

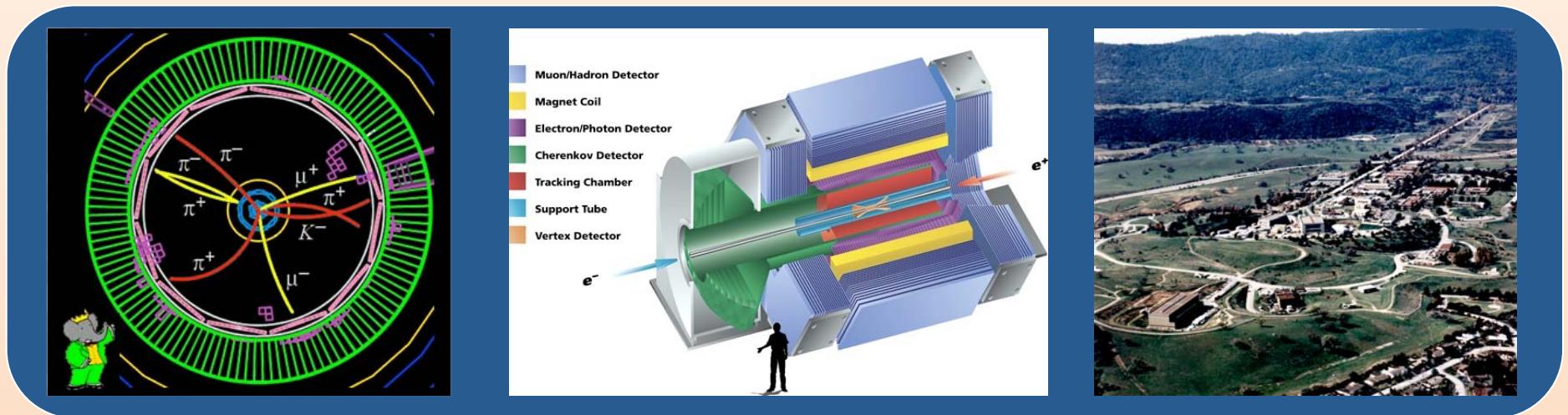


# A measurement of $|V_{us}|$ with 1-prong decays and testing lepton universality

## BaBar Collaboration

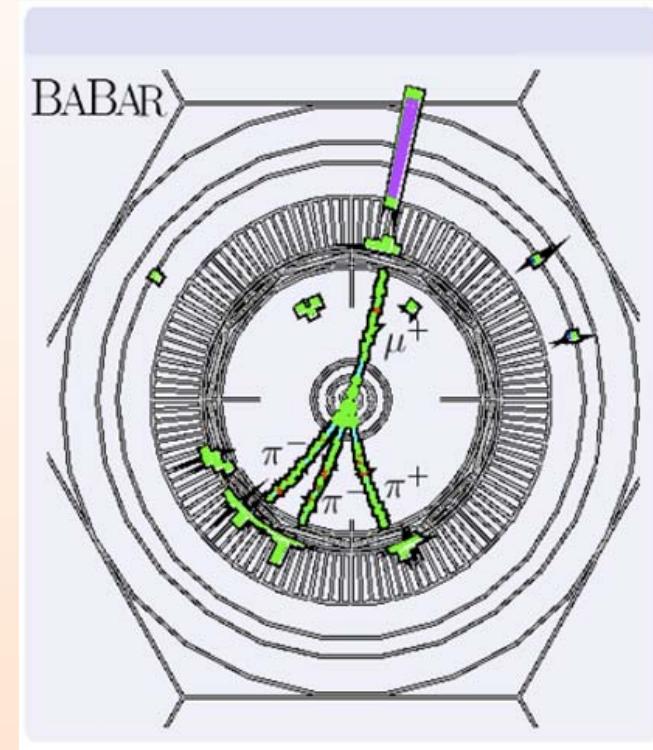
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# Outline

- Motivation
- BaBar detector and data set
- Selection and results
- Discussion
- Summary

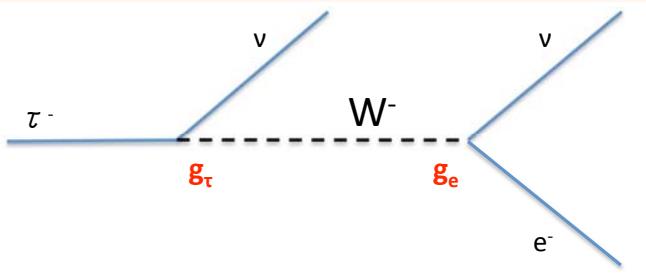


The results in this work have been published in Phys.Rev.Lett.105:051602,2010.

