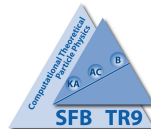


Constraining Supersymmetry using the relic density and the Higgs boson

in collaboration with S. Henrot-Versillé, R. Lafaye, T. Plehn, D. Zerwas, S. Plaszczynski, B. Rouillé d'Orfeuil and M. Spinelli,
Phys. Rev. D **89** (2014) 055017 [arXiv:1309.6958 [hep-ph]]

Michael Rauch | SUSY 2014, Jul 2014



INSTITUTE FOR THEORETICAL PHYSICS



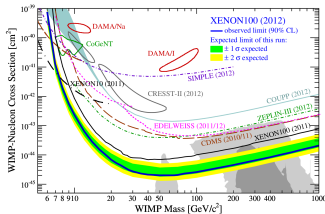
Experimental status:

- light Higgs found \Rightarrow hierarchy problem now real
- dark matter search experiments cutting into parameter space of weakly interacting dark matter
- direct searches:
 - Pessimist's view: no sign of additional SUSY particles
 - Optimist's view: first half already found, but no indication of second half yet

\Rightarrow available parameter space from indirect constraints

Models studied:

- mSUGRA/CMSSM
test case for models where Higgs sector, weak dark matter sector and strongly interacting sector linked at high scale
- 13-parameter TeV-scale pMSSM
bottom-up approach: no unification scheme imposed a priori
 \rightarrow ultimately determine high-scale unification from data



Input measurements

| measurement | value and error |
|--|--|
| m_h | $(126 \pm 0.4 \pm 0.4 \pm 3)$ GeV |
| $\Omega_{\text{cdm}} h^2$ Planck | $0.1187 \pm 0.0017 \pm 0.012$ |
| $\Omega_{\text{cdm}} h^2$ WMAP-9year | $0.1157 \pm 0.0023 \pm 0.012$ |
| $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ | $(3.2_{-1.2}^{+1.5} \pm 0.2) \times 10^{-9}$ |
| $\text{BR}(b \rightarrow X_s \gamma)$ | $(3.55 \pm 0.24 \pm 0.09) \times 10^{-4}$ |
| Δa_μ | $(287 \pm 63 \pm 49 \pm 20) \times 10^{-11}$ |
| m_t | $(173.5 \pm 0.6 \pm 0.8)$ GeV |

+ Xenon100 + Higgs couplings + EW precision
(in total 95 individual measurements)

Tools

- SUSY spectrum: SuSpect 2 [Djouadi, Kneur, Moultaka]
- Higgs BR: SUSY-Hit [Djouadi, Mühlleitner, Spira]
- Dark matter: micrOMEGAs [Bélanger, Boudjema, Pukhov, Semenov]
- Electroweak precision data: SUSYPope [Weber et al.]
- B decay & $(g - 2)_\mu$: SuSpect 2 + micrOMEGAs

Latest results by other groups:

- Fittino: LHC data + WMAP-7year on CMSSM and NUHM
- MasterCode: also including Xenon100 and Planck, CMSSM and NUHM
more general models work in progress
- C. Boehm et al.: Light neutralino DM with Planck + Higgs + Xenon100
in TeV-scale MSSM
- BayesFITS: Planck, Higgs, DM, . . . in CMSSM and 9-parameter MSSM
- Mühleitner, Walz et al.: global NMSSM fit in progress
- . . . (many papers looking at more specific aspects)

⇒ Only one other group going beyond high-scale unification models so far

⇒ Our analysis:

- wider explored SUSY parameter space
- updated measurements

Algorithms:

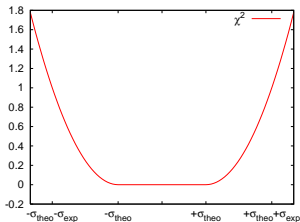
- Weighted Markov chain
- Cooling Markov chain (\sim simulated annealing)
- Modified gradient fit (Minuit)
- Grid scan
- Nested Sampling [Skilling; Feroz, Hobson]

Errors:

- three types:
 - Gaussian – arbitrary correlations possible (\rightarrow systematic errors)
 - Poisson
 - box-shaped (RFit) [CKMFitter]
- assignment as in exp. studies
- adaption to likelihood input easy

