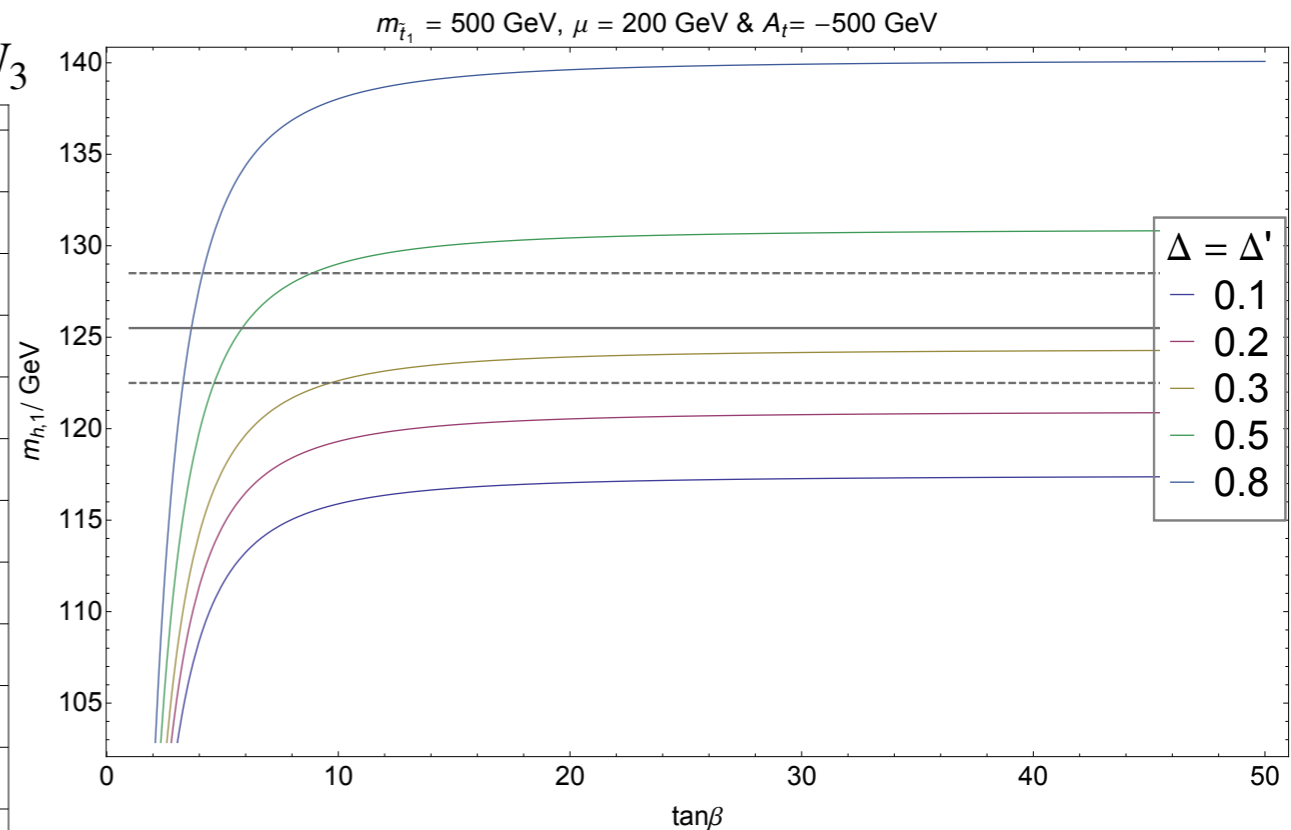
Sub 2 TeV stops  
for  $\Delta \geq 0.1$



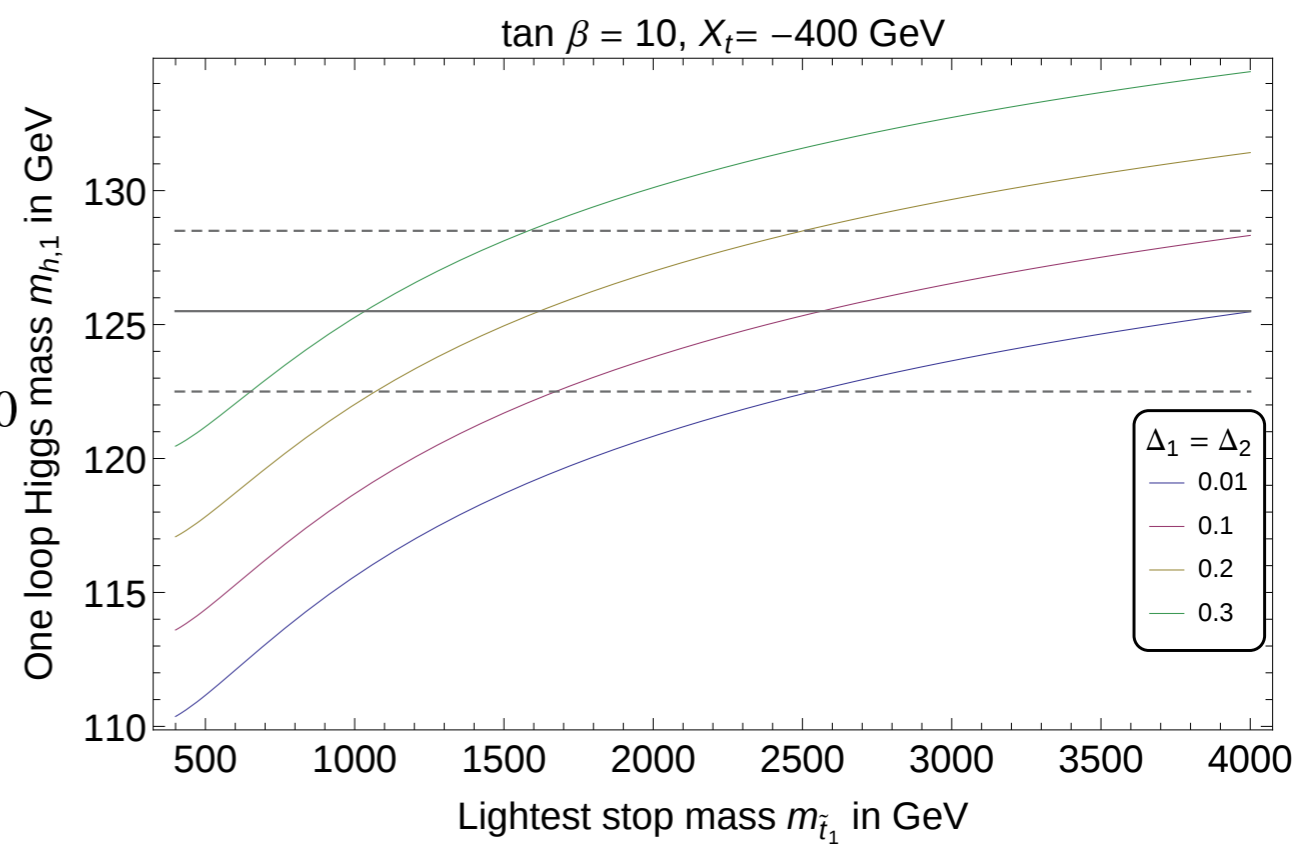
$m_h = 125.5 \text{ GeV}$ ,  $\text{Tan } \beta = 10$ ,  $m_{Q_3} = m_{U_3}$



The contribution from maximal mixing can be lowered

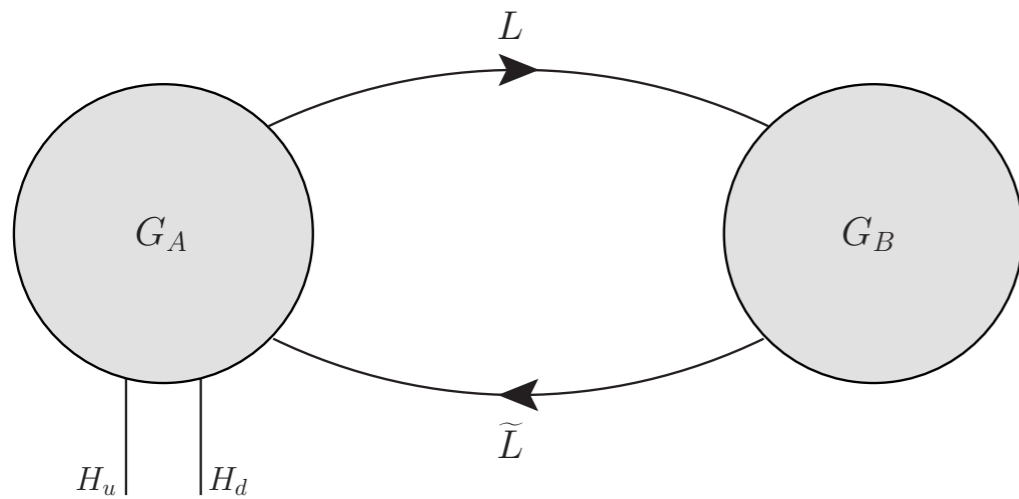


• D-term enhancement for ALL tanbeta

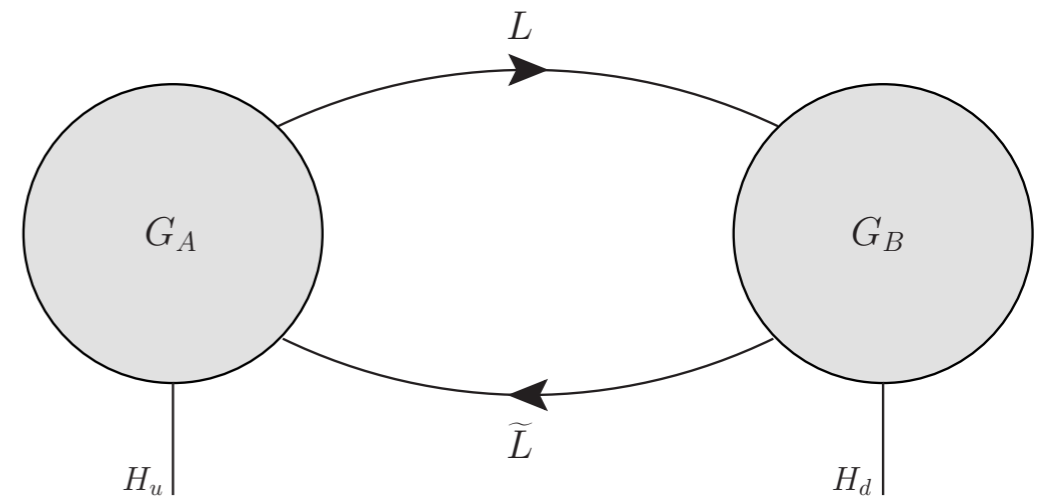


# There are two types

Vector-like



Chiral type



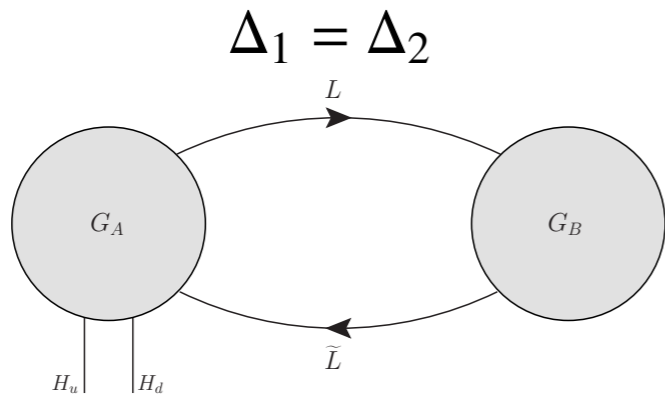
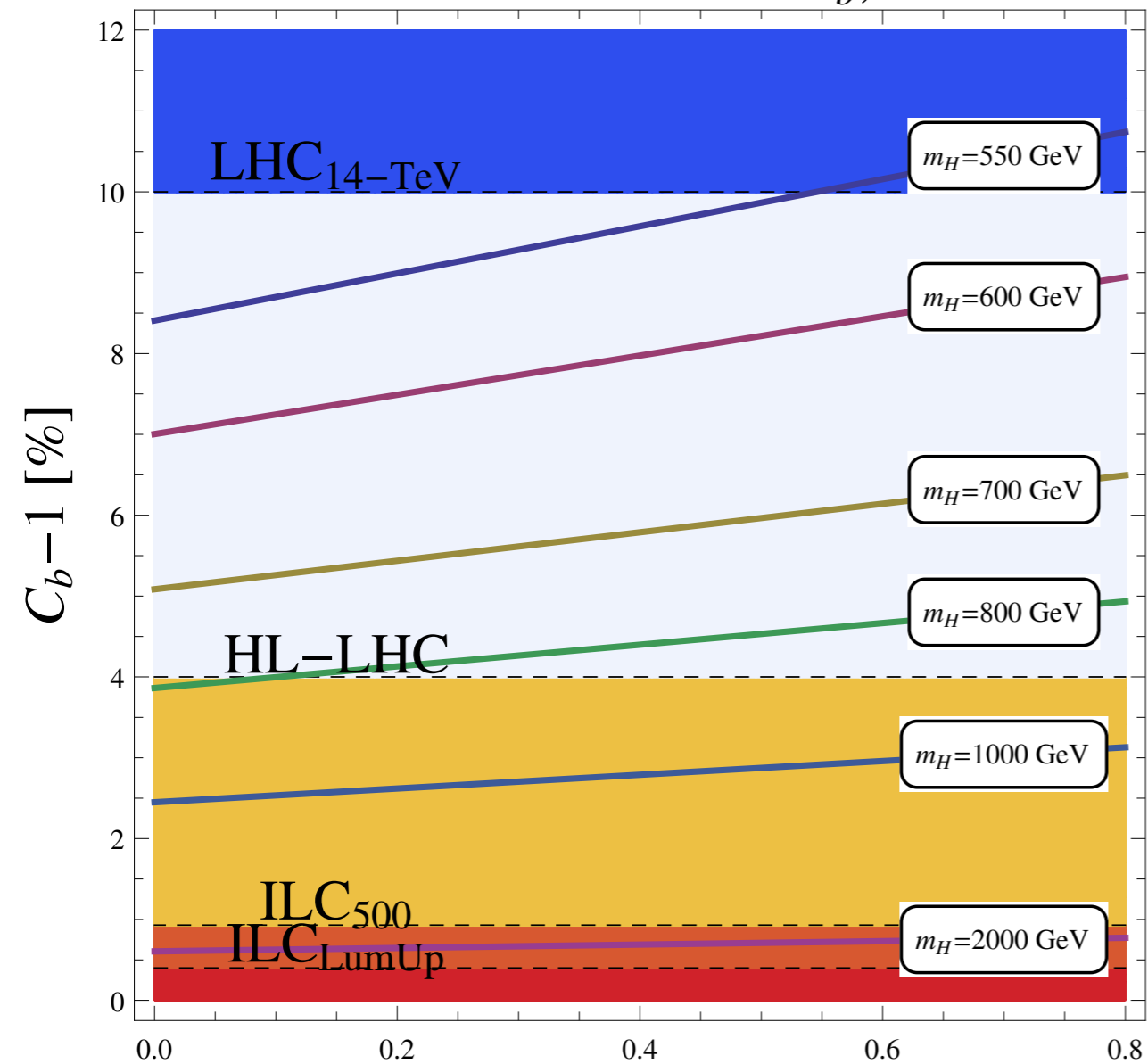
- Similar effect on Higgs mass
- Different effect on Higgs branching ratios
- Testable at the ILC

$$c_b^{\text{vector}} \simeq \left(1 - \frac{m_h^2}{m_H^2}\right)^{-1} \left(1 + \frac{[g_2^2(1 + \Delta_2) + \frac{3}{5}g_1^2(1 + \Delta_1)]v^2}{4m_H^2}\right)$$

$$c_b^{\text{chiral}} \simeq \left(1 - \frac{m_h^2}{m_H^2}\right)^{-1} \left(1 + \frac{[g_2^2(1 - \Omega_2) + \frac{3}{5}g_1^2(1 - \Omega_1)]v^2}{4m_H^2}\right)$$