# Lepton Universality

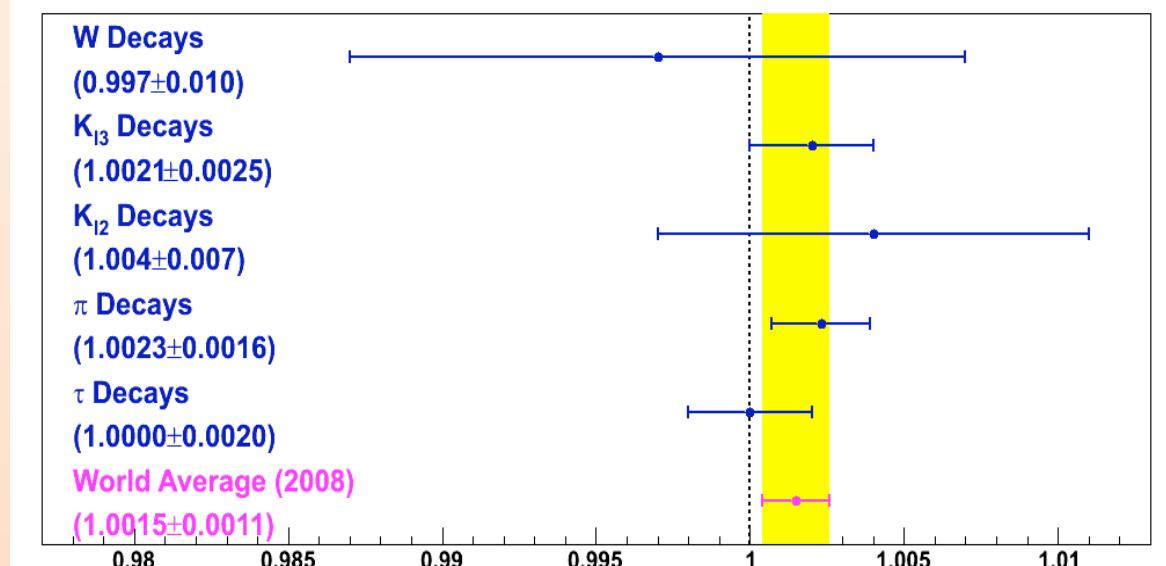
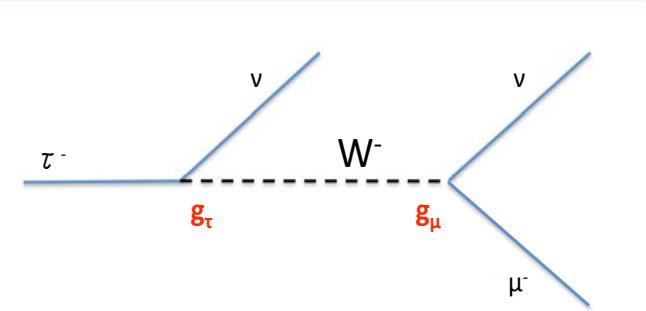


The SM assumes that the coupling of the W to the leptons is identical

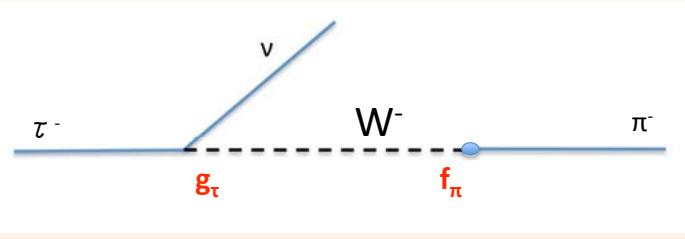


$$g_e = g_\mu = g_\tau$$

$$\left( \frac{g_\mu}{g_e} \right) = \frac{B(\tau^- \rightarrow \mu^- \nu \bar{\nu})}{B(\tau^- \rightarrow e^- \nu \bar{\nu})} \frac{f(m_e^2 / m_\tau^2)}{f(m_\mu^2 / m_\tau^2)}$$

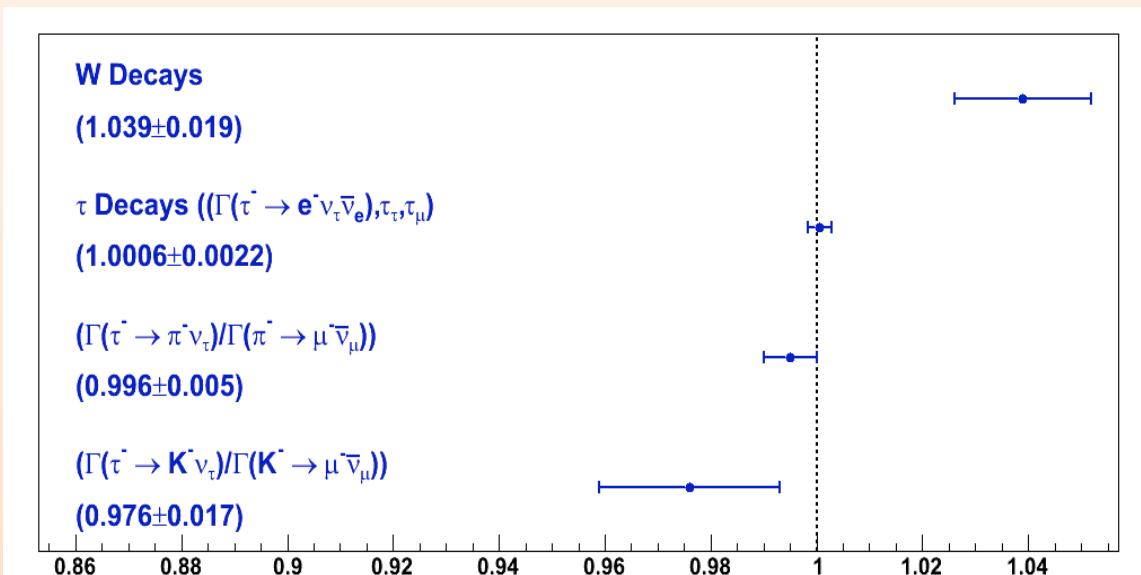
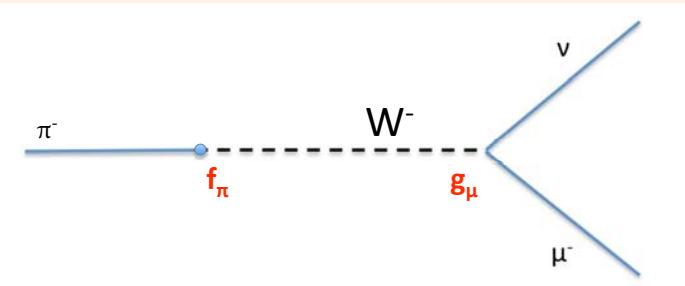