Output of SFitter:

- fully-dimensional log-likelihood map
- one- and two-dimensional distributions via
 - marginalization (Bayesian)
 - profile likelihood (Frequentist)
- list of best points

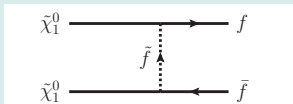


Assume lightest neutralino $\tilde{\chi}_1^0$ is the LSP

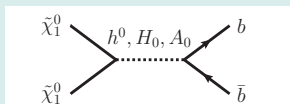
Neutralinos are linear combinations of gauge eigenstates (\tilde{B} , \tilde{W}^3 , \tilde{H}_1^1 , \tilde{H}_2^2)

Bulk relic density too high \rightarrow need reduction mechanism

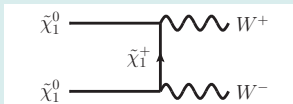
Bino LSP, light $\tilde{\chi}_1^0$



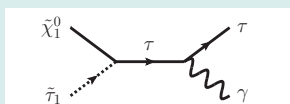
Higgs funnel, $m_{\tilde{\chi}_1^0} \simeq \frac{m_H}{2}$



Higgsino LSP



Coannihilation, $m_{\tilde{\chi}_1^0} \simeq m_{\tilde{\tau}_1}$



CMSSM as test case

Free parameters:

- m_0 common scalar mass parameter: $m_0 \in [0; 5] \text{ TeV}$
- $m_{1/2}$ common gaugino mass parameter $m_{1/2} \in [0; 5] \text{ TeV}$
- A_0 common trilinear mass parameter $A_0 \in [-4; 4] \text{ TeV}$
- $\tan \beta$ ratio of vevs $\tan \beta \in [1; 61]$
- $\text{sign}(\mu)$ sign of Higgsino mass parameter both cases (only $\mu > 0$ shown)
- m_t top mass

→ small number of parameters

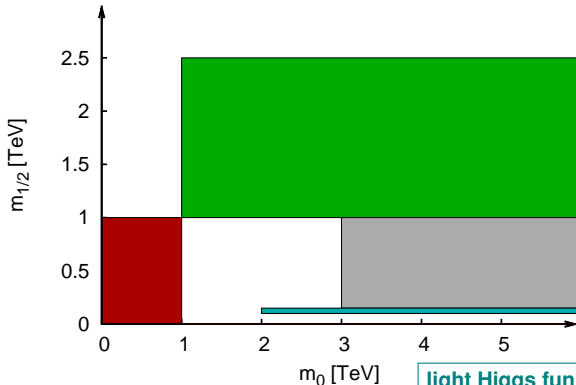
→ highly correlated

e.g.

$$A_t = A_0 \left(1 - \frac{0.75}{\sin^2 \beta} \right) - 3.5 m_{1/2} \left(1 - \frac{0.41}{\sin^2 \beta} \right) \approx \begin{cases} 0.62 A_0 - 2.8 m_{1/2} & \text{for } \tan \beta = 1 \\ 0.25 A_0 - 2.1 m_{1/2} & \text{for } \tan \beta \gg 1 \end{cases}$$

↔ driven by $m_{1/2}$ for larger $\tan \beta$ (→ Higgs mass)

Annihilation channels in CMSSM



A-funnel region

$\tan \beta \simeq 50$

$m_{\text{LSP}} \simeq \frac{1}{2} m_{A_0, H_0}$

Focus point region

ruled out by Xenon100
and LHC \tilde{g} exclusions
LSP mostly Higgsino-like ($\rightarrow WW$)

stau co-annihilation region

moderate $\tan \beta$

$m_{\text{LSP}} \simeq m_{\tilde{\tau}_1}$

light Higgs funnel region

$m_{h^0} \simeq 2m_{\text{LSP}} \simeq 126 \text{ GeV}$

LSP mostly Bino ($\sim 10\%$ Higgsino admixture)
ruled out by LHC \tilde{g} exclusion

