

How alive is constrained SUSY really ?



SUSY 2014, Manchester

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Outline

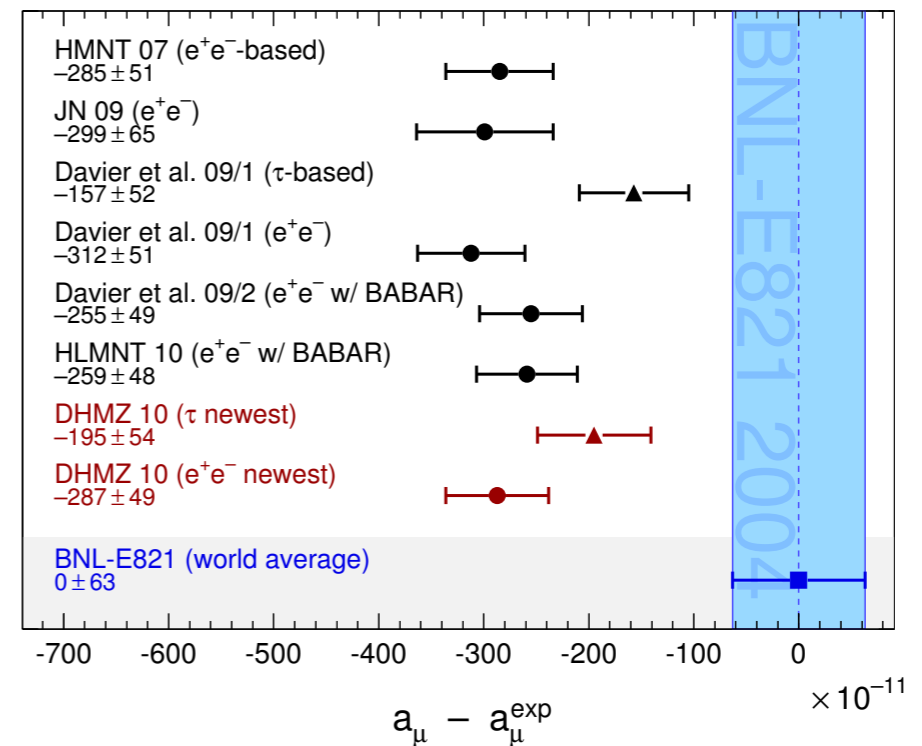
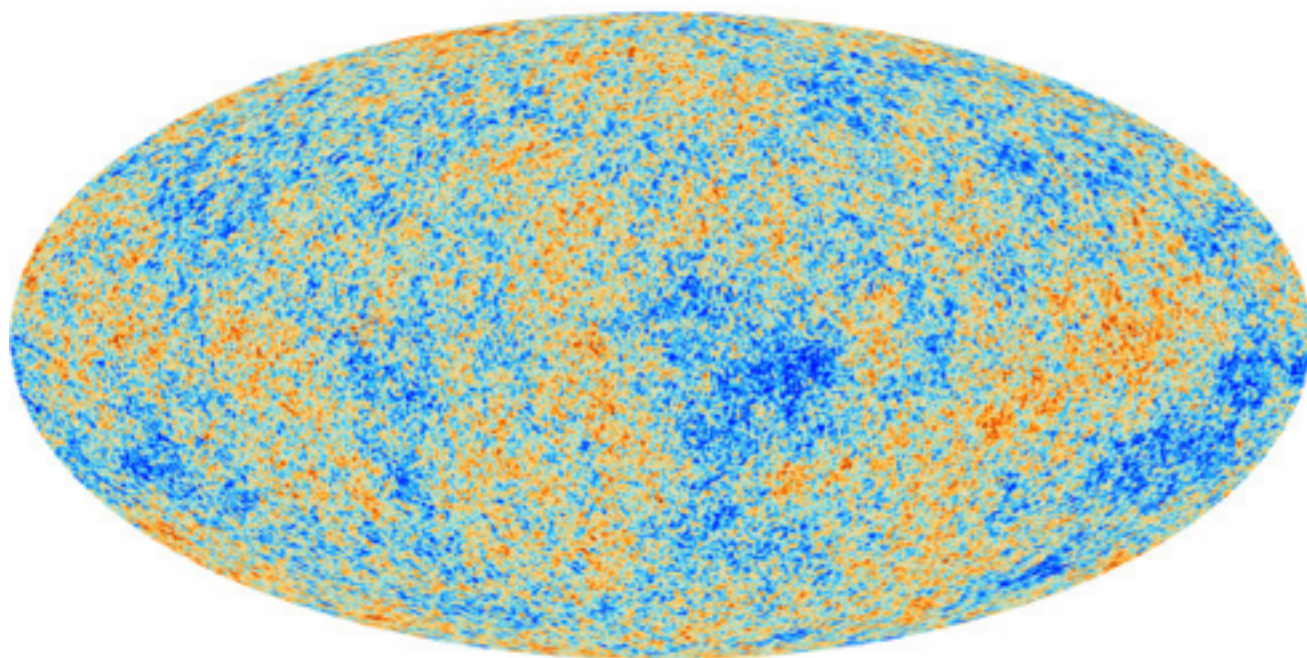
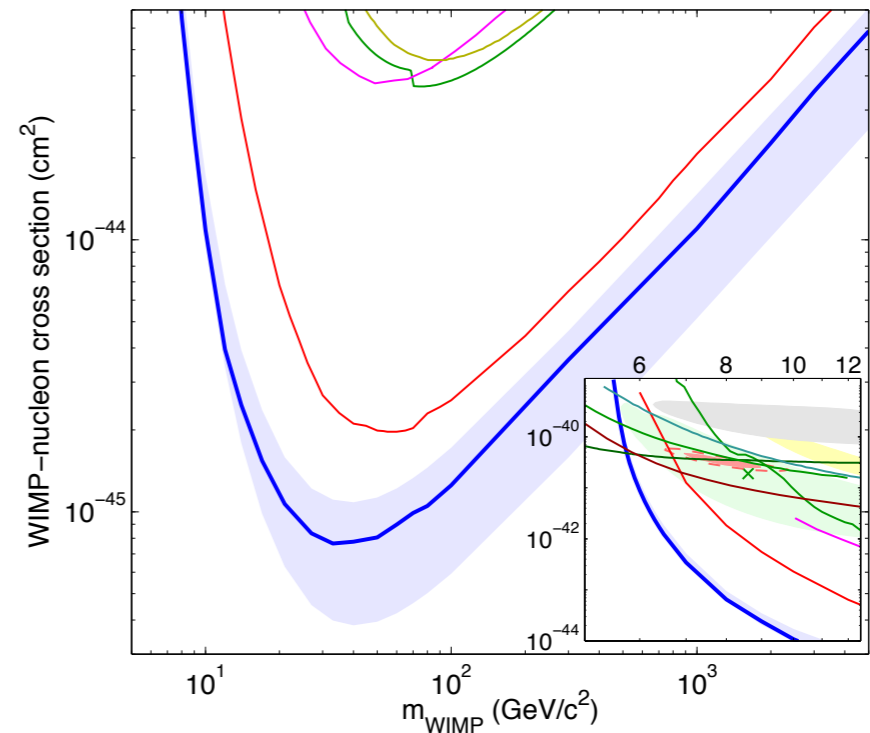
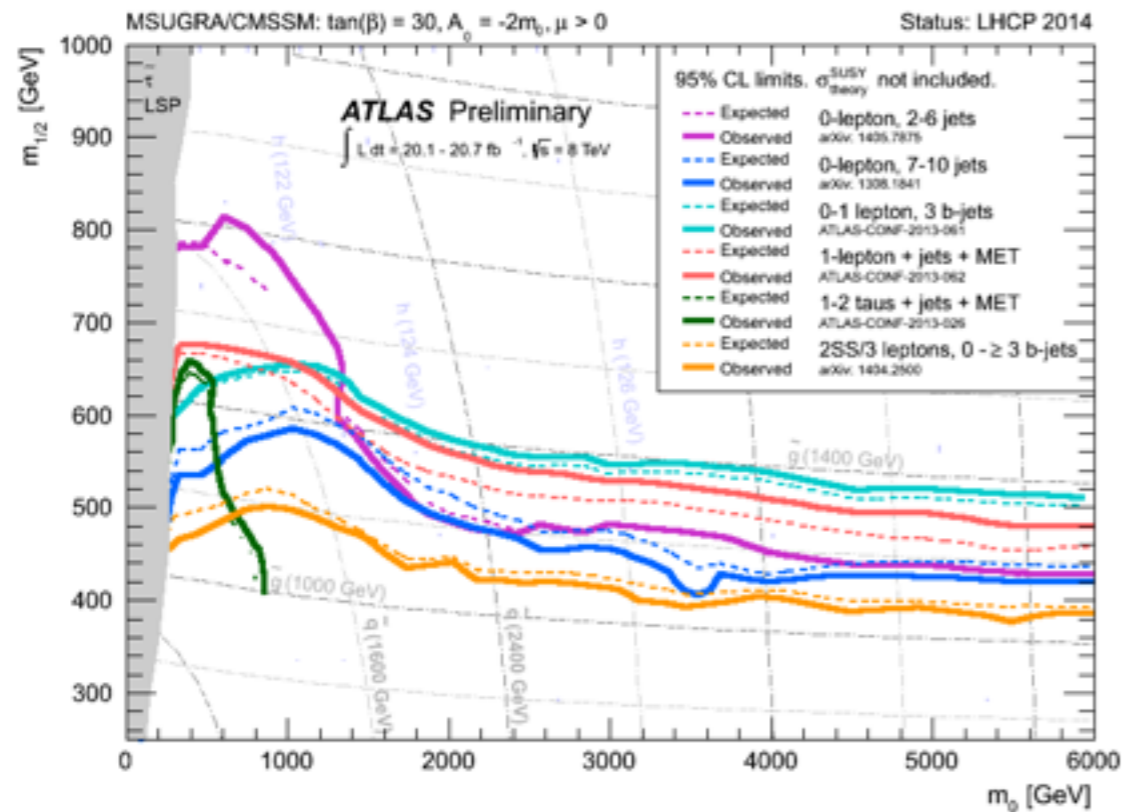
Sorry?
CMSSM?