# Lepton Universality



$$g_e = g_\mu = g_\tau$$

$$\left( \frac{g_\tau}{g_\mu} \right) = \frac{B(\tau^- \rightarrow h^- \nu)}{B(h^- \rightarrow \mu^- \nu)} \frac{2m_h m_\mu^2 \tau_h}{(1+\delta_h)m_\tau^3 \tau_\tau} \left( \frac{1 - m_\mu^2/m_h^2}{1 - m_\tau^2/m_\tau^2} \right)$$



# Status of $|V_{us}|$



One can use the unitarity constraint from the CKM matrix  
 $V_{ud}$  is well measured in super-allowed beta decays  
 $V_{ub}$  is negligible

$$|V_{ud}|^2 = 1 - |V_{us}|^2 - |V_{ub}|^2$$

$$|V_{us}| = 0.2262 \pm 0.0011$$

$$|V_{ud}| = 0.97425 \pm 0.00022$$

$$|V_{ub}| = (3.93 \pm 0.36) \times 10^{-3}$$

$V_{ud}$  from Towner and Hardy PR C79 055502 (2009)  
 $V_{ub}$  from PDG 2008

One can also use the inclusive measurement of all the strange hadronic decays to determine  $V_{us}$

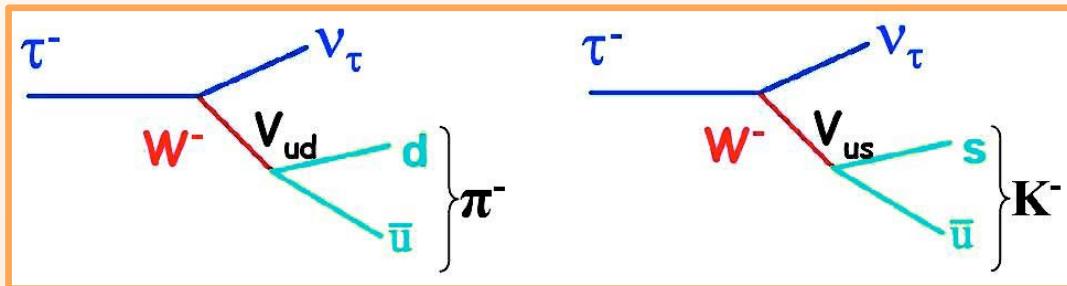
$$|V_{us}| = 0.2192 \pm 0.0035$$

ICHEP 2010

# Measurement of $V_{us}$



BaBar has measured  $V_{us}$  in two ways:



Use the kaon branching fraction

$$B(\tau^- \rightarrow K^- \bar{v}_\tau)$$

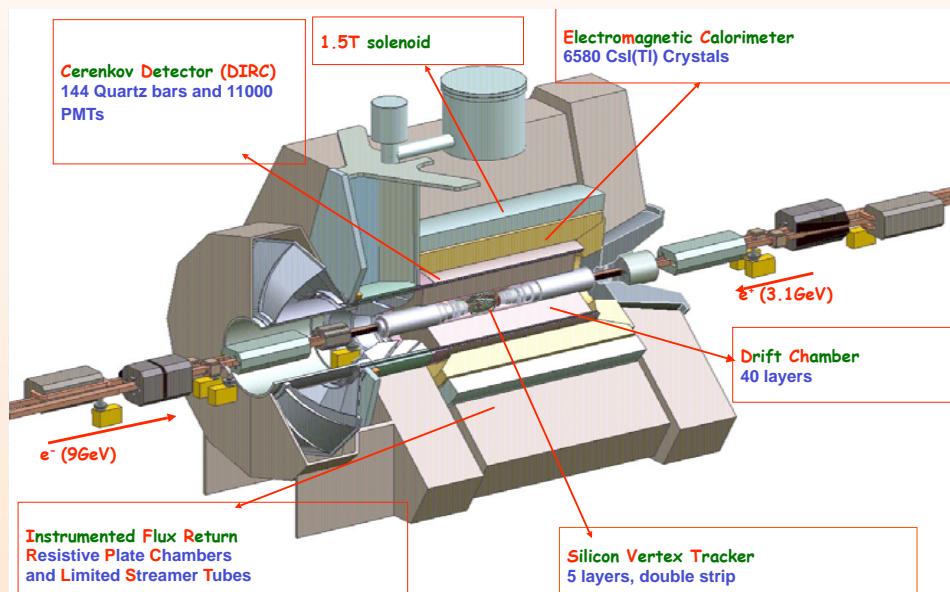
Use the ratio of kaon to pion branching fractions

$$\frac{B(\tau^- \rightarrow K^- \bar{v}_\tau)}{B(\tau^- \rightarrow \pi^- \bar{v}_\tau)}$$