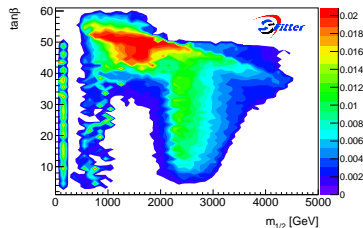
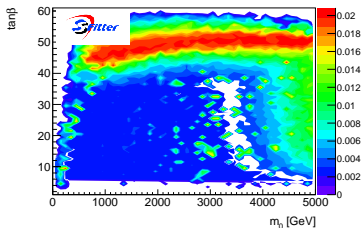
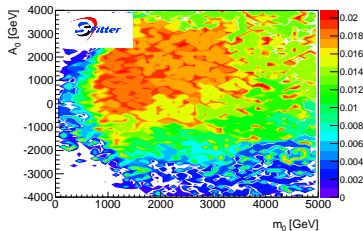
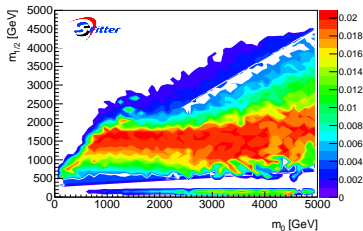
not in CMSSM parameter space:

neutralino-chargino co-annihilation region

containing H^0 funnel contribution

LSP mainly Wino or Higgsino

CMSSM results



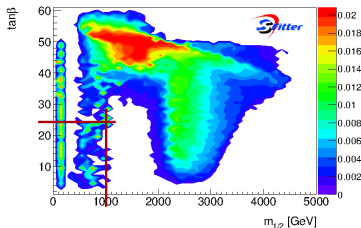
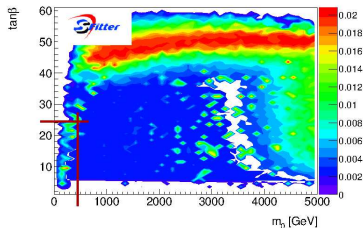
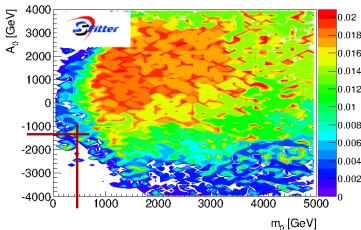
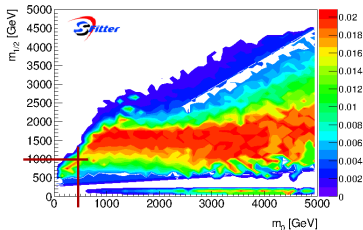
clearly structures visible \rightarrow identify with annihilation channels

CMSSM results

Coannihilation region

Best-fit point:

| m_0 | $m_{1/2}$ | $\tan \beta$ | A_0 | $-2 \log L/\text{dof}$ |
|---------|-----------|--------------|-----------|------------------------|
| 442 GeV | 999 GeV | 24.6 | -1347 GeV | 49.0/75 |

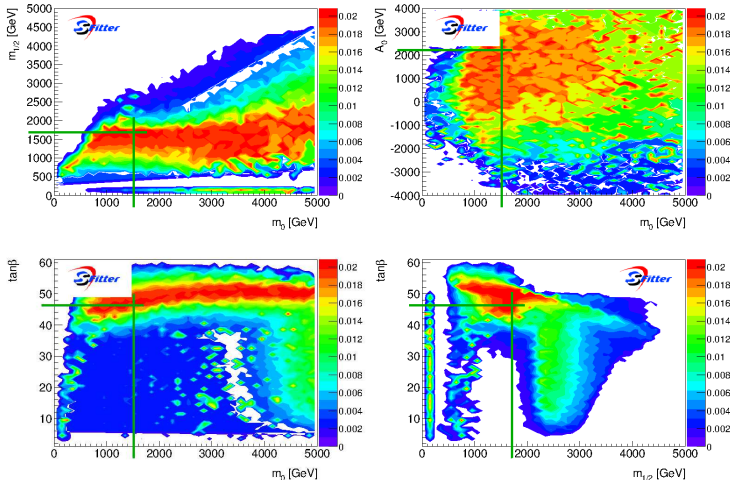


CMSSM results

A-funnel region

Best-fit point:

| m_0 | $m_{1/2}$ | $\tan \beta$ | A_0 | $-2 \log L/\text{dof}$ |
|----------|-----------|--------------|----------|------------------------|
| 1500 GeV | 1700 GeV | 46.5 | 2231 GeV | 49.2/75 |

