

# Natural MSSM after the LHC 8 TeV run

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**SUSY 14**  
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*Based on*

K. Kowalska and EMS

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**INNOVATIVE ECONOMY**  
NATIONAL COHESION STRATEGY

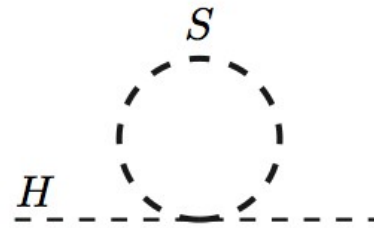
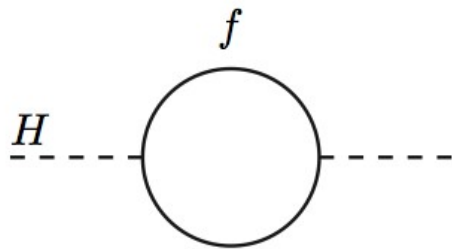


**EUROPEAN UNION**  
EUROPEAN REGIONAL  
DEVELOPMENT FUND



# Naturalness and fine tuning

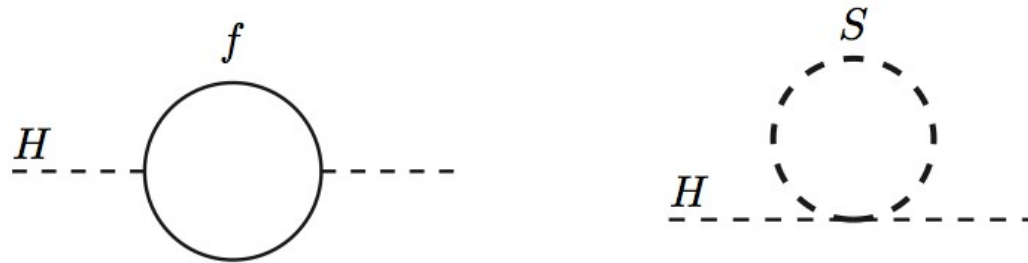
SUSY solves the hierarchy problem



$$\Delta m_h \sim \cancel{-2(y_t - y_t)\Lambda^2} - \frac{3y_t^2}{8\pi^2} (m_{\tilde{Q}_3}^2 + m_{\tilde{u}_3}^2 + |A_t|^2) \ln \left( \frac{\Lambda}{\text{TeV}} \right)$$

... but leaves logarithmic dependence...

# Naturalness and fine tuning



In MSSM minimization scalar potential yields

(limit of large  $\tan \beta$  )


$$\frac{M_Z^2}{2} \sim -\mu^2 - m_{H_u}^2 + \Delta m_{H_u}^2 \longrightarrow \text{Residual fine tuning!}$$

LEADING LOG APPROX

$$\Delta_{p_i} = \left| \frac{\partial \log M_Z^2}{\partial \log p_i^2} \right| = \frac{p_i^2}{M_Z^2} \left| \frac{\partial M_Z^2}{\partial p_i^2} \right|$$

$$p_i = \mu, m_{\tilde{Q}_3}, m_{\tilde{u}_3}, A_t, M_2, M_3$$

# Naturalness and fine tuning

$\max\{\Delta_{p_i}\} = 10$  (or 10% fine tuning) :  **Natural**

$$|\mu| \lesssim 200 \text{ GeV}$$

$$|M_2| \lesssim (1700 \text{ GeV}) \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1/2}$$

$$m_{\tilde{Q}_3}^2 + m_{\tilde{u}_3}^2 + |A_t|^2 \lesssim (1200 \text{ GeV})^2 \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1}$$

$$|M_3| \lesssim (2700 \text{ GeV}) \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1}$$

 (see K.Kowalska's talk on Friday)

$\max\{\Delta_{p_i}\} = 100$  (or 1% fine tuning) :  **This paper**

$$|\mu| \lesssim 645 \text{ GeV}$$

$$|M_2| \lesssim (5200 \text{ GeV}) \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1/2}$$

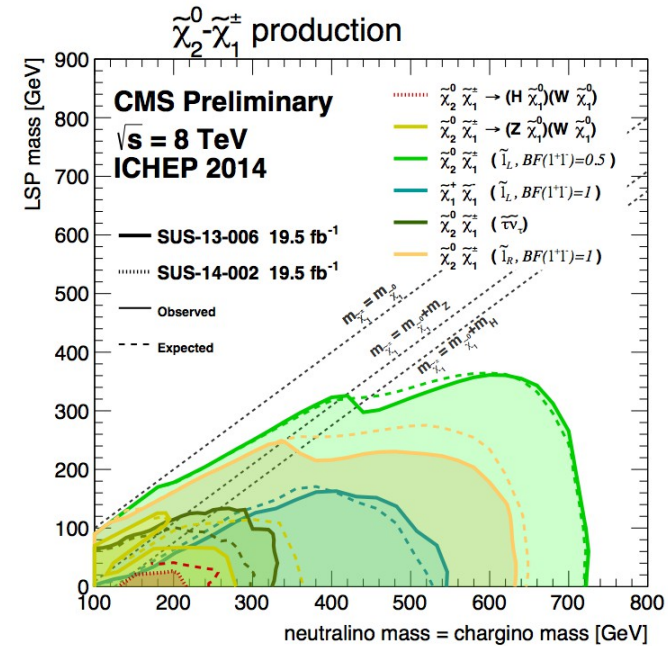
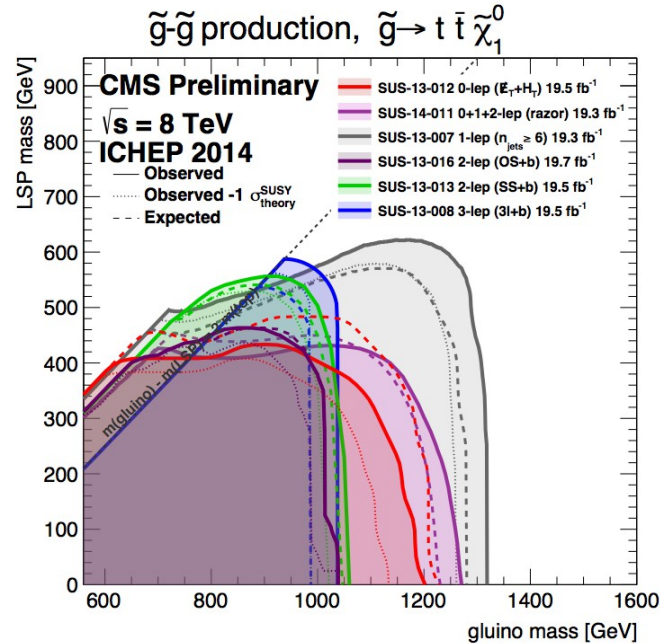
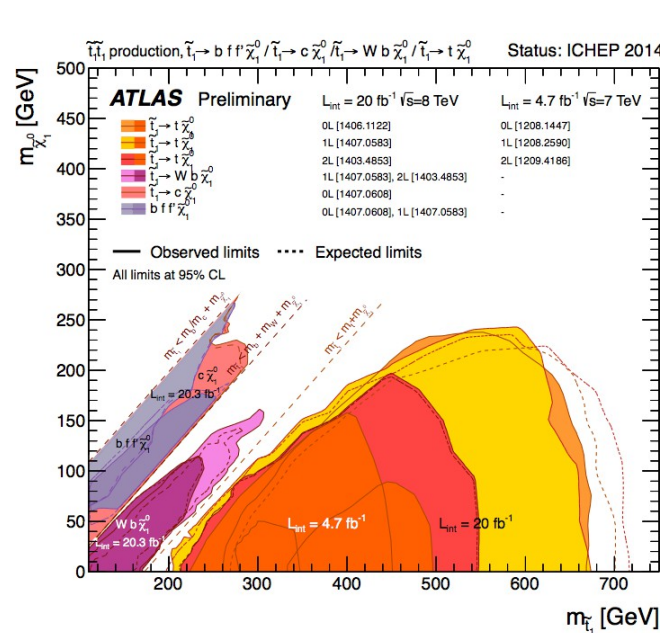
$$m_{\tilde{Q}_3}^2 + m_{\tilde{u}_3}^2 + |A_t|^2 \lesssim (4000 \text{ GeV})^2 \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1}$$

$$|M_3| \lesssim (8500 \text{ GeV}) \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1}$$

# Fine tuning vs LHC

Direct SUSY searches:

95% exc. limits on the masses of stops, sbottoms, gluinos, winos



Higgs mass at 125.5 GeV

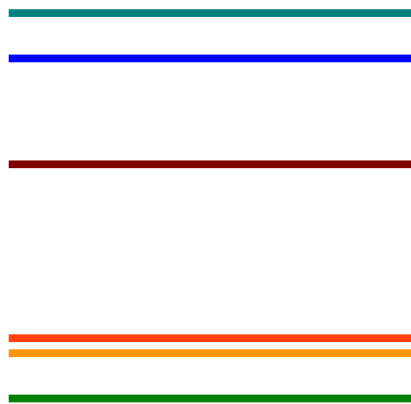
$$\Delta m_h^2 = \frac{3m_t^4}{4\pi^2 v^2} \left[ \ln \left( \frac{M_{\text{susy}}^2}{m_t^2} \right) + \frac{X_t^2}{M_{\text{susy}}^2} \left( 1 - \frac{X_t^2}{12M_{\text{susy}}^2} \right) \right]$$

How many realistic MSSM models with  $\Delta \leq 100$  survived LHC 8 TeV run?