This is so 2010!

Yeah, I think it's time to move
to another model.

- I. **How the CMSSM came into such troubles**
- II. **The *one more thing* which still has to be done**

Probing the CMSSM



Fittino

- Using the **C++ program** Fittino we combine a wide range of measurements sensitive to supersymmetry:
 - **indirect constraints** from low energy measurements
 - **Higgs boson** properties
 - **direct searches** for sparticles and BSM Higgs bosons
 - **astrophysical** observations
- Fittino uses
 - **public codes** to calculate model predictions
 - a χ^2 **function** to compare measurements and predictions
 - an auto-adaptive **Markov Chain** to sample the parameter space
 - **frequentist** interpretation

Fittino Timeline

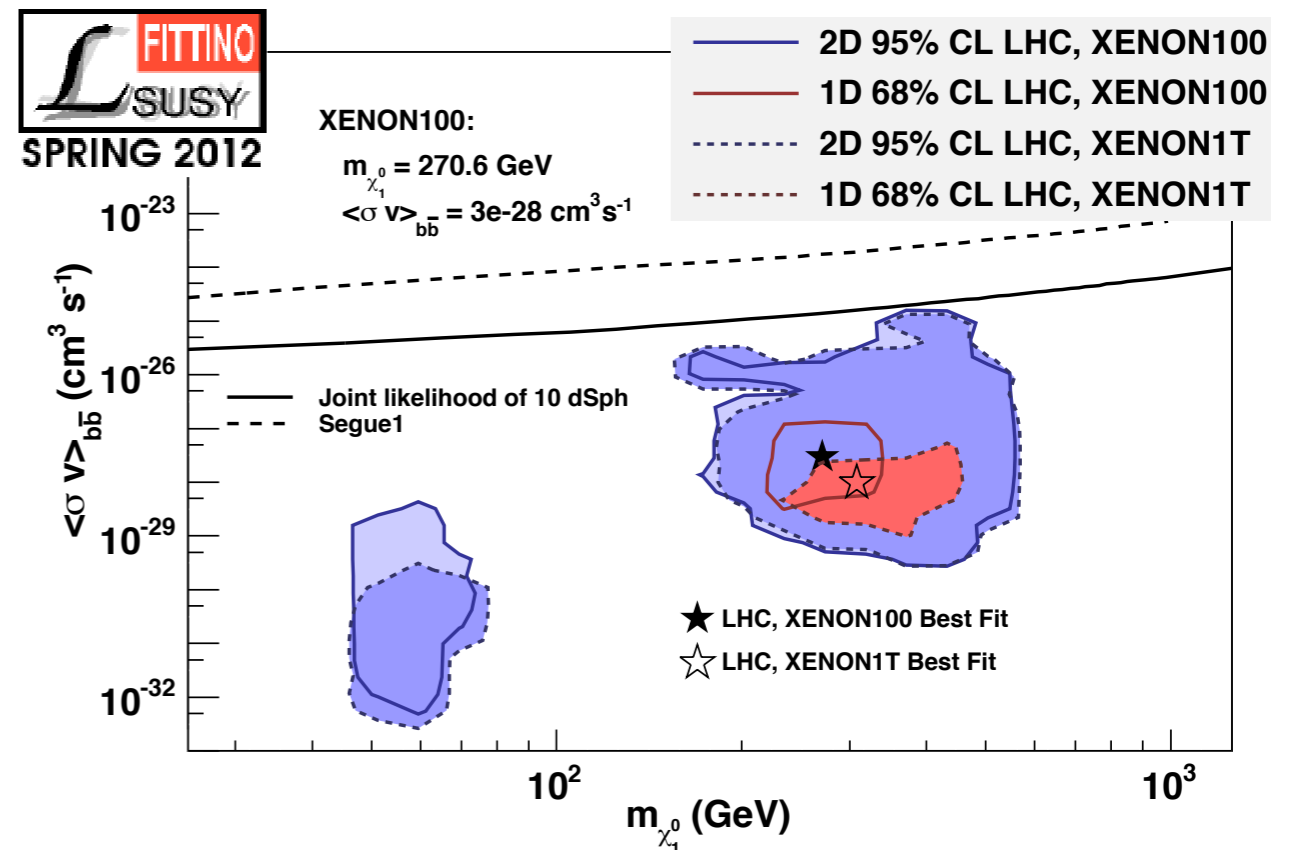
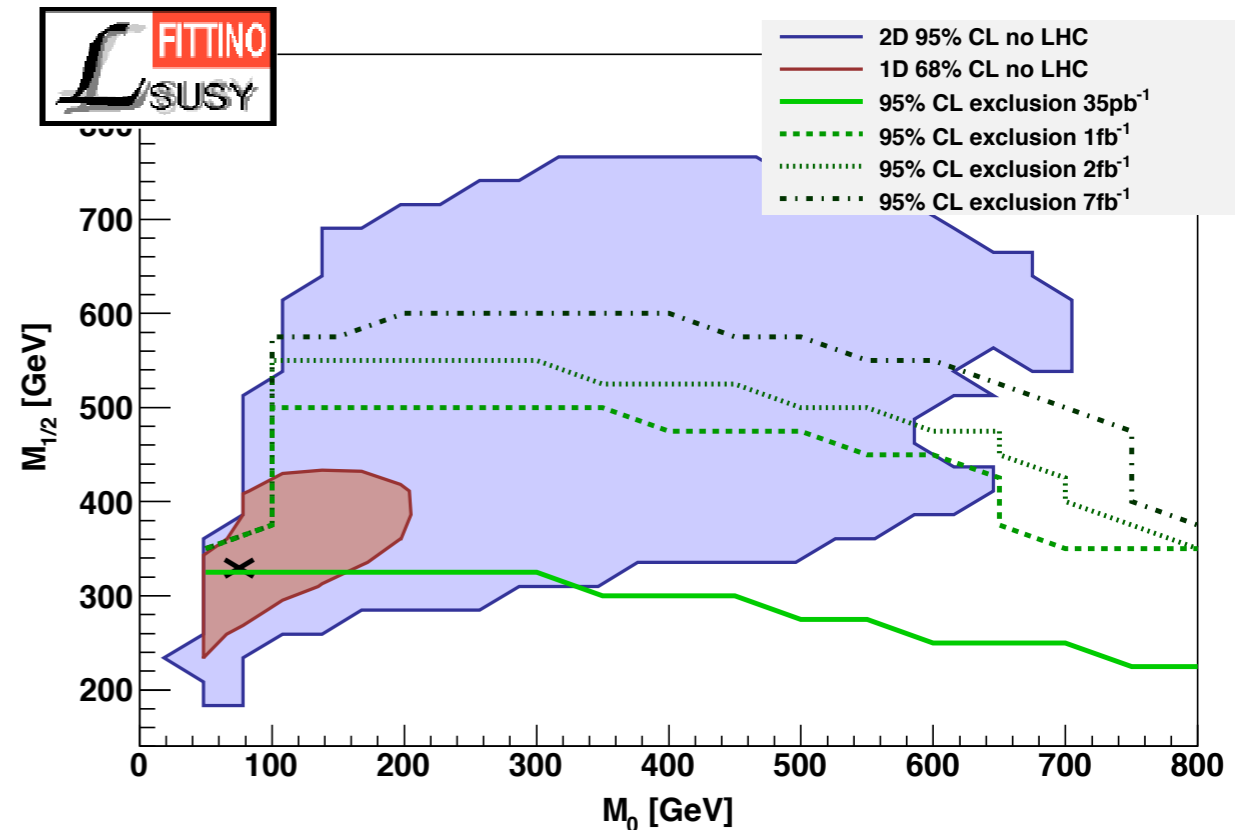
arXiv:1102.4693

