

Lepton number violation with Dirac neutrinos

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based on

J.H., PRD 88, 076004 (2013),

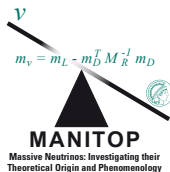
J.H. and Werner Rodejohann,
EPL 103, 32001 (2013).



INTERNATIONAL
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RESEARCH SCHOOL



FOR PRECISION TESTS
OF FUNDAMENTAL
SYMMETRIES



Baryon and lepton number

- B and L classically conserved in the Standard Model.
- $B + L$ theoretically broken non-perturbatively: $\Delta(B + L) = 6$.
- $B - L$ *globally* conserved.

Fate of fundamental $U(1)_{B-L}$ from **experiments**.

Linked to neutrino nature and matter–antimatter asymmetry.

- $B - L$ *locally* conserved after adding three ν_R .
 \Rightarrow Neutrinos massive!

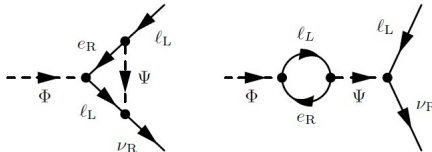
Three possibilities for (local) $U(1)_{B-L}$:

- 1 **Unbroken $B - L$** : Dirac neutrinos + leptogenesis.
- 2 **Majorana $B - L$** : $\Delta(B - L) = 2$, Majorana ν + leptogenesis.
- 3 **Dirac $B - L$** : $\Delta(B - L) = n \neq 2$, Dirac ν + Dirac leptogenesis.

Unbroken $B - L$

Almost¹ never considered, but very simple:

- Neutrinos are Dirac, with Yukawa couplings $Y_\nu \sim m_\nu / \langle H \rangle \lesssim 10^{-11}$.
- Baryon asymmetry via **neutrino genesis**:²
 - New scalars decay so that $\Delta(B - L) = \Delta L = 0$, but $\Delta L_{\text{left}} = -\Delta L_{\text{right}} \neq 0$.



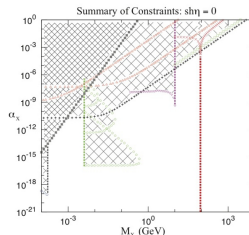
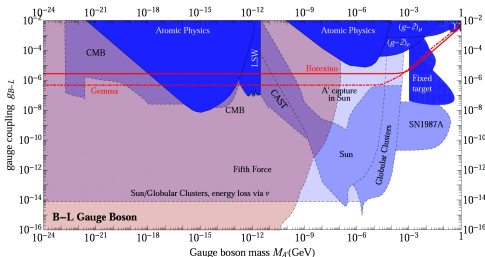
- Right-handed ν_R **not thermalized** due to tiny Yukawas.
 \Rightarrow Sphalerons only see ΔL_{left} , generate ΔB via $\Delta(B + L) = 6!$

¹D. Feldman, P. Fileviez Perez, and P. Nath, 1109.2901.

²K. Dick, M. Lindner, M. Ratz, and D. Wright, hep-ph/9907562.

Signatures

- No $0\nu 2\beta$ or other $\Delta(B - L) \neq 0$ processes. . .
- Z' with tiny coupling $\alpha' \lesssim 10^{-50}$ or Stückelberg mass.
- $M_{Z'}/g'$ not connected to m_ν or leptogenesis \Rightarrow no preferred scale!
- Limits, e.g. Williams et al., 1103.4556, Harnik et al., 1202.6073:



- Strong additional limits from $\bar{\nu}_R \gamma^\mu \nu_R Z'_\mu$ at BBN.³

\Rightarrow Unbroken (local) $B - L$ perfectly valid!

³J.H., in preparation.

Majorana $B - L$

- New scalar $\phi_{B-L=2}$ to break $U(1)_{B-L}$ by two units.