$\Lambda \sim 10$  TeV here

# Natural spectra

Scenario 1	Scenario 2	Scenario 3
$M_1 = 3$ TeV	$M_1 = 3$ TeV	$0.01 \text{ TeV} \leq M_1 \leq 0.4 \text{ TeV}$
$M_2 = 1.5$ TeV	$M_2 = 1.5$ TeV	$M_1 < M_2$
$M_3 = 1.6$ TeV	$0.1 \text{ TeV} \leq M_3 \leq 1.6 \text{ TeV}$	$0.1 \text{ TeV} \leq M_2 \leq 0.63 \text{ TeV}$
$m_{\tilde{L}_{1,2,3}} = m_{\tilde{e}_1} = m_{\tilde{e}_2} = m_{\tilde{e}_3} = 3$ TeV	$m_{\tilde{L}_{1,2,3}} = m_{\tilde{e}_1} = m_{\tilde{e}_2} = m_{\tilde{e}_3} = 3$ TeV	$0.1 \text{ TeV} \leq M_3 \leq 1.6 \text{ TeV}$
$0.075 \text{ TeV} \leq \mu \leq 0.63 \text{ TeV}$	$0.075 \text{ TeV} \leq \mu \leq 0.63 \text{ TeV}$	$0.1 \text{ TeV} \leq m_{\tilde{L}_{1,2,3}}, m_{\tilde{e}_1}, m_{\tilde{e}_2}, m_{\tilde{e}_3} \leq 0.63 \text{ TeV}$
$0.1 \text{ TeV} \leq m_{\tilde{Q}_3}, m_{\tilde{u}_3} \leq 1.4 \text{ TeV}$	$0.1 \text{ TeV} \leq m_{\tilde{Q}_3}, m_{\tilde{u}_3} \leq 1.4 \text{ TeV}$	$\mu = 0.63 \text{ TeV}$
$\tilde{t}_{1,2}, \tilde{b}_1, \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$	$\tilde{g}, \tilde{t}_{1,2}, \tilde{b}_1, \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$	$0.1 \text{ TeV} \leq m_{\tilde{Q}_3}, m_{\tilde{u}_3} \leq 1.4 \text{ TeV}$
		sleptons, $\tilde{g}, \tilde{t}_{1,2}, \tilde{b}_1, \tilde{\chi}_1^0, \tilde{\chi}_2^0, \tilde{\chi}_1^\pm$

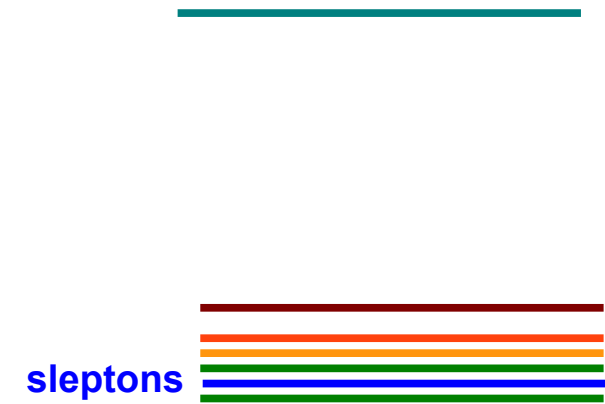
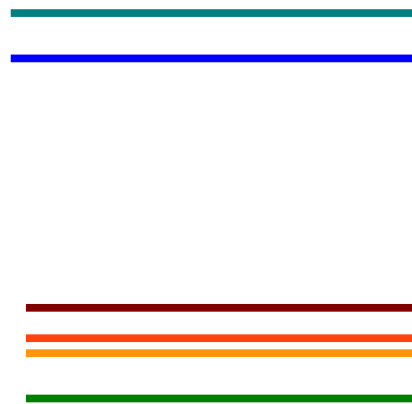


sleptons

gluino

b, t

higgsinos



sleptons

bino/wino

# Experimental constraints

Each case we generate 5000 model points that satisfy:

Measurement	Mean or range	Error: exp., th.	Distribution
$\Omega_\chi h^2$	0.1199	0.0027, 10%	$2\sigma$ upper limit
$\text{BR}(\bar{B} \rightarrow X_s \gamma) \times 10^4$	3.43	0.22, 0.21	$2\sigma$
$\text{BR}(B_s \rightarrow \mu^+ \mu^-) \times 10^9$	3.2	+1.5, -1.2, 10%	$2\sigma$
$\Delta M_{B_s} \times 10^{11}$	1.166 GeV	0.008 GeV, 0.158 GeV	$2\sigma$
$\sin^2 \theta_{\text{eff}}$	0.23146	0.00012, 0.00015	$2\sigma$
$M_W$	80.385 GeV	0.015 GeV, 0.015 GeV	$2\sigma$
$m_b(m_b)^{\overline{MS}}$	4.18 GeV	0.03 GeV, 0	Gaussian
$M_t$	173.5 GeV	1.0 GeV, 0	Gaussian
$\alpha_s$	0.1184 GeV	0.0007 GeV, 0	Gaussian

LHC limits →

Higgs mass at 125.5 GeV →

# LHC limits on SUSY

LHC limits for Simplified Models      Reinterpretation needed for complex scenarios.

ATLAS 1-lepton + 4(1b-) jets +  $E_T^{\text{miss}}$ ,  $21\text{fb}^{-1}$        $\longrightarrow$       Stops, sbottoms, gluinos  
CMS 0-leptons + (b-) jets +  $E_T^{\text{miss}}$  with  $\alpha_T$ ,  $12\text{fb}^{-1}$        $\longrightarrow$       Stops, sbottoms, gluinos  
CMS 3-lepton +  $E_T^{\text{miss}}$ ,  $9\text{fb}^{-1}$        $\longrightarrow$       Winos

## Our way to do:

- full simulation of event generation + detector response  
(PYTHIA6, PGS4)
- closely follows the experimental analysis  
$$s = \epsilon_A \times \sigma \times \int L$$
- validated against the official limits

## SUSY Likelihood:

$$\mathcal{L}_i(o_i, s_i, b_i) = \int P(o_i | s_i, \bar{b}_i) \exp\left(-\frac{(b - \bar{b})^2}{2\delta b^2}\right) d\bar{b}_i$$

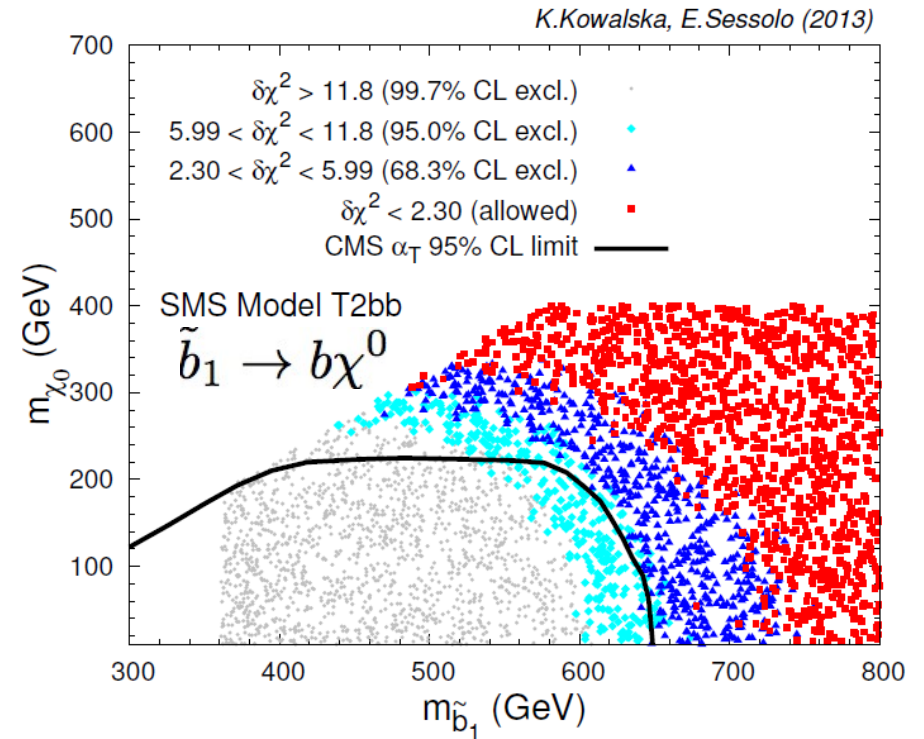
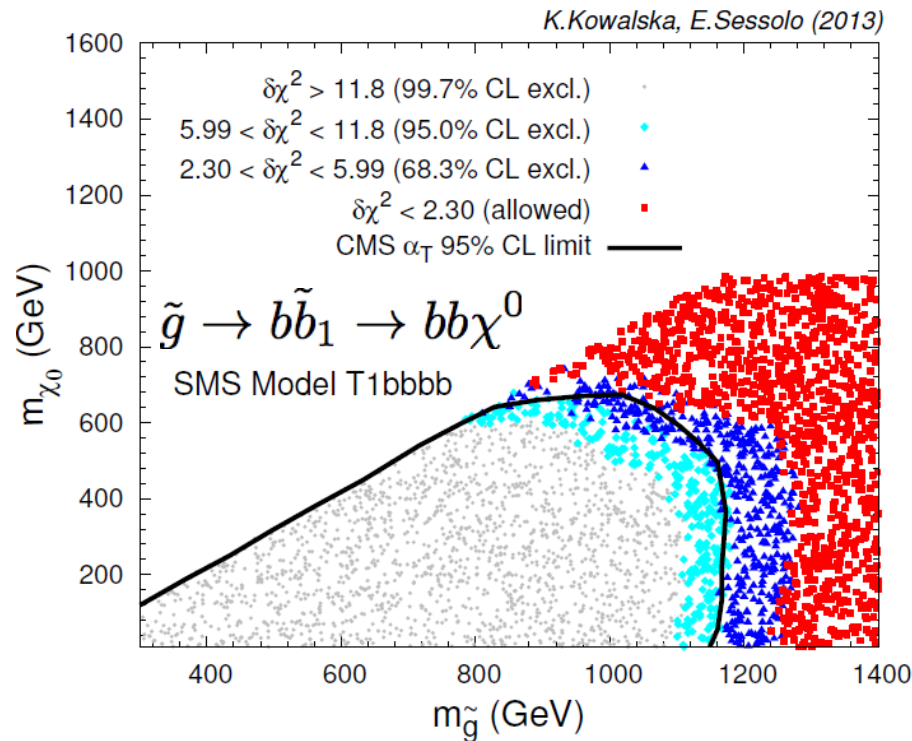
$$\sum_i \ln \mathcal{L}_i$$