some tension building up between **low energy observables** and **LHC**

arXiv:1204.4199

increasing tension

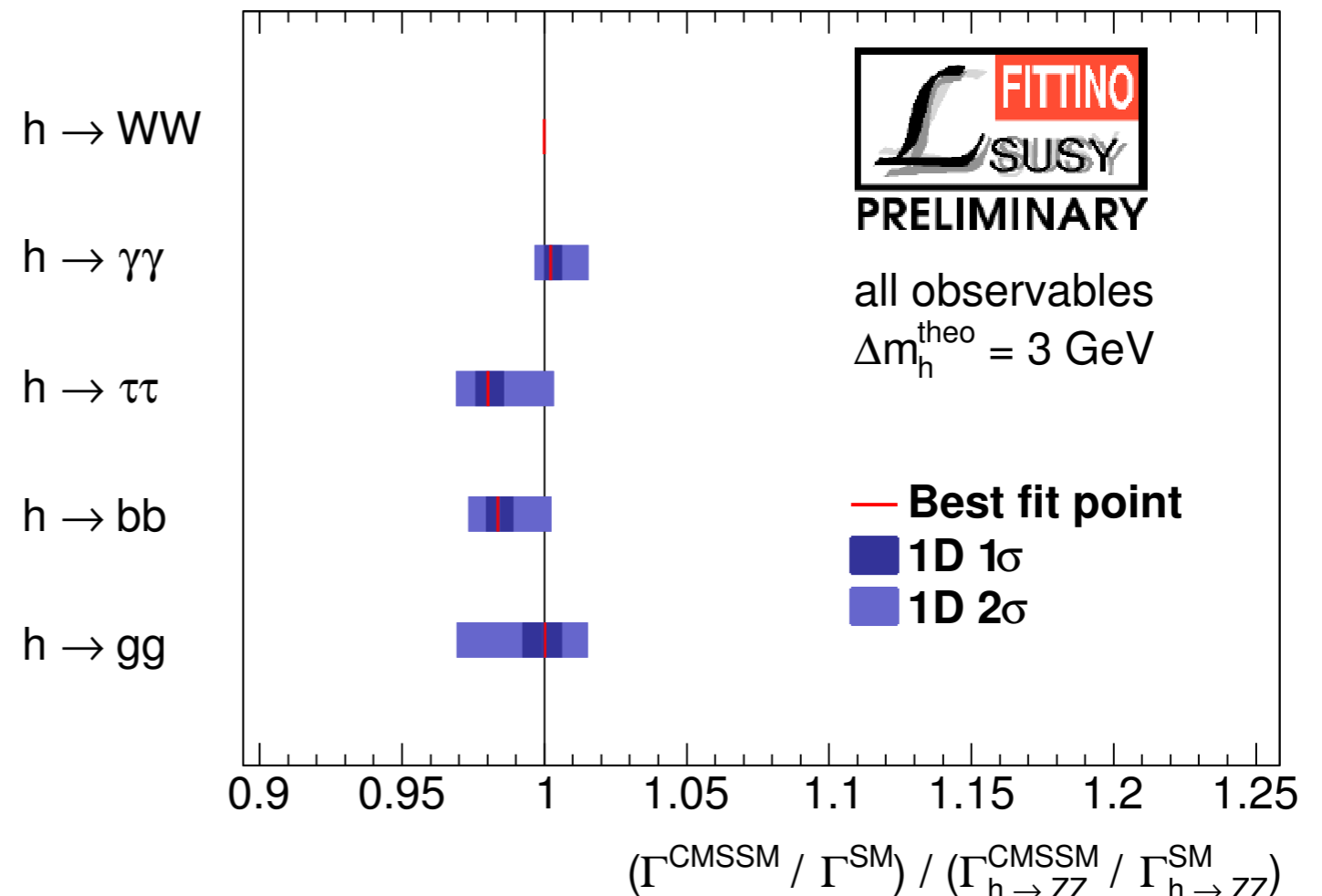
direct and indirect **astrophysical** detection experiments not yet sensitive to 2 sigma region



arXiv:1310.3045

SM like Higgs well described by CMSSM

χ^2/ndf decreases when the numerous Higgs measurements are taken into account



Updated measurements

Low energy observables

$\text{BR}(B_s \rightarrow \mu^+\mu^-)$	$(2.90 \pm 0.70 \pm 0.76_{\text{theo}}) \times 10^{-9}$	CMS + LHCb '13
$\text{BR}(B^\pm \rightarrow \tau^\pm \nu)$	$(1.14 \pm 0.22 \pm 0.07_{\text{theo}}) \times 10^{-4}$	PDG '13
$\text{BR}(b \rightarrow s \gamma)$	$(3.43 \pm 0.21 \pm 0.07 \pm 0.48_{\text{theo}}) \times 10^{-4}$	HFAG
Δm_s	$(17.719 \pm 0.036 \pm 0.023 \pm 4.200_{\text{theo}}) \text{ ps}^{-1}$	PDG '13
$a_\mu - a_\mu^{\text{SM}}$	$(28.7 \pm 8.0 \pm 2.0_{\text{theo}}) \times 10^{-10}$	Muon g-2, Davier et al
m_t	$(173.34 \pm 0.27 \pm 0.71) \text{ GeV}$	world average '14
m_W	$(80.385 \pm 0.015 \pm 0.010_{\text{theo}}) \text{ GeV}$	CDF + D0 '12
$\sin^2 \theta_{\text{eff}}$	$0.2311 \pm 0.00021 \pm 0.00012_{\text{theo}}$	LEP + SLD '06

Higgs boson properties and searches

- Higgs limits via **HiggsBounds**
- Higgs signals via **HiggsSignals**

Direct sparticle searches

- LEP chargino mass limit
- ATLAS MET + jets + 0 lepton search (20fb^{-1})

Astrophysical observables

- We require χ_1^0 to be the LSP
- $\Omega_{\text{CDM}}h^2 = 0.1187 \pm 0.0017 \pm 0.0119_{\text{theo}}$ (Planck '13)
- Direct detection limit from LUX

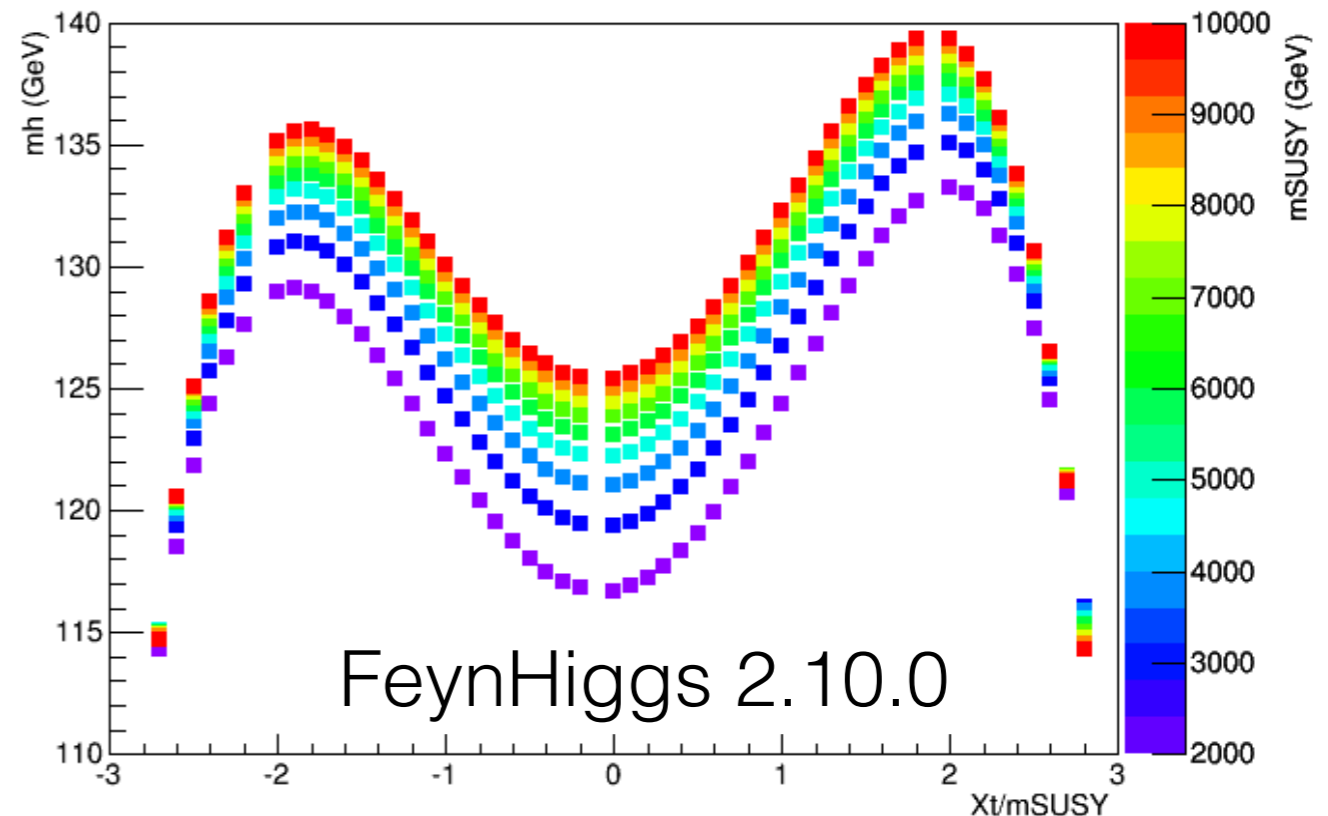
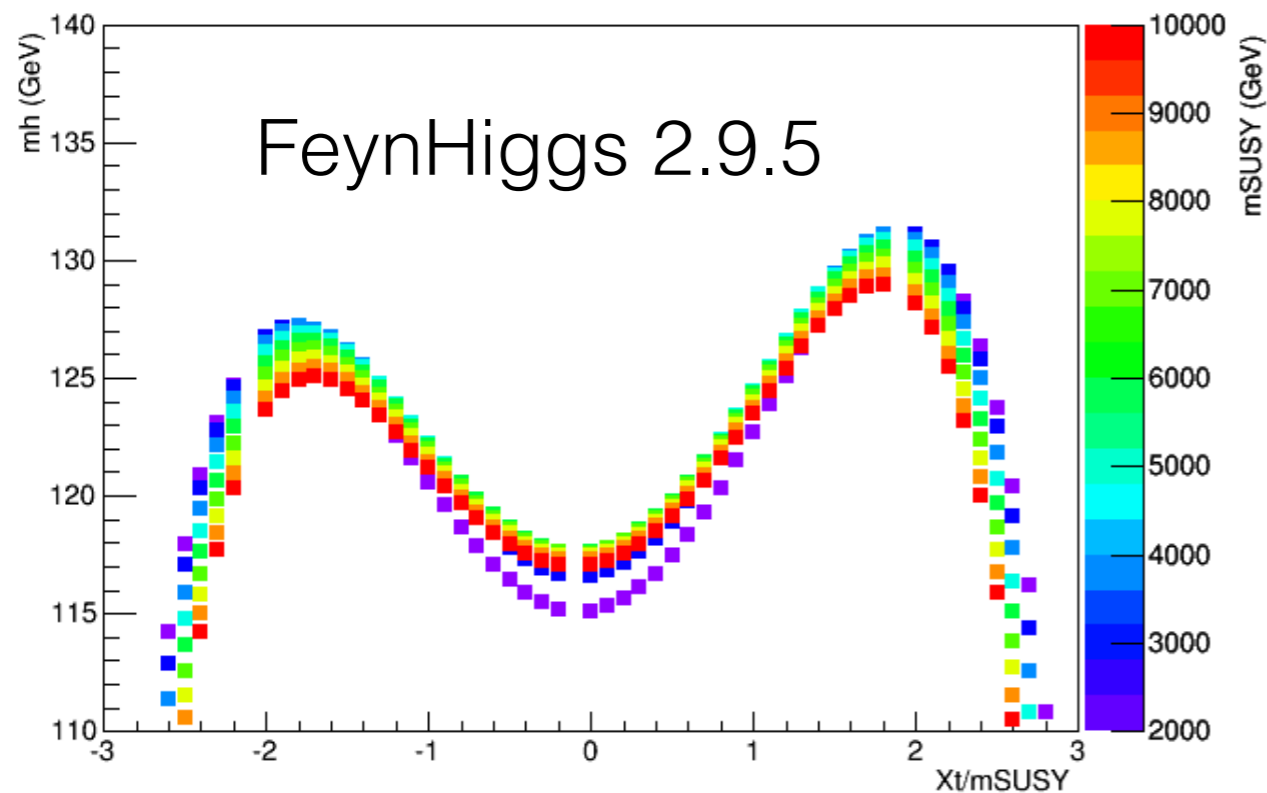
Model Predictions