# Detector and data sample

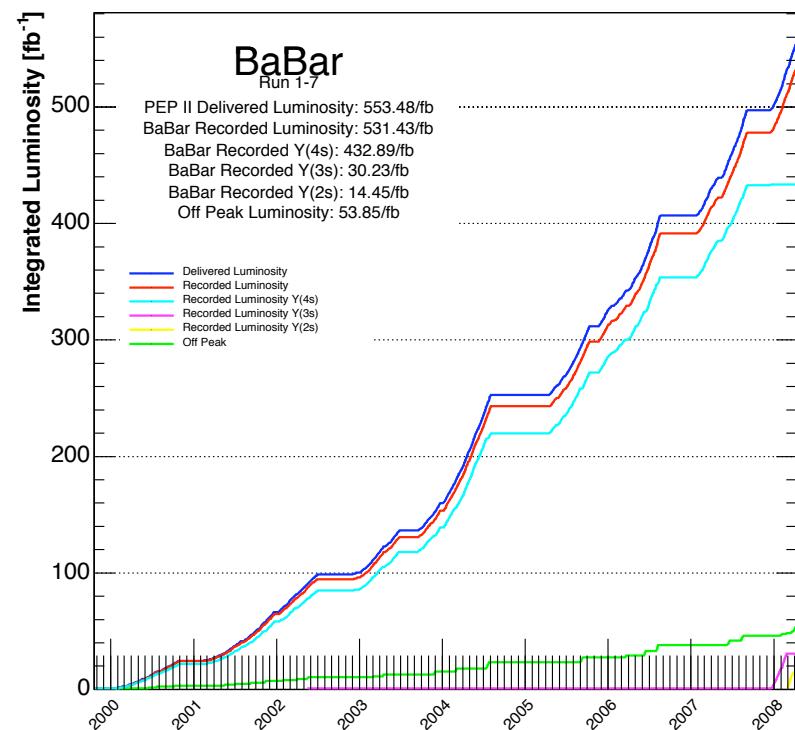


As of 2008/04/11 00:00

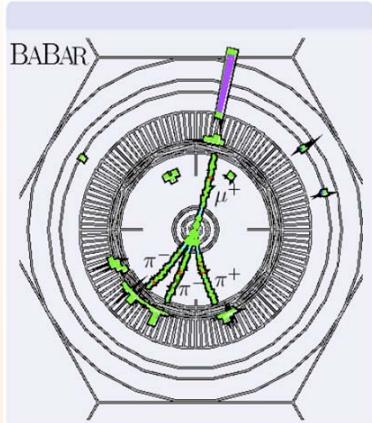


Using a data set based on a luminosity of  $467 \text{ fb}^{-1}$

Approximately 900 million tau leptons



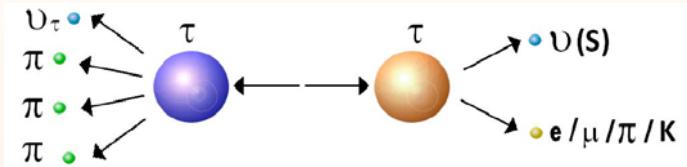
# Tau selection



## Select tau pair events

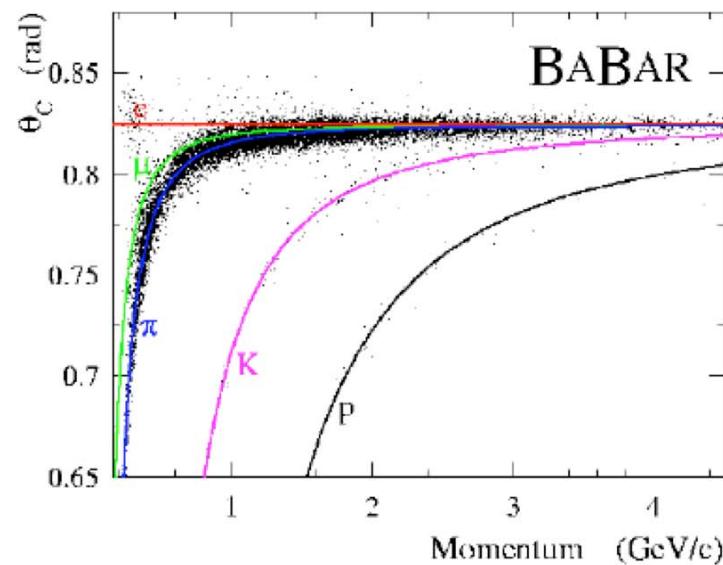
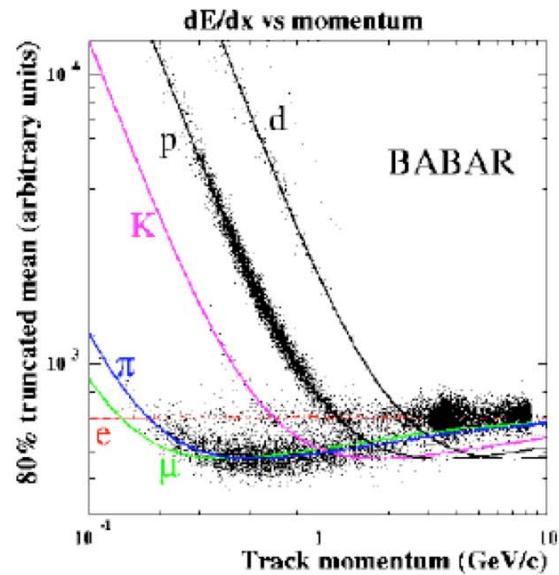
Use one tau decay as a “tag” to reduce background from hadronic events