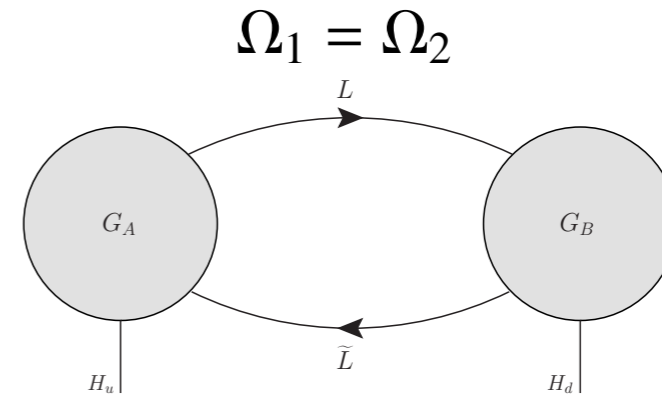
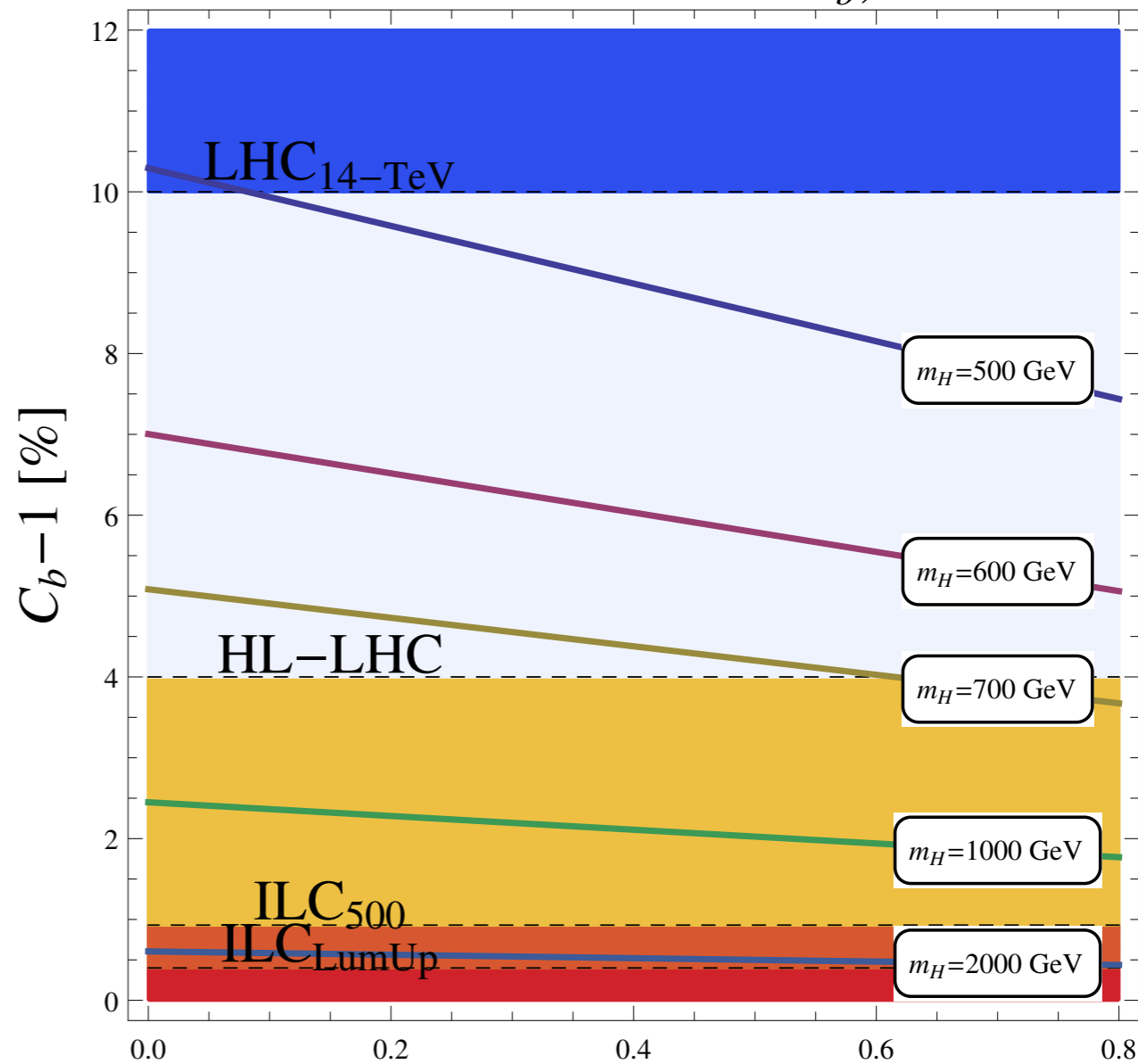
# Vector-like

LHC and ILC sensitivities to  $c_b$ , vector case



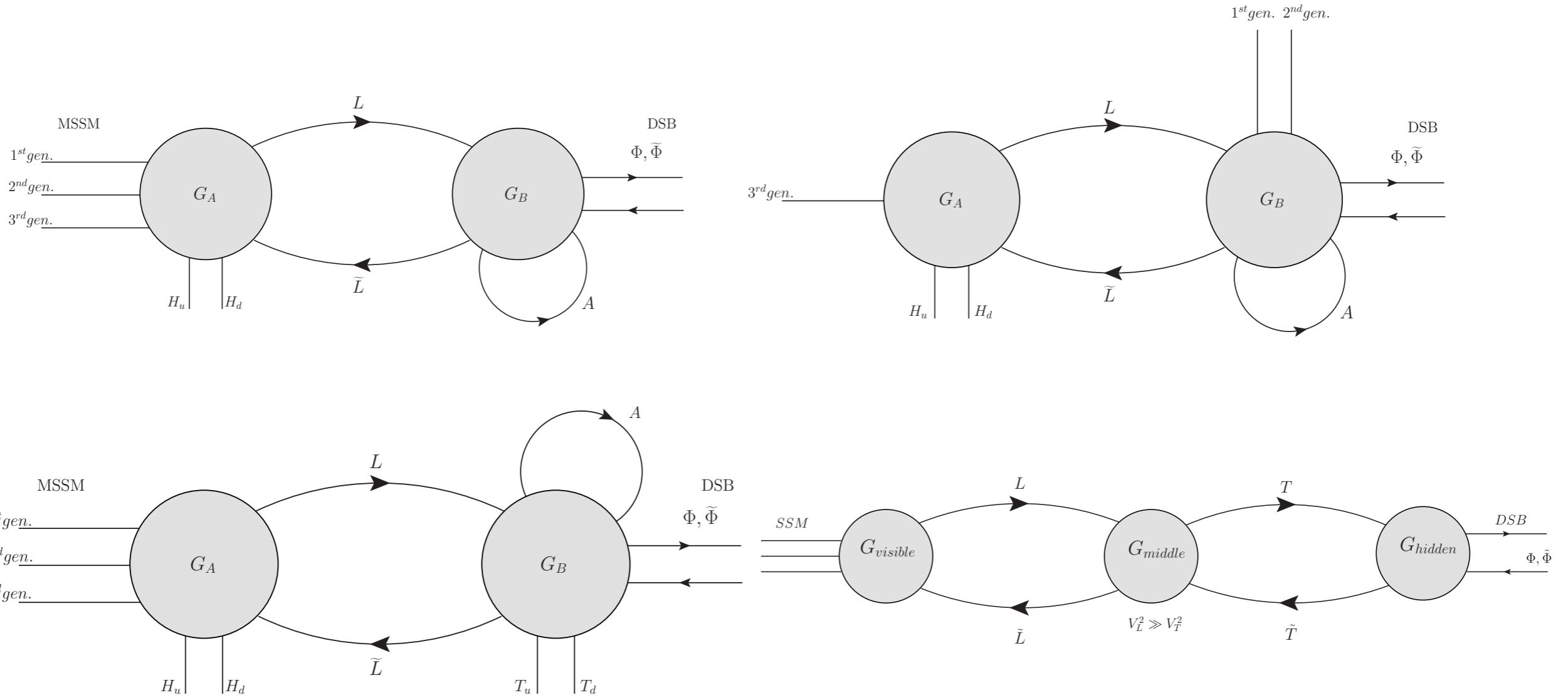
# Chiral type

LHC and ILC sensitivities to  $c_b$ , chiral case



# The Quiver Variations

## as UV completions

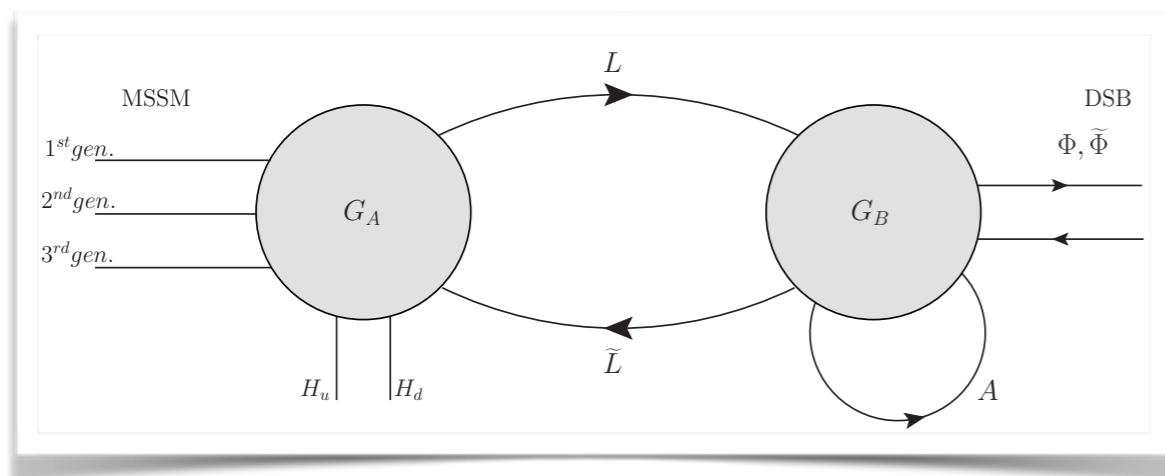




# A meta model

SF	Spin 0	Spin $\frac{1}{2}$	Generations	$(U(1)_A, SU(2)_B, SU(3)_c, U(1)_B, SU(2)_A)$	R-Parity
$\hat{q}$	$\tilde{q}$	$q$	3	$(\frac{1}{6}, 1, 3, 0, 2)$	-1
$\hat{l}$	$\tilde{l}$	$l$	3	$(-\frac{1}{2}, 1, 1, 0, 2)$	-1
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	1	$(-\frac{1}{2}, 1, 1, 0, 2)$	+1
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	1	$(\frac{1}{2}, 1, 1, 0, 2)$	+1
$\hat{d}$	$\tilde{d}_R^*$	$d_R^*$	3	$(\frac{1}{3}, 1, \bar{3}, 0, 1)$	-1
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	3	$(-\frac{2}{3}, 1, \bar{3}, 0, 1)$	-1
$\hat{e}$	$\tilde{e}_R^*$	$e_R^*$	3	$(1, 1, 1, 0, 1)$	-1
$\hat{L}$	$L$	$\psi_L$	1	$(-\frac{1}{2}, \bar{2}, 1, \frac{1}{2}, 2)$	+1
$\hat{\tilde{L}}$	$\tilde{L}$	$\psi_{\tilde{L}}$	1	$(\frac{1}{2}, 2, 1, -\frac{1}{2}, \bar{2})$	+1
$\hat{K}$	$K$	$\psi_K$	1	$(0, 1, 1, 0, 1)$	+1
$\hat{A}$	$A$	$\psi_A$	1	$(0, 3, 1, 0, 1)$	+1

**Table 2.** Matter fields of the model.



$$W_{\text{SSM}} = Y_u \hat{u} \hat{q} \hat{H}_u - Y_d \hat{d} \hat{q} \hat{H}_d - Y_e \hat{e} \hat{l} \hat{H}_d + \mu \hat{H}_u \hat{H}_d$$

$$W_{\text{Quiver}} = \frac{Y_K}{2} \hat{K} (\hat{L} \hat{\tilde{L}} - V^2) + Y_A \hat{L} \hat{A} \hat{\tilde{L}}$$

The most sophisticated model so far implemented into a spectrum generator (SARAH/SPHENO)  
 A meta-model i.e. independent of the type of supersymmetry breaking:  
 AMSB, mSUGRA, GMSB, phenomenological, other?

# Building a taylor made spectrum generator!

- We used SARAH (written by Florian Staub) mathematica package: “a spectrum generator *generator*” to write our own spectrum generator.
- We implemented 5 gauge groups with full 2-loop RGE’s and one loop self energies (soon 6 and 9 gauge groups!).
- Higgsing, and breaking to the diagonal 4 gauge groups, including all mixing matrices and assignment of Goldstones, Ghosts, RGEs of vevs, and Bmu at 2 loop.
- All 3 and 4 vertices of all fields computed, and self energies.
- All anomalous dimensions, tadpoles and running of all *additional soft terms and additional Yukawas, at 2 loop level.*
- finite shifts and threshold corrections also accounted for
- Can talk to FeynArts, FormCalc, CalcHep, HiggsSignals, HiggsBounds, WHIZARD, micrOMEGAS, Vevacious and more.