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Spontaneous symmetry breaking gives mass matrix for (ν_L, ν_R^c) :

$$\mathcal{M} = \begin{pmatrix} 0 & Y_\nu^T \langle H \rangle \\ Y_\nu \langle H \rangle & Y_R \langle \phi_{B-L=2} \rangle \end{pmatrix}.$$

- High scale $Y_R \langle \phi_{B-L=2} \rangle \gg Y_\nu \langle H \rangle$:
small seesaw Majorana mass for active neutrinos:

$$\mathcal{M}_\nu \simeq - \frac{\langle H \rangle^2}{\langle \phi_{B-L=2} \rangle} Y_\nu^T Y_R^{-1} Y_\nu.$$

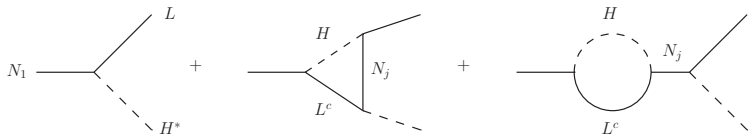
- Signature of Majorana $B - L$: neutrinoless double beta decay

$$(A, Z) \rightarrow (A, Z + 2) + 2e^- \quad \Leftrightarrow \quad \Delta(B - L) = 2.$$

Majorana $B - L$: Leptogenesis

$$\mathcal{L} \supset Y_\nu \bar{\nu}_R H L + \frac{1}{2} Y_R \bar{\nu}_R \nu_R^c \phi_{B-L=2}^* + \text{h.c.}$$

- Heavy ($\mathcal{M}_R \simeq Y_R \langle \phi_{B-L=2} \rangle \gtrsim 10^8 \text{ GeV}$) Majorana neutrinos $N = \nu_R + \nu_R^c$ decay out-of-equilibrium in early Universe.



- If CP violated in loops: $\Gamma(N \rightarrow HL) \neq \Gamma(N \rightarrow H^* \bar{L})$
 \Rightarrow Lepton asymmetry $\Delta_L!$
- Sphalerons with $\Delta B = \Delta L = 3$ above $T \gtrsim \text{TeV}$ transfer Δ_L to baryon asymmetry Δ_B .

Dirac $B - L$

Break $B - L$, but by $n \neq 2$ units.⁴

⇒ Lepton number violating Dirac neutrinos.

- All fermions in $SM + \nu_R$ are odd under $B - L$
 ⇒ only **even** $\Delta(B - L)$ possible.
 ⇒ Lowest order new processes: $\Delta(B - L) = 4$:

$$\mathcal{O}_{d=6} : \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=8} : |H|^2 \bar{\nu}_R^c \nu_R \bar{\nu}_R^c \nu_R, (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, F_Y^{\mu\nu} \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R \bar{\nu}_R^c \nu_R$$

$$\mathcal{O}_{d=10} : (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L), |H|^2 (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \nu_R, \\ F_Y^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, W_a^{\mu\nu} (\bar{L}^c \tilde{H}^*)(\tilde{H}^\dagger \tau^a L) \bar{\nu}_R^c \sigma_{\mu\nu} \nu_R, \\ (\bar{u}_R d_R^c)(\bar{d}_R \tilde{H}^\dagger L)(\bar{\nu}_R^c \nu_R), \dots$$

$$\mathcal{O}_{d=18} : (\bar{d}_R d_R^c \bar{u}_R u_R \bar{e}_R e_R)(\bar{d}_R d_R^c \bar{u}_R u_R \bar{e}_R e_R), \dots$$

$$\mathcal{O}_{d=20} : \left[((D_\mu L)^c \tilde{H})(H^\dagger D_\nu L) \right]^2 \supset (\bar{e}_L^c W_\mu^+ W_\nu^+ e_L)(\bar{e}_L^c W^{+\mu} W^{+\nu} e_L), \dots$$

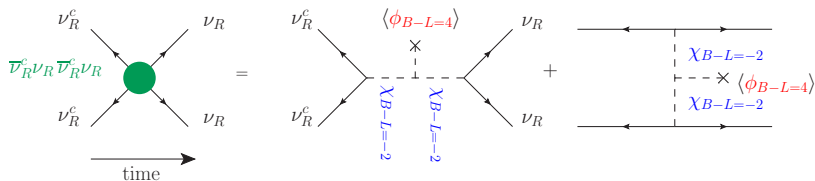
⁴Witten, hep-ph/0006332.