To evaluate the corresponding model predictions we use:

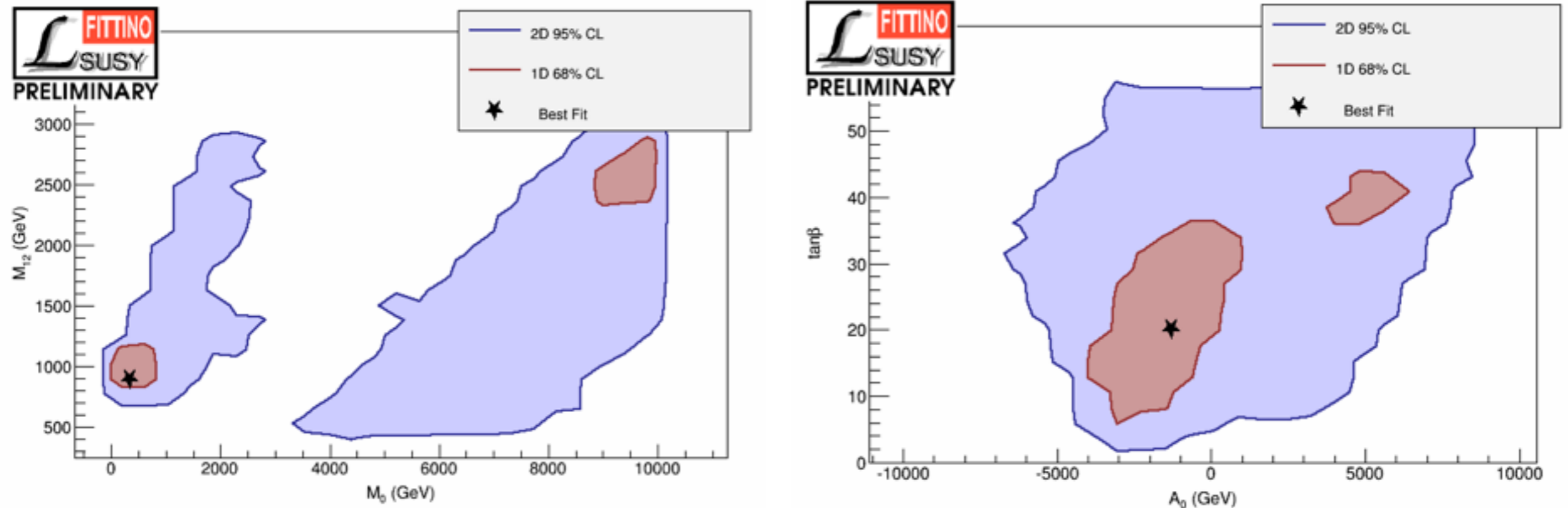
- **SPheno** for spectrum calculation
- **FeynHiggs** for Higgs properties, $a_\mu - a_\mu^{\text{SM}}$, $\sin^2 \theta_{\text{eff}}$, m_W
- **SuperIso** for $\text{BR}(B_s \rightarrow \mu^+\mu^-)$, $\text{BR}(B^\pm \rightarrow \tau^\pm \nu)$, $\text{BR}(b \rightarrow s\gamma)$
- **Prospino**, **Herwig++**, **Delphes** for direct sparticle searches
- **micrOMEGAs** for dark matter relic density
- **DarkSUSY** via **AstroFit** for direct detection cross section

Impact of new Higgs mass calculation

- Of course there are also improvements on the [theory side](#)
- The new Higgs mass calculation contained in [FeynHiggs 2.10.0](#) makes it significantly easier to reach high Higgs masses

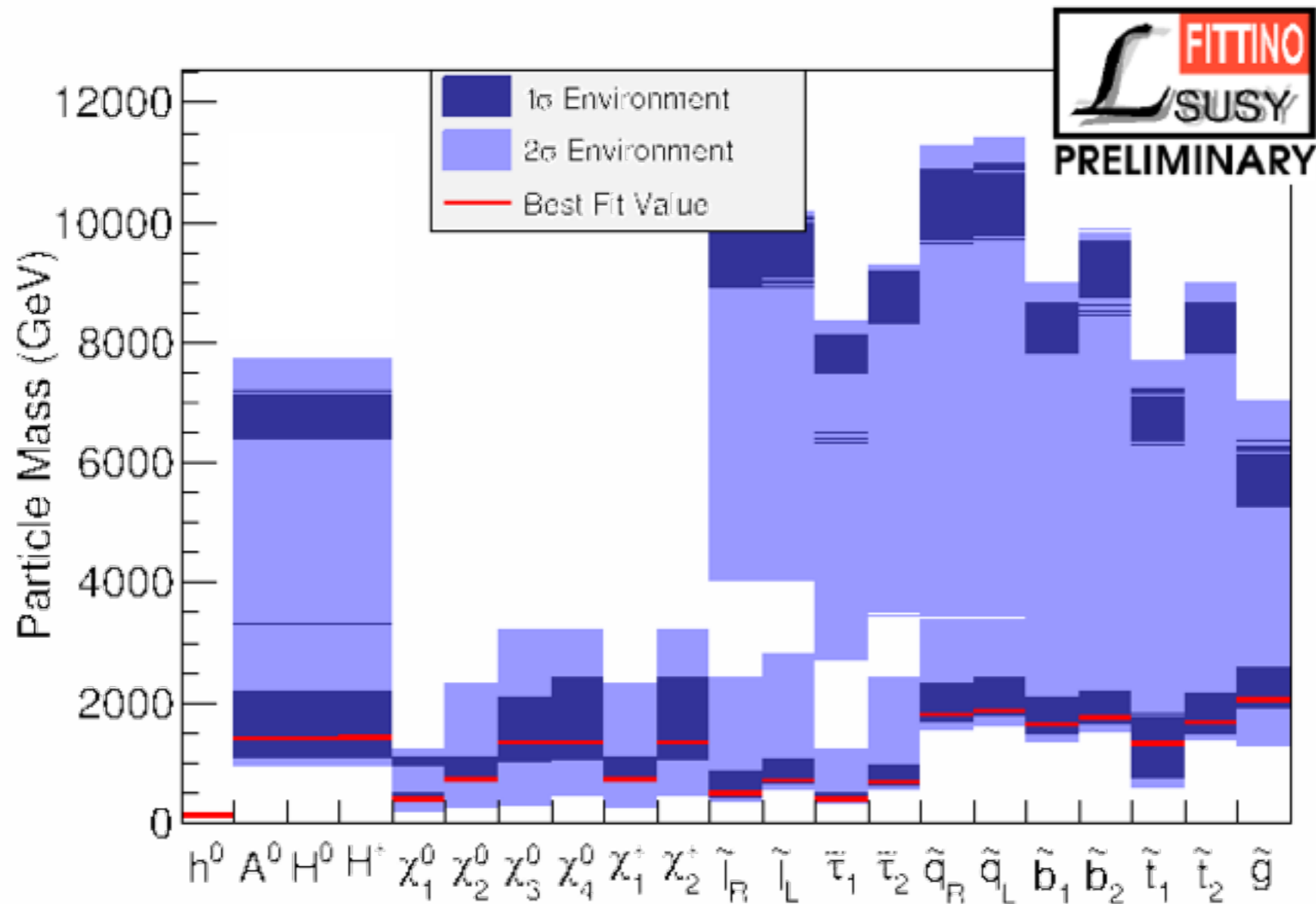


Preferred parameter region



- $\chi^2/\text{ndf} = 26.5/15$
- High mass region allowed at 1D 1sigma due to new Higgs mass calculation

Predicted mass spectrum



- squark and gluino masses at best fit point about 2 TeV
- But now also masses of 10 TeV allowed at 1 sigma

Summary of part I

- In the CMSSM there is **some tension** between **low energy observables** and exclusions from **LHC**
- The CMSSM is in agreement with **astrophysical** measurements but on the other hand **no convincing direct or indirect detection hints** are found
- A SM like **Higgs** is well described by the CMSSM with **large particle masses** but no BSM Higgs sector is found

What do we do with the CMSSM now?