Quiver @  
M messenger

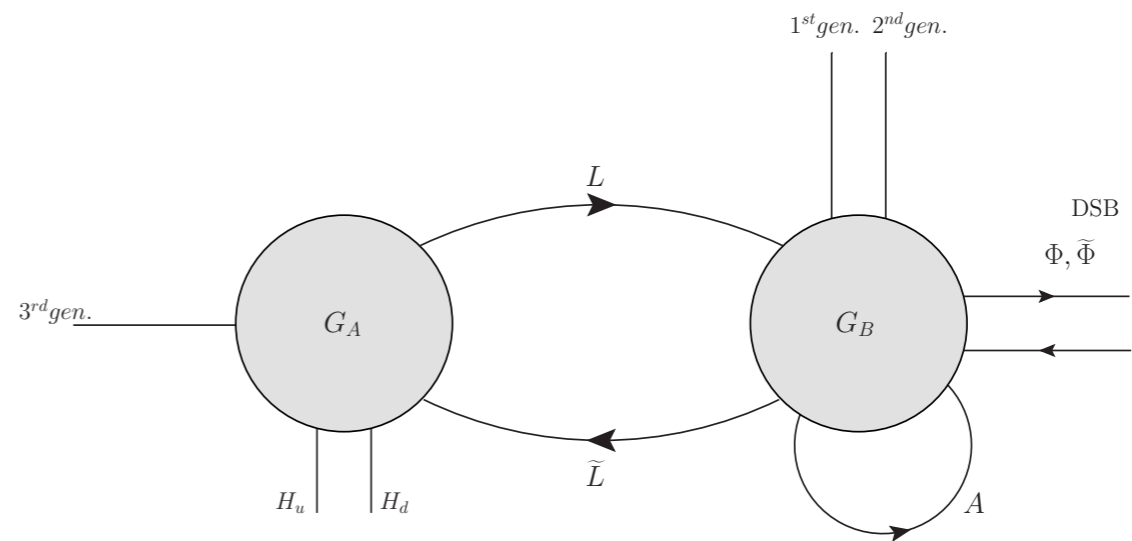
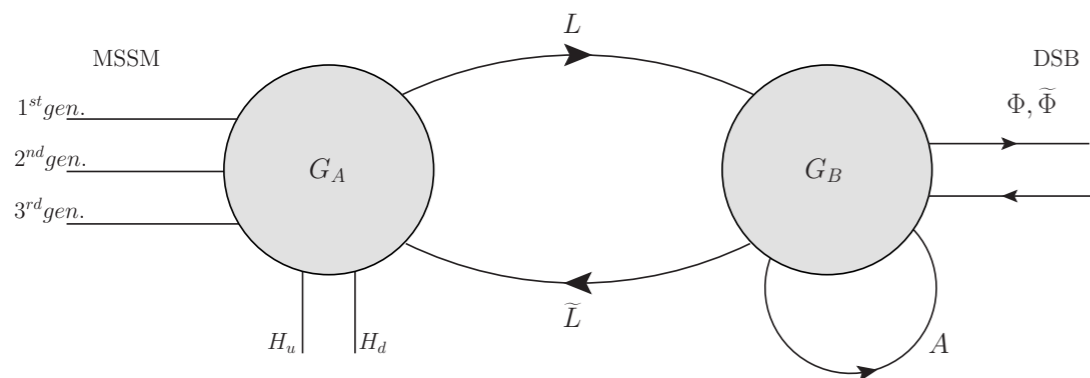
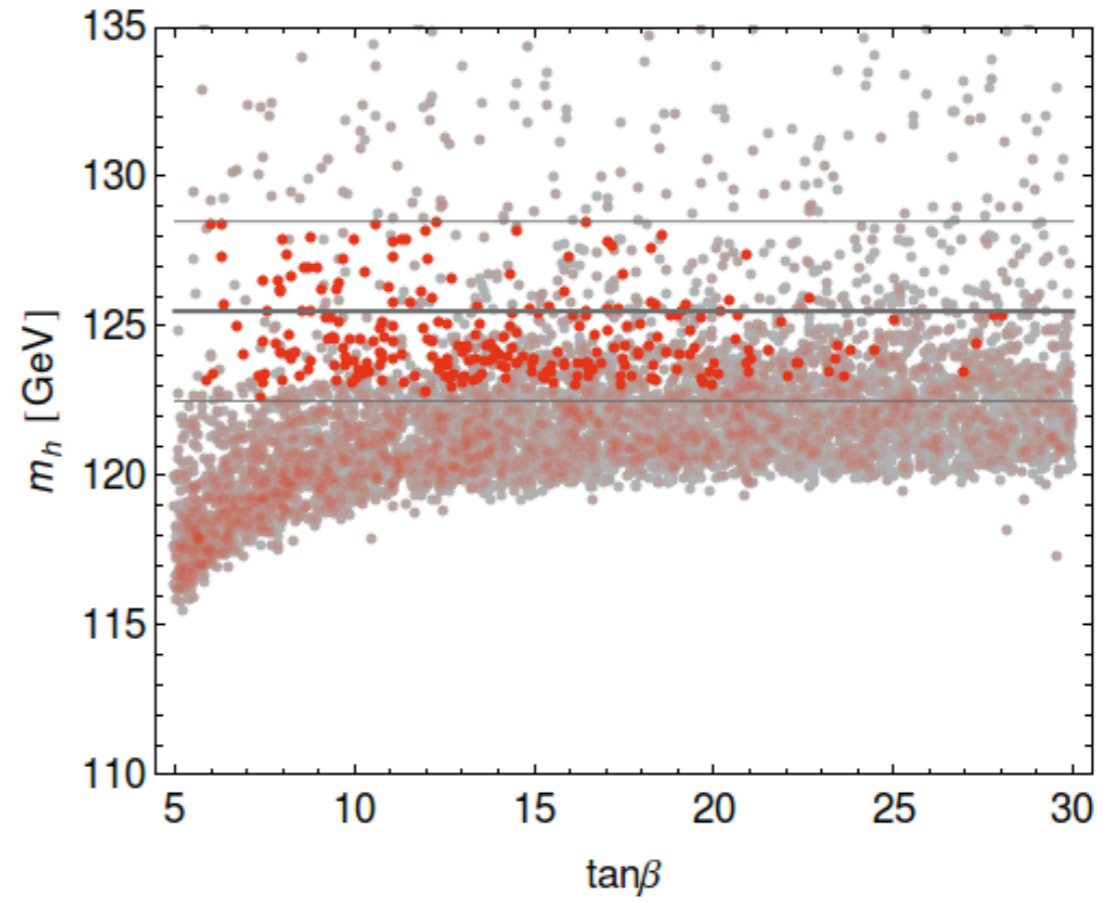
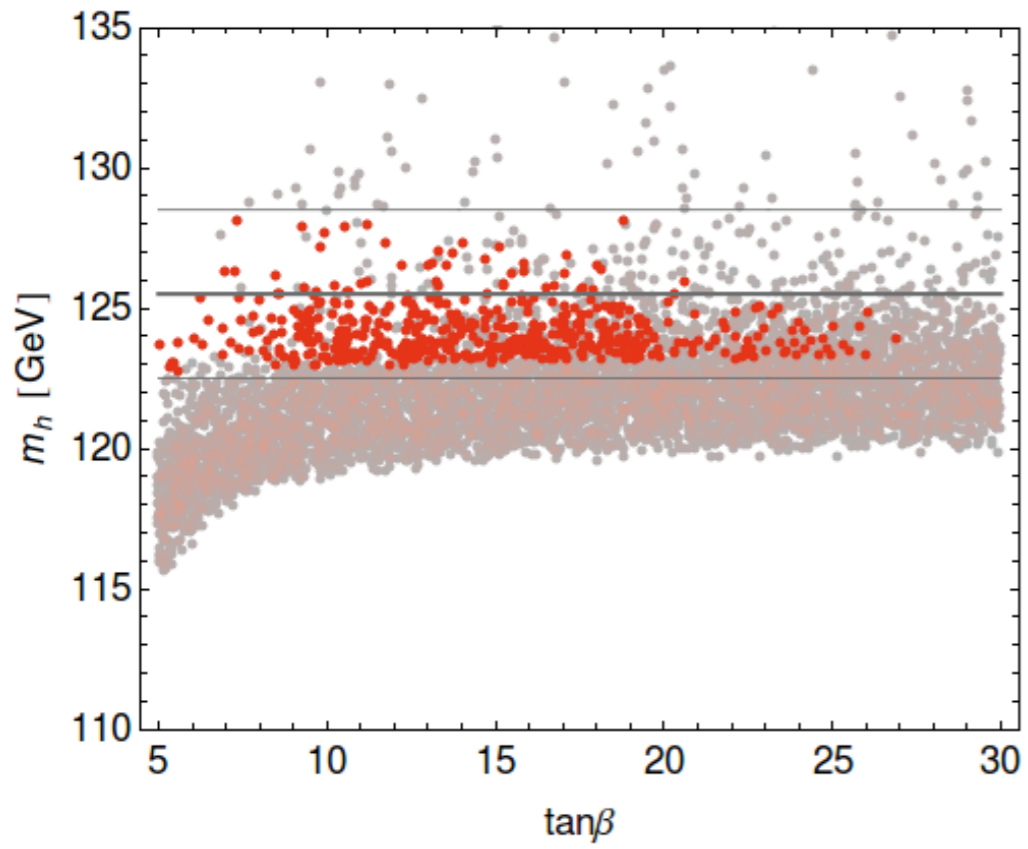


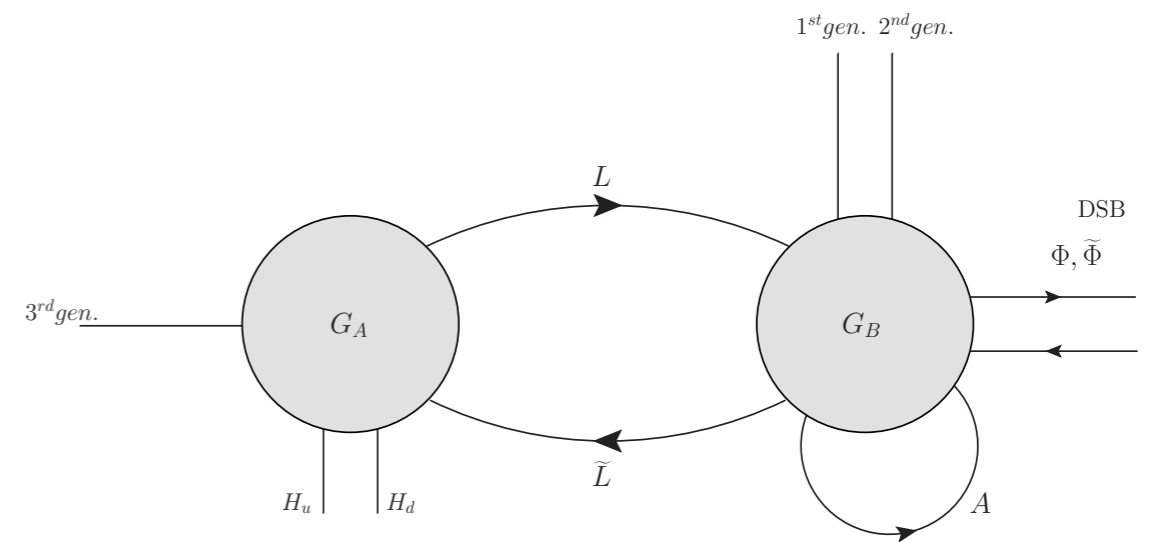
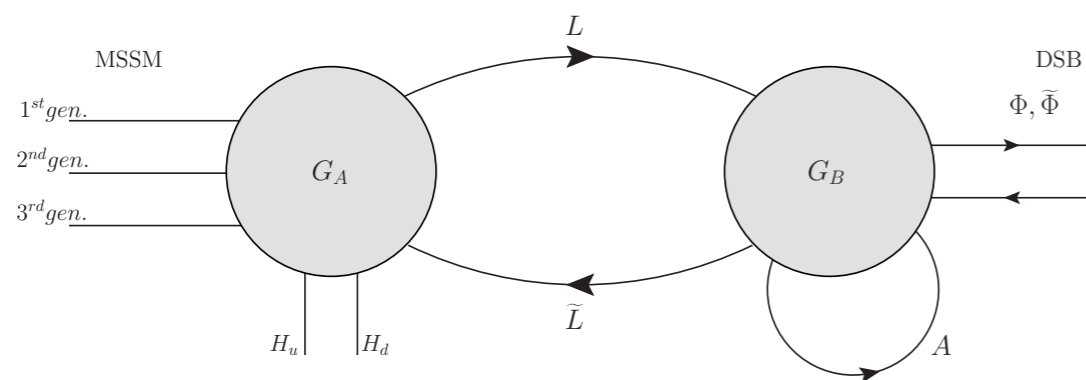
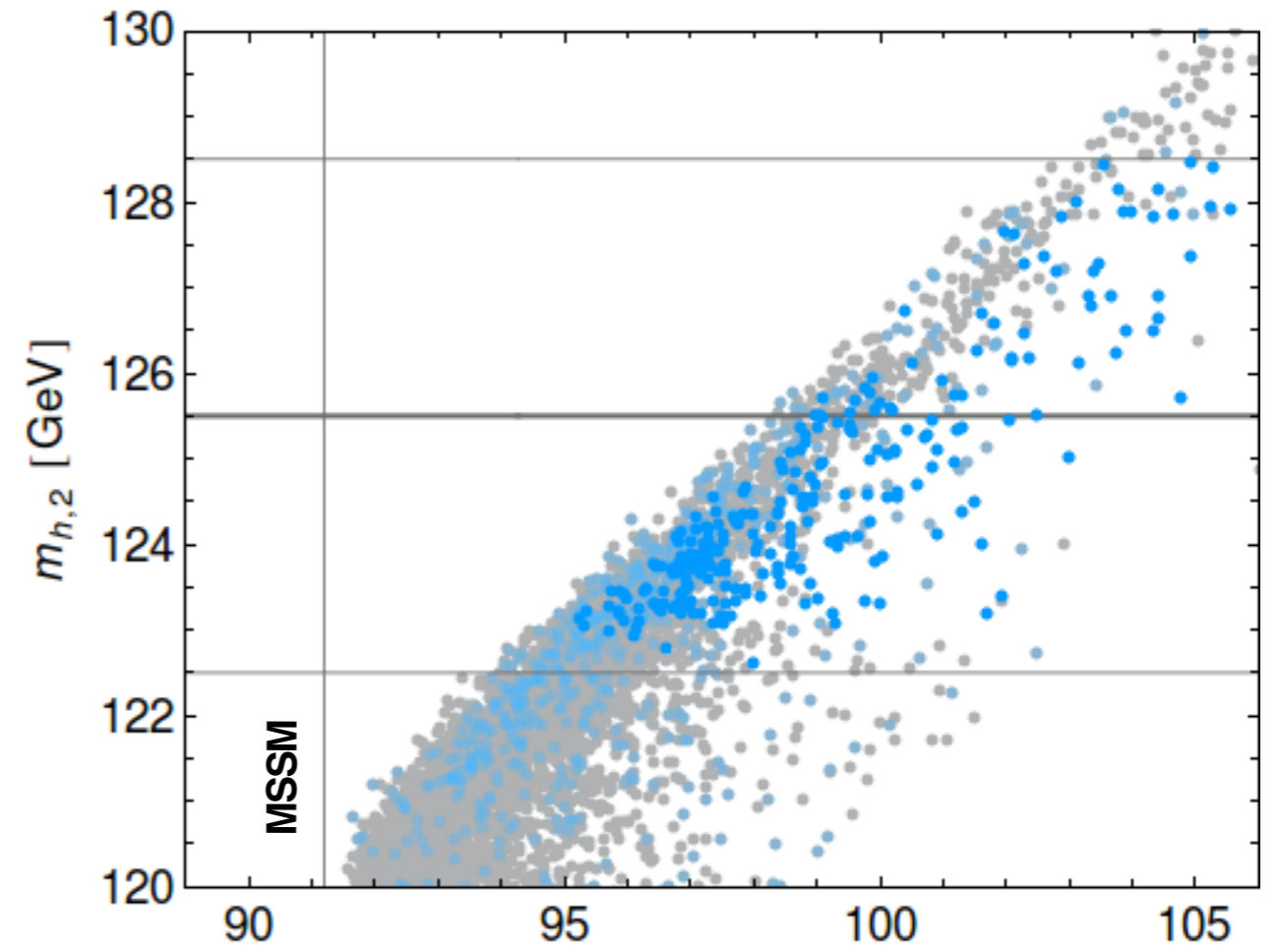
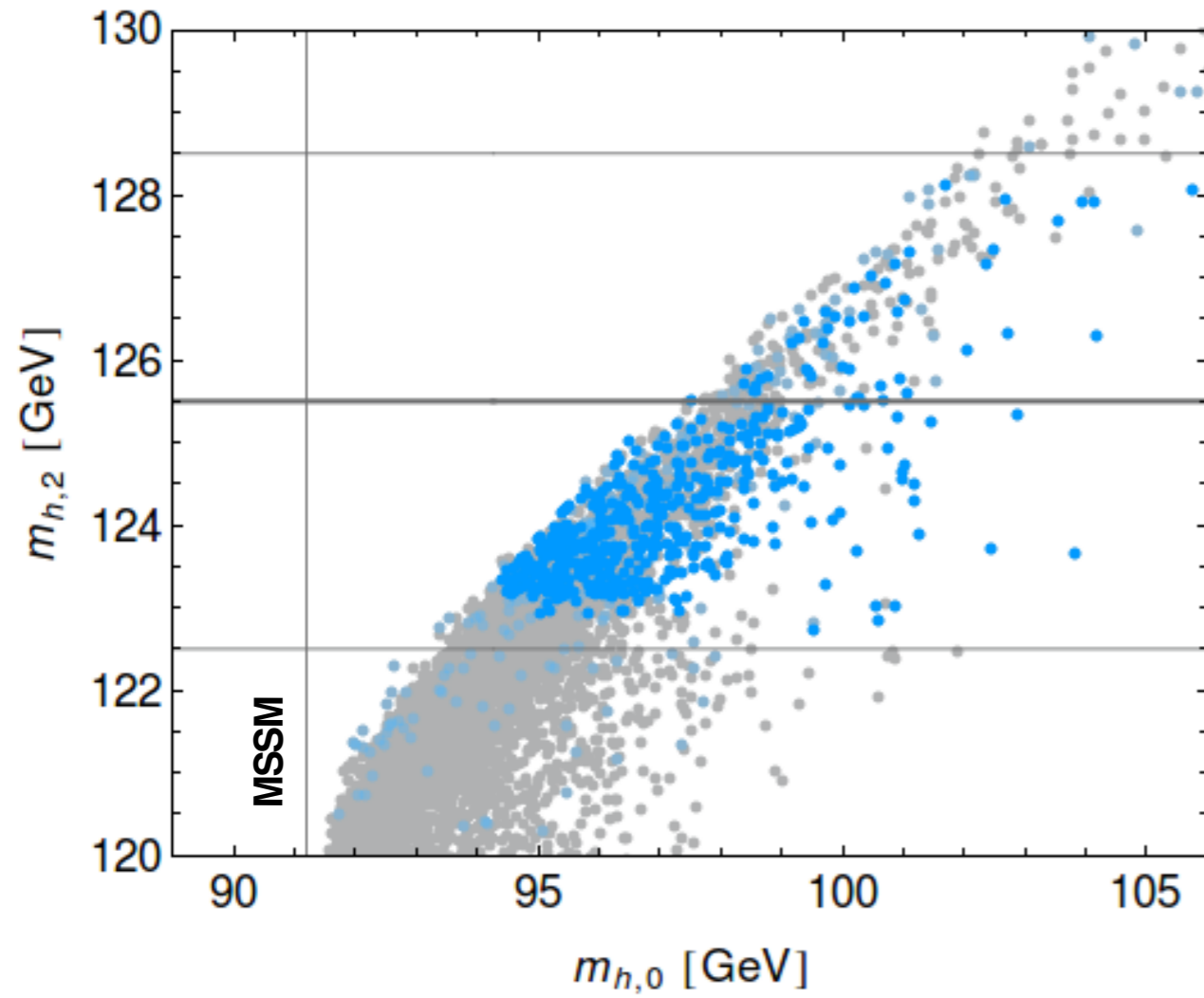
Threshold  
scale:  
MSSM