Allows for combination  
of searches



# Validation

(In this paper we didn't consider compressed spectra)

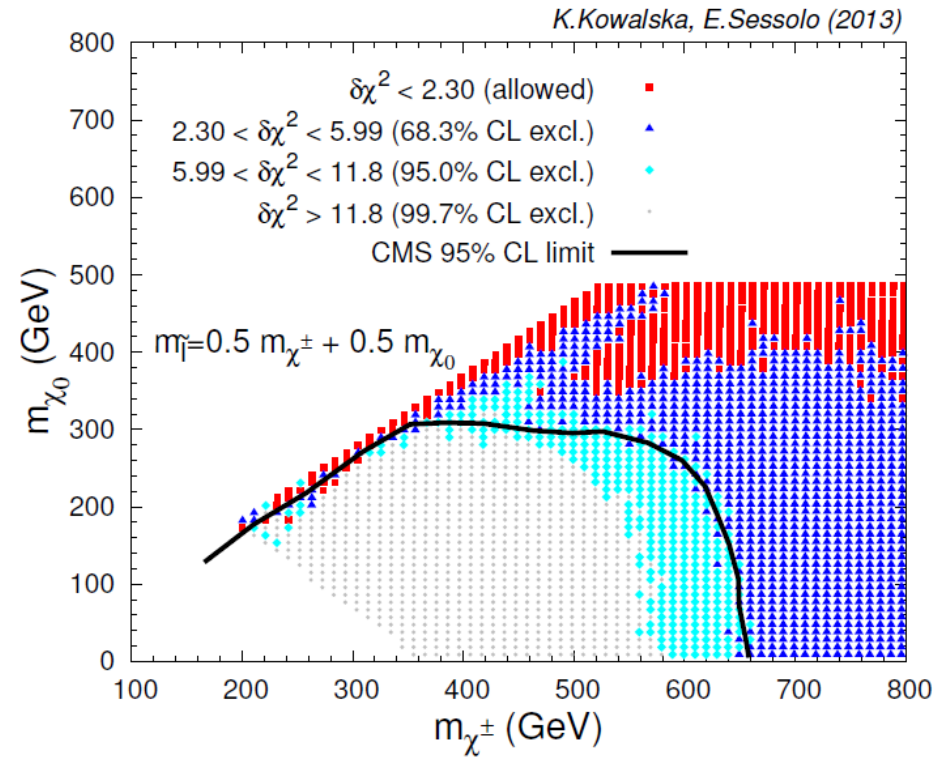
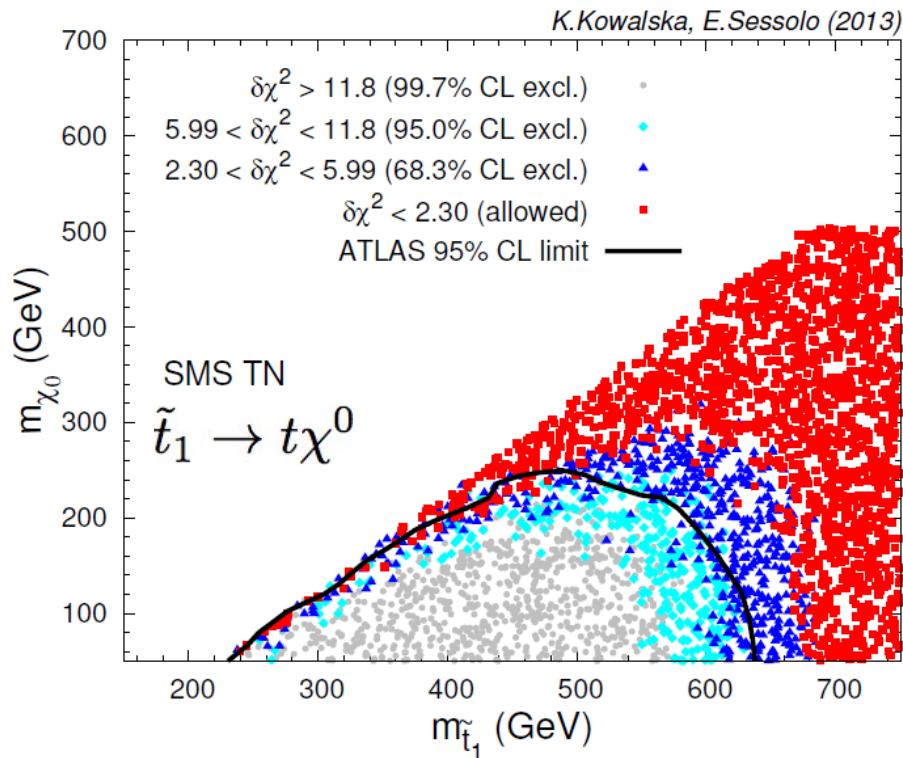


CMS 0-leptons + ( $b$ -) jets +  $E_T^{\text{miss}}$  with  $\alpha_T$ ,  $12\text{fb}^{-1}$

CMS-SUS-12-028

# Validation

(In this paper we didn't consider compressed spectra)



ATLAS 1-lepton + 4(1b-) jets +  $E_T^{\text{miss}}$ ,  $21\text{fb}^{-1}$

ATLAS-CONF-2013-037

CMS 3-lepton +  $E_T^{\text{miss}}$ ,  $9\text{fb}^{-1}$

CMS-SUS-12-022

# Scenario 1 – light stops and higgsinos

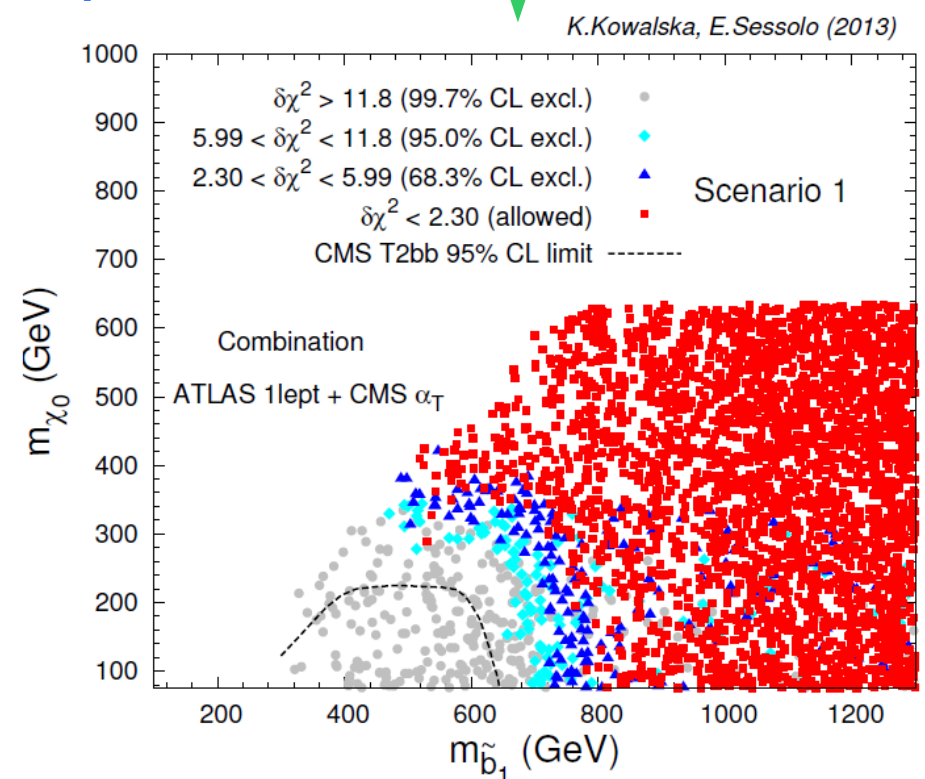
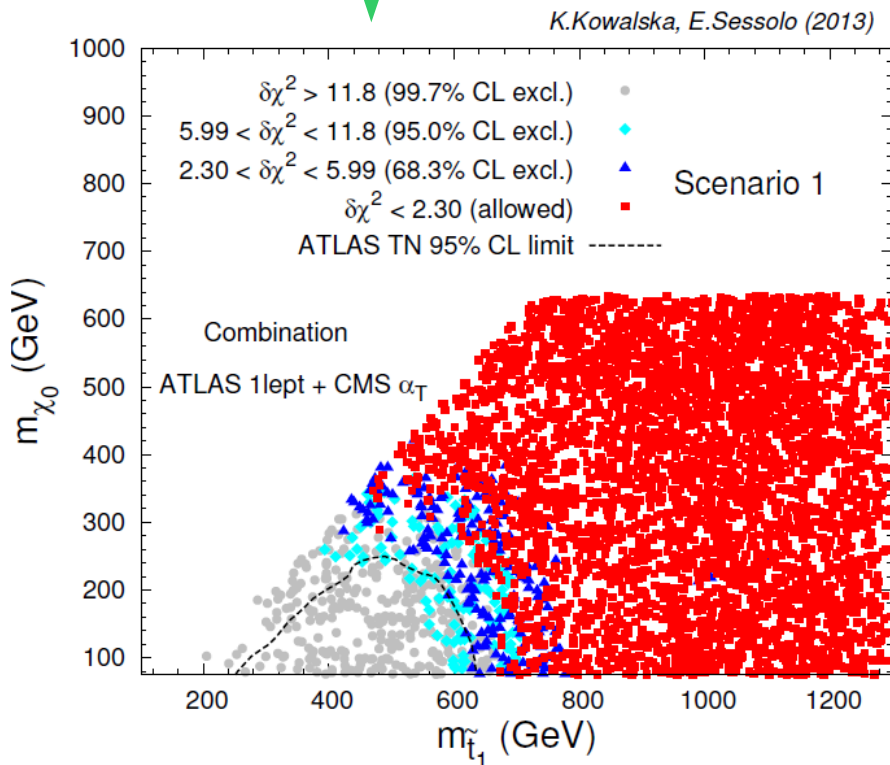
Dominant decay channels:

$$\tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$$

$$\tilde{b}_1 \rightarrow t\tilde{\chi}_1^- \text{ chargino invisible}$$

$$m_{\tilde{t}_1} < m_{\tilde{b}_1}$$

ATLAS 1 lepton  
CMS 0 leptons



# Scenario 1 – light stops and higgsinos

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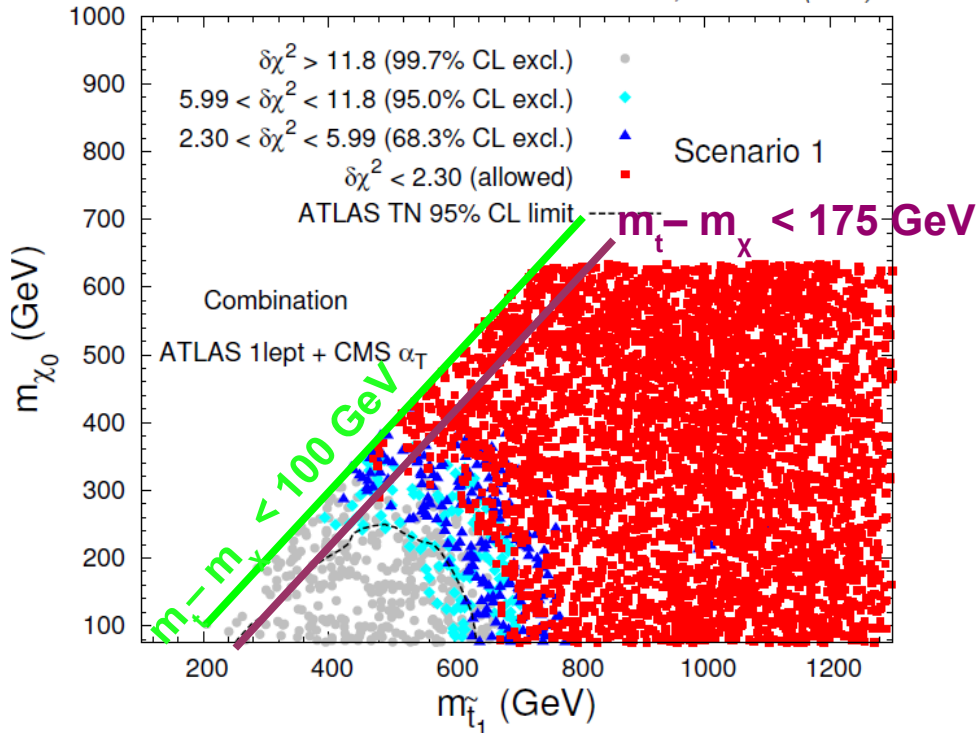
$$\tilde{t}_1 \rightarrow b\tilde{\chi}_1^- \rightarrow 0 \text{ leptons b-jets}$$

ATLAS 1 lepton  
CMS 0 leptons

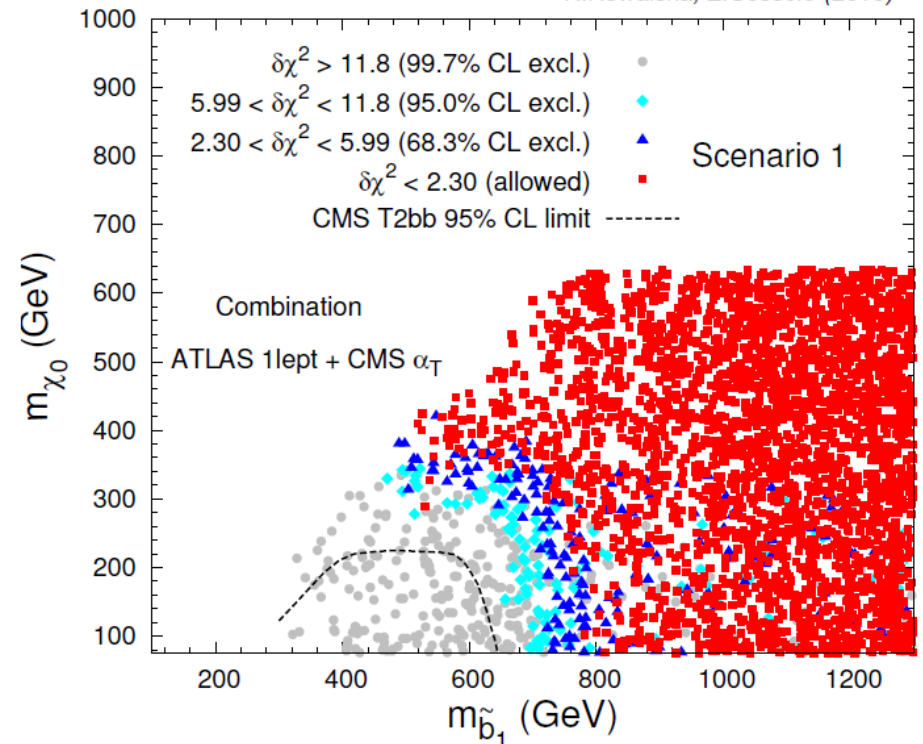
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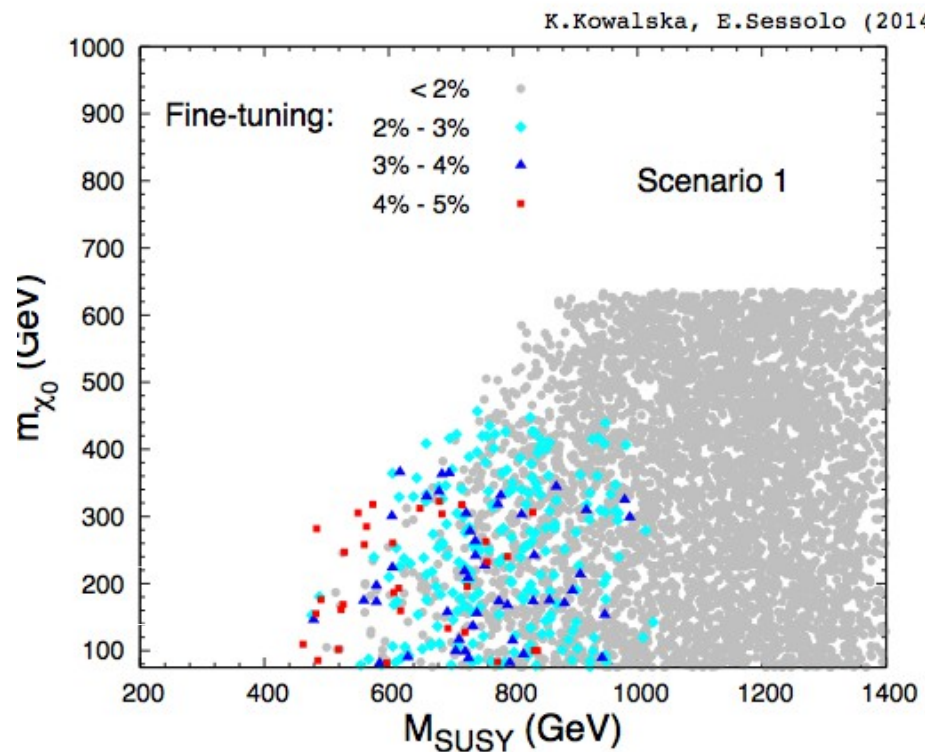
K.Kowalska, E.Sessolo (2013)



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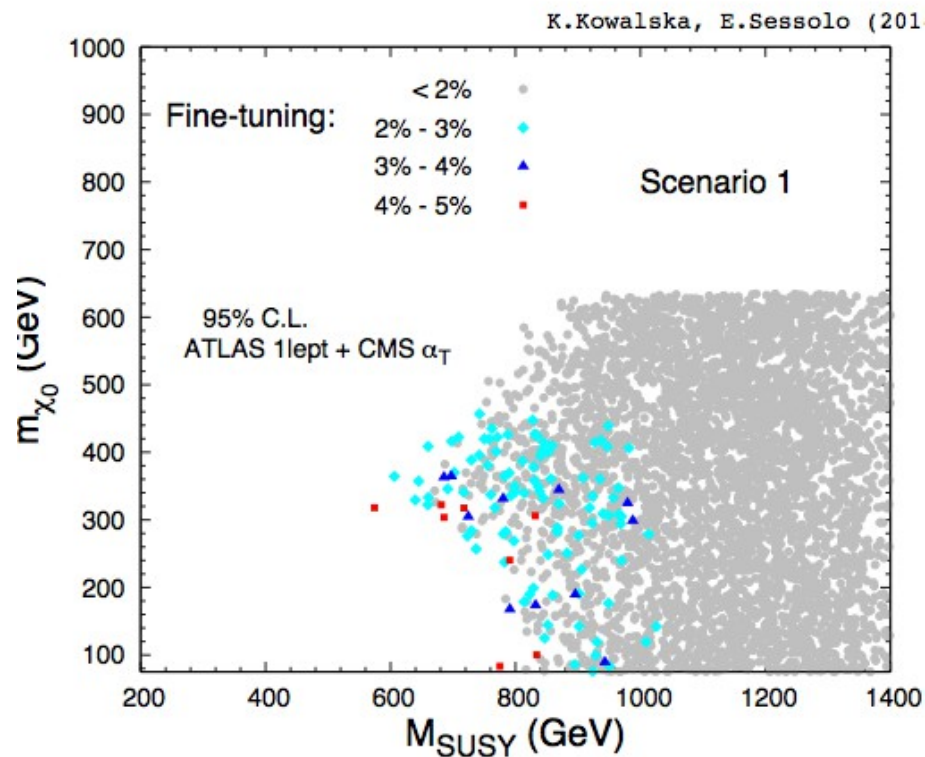