Use tau 3-prong decays as “tag decay” for the study of 1-prong decay modes

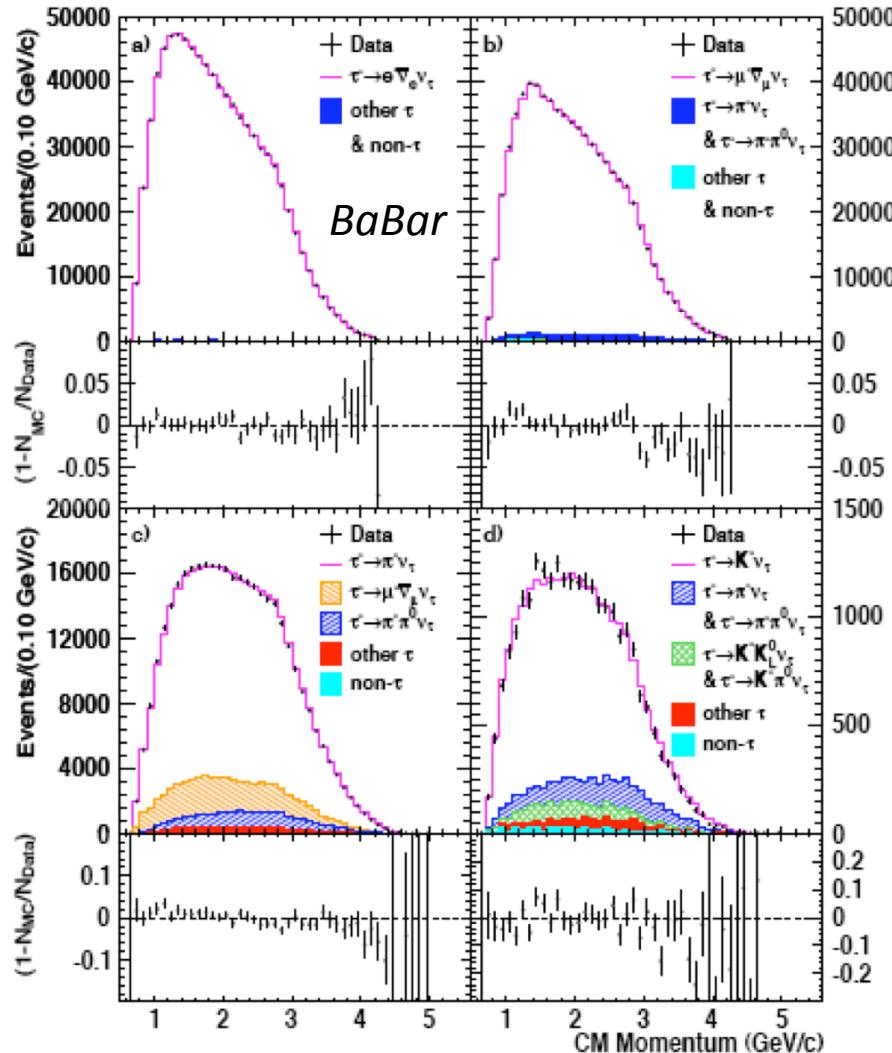


Measure muon, pion and kaon branching fractions relative to the electron mode to reduce systematic errors.

## Excellent K/ $\pi$ Separation



# Results



$\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$	$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$
$\tau^- \rightarrow \pi^- \nu_\tau$	$\tau^- \rightarrow K^- \nu_\tau$

	$\mu$	$\pi$	$K$
$N^D$	731102	369091	25123
Purity	97.3%	78.7%	76.6%
Total Efficiency	0.485%	0.324%	0.330%
Particle ID Efficiency	74.5%	74.6%	84.6%
Systematic uncertainties:			
Particle ID	0.32	0.51	0.94
Detector response	0.08	0.64	0.54
Backgrounds	0.08	0.44	0.85
Trigger	0.10	0.10	0.10
$\pi^- \pi^- \pi^+$ modelling	0.01	0.07	0.27
Radiation	0.04	0.10	0.04
$\mathcal{B}(\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau)$	0.05	0.15	0.40
$\mathcal{L}\sigma_{e^+ e^- \rightarrow \tau^+ \tau^-}$	0.02	0.39	0.20
Total [%]	0.36	1.0	1.5

# Branching fractions



Measure branching fractions relative to electron mode

$$R_\mu = 0.9796 \pm 0.0016 \pm 0.0036$$

$$R_\pi = 0.5945 \pm 0.0014 \pm 0.0061$$

$$R_K = 0.03882 \pm 0.00032 \pm 0.00057$$

$$R_X = \frac{B(\tau^- \rightarrow X^- \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$$

Branching fractions based on  $B(\tau^- \rightarrow e^- \nu \bar{\nu}) = (17.82 \pm 0.05)\%$

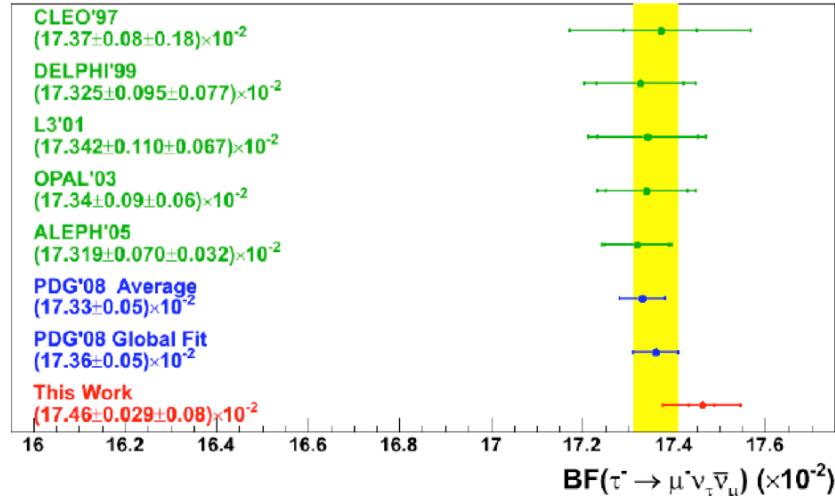
PDG2008

$$B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau) = (17.46 \pm 0.03 \pm 0.08)\%$$