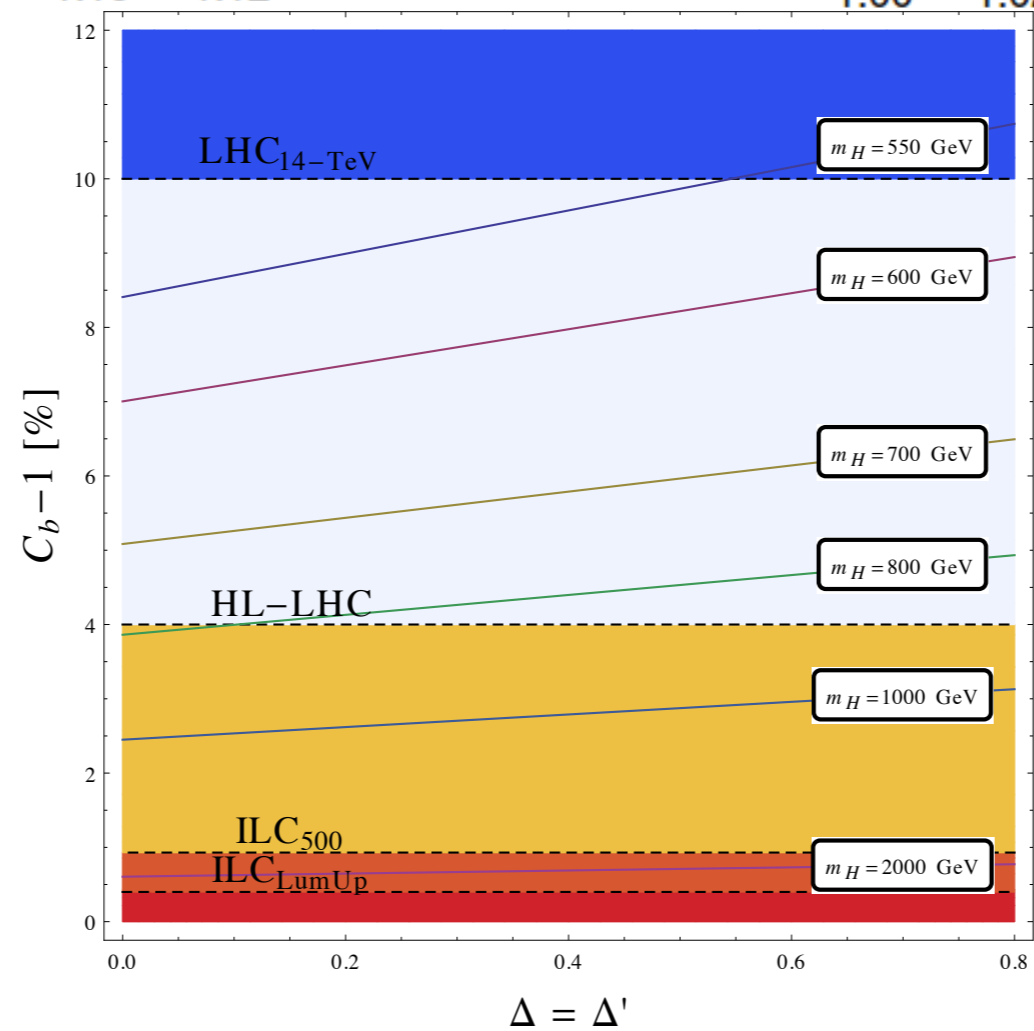
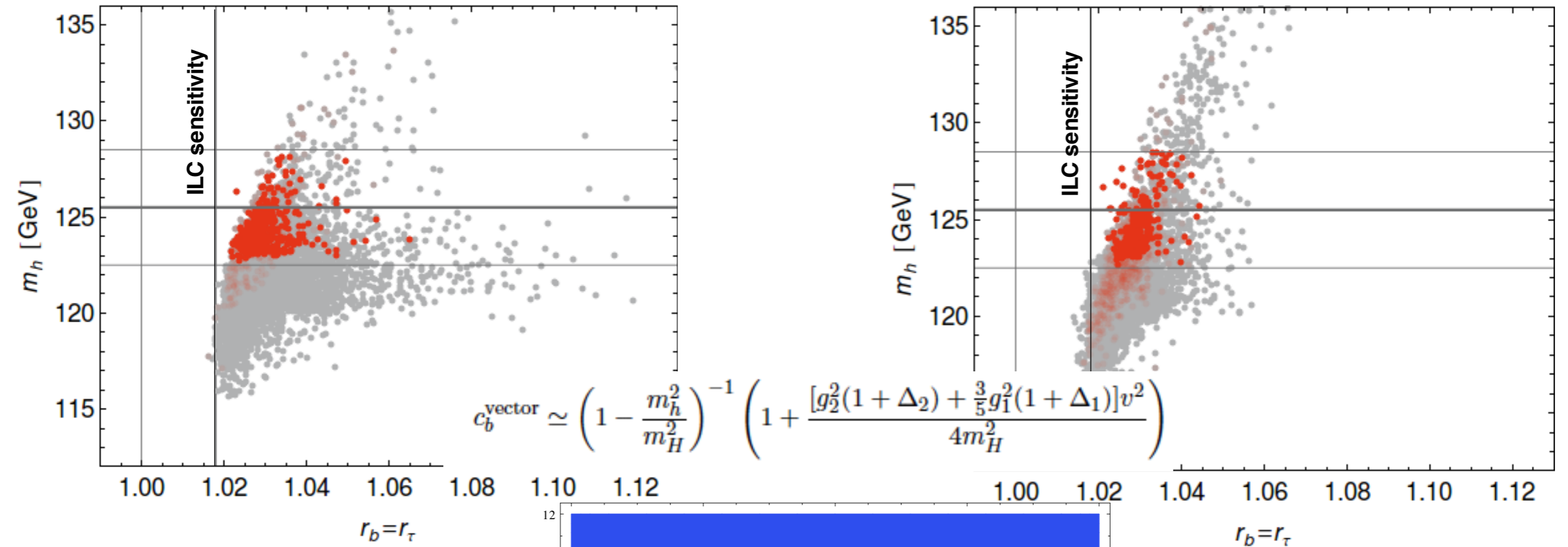
LHC

Same precision as SOFTSUSY, SPheno, SUSPECT

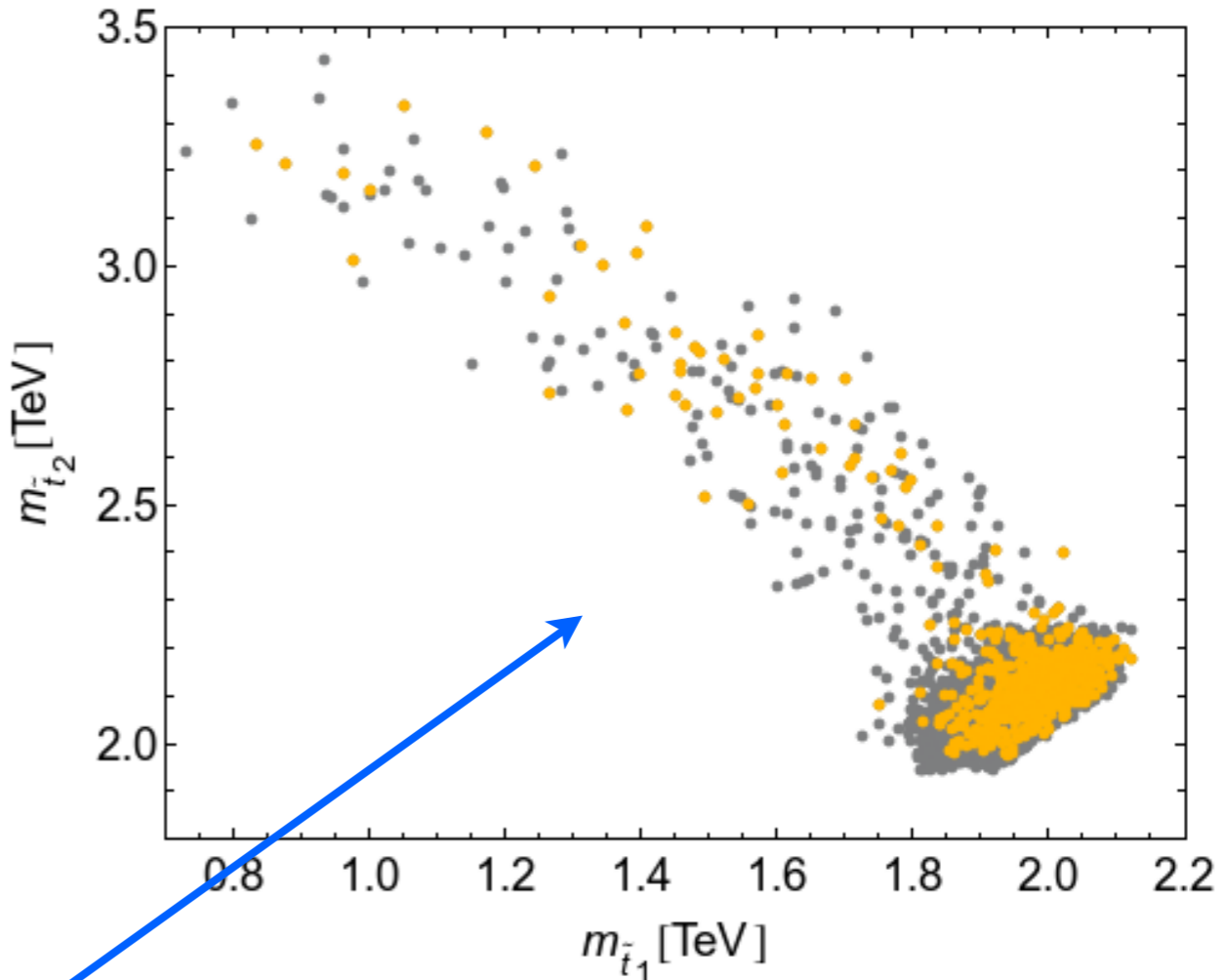
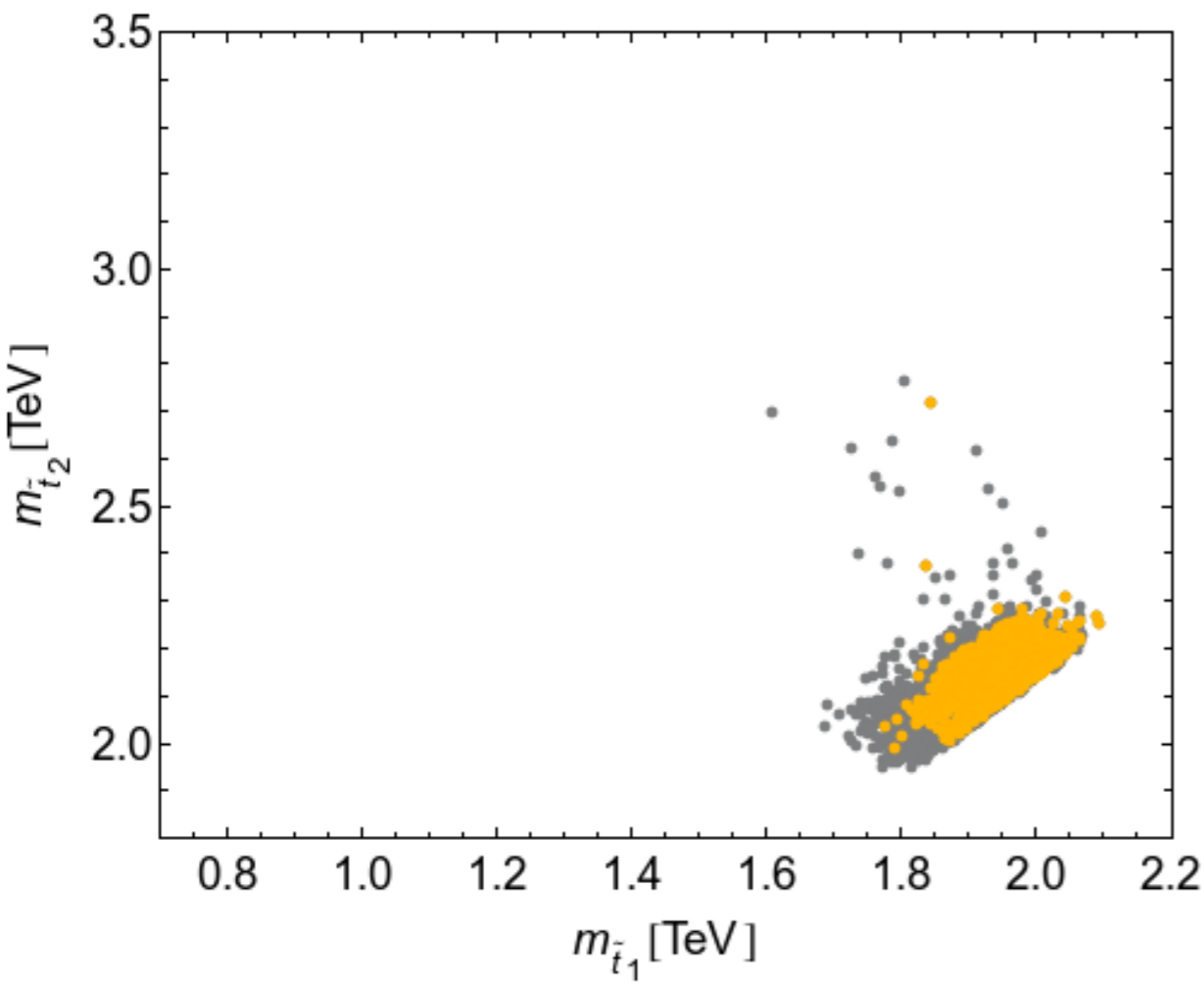