UV completion

- One scalar $\phi_{B-L=4}$ to break $B - L$, one scalar $\chi_{B-L=-2}$ as mediator.

$$\mathcal{L} \supset y_{\alpha\beta} \bar{L}_\alpha H \nu_{R,\beta} + \kappa_{\alpha\beta} \chi_{B-L=-2} \bar{\nu}_{R,\alpha} \nu_{R,\beta}^c + \text{h.c.}$$

- Neutrinos are Dirac (and $\Delta L = 2$ forbidden) if $\langle \chi_{B-L=-2} \rangle = 0$.
- Scalar potential $V \supset \mu \phi_{B-L=4} (\chi_{B-L=-2})^2 + \text{h.c.}$
- Lepton number violation $\Delta L = 4$ still possible!⁵

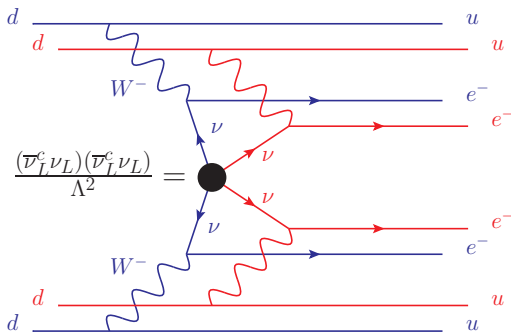


⁵J.H. and W. Rodejohann, EPL **103**, 32001 (2013) [arXiv:1306.0580].

$\Delta L = 4$ signature?

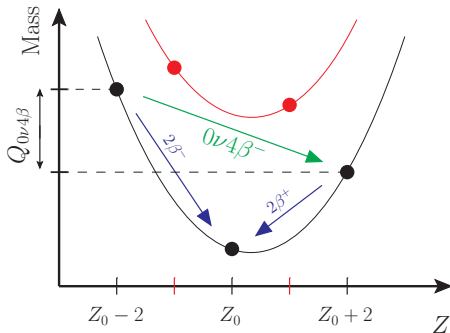
Neutrinoless quadruple beta decay $0\nu 4\beta$

$(\mathbf{A}, \mathbf{Z}) \rightarrow (\mathbf{A}, \mathbf{Z} + 4) + 4 e^-$ via $\mathcal{O} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2$:



Candidate nuclei

- Experimental aspects of $0\nu 4\beta$ independent of underlying mechanism.
- Need beta-stable initial state:



- Decay modes: $0\nu 4\beta$ and $2\nu 2\beta$ ($0\nu 2\beta$ forbidden here).

Candidates for nuclear $\Delta L = 4$ processes

	$Q_{0\nu 4\beta}$	other decays	NA/%	experiment (2β)
${}^{96}_{40}\text{Zr} \rightarrow {}^{96}_{44}\text{Ru}$	0.629 MeV	$\tau_{2\nu 2\beta} \simeq 2 \times 10^{19} \text{ y}$	2.8	NEMO
${}^{136}_{54}\text{Xe} \rightarrow {}^{136}_{58}\text{Ce}$	0.044 MeV	$\tau_{2\nu 2\beta} \simeq 2 \times 10^{21} \text{ y}$	8.9	EXO/KZ/NEXT
${}^{150}_{60}\text{Nd} \rightarrow {}^{150}_{64}\text{Gd}$	2.079 MeV	$\tau_{2\nu 2\beta} \simeq 7 \times 10^{18} \text{ y}$	5.6	NEMO
	$Q_{0\nu 4EC}$			
${}^{124}_{54}\text{Xe} \rightarrow {}^{124}_{50}\text{Sn}$	0.577 MeV	—	0.095	
${}^{130}_{56}\text{Ba} \rightarrow {}^{130}_{52}\text{Te}$	0.090 MeV	$\tau_{2\nu 2EC} \sim 10^{21} \text{ y}$	0.106	
${}^{148}_{64}\text{Gd} \rightarrow {}^{148}_{60}\text{Nd}$	1.138 MeV	$\tau_{\alpha} \simeq 75 \text{ y}$	—	
${}^{154}_{66}\text{Dy} \rightarrow {}^{154}_{62}\text{Sm}$	2.063 MeV	$\tau_{\alpha} \simeq 3 \times 10^6 \text{ y}$	—	

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- Existing 2β experiments can also look for $0\nu 4\beta$!