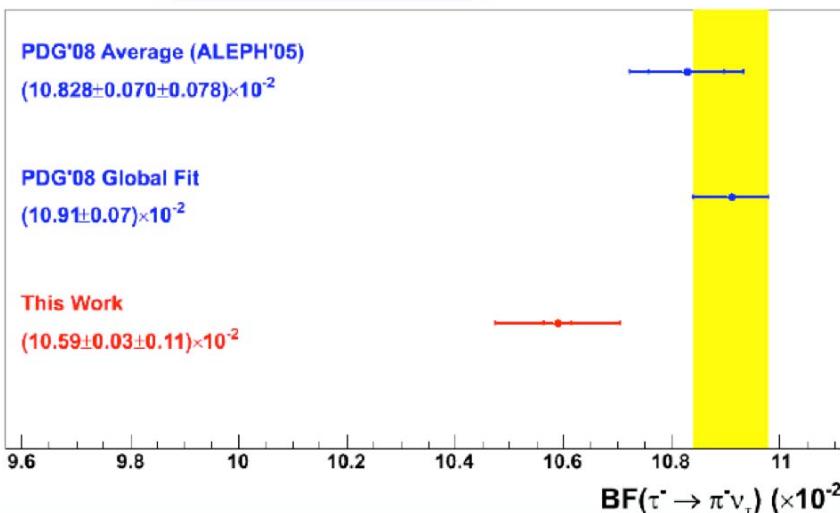
$$B(\tau^- \rightarrow \pi^- \nu_\tau) = (10.59 \pm 0.03 \pm 0.11)\%$$

$$B(\tau^- \rightarrow K^- \nu_\tau) = (0.692 \pm 0.006 \pm 0.010)\%$$

$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \bar{\nu}_\tau$



$\tau^- \rightarrow \pi^- \bar{\nu}_\tau$



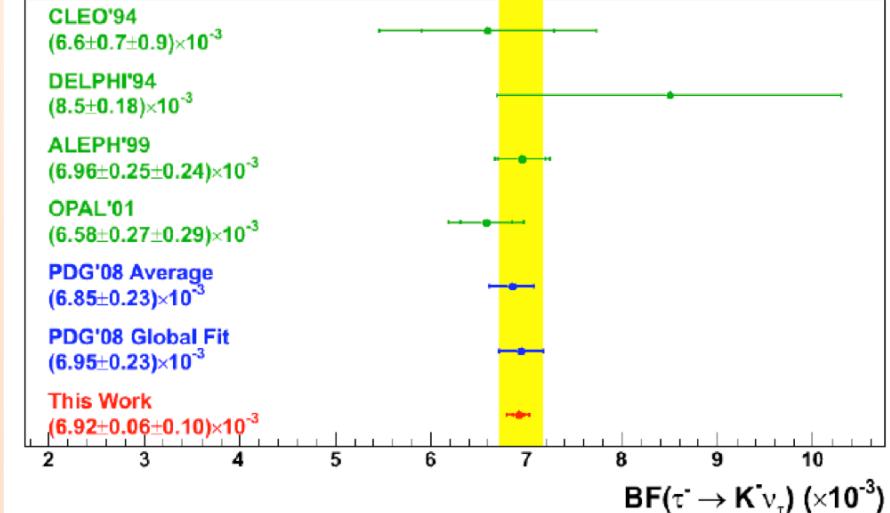
## Comparison with previous measurements

$$B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \bar{\nu}_\tau) = (17.46 \pm 0.03 \pm 0.08)\%$$

$$B(\tau^- \rightarrow \pi^- \bar{\nu}_\tau) = (10.59 \pm 0.03 \pm 0.11)\%$$

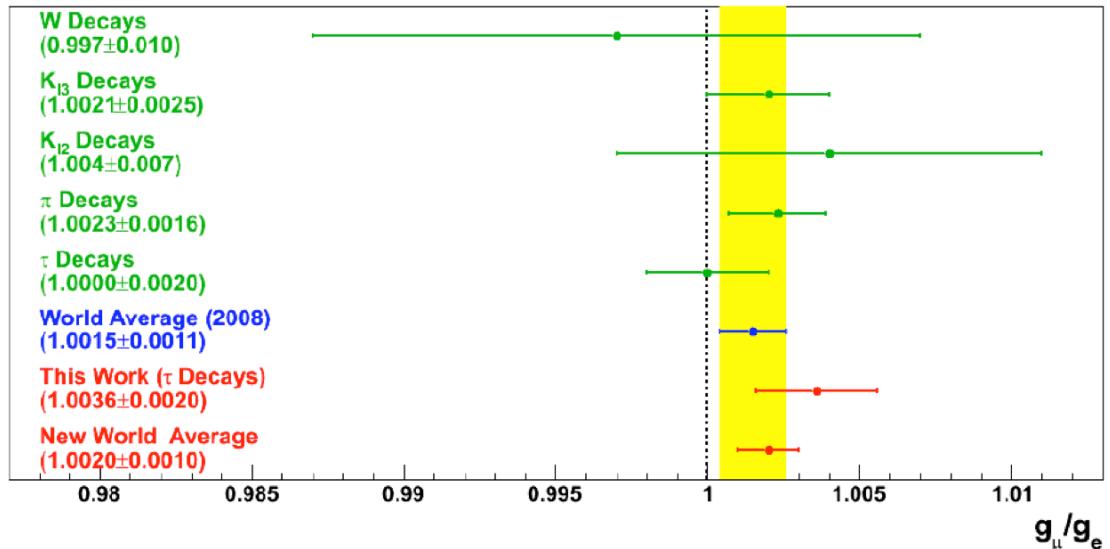
$$B(\tau^- \rightarrow K^- \bar{\nu}_\tau) = (0.692 \pm 0.006 \pm 0.010)\%$$