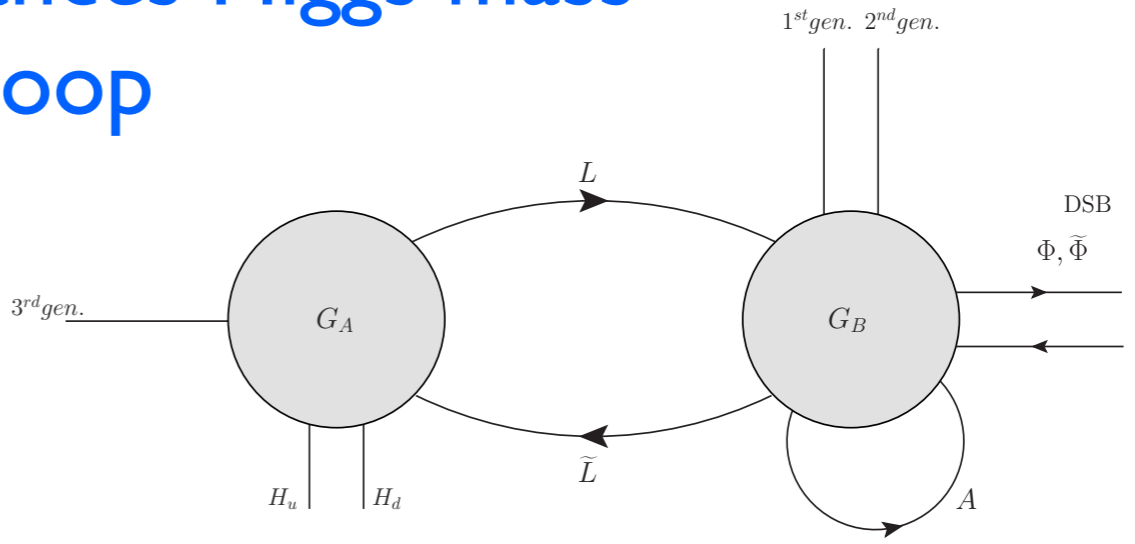
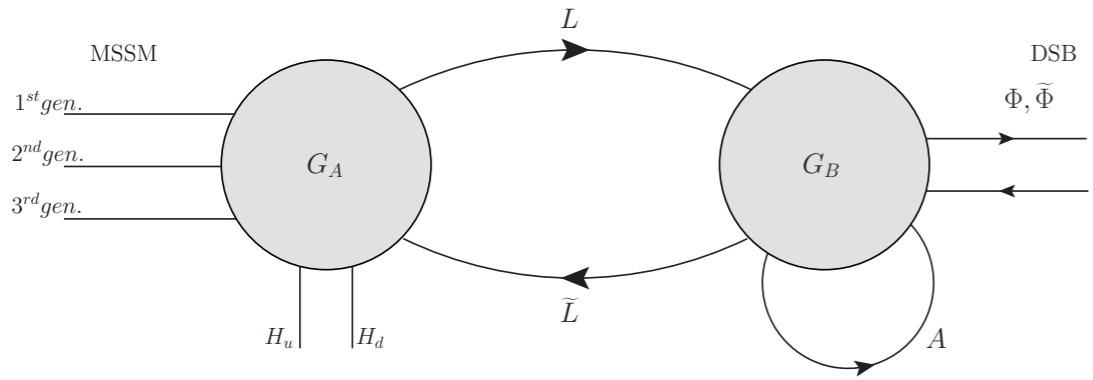
# Testable at ILC!



$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left(1 - \frac{X_t^2}{12m_{\tilde{t}}^2}\right) \right] + \Delta m_{h,1}^2 = \frac{3m_Z^2}{16\pi^2 v_{ew}^2} \left(1 - \frac{8}{3} \sin^2 \theta_W\right) \cos 2\beta m_t^2 \ln \left( \frac{m_{\tilde{q}_L^3}^2}{m_{\tilde{u}_R^3}^2} \right)$$



## Stop splitting enhances Higgs mass @ 1-loop



	MI	MIa	MIb
Input values			
M	233 TeV	288 TeV	260 TeV
$\Lambda_{1,2}$	44.9 TeV	85.6 TeV	111 TeV
$\Lambda_3$	190 TeV	206 TeV	208 TeV
$m_L^2$	47.3 TeV <sup>2</sup>	83.3 TeV <sup>2</sup>	86.2 TeV <sup>2</sup>
$v$	26.2 TeV	26.5 TeV	25.4 TeV
$\theta_1, \theta_2$	1.18, 1.13	1.09, 1.33	1.05, 1.04
$\tan \beta$	16	12	28
Squark sector			
$m_{\tilde{t}_1}$	1.84 TeV	1.99 TeV	409 GeV
$m_{\tilde{t}_2}$	1.98 TeV	2.06 TeV	3.49 TeV
$A_t$	-442 GeV	-146 GeV	-141 GeV
$m_{\tilde{b}_R}$	1.95 TeV	2.05 TeV	2.56 TeV
$m_{\tilde{q}_{12,L}}$	2.05 TeV	2.12 TeV	2.19 TeV
$m_{\tilde{q}_{12,R}}$	1.97 TeV	2.10 TeV	2.14 TeV
Slepton sector			
$m_{\tilde{l}_{12,L}}$	738 GeV	314 GeV	515 GeV
$m_{\tilde{l}_{3,L}}$	736 GeV	315 GeV	440 GeV
$m_{\tilde{l}_{12,R}}$	901 GeV	183 GeV	262 GeV
$m_{\tilde{l}_{3,R}}$	899 GeV	110 GeV	4.31 TeV
Gaugino sector			
$m_{\tilde{\chi}_1^0}$	53.2 GeV	116 GeV	154 GeV
$m_{\tilde{\chi}_2^0}$	99.3 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_3^0}$	187 GeV	750 GeV	818 GeV
$m_{\tilde{\chi}_4^0}$	222 GeV	755 GeV	823 GeV
$m_{\tilde{\chi}_1^\pm}$	96.8 GeV	242 GeV	306 GeV
$m_{\tilde{\chi}_2^\pm}$	225 GeV	756 GeV	823 GeV
$m_{\tilde{g}}$	1.62 TeV	1.66 TeV	1.75 TeV
Higgs sector			
$m_{h_0}$	125 GeV	127 GeV	125 GeV
$m_{H_0}$	720 GeV	792 GeV	885 GeV
$m_{A_0}$	721 GeV	796 GeV	894 GeV
$m_{H_\pm}$	726 GeV	799 GeV	893 GeV

## Extensions:

- 6 gauge groups
- resolve issue of  $M_{Hu}^2$  and  $V$
- Other SUSY breaking parameterisations?
- Single regime spectrum generator
- Add the states to PDG etc....

A renormalisable way to model an extra dimension

**Ex. KK gluons, gluinos,  $Z'$ ,  
KK  $W$ 's**

Can talk to FeynArts, Formcalc, CalcHep,  
HiggsSignals, HiggsBounds,  
WHIZARD, microOMEGA, Vevacious and more

# Conclusions

- Bottom up approach: D-terms are testable at the ILC
- Top down approach: Spectrum generators are available for use

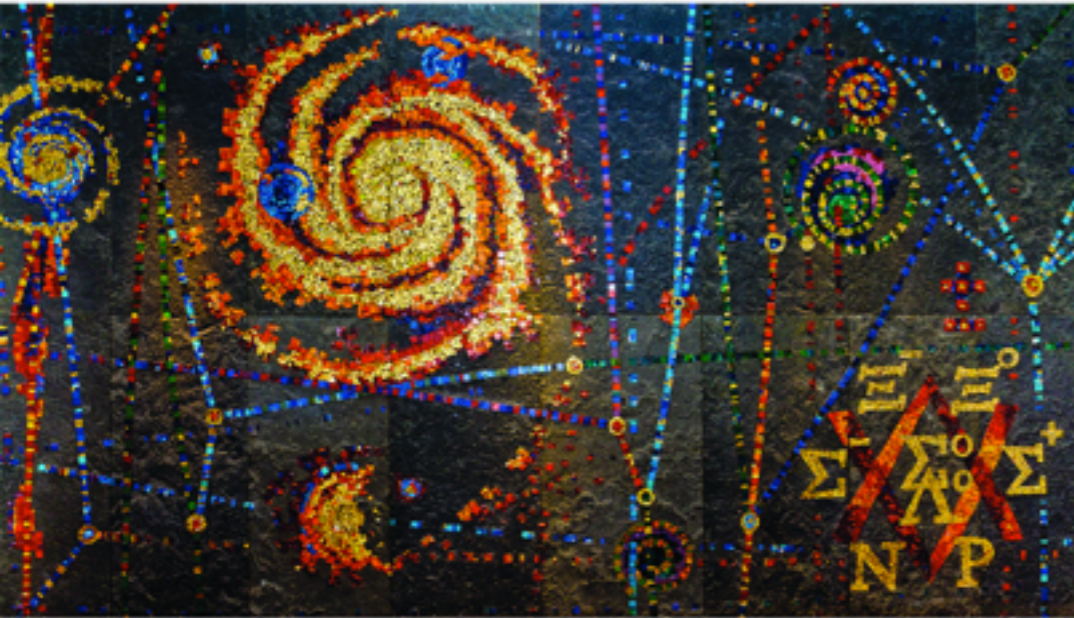


21 - 26 JULY 2014, MANCHESTER, ENGLAND

# SUSY2014

THE 22ND INTERNATIONAL CONFERENCE ON SUPERSYMMETRY  
AND UNIFICATION OF FUNDAMENTAL INTERACTIONS

<http://www.susy2014.manchester.ac.uk>



Moritz McGarrie

or is it?!

# SUSI 2014

13<sup>th</sup> International Conference  
on Structures Under Shock  
and Impact



**additional slides**

# “Large At Without the Desert”

A.Abdalgabar, A.Cornell, A.Deandrea, MM 1405:1038

$$\mathbf{a}_u \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_t \end{pmatrix}, \quad \mathbf{a}_d \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_b \end{pmatrix}, \quad \mathbf{a}_e \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a_\tau \end{pmatrix},$$

UV

In many models  $A_t = 0$  in UV



$A_t$  runs negative

IR

typically ends up negative a few 100 GeV

Not sufficient to get the correct Higgs mass....

**Question: Can we accelerate its running?**

# .The Higgs mass 126 GeV

## The MSSM at one-loop

$$m_h^2 \simeq m_z^2 \cos^2(2\beta) + \frac{3}{(4\pi)^2} \frac{m_t^4}{v_{ew}^2} \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

top mass

average stop mass

$$126^2 = 91^2 + 81^2$$

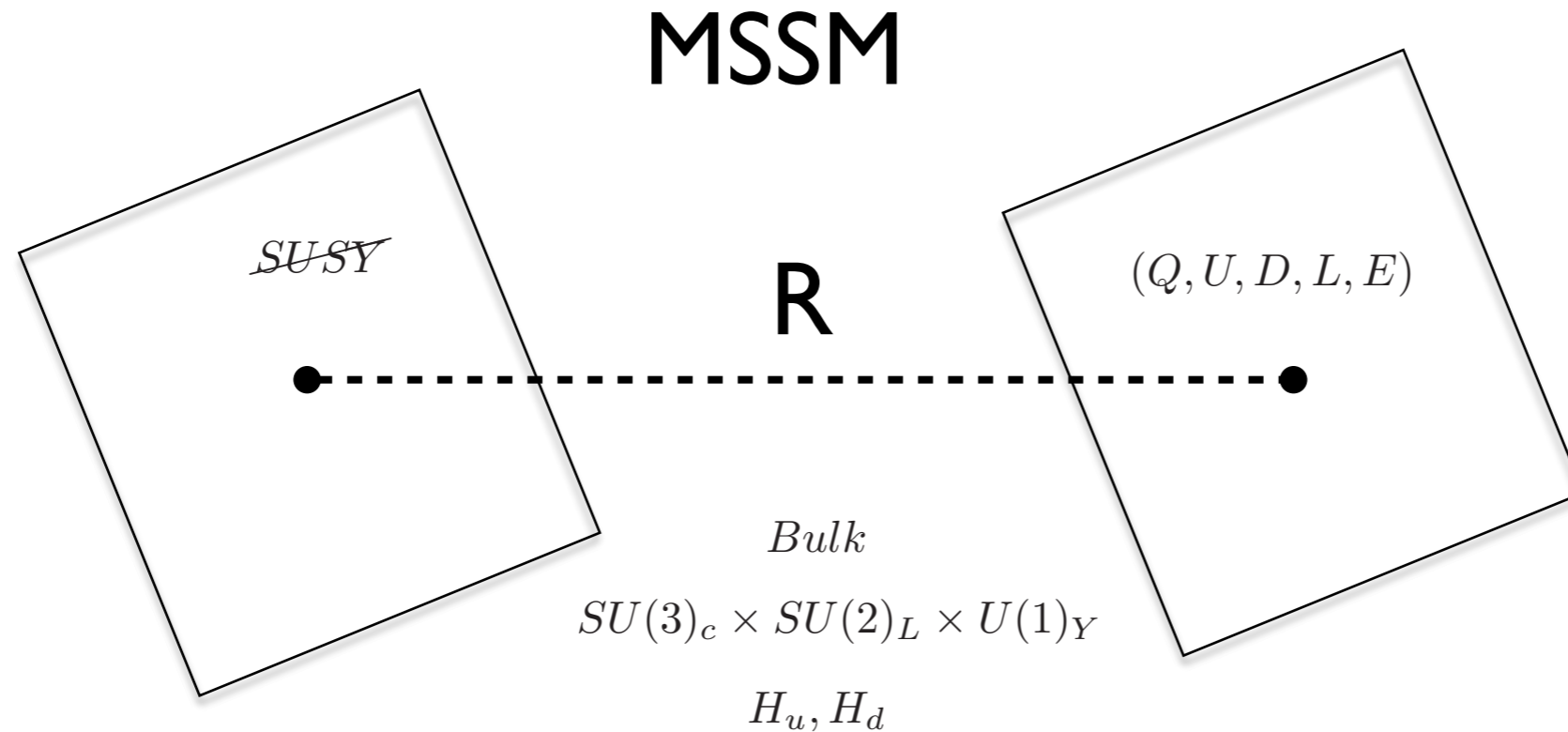
$$X_t = A_t - \mu \cot \beta$$

stop mixing

- Radiative corrections are same order as tree level piece
- corrections run logarithmically in SUSY
- MSSM case implies either heavy stops or large  $X_t = A_t + \dots$
- Need 1-2 TeV  $A_t$  or stops to get Higgs mass correct

# In 5D you can get large $A_t$ !

“Power law running”



An extra dimension of radius  $R$ .