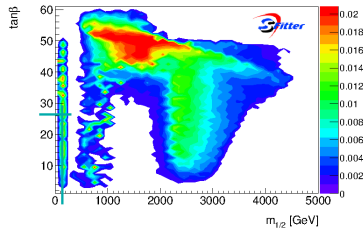
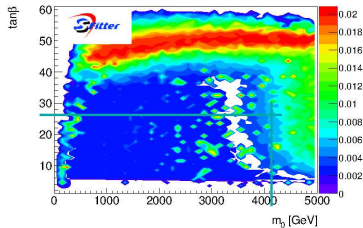
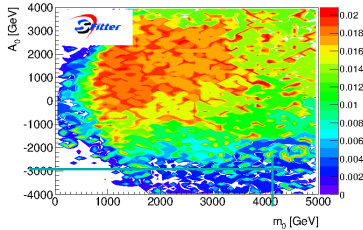
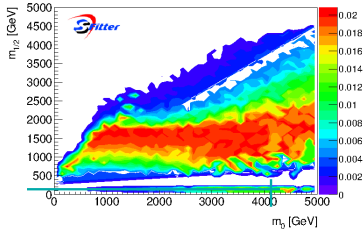


CMSSM results

h^0 -funnel region $m_{\tilde{g}} = 476$ GeV \rightarrow ruled out by LHC \tilde{g} searches

Best-fit point:

| m_0 | $m_{1/2}$ | $\tan \beta$ | A_0 | $-2 \log L/\text{dof}$ |
|----------|-----------|--------------|-----------|------------------------|
| 4232 GeV | 135 GeV | 26.6 | -2925 GeV | 46.1/75 |



Assumptions:

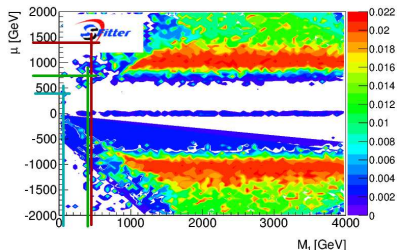
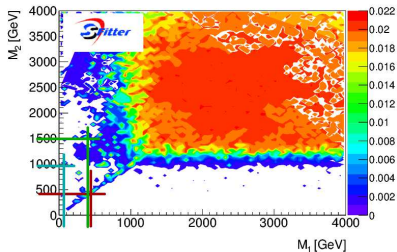
- all squark and gluino masses above LHC actual limits
⇒ $M_{\tilde{q}_{1,L}} = M_{\tilde{q}_{2,L}} = M_{\tilde{u}_R, \tilde{d}_R, \tilde{c}_R, \tilde{s}_R, \tilde{b}_R} = M_3 = 2 \text{ TeV}$
- $A_b = 0$

⇒ 13-parameter pMSSM:

- | | | | |
|----------------|---------------|---|--------------|
| ■ $\tan \beta$ | ∈ [1; 61] | ■ $M_{\tilde{e}_L} = M_{\tilde{\mu}_L}$ | ∈ [0; 5] TeV |
| ■ M_1 | ∈ [0; 4] TeV | ■ $M_{\tilde{e}_R} = M_{\tilde{\mu}_R}$ | ∈ [0; 5] TeV |
| ■ M_2 | ∈ [0; 4] TeV | ■ $M_{\tilde{\tau}_L}$ | ∈ [0; 5] TeV |
| ■ μ | ∈ [-2; 2] TeV | ■ $M_{\tilde{\tau}_R}$ | ∈ [0; 5] TeV |
| ■ m_A | ∈ [0; 5] TeV | ■ $M_{\tilde{q}_{3,L}}$ | ∈ [0; 5] TeV |
| ■ A_τ | ∈ [-4; 4] TeV | ■ $M_{\tilde{t}_R}$ | ∈ [0; 5] TeV |
| ■ A_t | ∈ [-4; 4] TeV | ■ | |
| ■ m_t | | | |

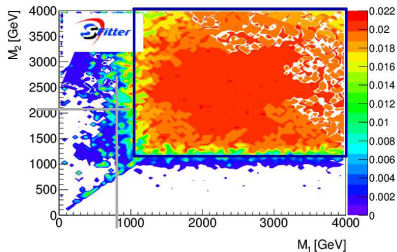
→ decouples strongly interacting MSSM sector
from weak sector (Higgs and DM predictions)