$\tau^- \rightarrow K^- \bar{\nu}_\tau$





# Lepton universality results



Ratio of the muon and electron coupling using the measured branching fractions

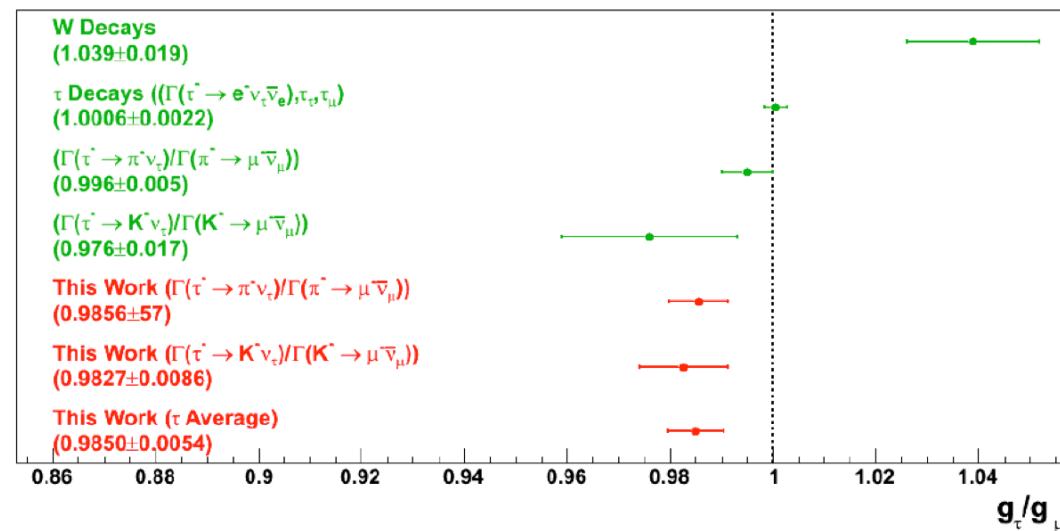
$$\left( \frac{g_\mu}{g_e} \right) = 1.0036 \pm 0.0020$$

*Consistent the lepton universality*

$$\left( \frac{g_\mu}{g_e} \right)^2 = \frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)} \frac{f(m_e^2 / m_\tau^2)}{f(m_\mu^2 / m_\tau^2)}$$

$$f(x) = 1 - 8x + 8x^3 - x^4 + 12x^2 \log x$$

# More lepton universality results



Ratio of the muon and tau coupling using the measured branching fractions

$$\left( \frac{g_\tau}{g_\mu} \right)_\pi = 0.9856 \pm 0.0057$$

$$\left( \frac{g_\tau}{g_\mu} \right)_K = 0.9827 \pm 0.0086$$

$$\left( \frac{g_\tau}{g_\mu} \right)^2 = \frac{B(\tau^- \rightarrow h^- \bar{\nu}_\tau)}{B(h^- \rightarrow \mu^- \bar{\nu}_\tau)} \frac{2m_h m_\mu^2 \tau_h}{(1 + \delta_h)m_\tau^3 \tau_\tau} \frac{(1 - m_\mu^2/m_h^2)}{(1 - m_h^2/m_\tau^2)}$$

Radiative corrections:

$$\delta_\pi = (0.16 \pm 0.14)\% \quad \delta_K = (0.90 \pm 0.22)\%$$

*Consistent the lepton universality*

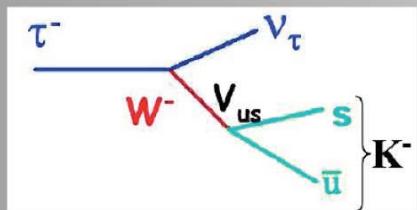
# $V_{us}$ results



One can extract  $V_{us}$  from the kaon branching fraction

$$B(\tau^- \rightarrow K^- \nu_\tau) = \frac{G_F^2 f_K^2 |V_{us}|^2 m_\tau^3 \tau_\tau}{16\pi\hbar} \left(1 - \frac{m_K^2}{m_\tau^2}\right)^2 S_{EW}$$

$$S_{EW} = 1.0201 \pm 0.0003$$



$$|V_{us}| = 0.2193 \pm 0.0032$$

# More results on $V_{us}$

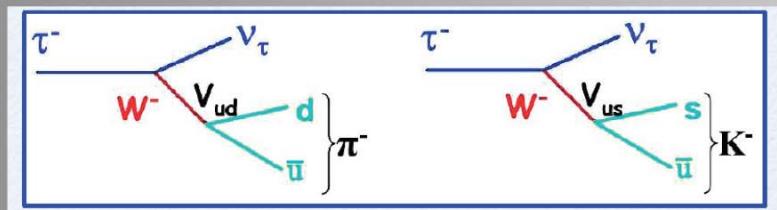


One can determine  $V_{us}$  by the ratio of kaon/pion BFs

$$\frac{B(\tau^- \rightarrow K^- \nu_\tau)}{B(\tau^- \rightarrow \pi^- \nu_\tau)} = \frac{f_K^2}{f_\pi^2} \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{(1 - m_K^2/m_\tau^2)}{(1 - m_\pi^2/m_\tau^2)} (1 + \delta_{LD})$$