There's at least one more thing to do!

How well does the CMSSM describe the data quantitatively?

P-Value

If the best fit point is realised in nature

doing a global fit to the measurement

how probable is it to get

a minimal χ^2 at least as bad as the one observed?

Difficulties

- If our χ^2 - function would be χ^2 - distributed we could just look up the integral

$$\int_{\chi_{\min}^2}^{\infty} P_{\chi_{\text{ndf}}^2}(x) dx$$

- Unfortunately this is not necessarily true because of:
 - **Non - linear** dependence of observables on parameters
 - **Non - gaussian** uncertainties
- Thus also χ^2/ndf isn't the appropriate goodness-of-fit measure

How well does the CMSSM describe the data quantitatively?

P-Value

If the best fit point is realised in nature

fitting the model to the measurements

how probable is it to get

a minimal χ^2 at least as bad as the one observed?

Toy fits

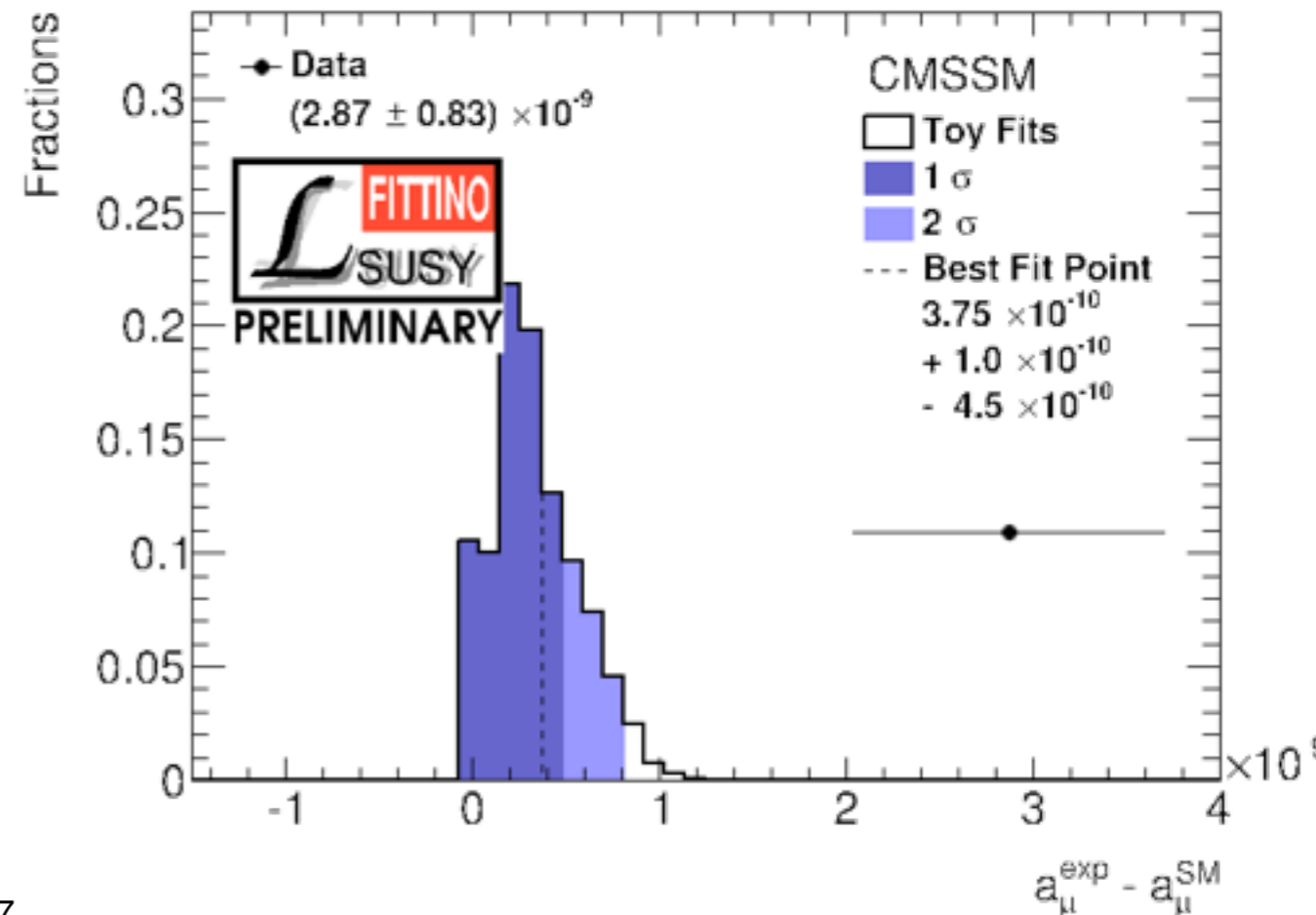
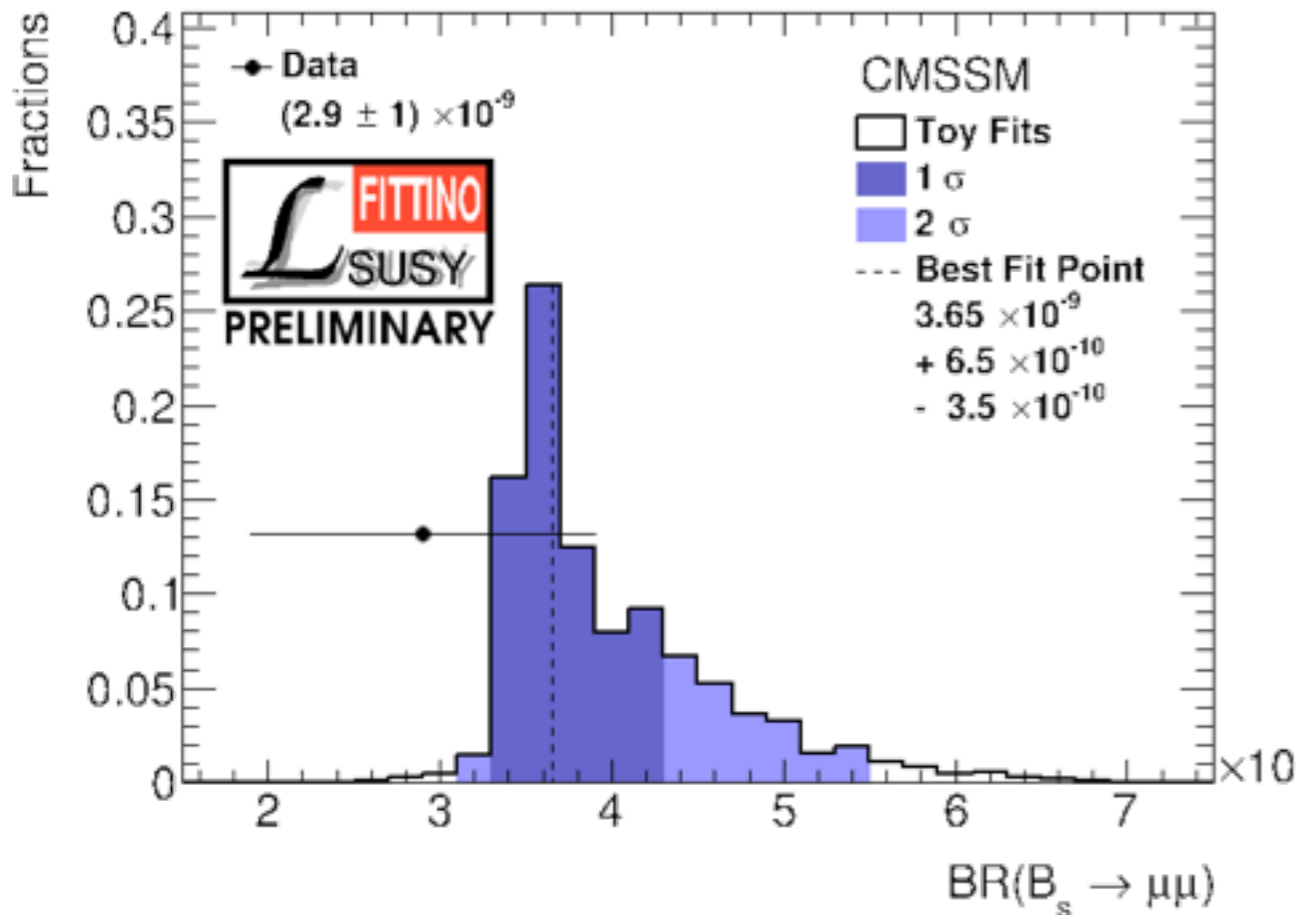
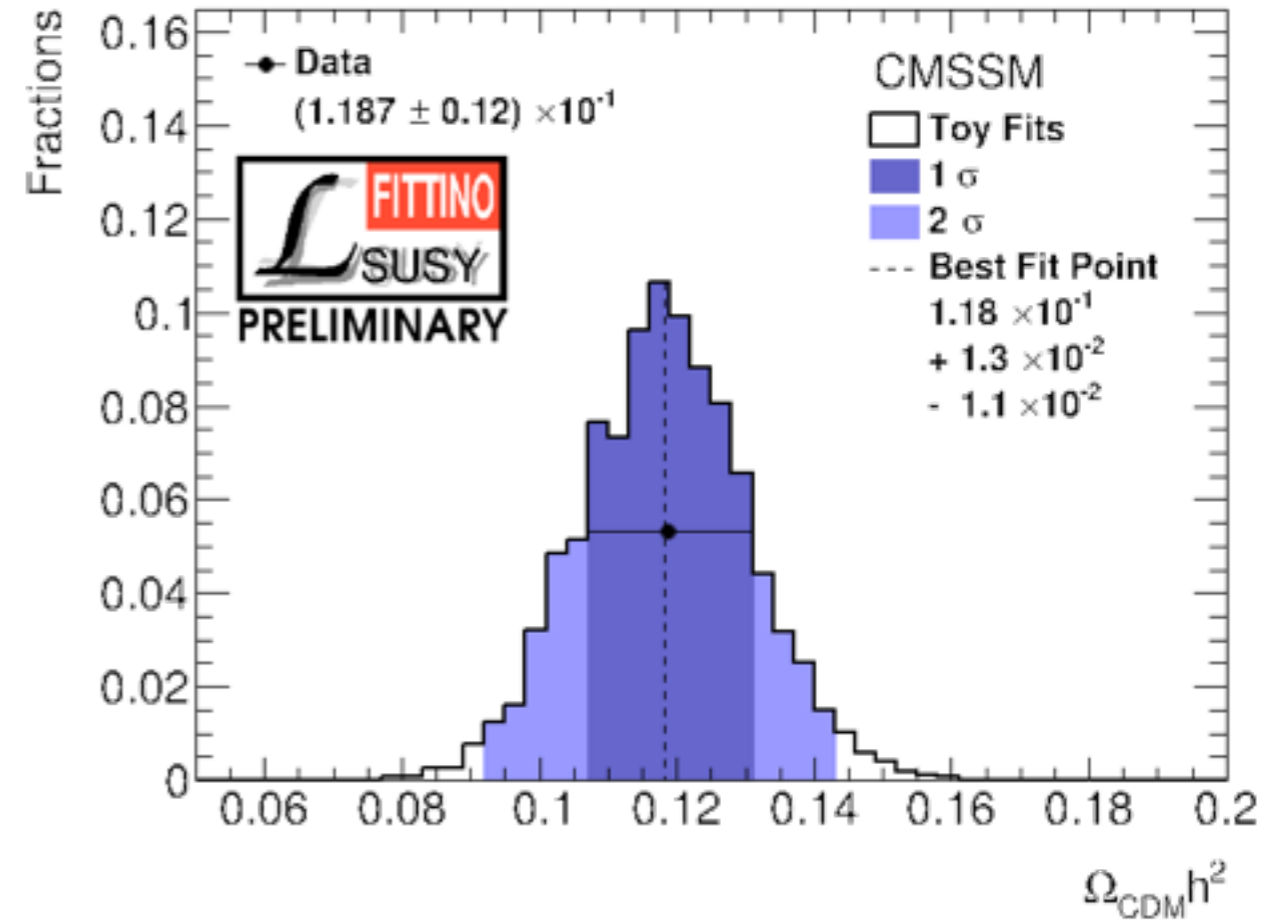
Smearing observables around the best fit prediction

