

# Tau lepton physics at **Belle** and Belle II/SuperKEKB



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# Contents

## ■ Belle II/SuperKEKB Projects

- ◆ Naming: KEKB → superKEKB (machine)  
Belle → Belle II (detector)  
 →  (logo)

## ■ Prospect of $\tau$ Physics at Belle and Belle II

- Lepton Flavor Violation
- CP Violation
- Lepton Universality
- Hadronic Decays, Spectral Functions, Form Factors
- Others

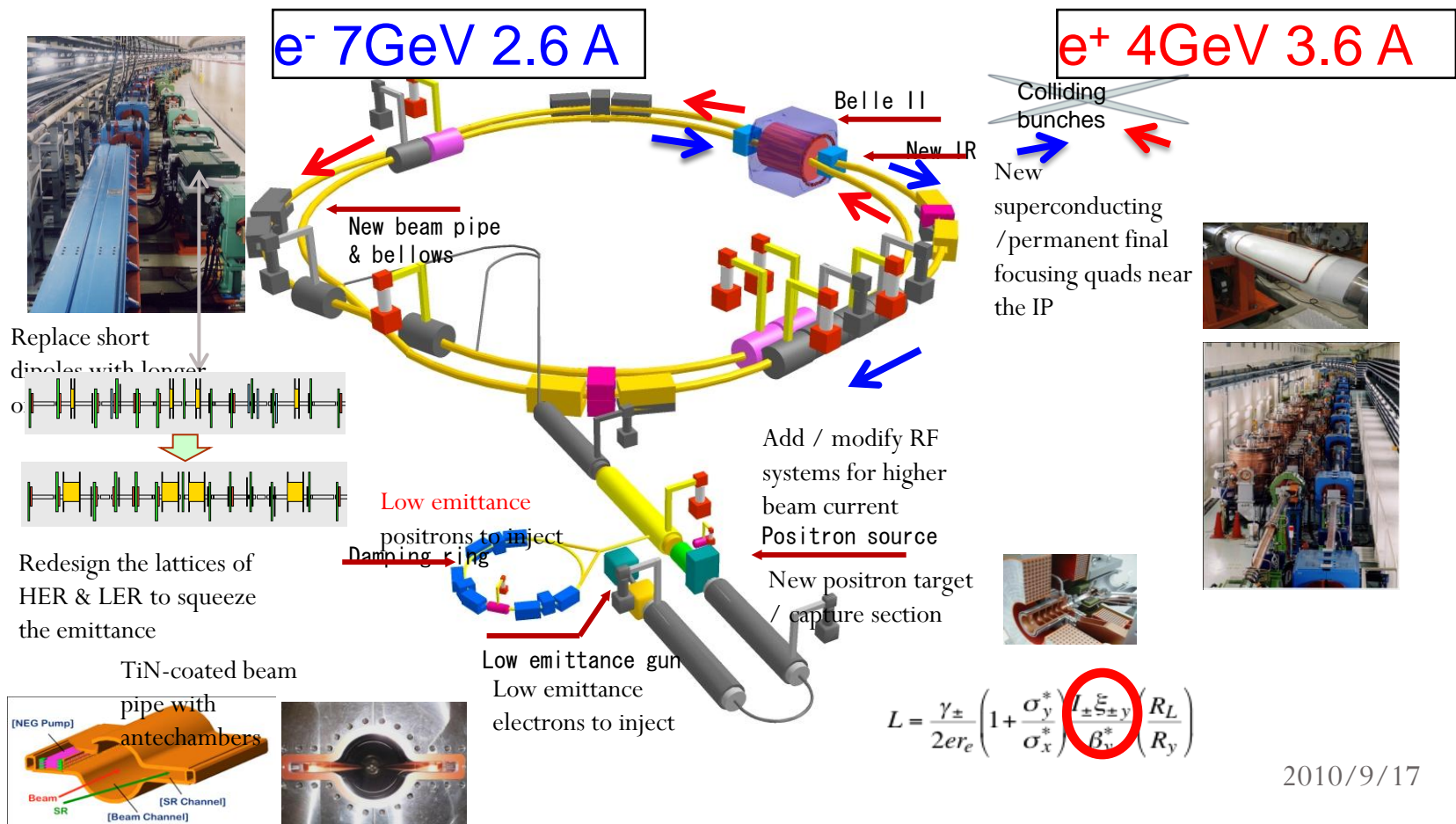
### ◆ BelleII/SuperKEKB documents

- ◆ T. Aushev et al., (2010) arxiv: 1002.5012
- ◆ A.G. Akeroyd et al., (SuperKEKB Physics Working Group) (2004) arxiv: hep-ex/0406071