Additional Kaluza Klein modes enter RGEs @  $Q > 1/R$

Large  $A_t$ : Independent of the details of SUSY breaking

Split families: Locate different generations in brane or bulk  
aesthetically Natural!

$$m_{(Q,U,D)3}^2 \ll m_{(Q,U,D)1,2}^2$$

# Power law running

$$\alpha^{-1}(Q) = \alpha^{-1}(m_z) - \frac{b}{2\pi} \log \frac{Q}{m_z} + \frac{\tilde{b}}{2\pi} \log \frac{Q}{m_{KK}} - \frac{\tilde{b}}{2\pi} \left( \frac{Q^d}{m_{KK}} - 1 \right) c_d$$

(K.Dienes, E.Dudas, T. Gherghetta) [9803466](#)

(K.Dienes, E.Dudas, T. Gherghetta) [9806292](#)

“The finite power-law corrections to the Yukawa couplings have the right sign and magnitude to cancel the tree-level terms. This can help to explain the hierarchical structure of the fermion Yukawa couplings.”

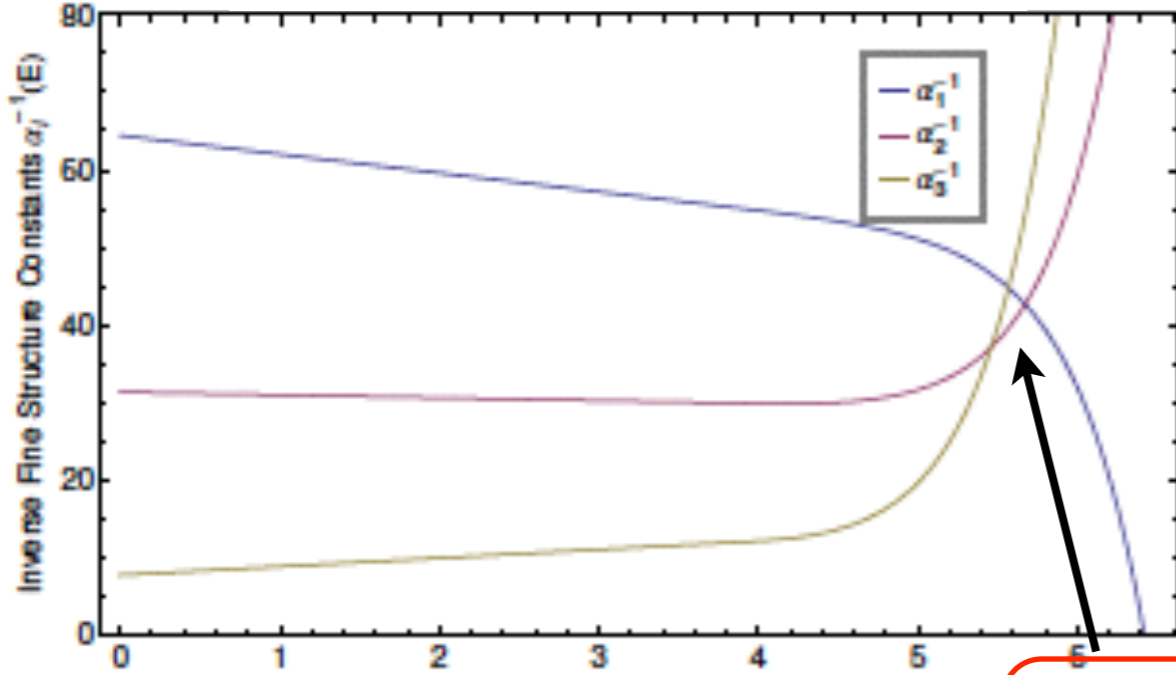
(A.Abdalagbar, A.Cornell, A.Deandrea, MM) [1405:1038](#)

“Perhaps we can use this to accelerate the value of  $A_t$ ?”

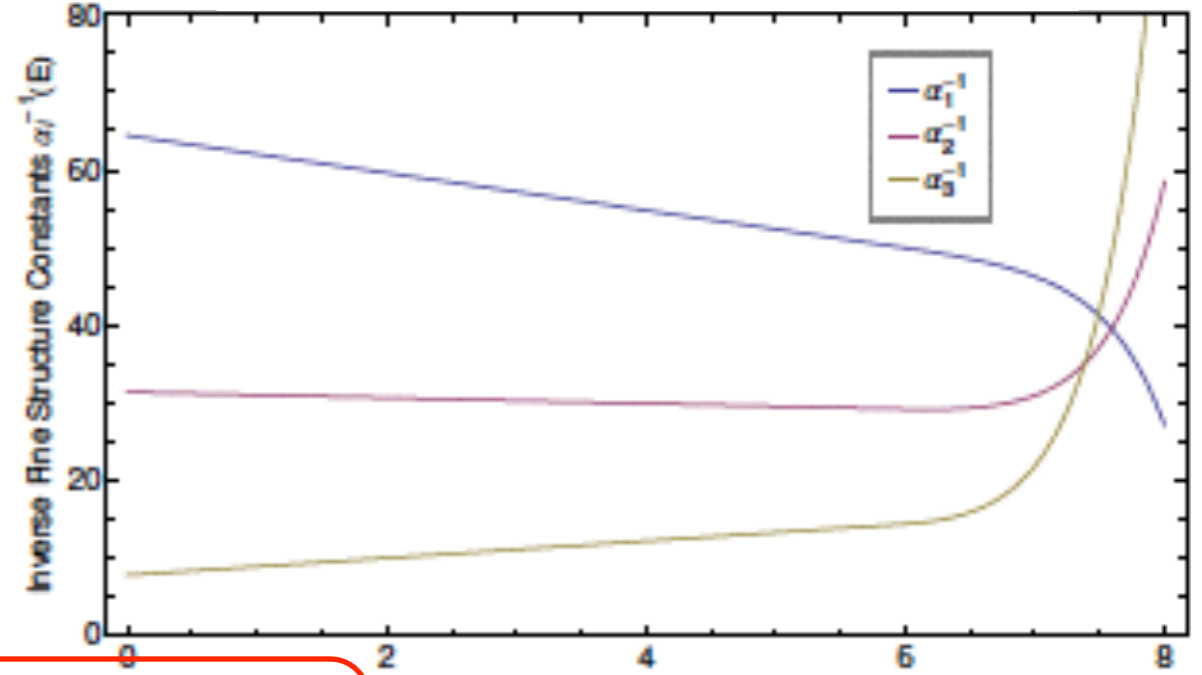
4+d dimensional MSSM

- ✓ Always unify
- ✓ No proton decay
- ✓ Explains flavour
- ✓ Large  $A_t$

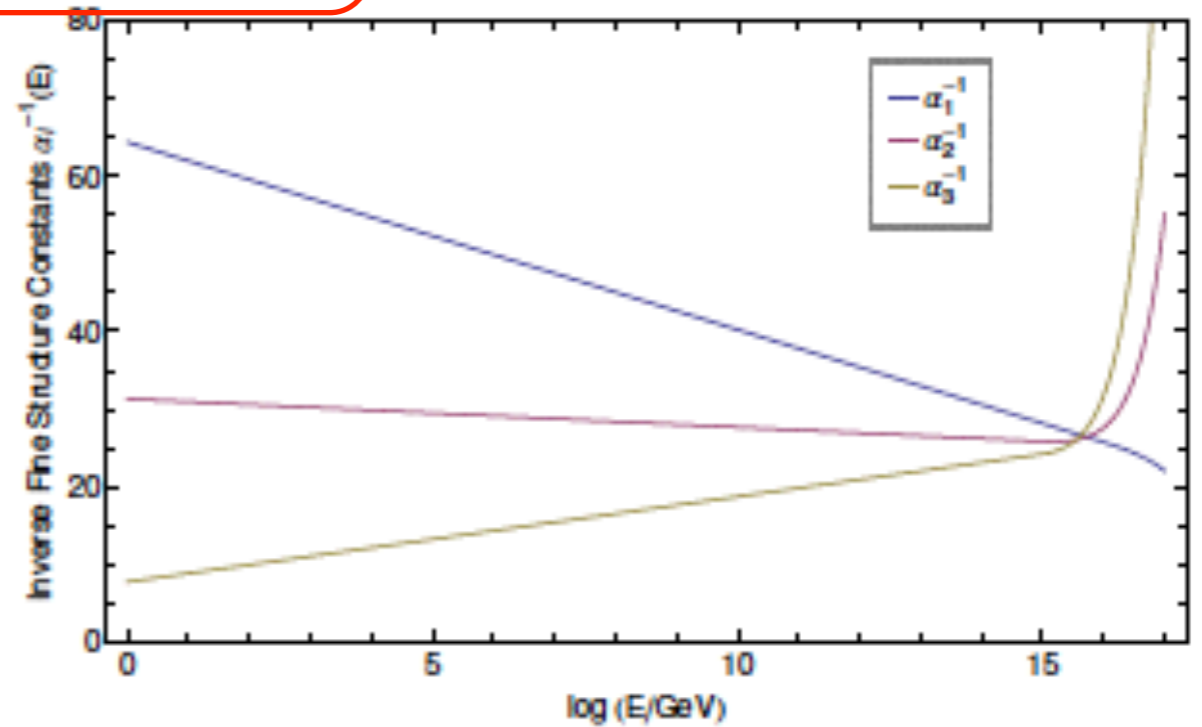
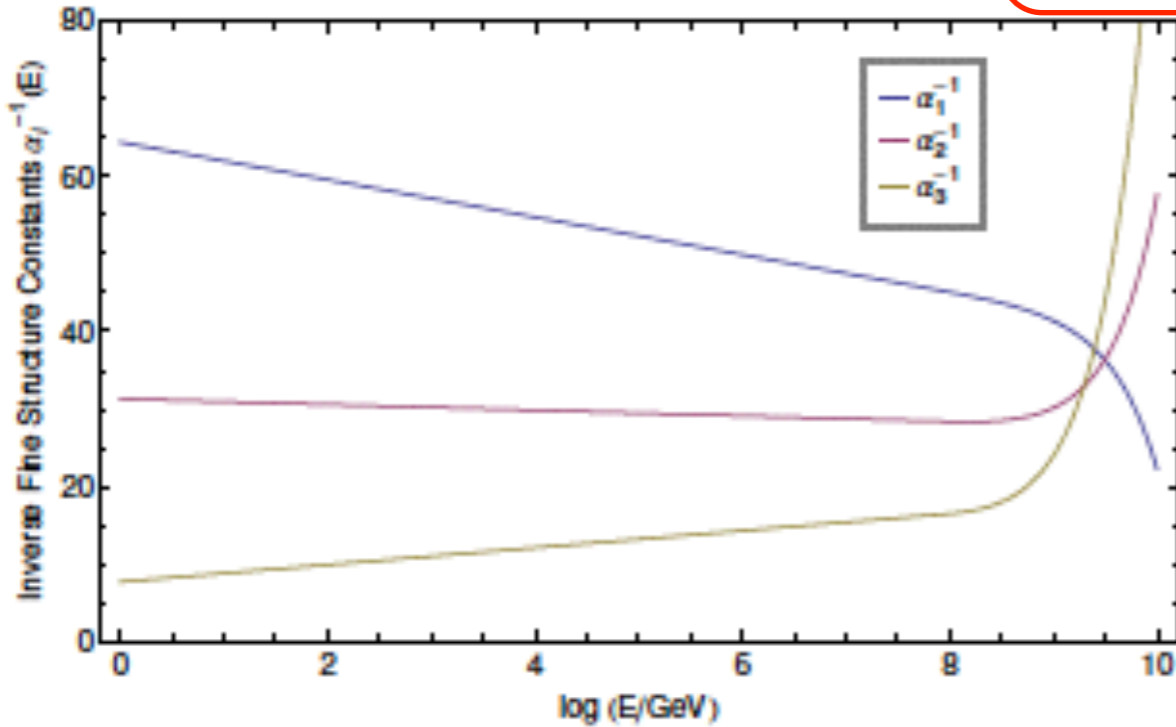
Compactification scale 10 TeV



Compactification scale 10<sup>3</sup> TeV



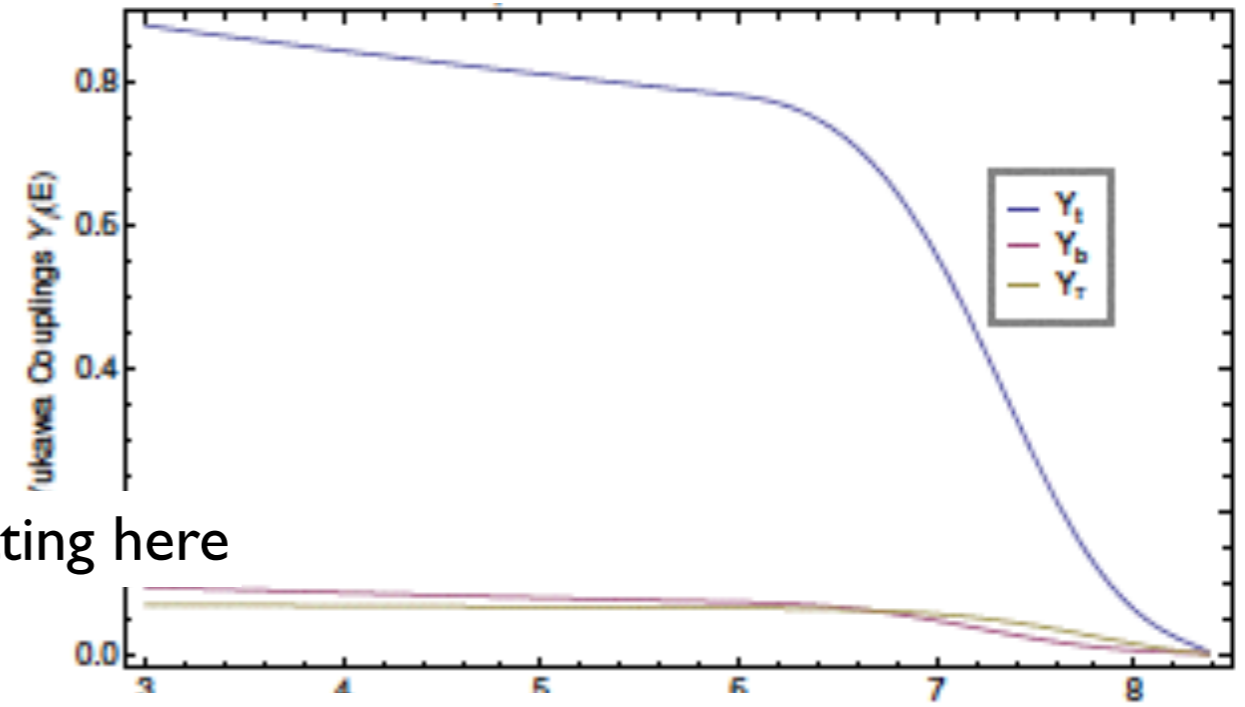
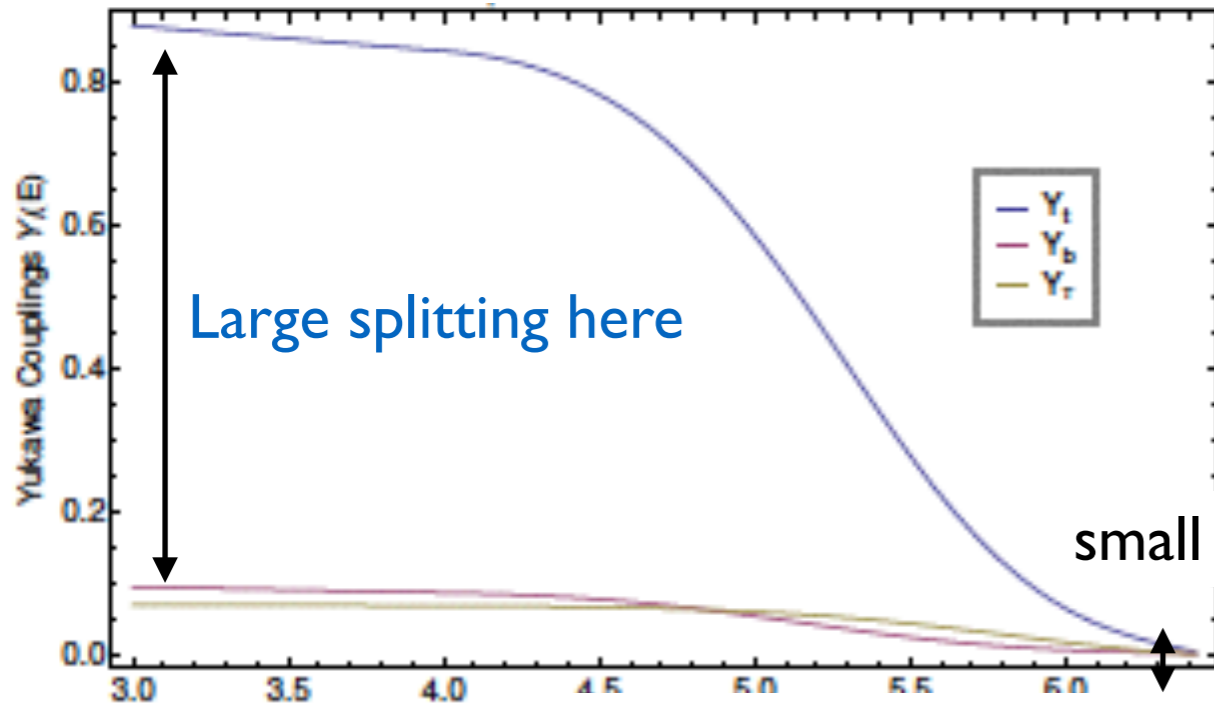
Compactification scale 10<sup>5</sup> TeV **Unification @ 10<sup>6</sup> GeV** Compactification scale 10<sup>12</sup> TeV