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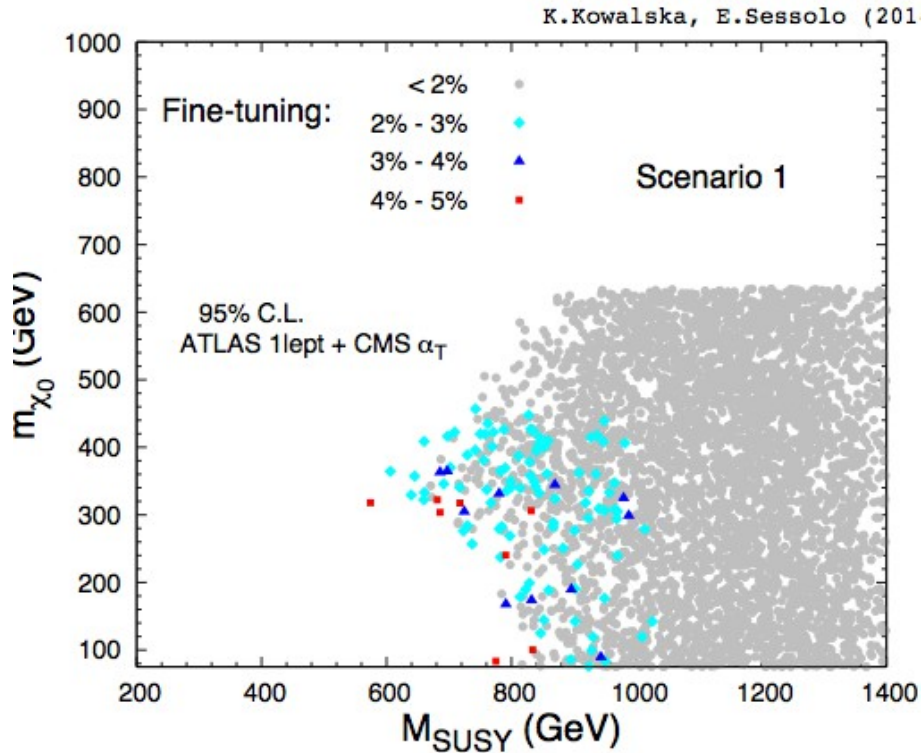
No points fine tuning  $> 5\%$   
Mostly due to  $b \rightarrow s$  gamma

# Scenario 1 – light stops and higgsinos

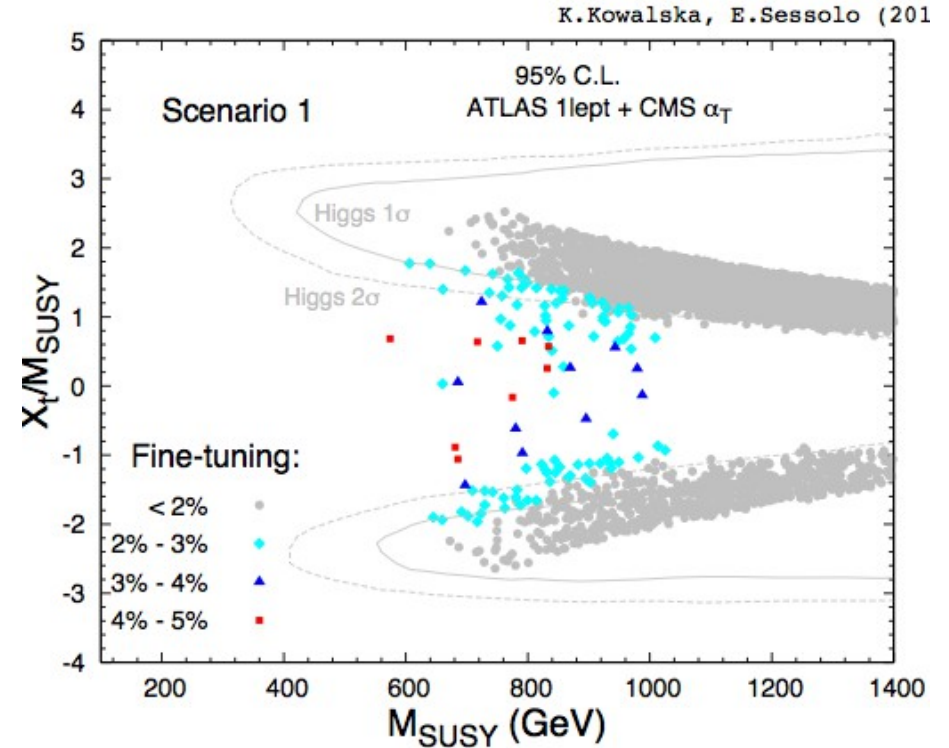


LHC cuts most point FT > 3%  
(but some left)

# Scenario 1 – light stops and higgsinos



LHC cuts most point FT > 3%  
(but some left)



Higgs mass cuts all FT > 3%  
(3 GeV th. err.)

# Scenario 2 – stops, gluinos and higgsinos

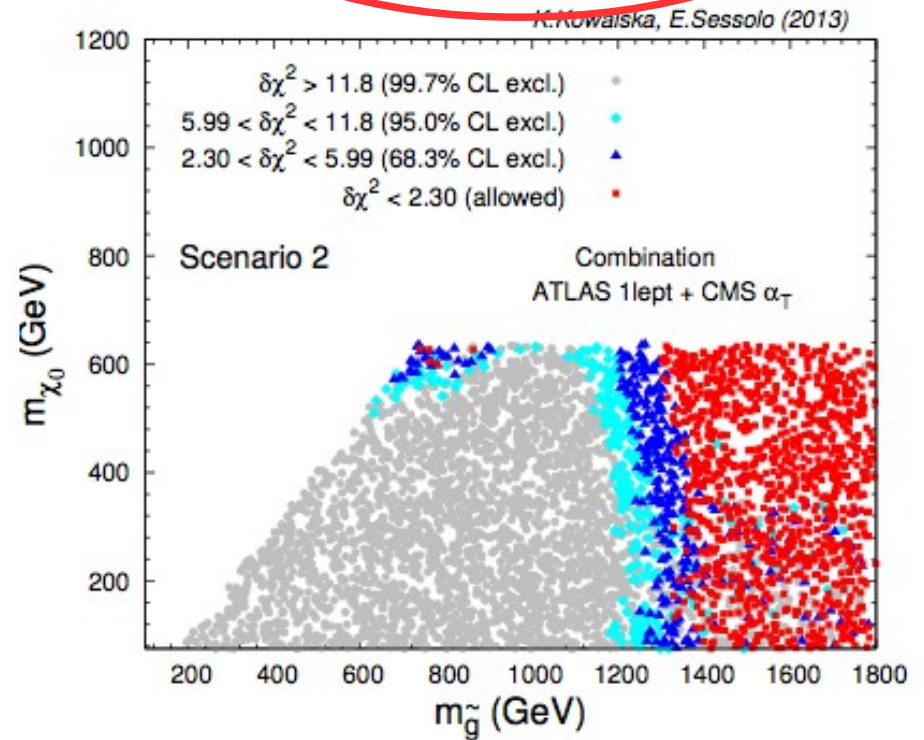
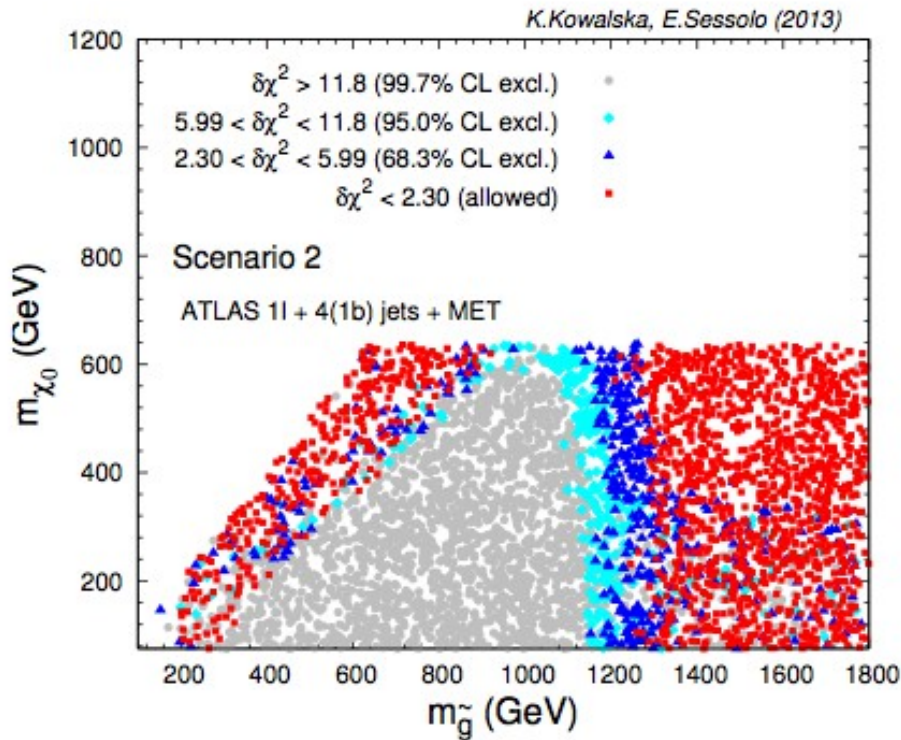
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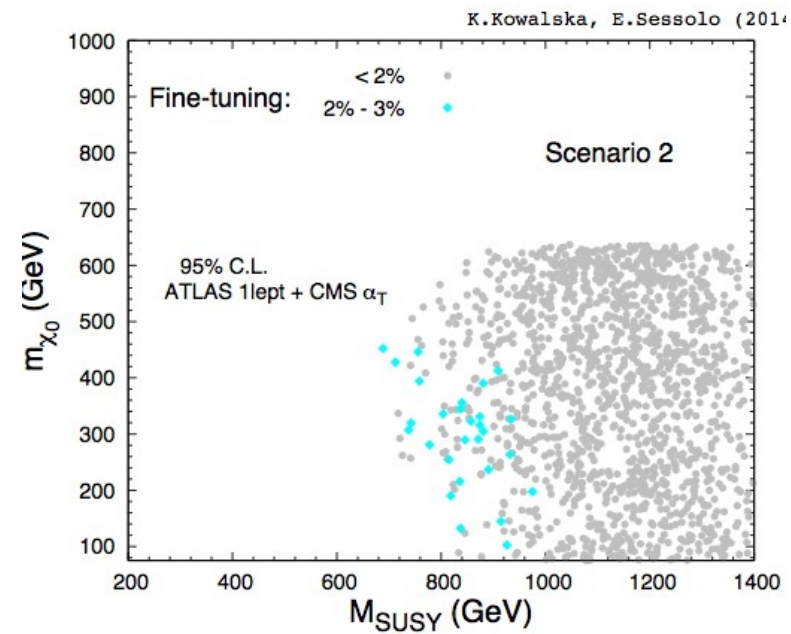
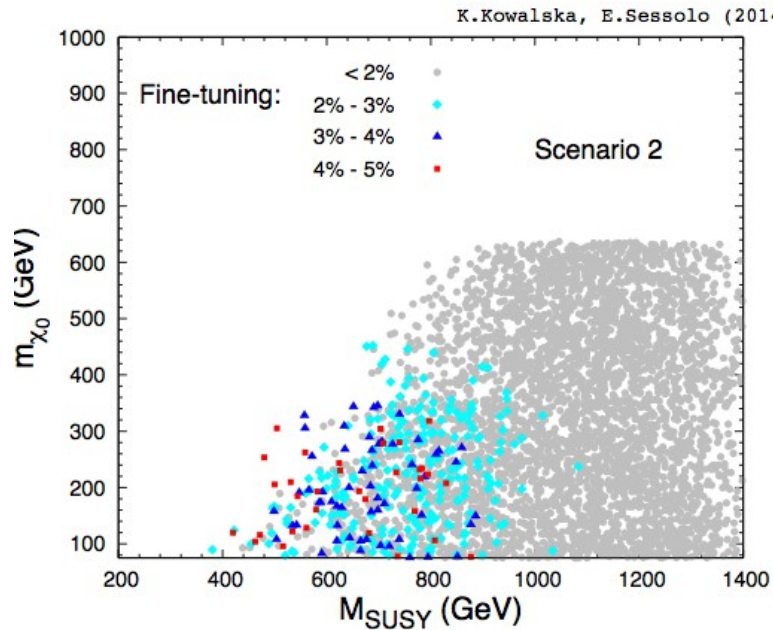
$$\tilde{g} \rightarrow q\bar{q}\tilde{\chi}_1^0$$