and fitting the model to each of these toy measurements

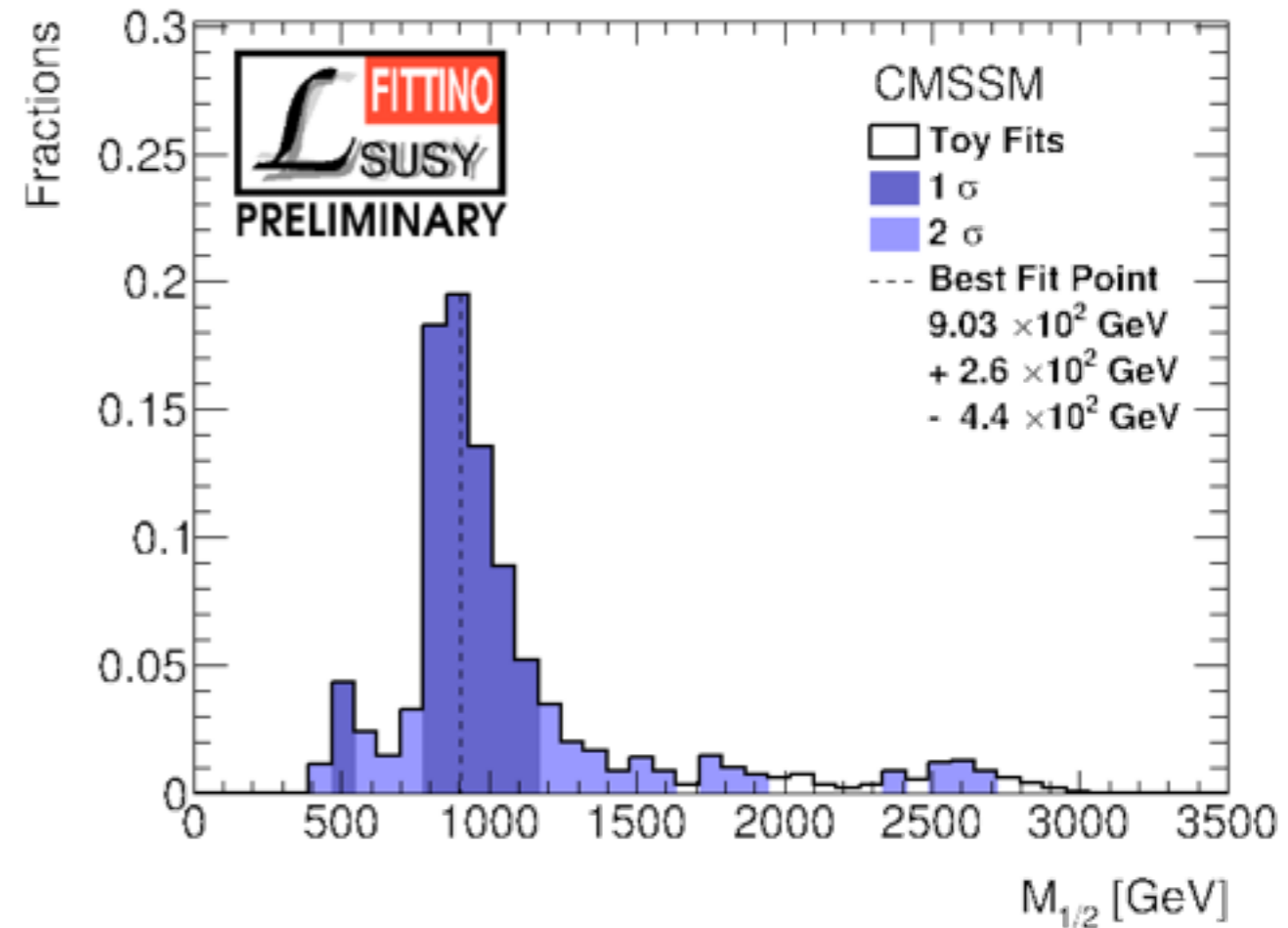
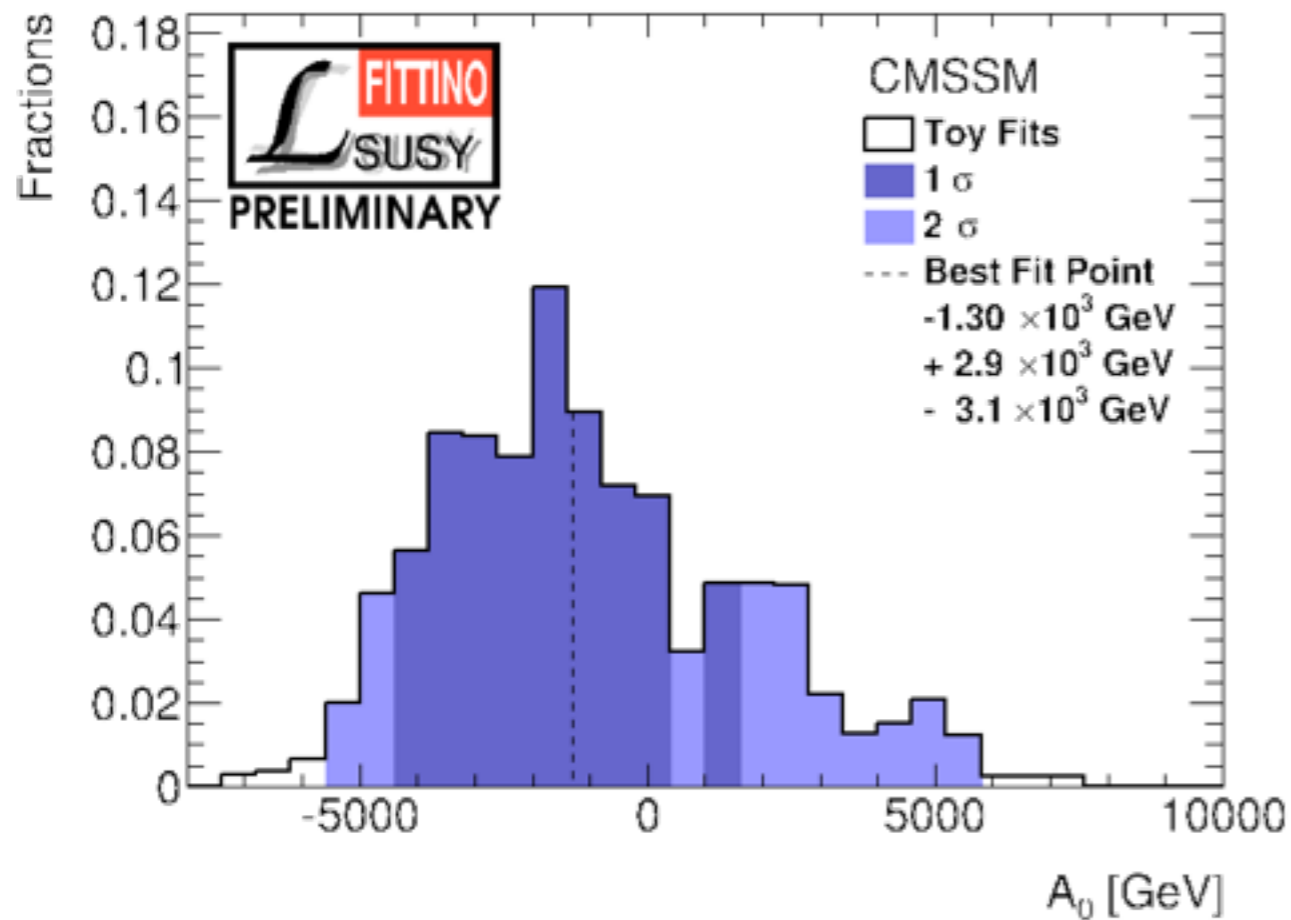
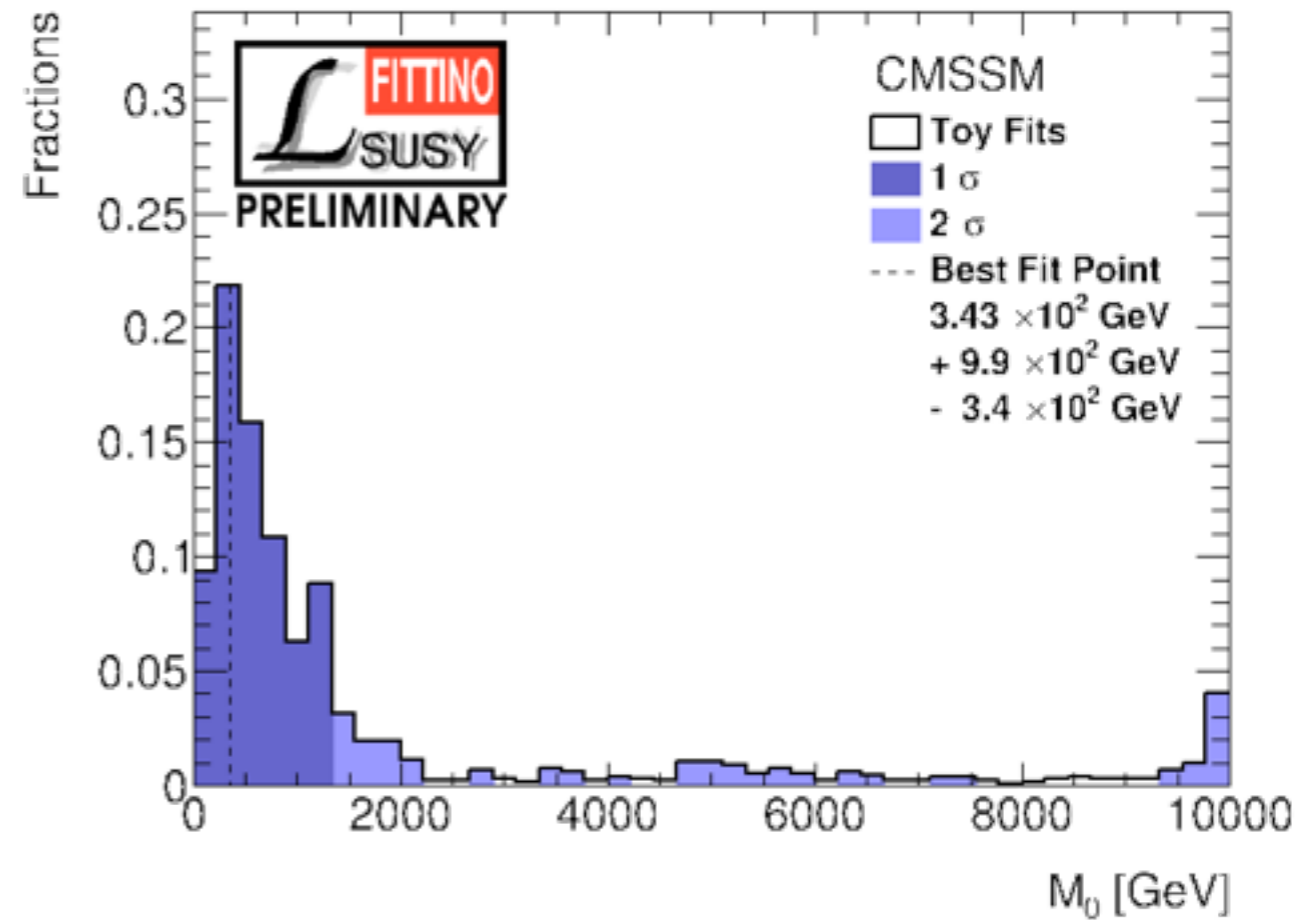
how often do you get

- Very common in HEP