Best candidate: Neodymium $^{150}_{60}\text{Nd}$

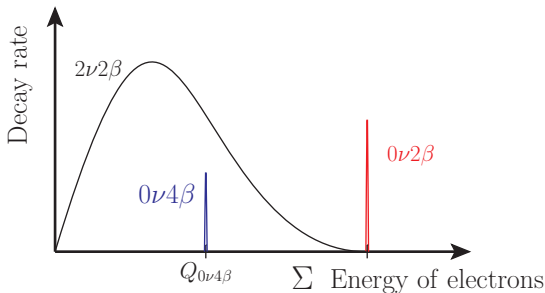
Decay channels:

- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{62}\text{Sm}$ via $2\nu 2\beta$ ($\tau_{1/2}^{2\nu 2\beta} \simeq 7 \times 10^{18}$ y):

$$0 < \sum E_{e,i} < 3.371 \text{ MeV.}$$

- $^{150}_{60}\text{Nd} \rightarrow ^{150}_{64}\text{Gd}$ via $0\nu 4\beta$:

$$\sum E_{e,i} = Q_{0\nu 4\beta} = 2.079 \text{ MeV.}$$



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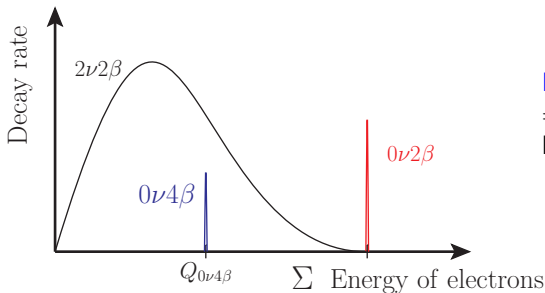
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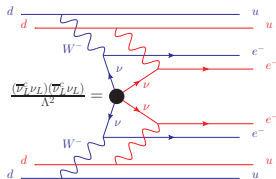
$$\sum E_{e,i} = Q_{0\nu 4\beta} = 2.079 \text{ MeV.}$$



NEMO has **tracking**
 \Rightarrow Count electrons,
 kill 2β background!

The catch: $0\nu 4\beta$ rates

$$(A, Z) \rightarrow (A, Z + 4) + 4 e^- \text{ via } \mathcal{O} = (\bar{\nu}_L^c \nu_L)^2 / \Lambda^2:$$



- Very naive comparison with competing channel $2\nu 2\beta$:

$$\frac{\tau_{1/2}^{0\nu 4\beta}}{\tau_{1/2}^{2\nu 2\beta}} \simeq \left(\frac{Q_{0\nu 2\beta}}{Q_{0\nu 4\beta}} \right)^{11} \left(\frac{\Lambda^4}{q^{12} G_F^4} \right) \simeq 10^{46} \left(\frac{\Lambda}{\text{TeV}} \right)^4,$$

with $|q| \sim p_\nu \sim 1 \text{ fm}^{-1} \simeq 100 \text{ MeV}$.

- **Estimated rate in toy model unobservably small.**
 Elaborate models with resonances overcome this???
- Resonant $0\nu 4\beta$ possible?

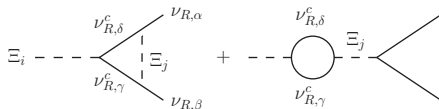
Dirac $B - L$: Leptogenesis

$\Delta L = 4$ easily relevant in early universe: new Dirac leptogenesis!⁶

- Scalar potential $V(H, \phi, \chi) \supset -\mu \phi_{B-L=4} (\chi_{B-L=-2})^2$ breaks complex $\chi_{B-L=-2} = (\Xi_1 + i \Xi_2) / \sqrt{2}$ into two real scalars with mass

$$m_1^2 = m_c^2 - 2\mu \langle \phi_{B-L=4} \rangle, \quad m_2^2 = m_c^2 + 2\mu \langle \phi_{B-L=4} \rangle.$$

- Heavy mediator scalar Ξ_j decays to $\nu_R \nu_R$ or $\bar{\nu}_R \bar{\nu}_R$ out-of-equilibrium in early Universe.



- CP violation requires *second* scalar $\chi_{B-L=-2}$.

Asymmetry in ν_R . ✓ How to translate to baryon asymmetry?

⁶J.H., PRD **88**, 076004 (2013) [arXiv:1307.2241].