$$\tilde{g} \rightarrow b\bar{b}\tilde{\chi}_1^0 \quad \tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$$

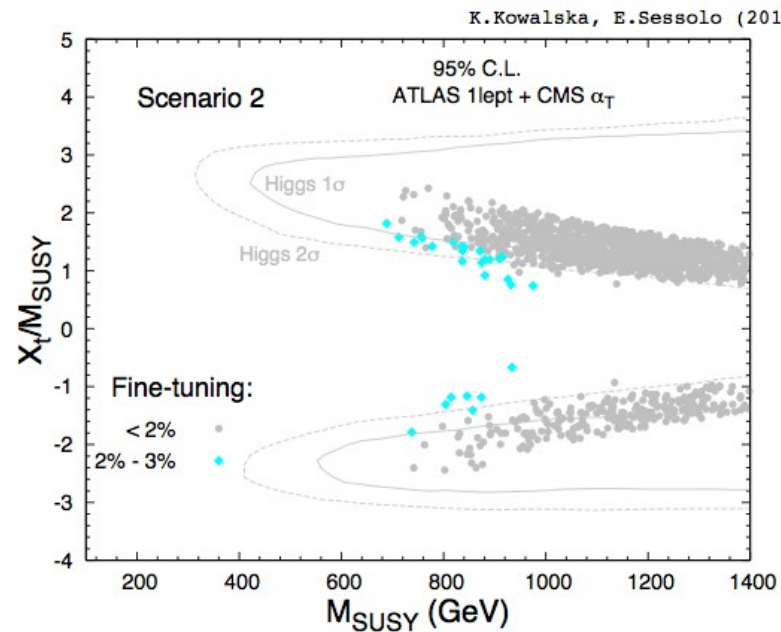




# Scenario 2 – stops, gluinos and higgsinos



Pre LHC



Post LHC

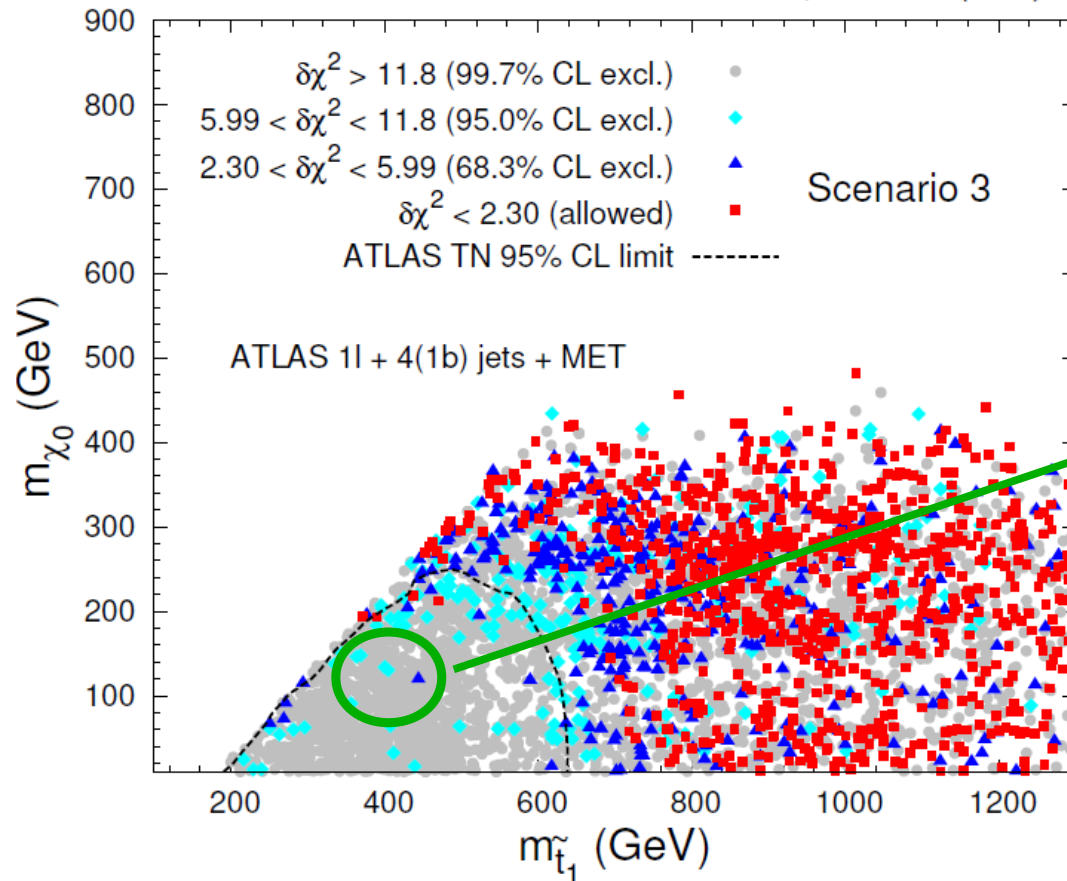
Higgs

# Scenario 3 – stops, gluinos and EW-inos

## Combination of searches:

- stronger bounds due to various topologies
- bounds can be weakened by long decay chains