- Hasn't been done in global SUSY fits (extremely CPU intensive)

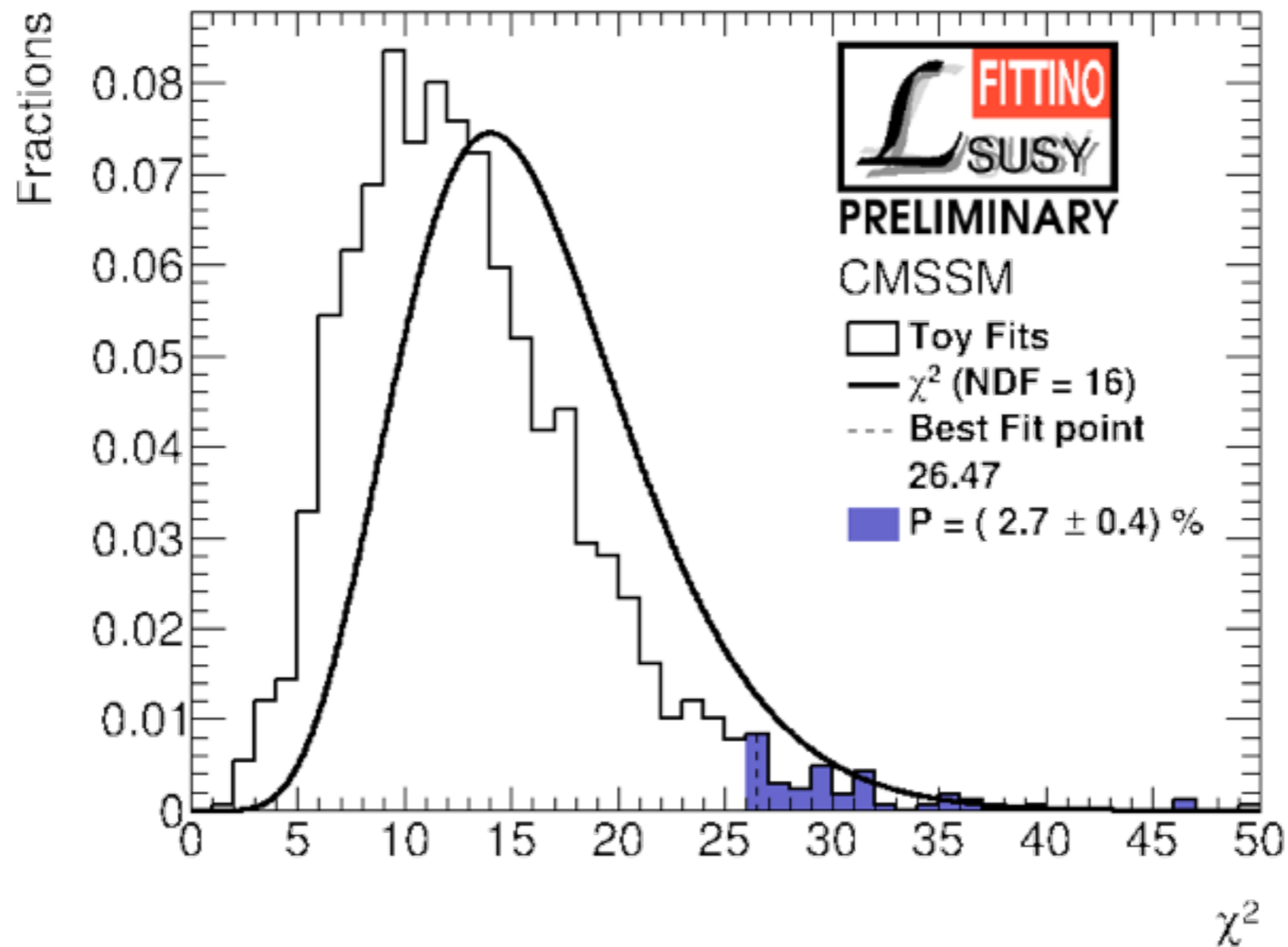
We repeat the fit described above **1600** times with smeared observables and get these **predicted observable values** at the best fit points.