Baryon asymmetry

$$Y_{\nu_R} \equiv \frac{n_{\nu_R}}{s} \sim \frac{1}{g_*} \frac{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) - \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}{\Gamma(\Xi_i \rightarrow \nu_R \nu_R) + \Gamma(\Xi_i \rightarrow \nu_R^c \nu_R^c)}.$$

- Dirac-Yukawa coupling $Y_\nu = m_\nu / \langle H \rangle$ too small to equilibrate $\nu_R \dots$

Add second Higgs doublet H_2 with large Yukawa $\bar{L} H_2 \nu_R$:

- **Neutrophilic** H_2 with small VEV $\langle H_2 \rangle \sim 1 \text{ eV}$.
 \Rightarrow Dirac neutrinos light with large Yukawas.⁷
- H_2 moves Y_{ν_R} to Y_{ν_L} .
- Sphalerons move Y_{ν_L} to Y_B .

\Rightarrow Different from **neutrinogenesis**, similar to standard leptogenesis!

- Necessary thermalization of $\nu_R \Rightarrow N_{\text{eff}} > 3!$
- $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$ depending on H_2^+ mass and Yukawa coupling.
- Specific collider signatures of neutrophilic H_2 .⁷

⁷Davidson and Logan, 0906.3335.

Summary

name	$\Delta(B - L)$	neutrino	BAU	signatures
Unbroken $B - L$	0	Dirac	neutrino genesis	$Z'(?), N_{\text{eff}} \simeq 3$
Majorana $B - L$	2	Majorana	leptogenesis	$0\nu 2\beta$
Dirac $B - L$	> 2 , e.g. 4	Dirac	Dirac leptogenesis	$0\nu 4\beta, N_{\text{eff}} \gtrsim 3.14$

- $B - L$ mystery: global, local, unbroken, broken by 2, 4, ... units?
- Currently testing: $\Delta L = 2$ via $0\nu 2\beta$.
- In principle: $\Delta L = 4$ via $0\nu 4\beta$;
experimentally (and theoretically) challenging.
- Lepton number violation not synonymous with Majorana neutrinos.
- $\Delta L = 4$ lowest LNV of Dirac neutrinos.
- New Dirac leptogenesis ($3.14 \lesssim N_{\text{eff}} \lesssim 3.29$).

Phenomenology of LNV Dirac neutrinos

Quick summary:

- Even with Dirac neutrinos, we can have LNV.
- Lowest order is then $\Delta(B - L) = \Delta L = 4$, via $\mathcal{O}_{d=6} = (\bar{\nu}_R^c \nu_R)^2 / \Lambda^2$.

How to check for $\Delta L = 4$?

- Neutrinoless quadruple beta decay $(A, Z) \rightarrow (A, Z + 4) + 4 e^-$.
- Collider processes:
 - LHC: $pp \rightarrow W^- W^- W^- W^- \ell^+ \ell^+ \ell^+ \ell^+ + X$,
 - Like-sign lepton collider: $e^- e^- \rightarrow W^- W^- W^- W^- \ell^+ \ell^+$.
- Rare meson decays etc.?

All tough, many particles in final state!

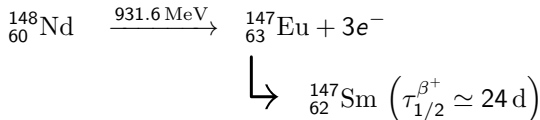
$\Delta L = 4$ can however easily be relevant in the early Universe

\Rightarrow new Dirac leptogenesis mechanism predicting $3.14 \lesssim N_{\text{eff}} \lesssim 3.29$.⁸

⁸J.H., PRD **88**, 076004 (2013) [arXiv:1307.2241].

Comments on $0\nu 4\beta$

- Background: electrons from $2\nu 2\beta$ kick out two more e^- .
 $\Rightarrow 4 e^-$ with $\sum E_i \sim Q_{0\nu 4\beta}$ possible.
- $0\nu 4\beta$ to excited state $^{150}_{64}\text{Gd}^*$: Q reduced by 0.6 MeV (2^+) or 1.2 MeV (0^+), but more photons...
- Nuclear matrix elements impossible (?) to calculate.
 \Rightarrow No way to extract fundamental couplings from $\tau_{0\nu 4\beta}$ (?)
- $0\nu 6\beta$ etc. all involve beta-unstable nuclei.
 $\Rightarrow 0\nu 2\beta$ and $0\nu 4\beta$ somewhat unique.
- Very different $\Delta(B - L) = 4$ decay: $4n \rightarrow 3p + 3e^-$, mimics $0\nu 3\beta$.
 Candidate:



followed by the β^+ decay into ${}^{147}_{62}\text{Sm}$ with half-life 24 d.