*K.Kowalska, E.Sessolo (2013)*



$$\tilde{t} \rightarrow b\tilde{\chi}_1^+$$

$$\tilde{\chi}_1^+ \rightarrow \tau^+ \nu_\tau \tilde{\chi}_1^0$$

$$\tau^+ \rightarrow \text{hadronically}$$

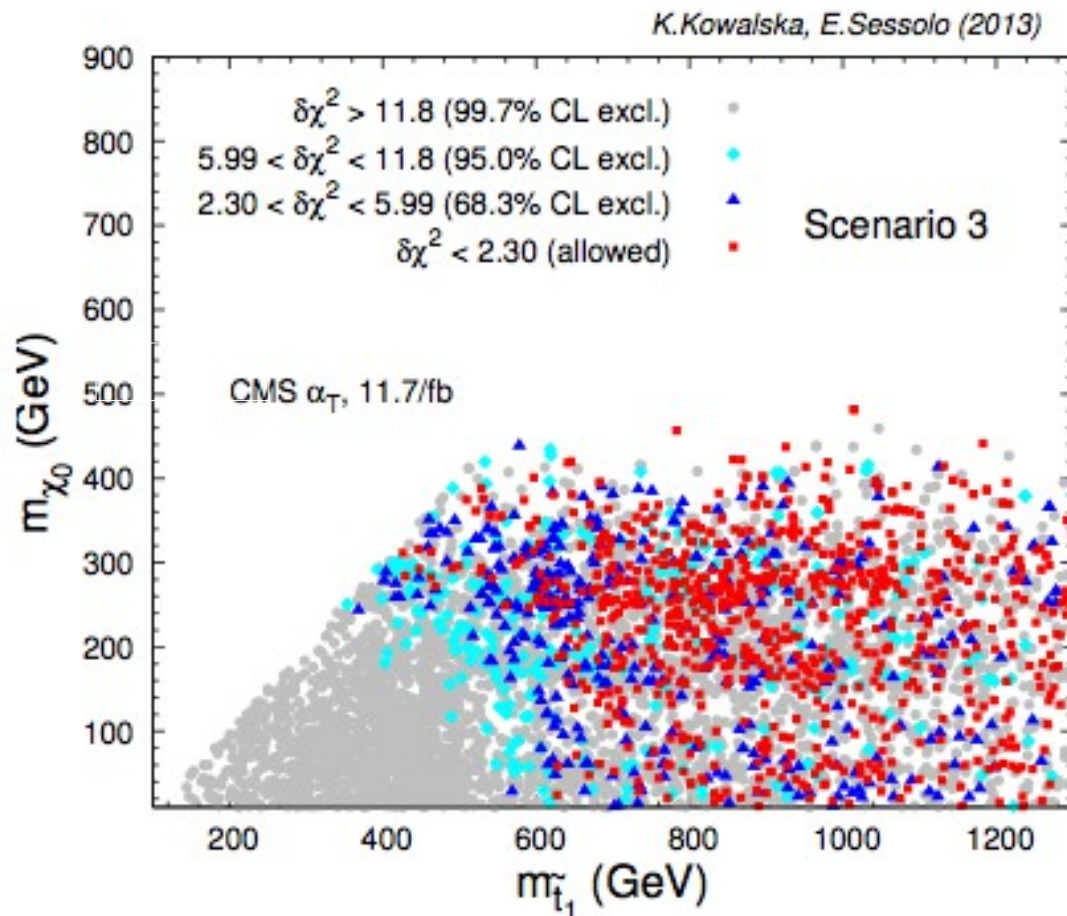


No hard leptons in the final state

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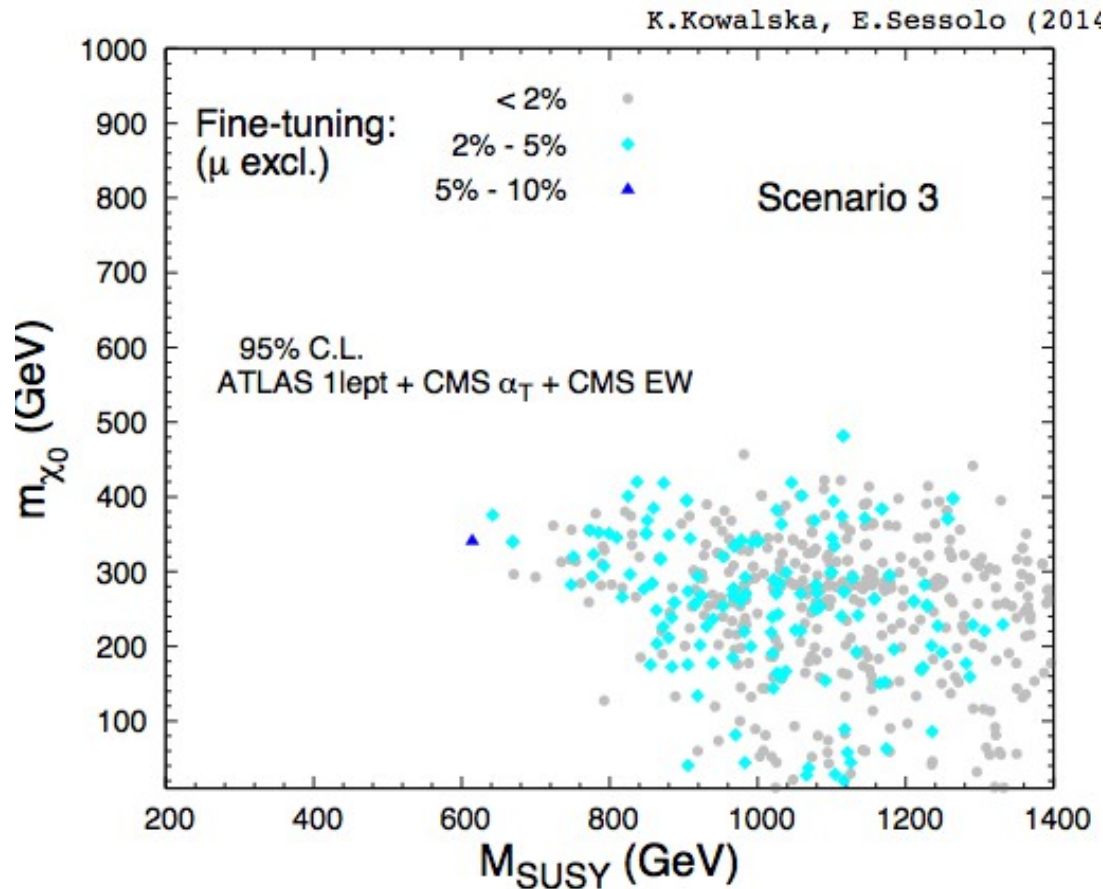


Hadronic search excludes

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Hadronic search excludes

1 point FT = 5%-10% left

# Conclusions

- LHC provides strong limits for natural SUSY spectra, but most gen. definition of naturalness already in trouble because of Higgs and other constraints.
- $\Lambda \sim 10$  TeV:  
Compressed spectra  $\implies$  maybe FT  $> 5\%$   
Higgs  $\implies$  FT  $< 3\%$ .
- Two competing effects:
  1. Complex decay chain soften simplify model limits
  2. Statistical combinations strengthen simp.mod. limits

# BACKUP

# Outline

1. Definition of fine tuning
2. Reinterpretation of the LHC exclusion bounds
3. Limits on natural spectra
4. Conclusions

# Comparison with other tools

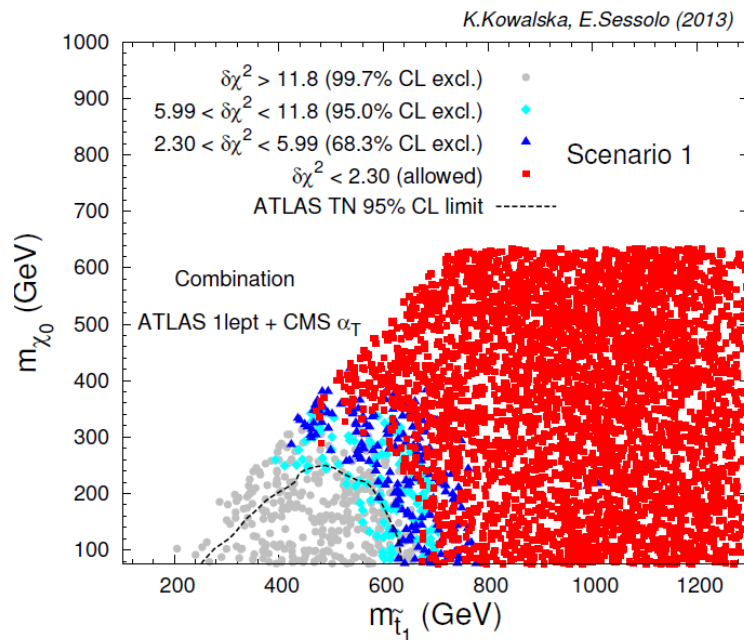
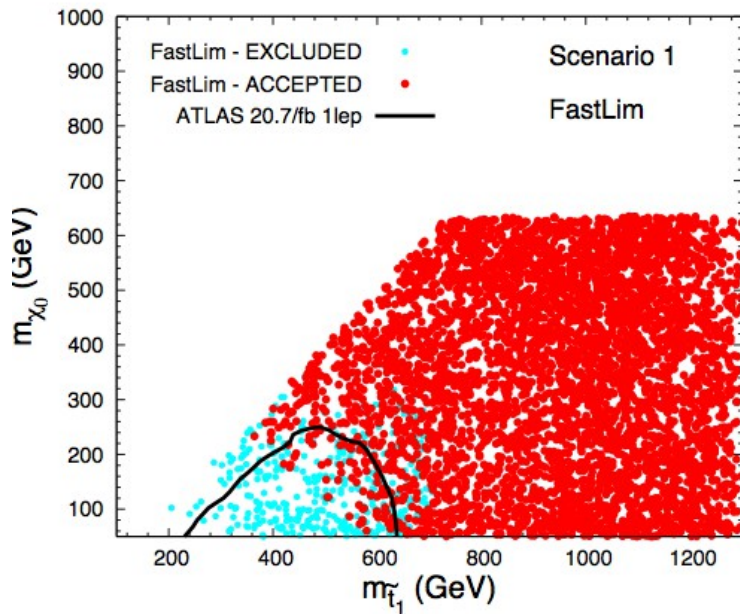
11 ATLAS searches at 21  $f^{-1}$

Point excluded if it is excluded in any bin

FASTLIM

M. Papucci, K. Sakurai, A. Weiler, L. Zeune

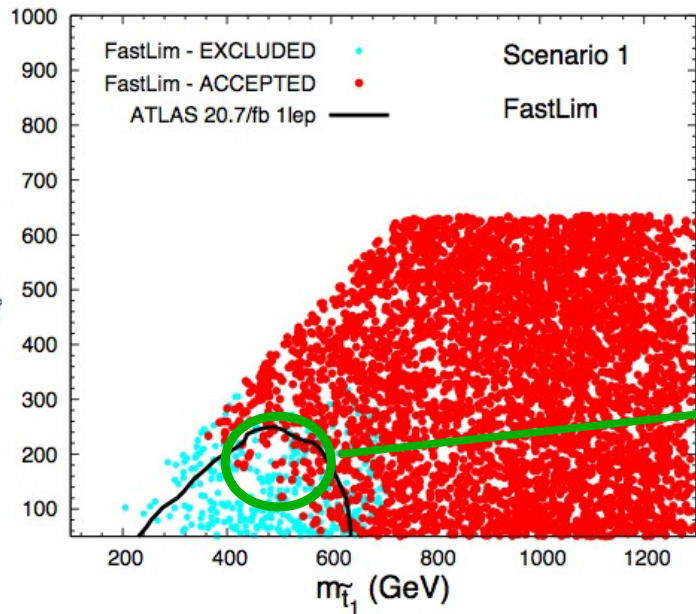
[ArXiv:1402.0492](https://arxiv.org/abs/1402.0492)