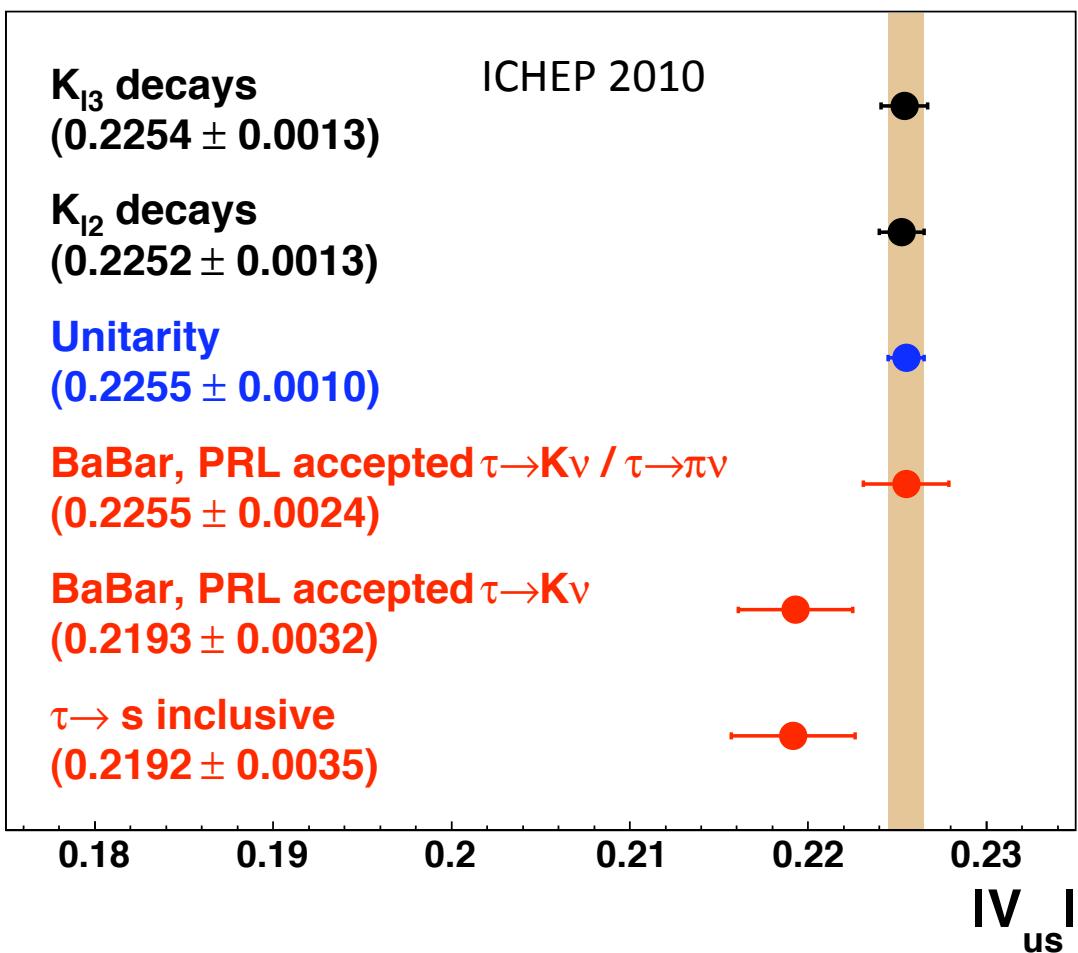
$$f_K/f_\pi = 1.189 \pm 0.007$$

$$\delta_{LD} = (0.03 \pm 0.44)\%$$



$$|V_{us}| = 0.2255 \pm 0.0024$$

# $V_{us}$ summary



Results are in good agreement between CKM unitarity constraint, kaon decays and tau decays



# Summary

BaBar has made measurements of the one-prong tau decay modes

The results are used to test lepton universality and found to be consistent with unity.

The pion and kaon BFs are also used to measure  $V_{us}$

The results are consistent with value obtained from CKM Unitarity but above the value obtained from the inclusive strange BFs

$$B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau) = (17.46 \pm 0.03 \pm 0.08)\%$$

$$B(\tau^- \rightarrow \pi^- \nu_\tau) = (10.59 \pm 0.03 \pm 0.11)\%$$

$$B(\tau^- \rightarrow K^- \nu_\tau) = (0.692 \pm 0.006 \pm 0.010)\%$$

$$\text{Kaon BF} : |V_{us}| = 0.2193 \pm 0.0032$$

$$\text{Kaon:Pion BF} : |V_{ud}| = 0.2255 \pm 0.0024$$

The results in this work have been published in Phys.Rev.Lett.105:051602,2010.