↔ stop part retained due to large effect on Higgs sector



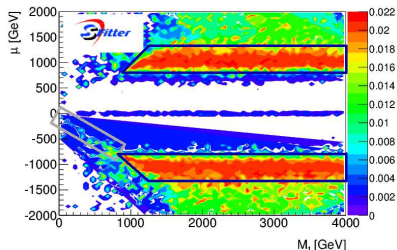
Recover regions of CMSSM scenario:

- **stau co-annihilation**
diagonal strip at small M_1, M_2
e.g. $m_{\tilde{\chi}_0^1} = 429$ GeV,
 $m_{\tilde{\tau}_1} = 429.7$ GeV
- **h^0 funnel**
 $M_1 \sim 63$ GeV
almost independent of M_2
gluino mass now
independent parameter
⇒ no longer constrained by
direct searches
- **A funnel**
e.g. $M_1 = 400$ GeV, $M_2 = 1500$ GeV,
 $\mu = 750$ GeV
same behaviour as in CMSSM



New allowed regions show up:

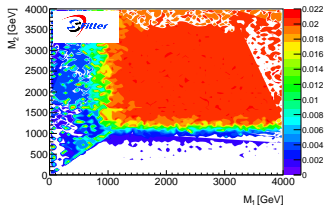
- bino-higgsino region
strip in M_1 - μ plane for $\mu < 0$,
 $M_1 \sim |\mu|$
including chargino co-annihilation
e.g. $M_1 = 800$ GeV, $\mu = -800$ GeV
- large higgsino region
 $M_1, M_2 > 1.2$ TeV with $|\mu| \sim 1.2$ TeV
dominated by
chargino co-annihilation



Impact of Planck

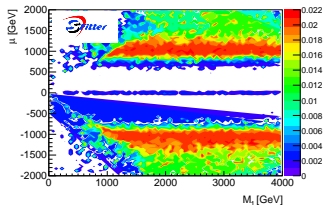
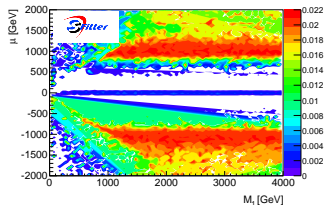
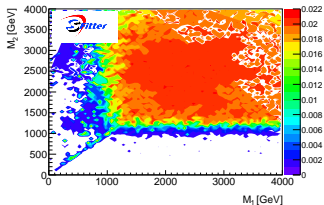
WMAP

$$\Omega_{\text{cdm}} h^2 = 0.1157 \pm 0.0023 \pm 0.012$$



Planck:

$$\Omega_{\text{cdm}} h^2 = 0.1187 \pm 0.0017 \pm 0.012$$



only small differences visible

- bino-higgsino region less constrained with WMAP data
- stricter constraints for larger μ in higgsino LSP scenario
- h^0 funnel more constrained

Analysis of MSSM parameter space

- CMSSM and 13-parameter pMSSM
- bottom-up approach for latter
→ determine high-scale unification from data
- include constraints from
 - cosmological studies
 - direct dark matter searches
 - collider measurements (e.g. Higgs mass)
 - direct and indirect collider constraints

Classification by dark matter annihilation channel

- regions in both CMSSM and pMSSM13:
stau co-annihilation, A -funnel
- new channels for pMSSM13 only:
light-Higgs funnel, mixed bino-higgsino region, large higgsino region

→ SUSY pushed towards **high new-physics mass scale**

→ **little tension** from non-observation at 8 TeV run of LHC

Supersymmetric particles' masses (in GeV) for the three best-fit points:

| | co-ann | A | h | | co-ann | A | h |
|------------------------|--------|------|------|--------------------|--------|-------|------|
| \tilde{e}_L | 792 | 1860 | 4210 | \tilde{g} | 2178 | 3596 | 476 |
| \tilde{e}_R | 575 | 1621 | 4223 | $\tilde{\chi}_1^0$ | 429 | 745 | 59 |
| $\tilde{\nu}_{eL}$ | 788 | 1858 | 4209 | $\tilde{\chi}_2^0$ | 809 | 1379 | 118 |
| $\tilde{\mu}_L$ | 792 | 1860 | 4210 | $\tilde{\chi}_3^0$ | -1407 | -1588 | -507 |
| $\tilde{\mu}_R$ | 575 | 1621 | 4223 | $\tilde{\chi}_4^0$ | 1412 | 1603 | 512 |
| $\tilde{\nu}_{\mu L}$ | 788 | 1858 | 4209 | $\tilde{\chi}_1^+$ | 810 | 1379 | 119 |
| $\tilde{\tau}_1^-$ | 430 | 1103 | 3920 | $\tilde{\chi}_2^+$ | 1412 | 1603 | 514 |
| $\tilde{\tau}_2^-$ | 756 | 1666 | 4062 | | | | |
| $\tilde{\nu}_{\tau L}$ | 744 | 1661 | 4061 | | | | |

| | co-ann | A | h | | co-ann | A | h |
|---------------|--------|------|------|-------|--------|-------|-------|
| \tilde{q}_L | 2020 | 3527 | 4174 | h | 123.0 | 123.0 | 124.8 |
| \tilde{q}_R | 1939 | 3397 | 4192 | H | 1423 | 1498 | 3624 |
| \tilde{b}_1 | 1754 | 3046 | 3190 | A | 1423 | 1498 | 3624 |
| \tilde{b}_2 | 1849 | 3101 | 3877 | H^+ | 1425 | 1500 | 3625 |
| \tilde{t}_1 | 1426 | 2771 | 2374 | | | | |
| \tilde{t}_2 | 1791 | 3105 | 3212 | | | | |

MSSM best-fit points and particle masses

| | co-ann | A-funnel | h-funnel | bino-higgs | higgsino |
|------------------------|---------|----------|----------|------------|----------|
| $\tan \beta$ | 25 | 18 | 26.6 | 54 | 29 |
| M_1 | 430 | 400 | 59 | 800 | 1543 |
| M_2 | 788 | 1500 | 960 | 2174 | 2898 |
| μ | 1400 | 750 | 484 | -800 | 1070 |
| $M_{\tilde{\mu}_L}$ | 791 | 1586 | 4210 | 3994 | 2884 |
| $M_{\tilde{\mu}_R}$ | 573 | 2789 | 4223 | 1002 | 2790 |
| $M_{\tilde{\tau}_L}$ | 747 | 1067 | 4062 | 3744 | 3355 |
| $M_{\tilde{\tau}_R}$ | 440 | 2789 | 3921 | 2040 | 2058 |
| A_τ | -1690 | -3038 | -2570 | 2338 | -3533 |
| $M_{\tilde{g}_{3L}}$ | 1744 | 3938 | 3162 | 1683 | 2210 |
| $M_{\tilde{t}_R}$ | 1441 | 3997 | 2319 | 2111 | 2984 |
| A_t | -2142 | -3158 | -1230 | -2162 | -3026 |
| m_A | 1423 | 781 | 3626 | 1000 | 784 |
| m_t | 174.0 | 173.5 | 173.5 | 173.6 | 173.5 |
| $-2 \log L/\text{dof}$ | 47.9/65 | 44.2/65 | 46.5/65 | 42.5/65 | 37.8/65 |

| | co-ann | A-funnel | h-funnel | bino-higgs | higgsino |
|----------------------|--------|----------|----------|------------|----------|
| $\tilde{\chi}_1^0$ | 429 | 398 | 58.5 | 768 | 1066 |
| $\tilde{\chi}_2^0$ | 783 | 749 | 480 | -801 | -1071 |
| $\tilde{\chi}_3^0$ | -1402 | -751 | -488 | 829 | 1545 |
| $\tilde{\chi}_4^0$ | 1406 | 1506 | 969 | 2178 | 2900 |
| $\tilde{\chi}_1^\pm$ | 784 | 747 | 480 | 799 | 1069 |
| $\tilde{\chi}_2^\pm$ | 1407 | 1506 | 969 | 2178 | 2900 |
| h | 123.2 | 125.3 | 122.1 | 123.2 | 124.5 |
| H | 1423 | 781 | 3626 | 1000 | 784 |
| A | 1423 | 781 | 3626 | 1000 | 784 |
| H^\pm | 1425 | 785 | 3627 | 1003 | 788 |