Corresponding underlying
CMSSM **parameter values**
at the best fit points



World's first *very preliminary!* p-value for the CMSSM

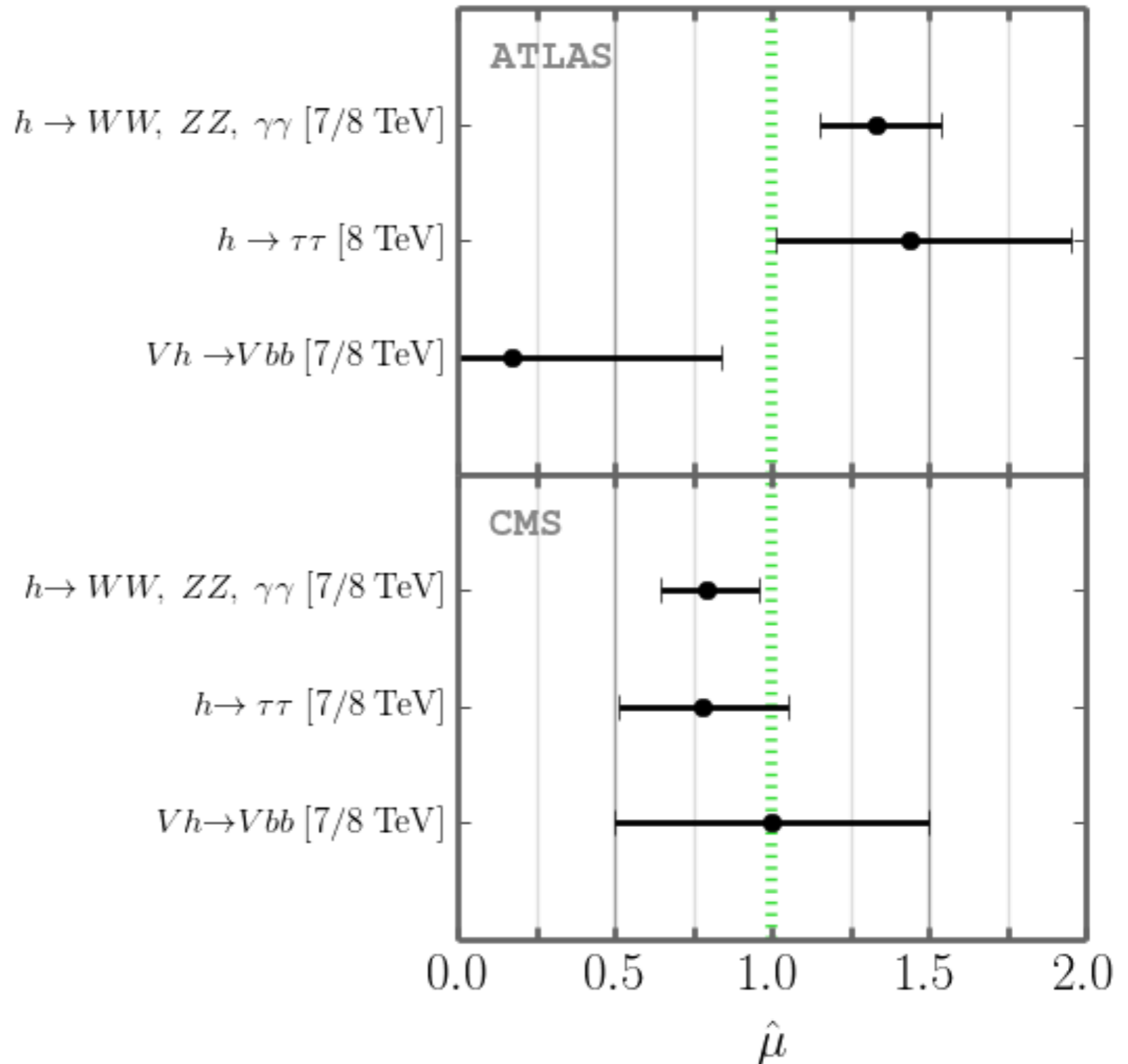


χ^2 /ndf overestimates goodness of fit.

Dependence on the input and its parametrization?

p-Value describes agreement with given selected data

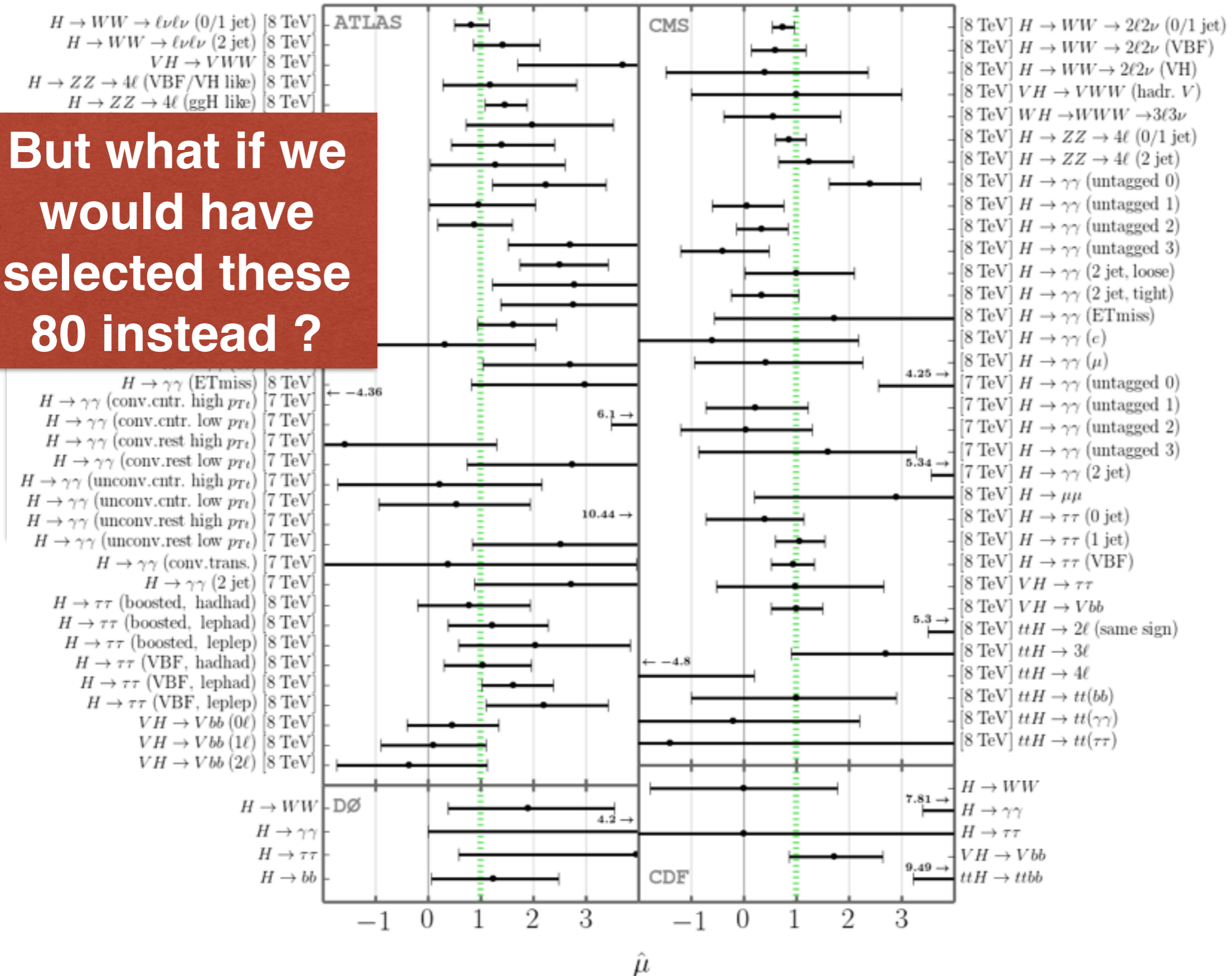
e. g. we selected these Higgs rate measurements, adding 6 ndf



Dependence on the input and its parametrization?

p-Value describes agreement with given selected data

But what if we would have selected these 80 instead ?



Summary of part II and outlook

- For the first time a **p-value** for a SUSY model has been calculated using global toy fits
- This gives an appropriate measure for the agreement between the **model and the selected data**
 - Possible dependance of p-value on (Higgs-) observable parametrisation will be studied
- We applied the procedure to the **CMSSM**
 - Applying it to more general models which decouple the Higgs, electroweak and strong sector will finally quantify how much better they perform

Backup

χ^2 contributions

At each parameter point \vec{P} calculate:

$$\chi^2 = \left(\vec{O}_{\text{meas}} - \vec{O}_{\text{pred}}(\vec{P}) \right)^T \text{cov}^{-1} \left(\vec{O}_{\text{meas}} - \vec{O}_{\text{pred}}(\vec{P}) \right) + \chi_{\text{limits}}^2$$