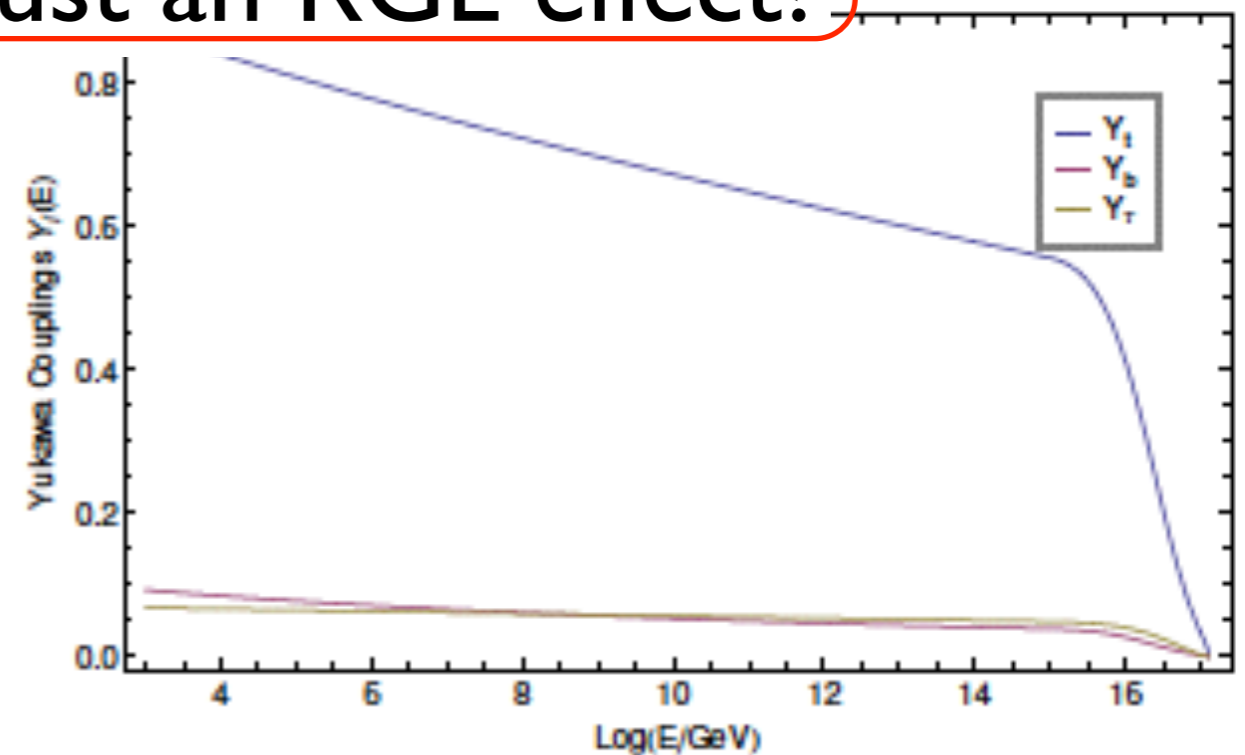
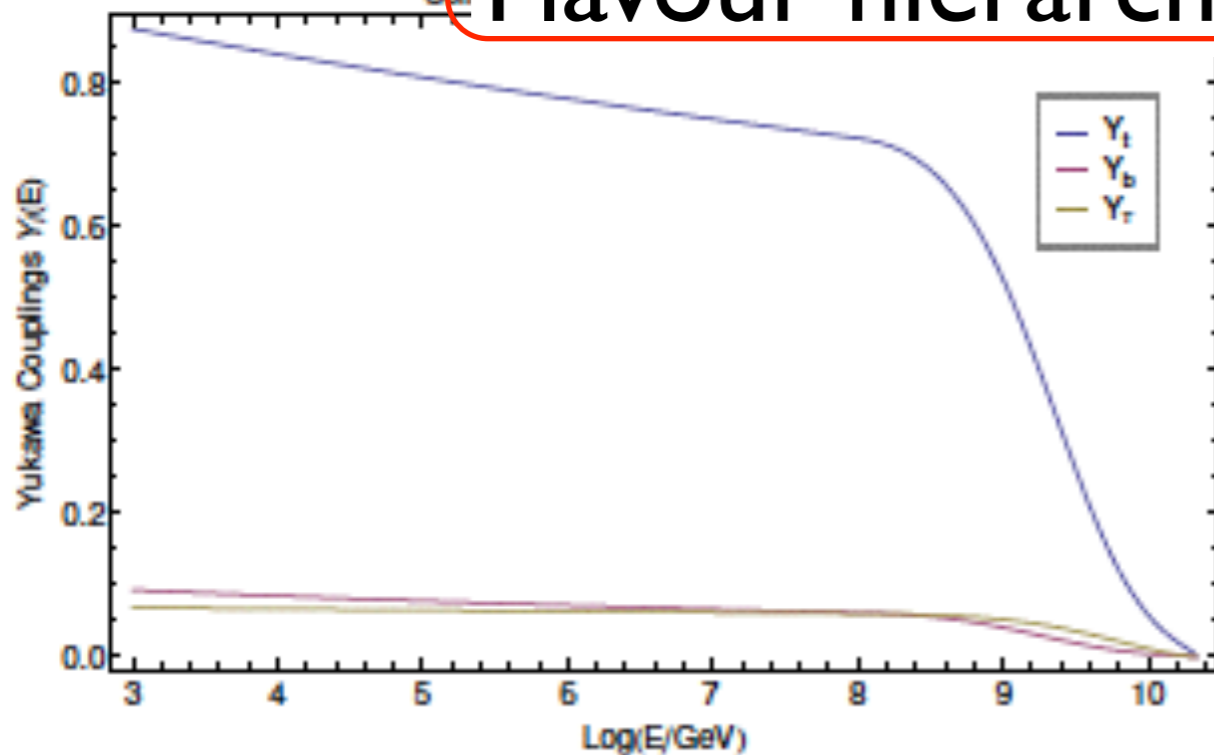
**Figure 1.** Running of the inverse fine structure constants  $\alpha^{-1}(E)$ , for three different values of the compactification scales 10 TeV (top left panel), 10<sup>3</sup> TeV (top right), 10<sup>5</sup> TeV (bottom left) and 10<sup>12</sup> TeV (bottom right), with  $M_3$  of 1.7 TeV, as a function of  $\log(E/\text{GeV})$ .

Compactification scale 10 TeV

Compactification scale  $10^3$  TeV



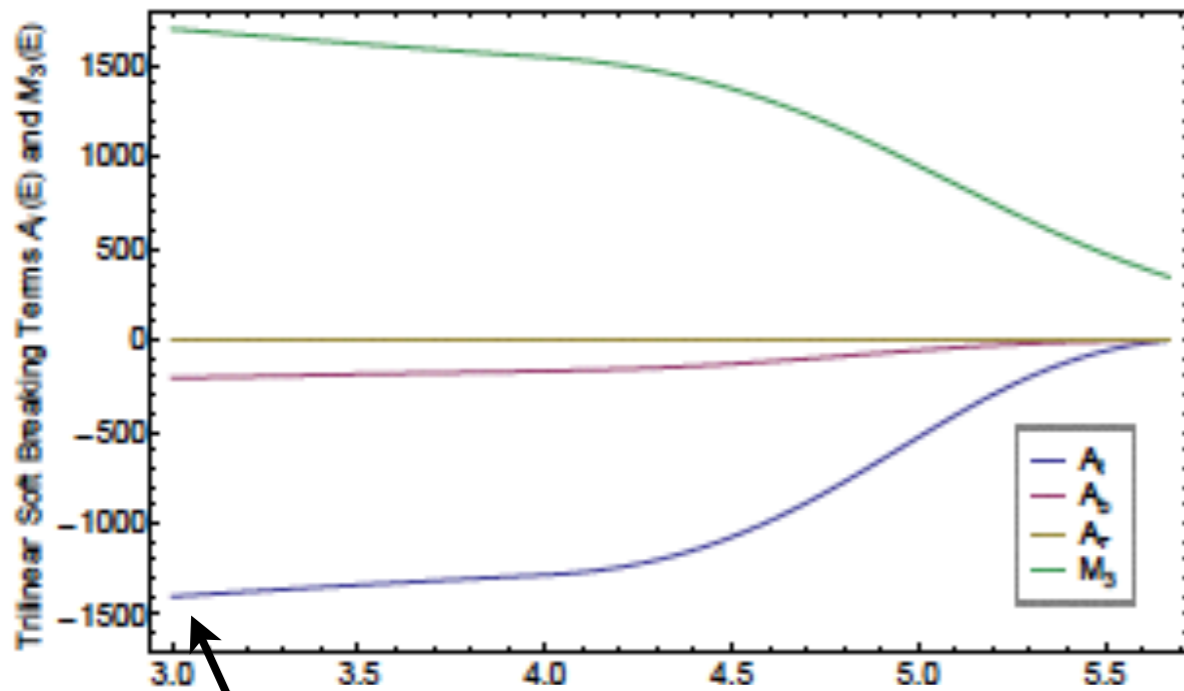
Flavour hierarchy just an RGE effect?



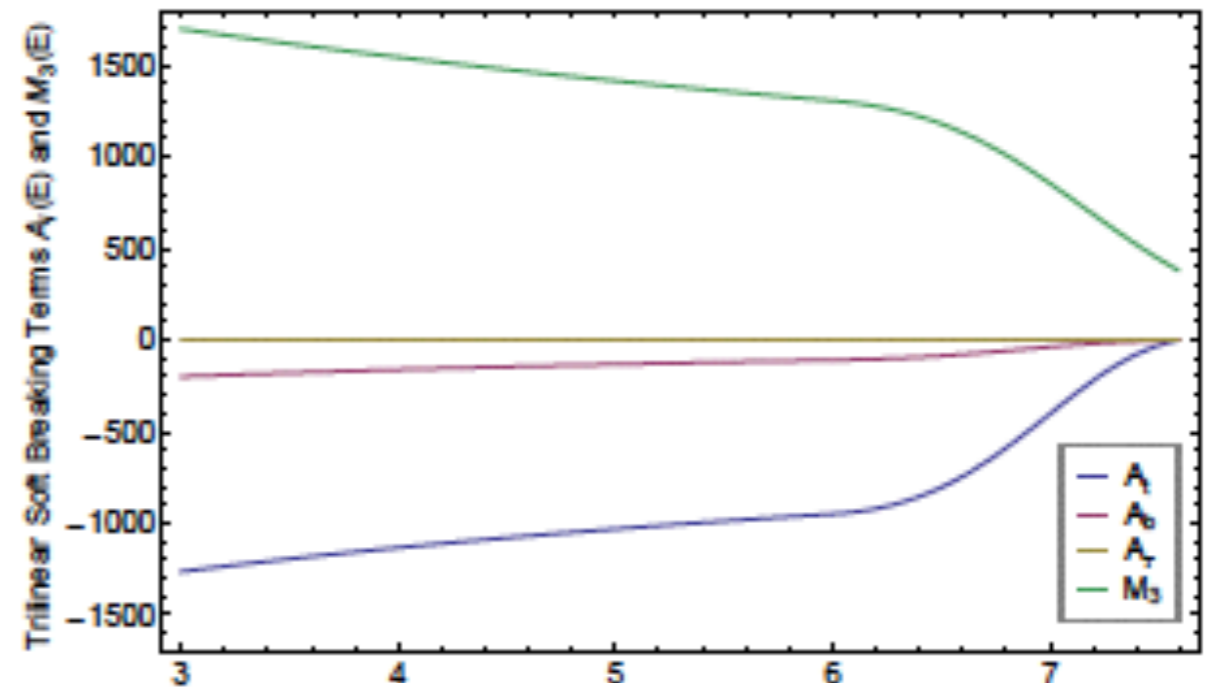
**Figure 2.** Running of Yukawa couplings  $Y_i$ , for three different values of the compactification scales: 10 TeV (top left panel),  $10^3$  TeV (top right),  $10^5$  TeV (bottom left) and  $10^{12}$  TeV (bottom right), with  $M_3[10^3]$  of 1.7 TeV, as a function of  $\log(E/\text{GeV})$ .