Enrico Maria Sessolo



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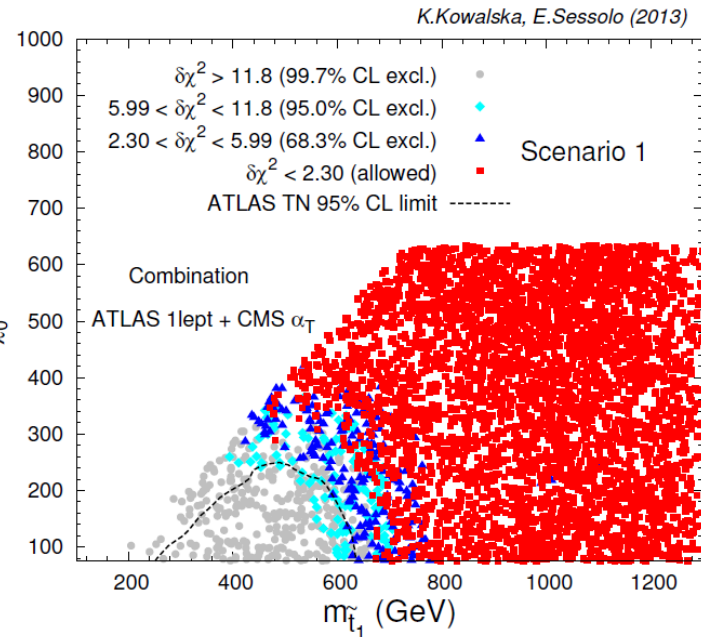
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M. Papucci, K. Sakurai, A. Weiler, L. Zeune

[ArXiv:1402.0492](https://arxiv.org/abs/1402.0492)

Points “almost” excluded,  
eg:  $CL_s = 0.053$  in one bin



Statistical combination of likelihoods from all bins → slightly stronger exclusion

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# Scenario 3 – light sleptons, winos, binos

Dominant decay channels:

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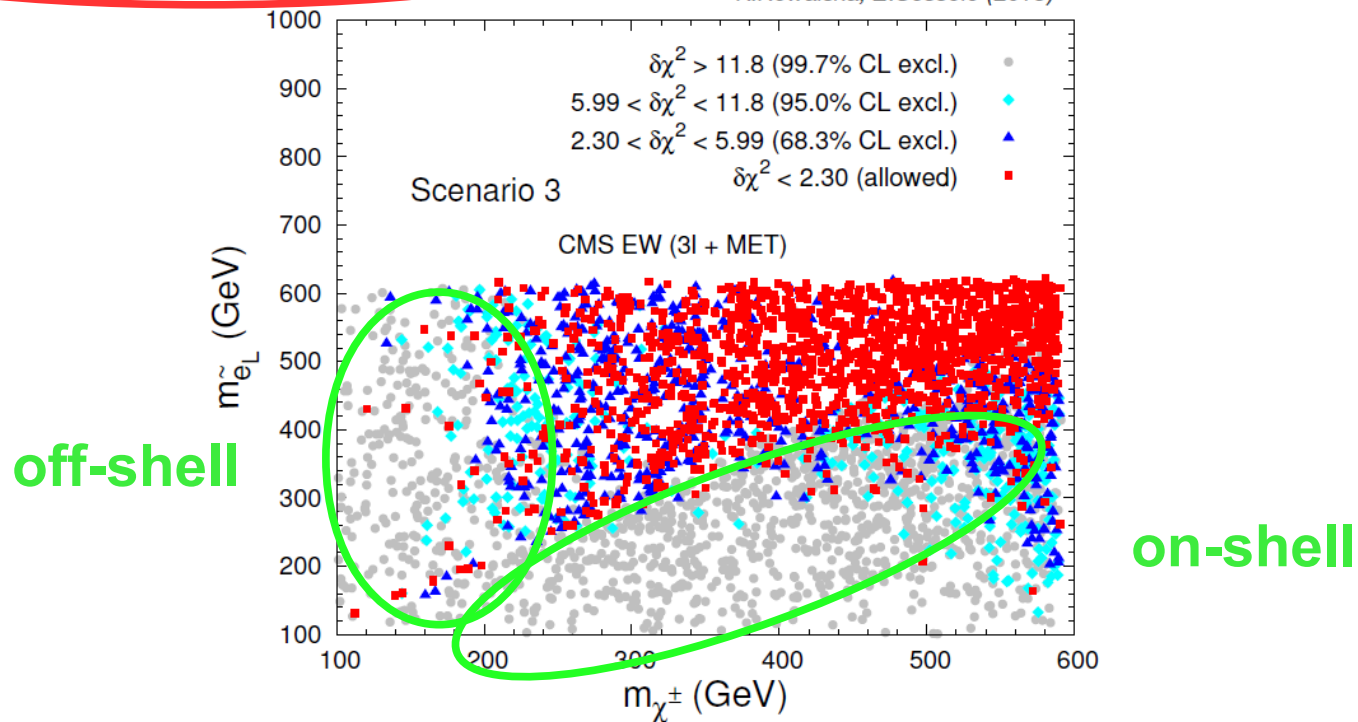
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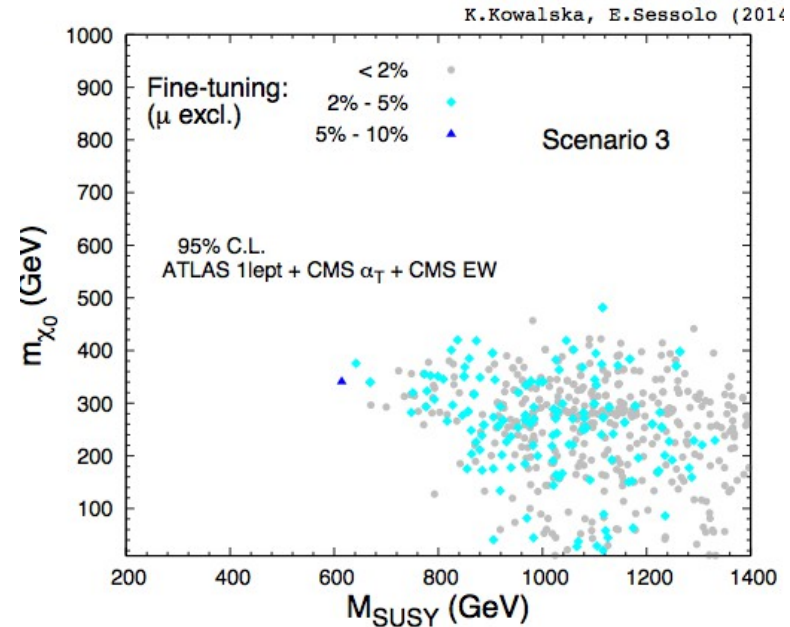
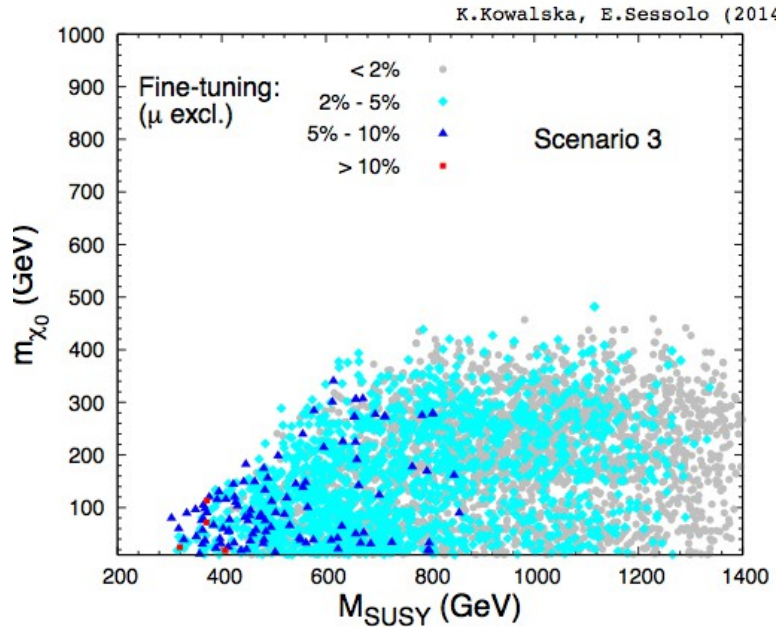
$$\tilde{\chi}_1^\pm \rightarrow \nu_l l^\pm \tilde{\chi}_1^0$$

$$\tilde{\chi}_2^0 \rightarrow l^+ l^- \tilde{\chi}_1^0$$

*K.Kowalska, E.Sessolo (2013)*

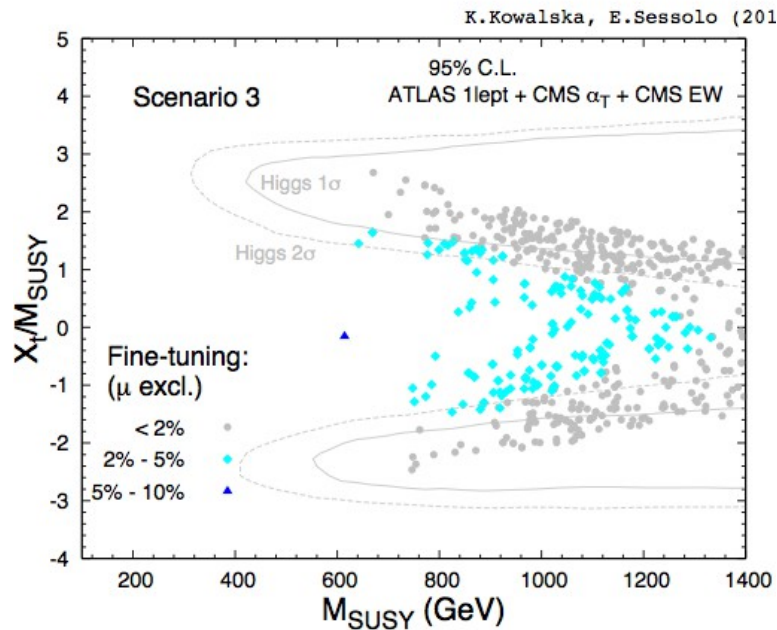


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$\Lambda \sim 10^{16} \text{ GeV}$  (but see K.Kowalska's talk on Friday)

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$$|\mu| \lesssim 645 \text{ GeV}$$

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$$|M_2| \lesssim \frac{(5200 \text{ GeV})}{5} \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1/2}$$

$$|M_3| \lesssim \frac{(8500 \text{ GeV})}{30} \ln \left( \frac{\Lambda}{\text{TeV}} \right)^{-1}$$