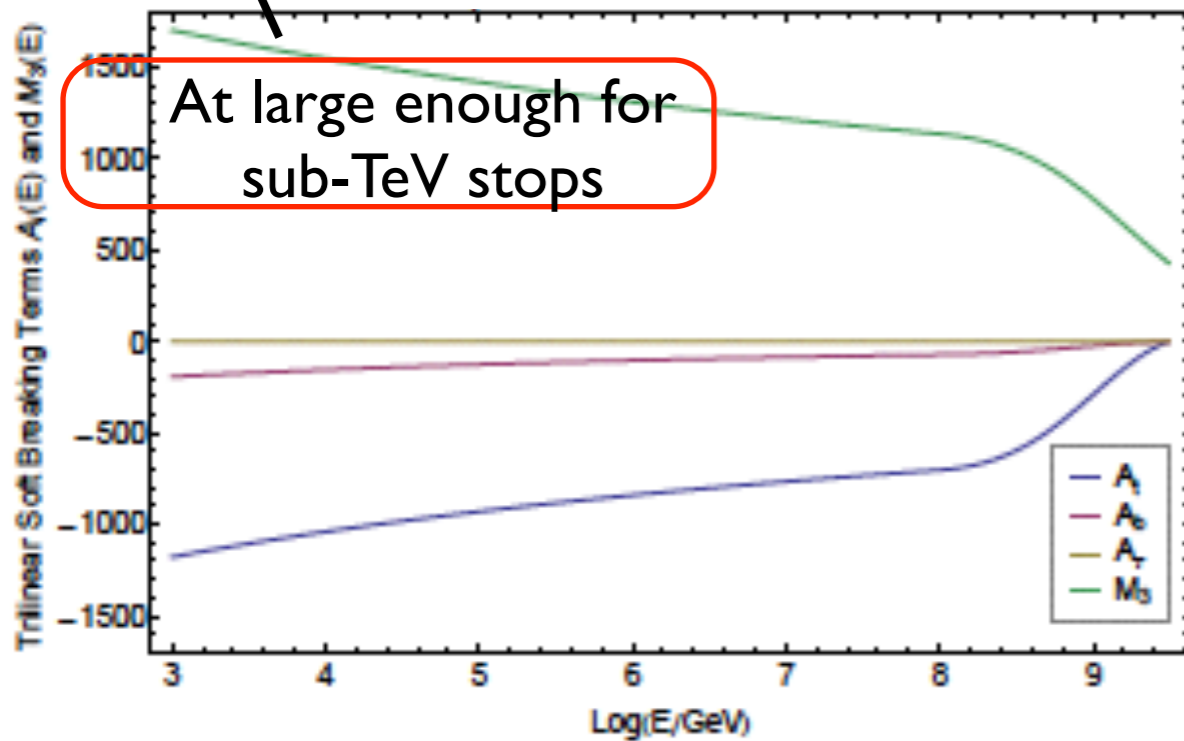
Compactification scale 10 TeV



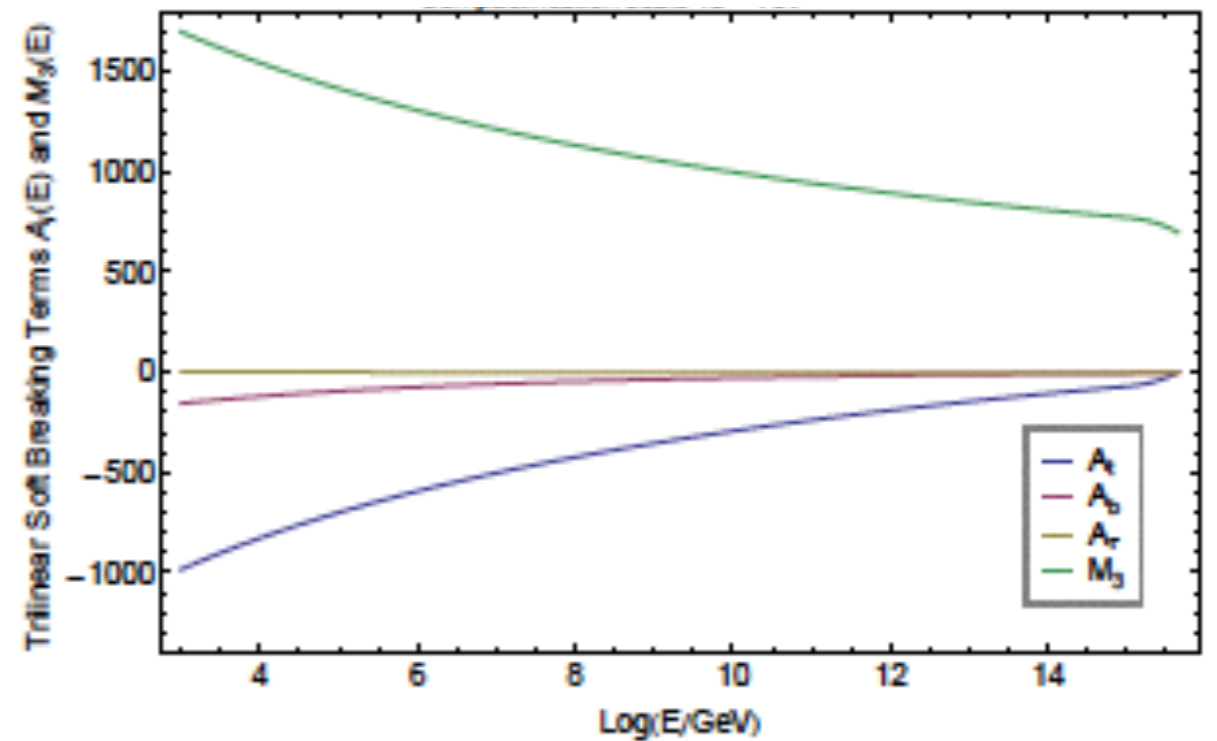
Compactification scale  $10^3$  TeV



Compactification scale  $10^5$  TeV

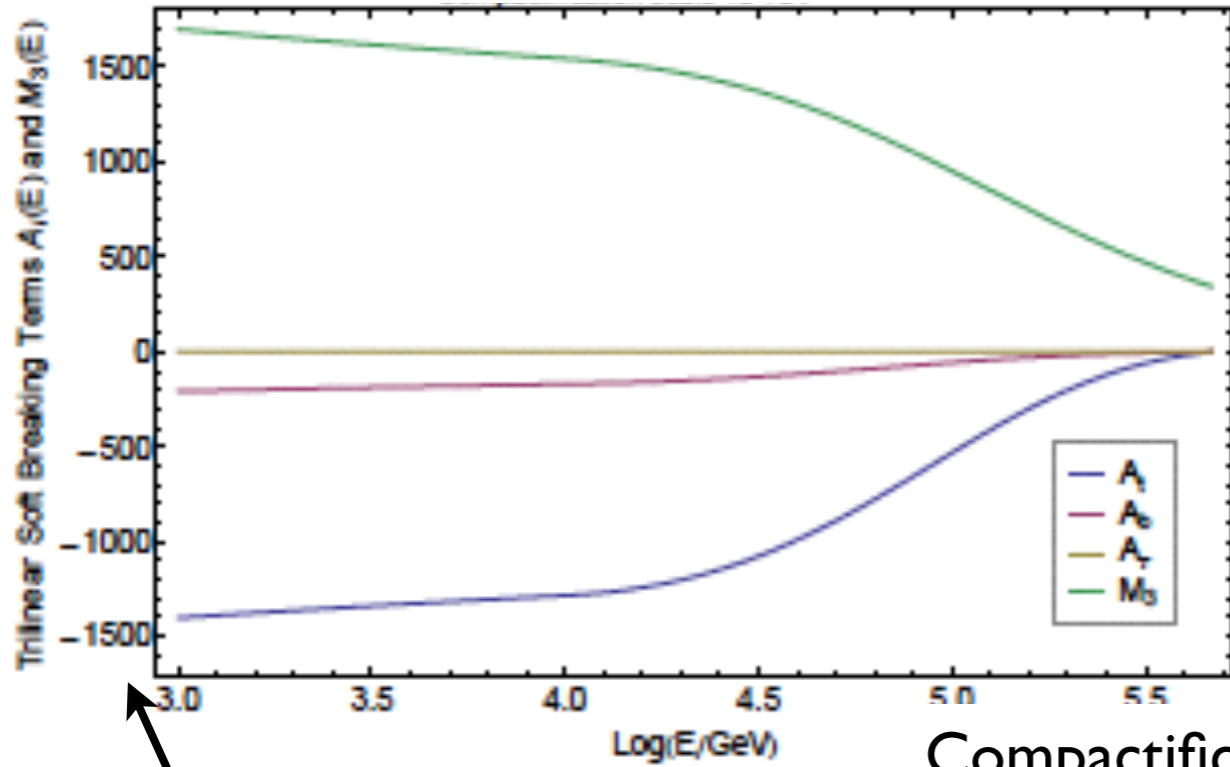


Compactification scale  $10^{12}$  TeV

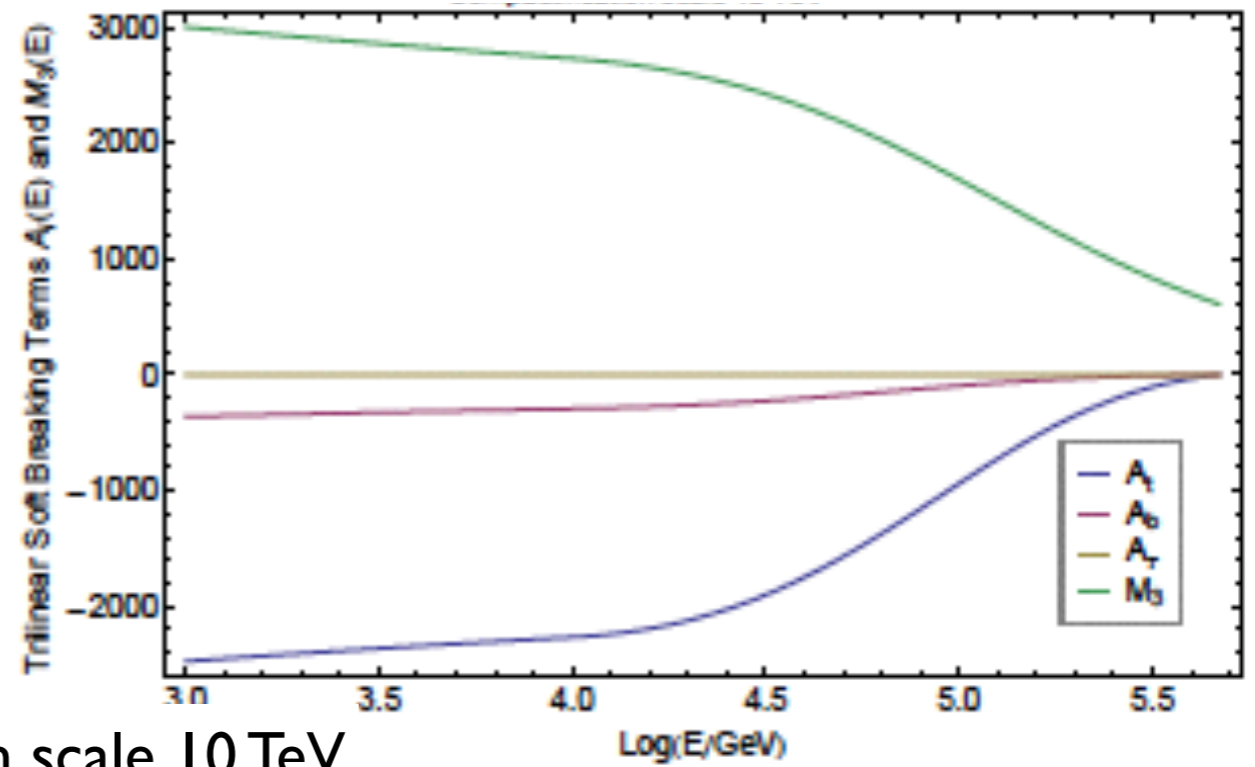


**Figure 3.** Running of trilinear soft terms  $A_i(3,3)(E)$ , for three different values of the compactification scales 10 TeV (top left panel),  $10^3$  TeV (top right),  $10^5$  TeV (bottom left) and  $10^{12}$  TeV (bottom right), with  $M_3[10^3]$  of 1.7 TeV, as a function of  $\log(E/\text{GeV})$ .

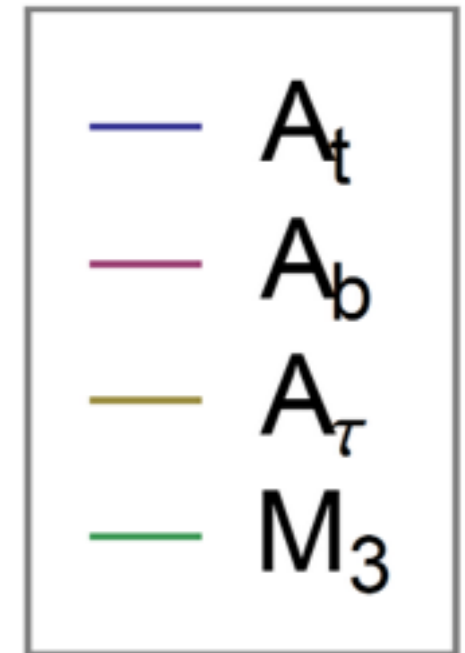
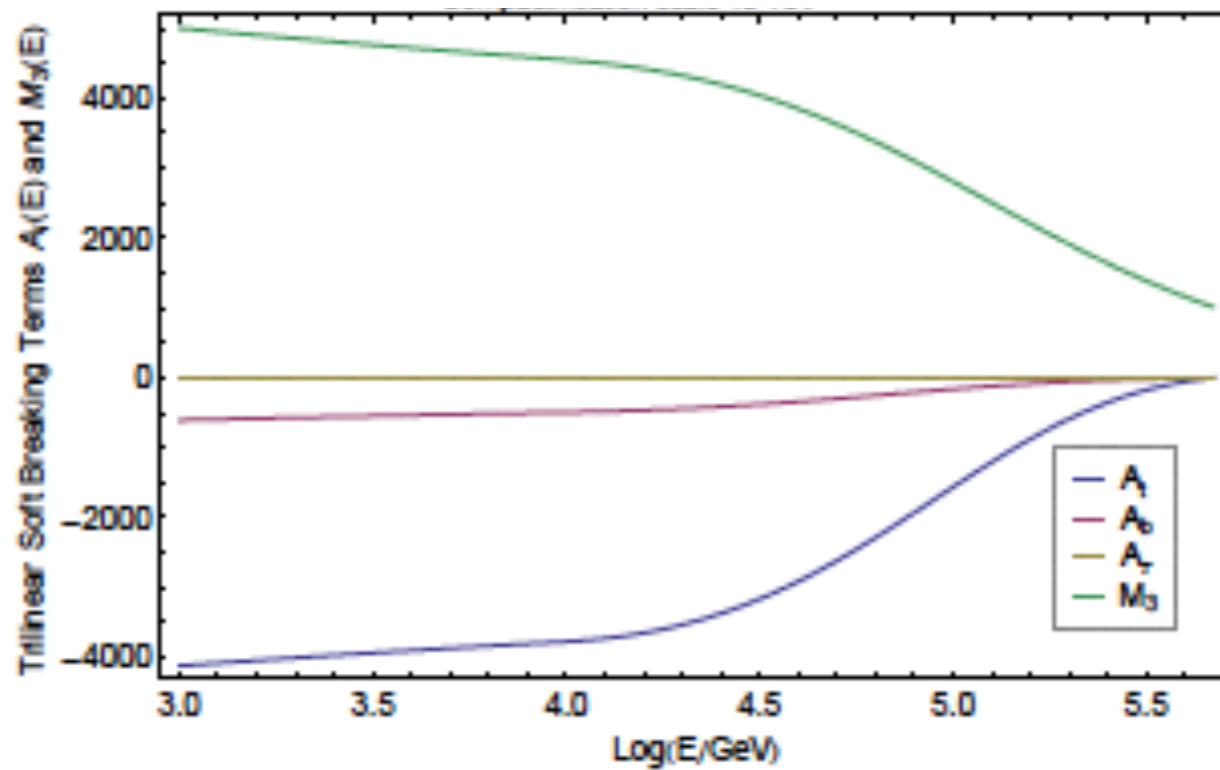
Compactification scale 10 TeV



Compactification scale 10 TeV



Compactification scale 10 TeV



At large enough for sub-TeV stops

Larger gluino gives larger  $A_t$

# Conclusions

- Large  $A_t$  with a low unification & SUSY breaking scale
- Is more natural than 4D models
- Can achieve the correct Higgs mass
- Can get light stops and heavy 1st/2nd gen.
- Helps to explain flavour
- Preserves unification and other nice features