2010/9/17

# Super KEKB collider

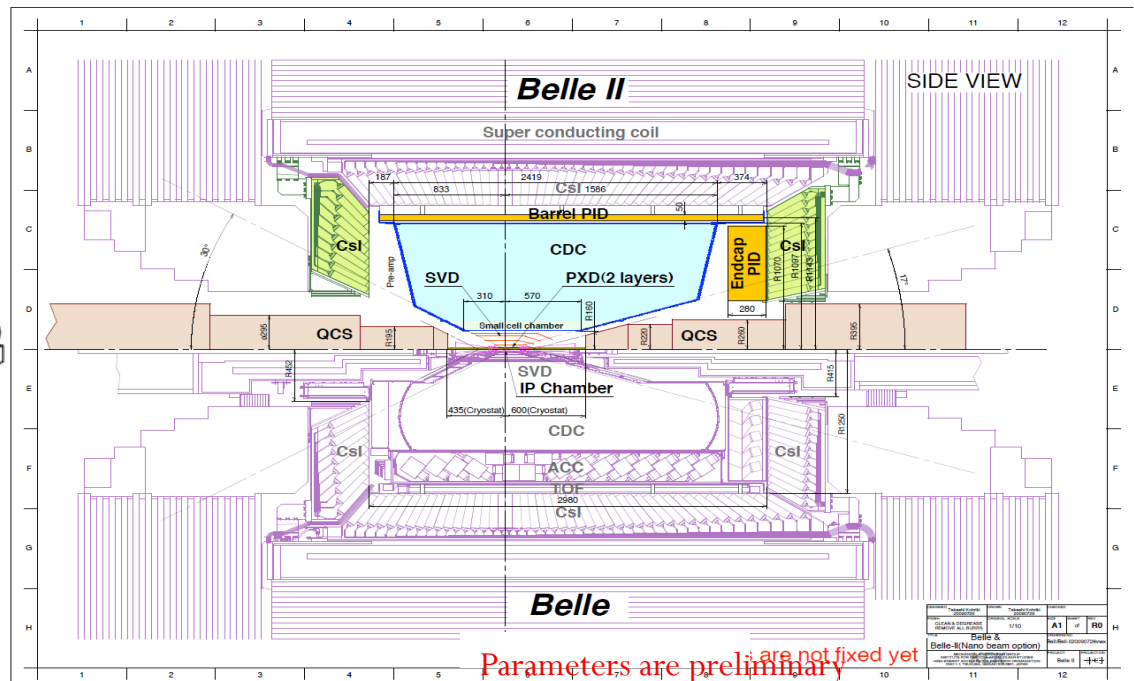
- Target Luminosity  $8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- Accumulate  $50 \text{ ab}^{-1}$ , x 50 as large as the luminosity achieved by KEKB, within 5 years after end of construction.



$$L = \frac{\gamma_{\pm}}{2e r_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{\pm y}}{\beta_y^*} \left( \frac{R_L}{R_y} \right)$$

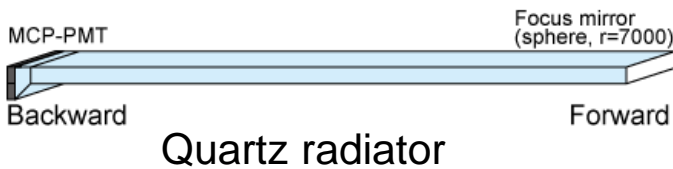
# Belle II Detector

- Very Precise vertex determination with Pixel detectors and Si strip detectors.
- Tracking : Larger volume + larger sampling + improve dEdx
- Calorimeter: CsI(Tl) with wave form sampling. less materials in front.
- Particle ID : TOP counter + A-RICH; (Reconstruct Č Ring-image ) improved performance of Kaon ID
- muon/KL: Scintillation counters instead of RPC
- New DAQ system,
- New trigger



Parameters are preliminary, are not fixed yet

Time Of Propagation counter  
= Compact DIRC



MCP-PM = Micro-Channel Plate Photomultiplier

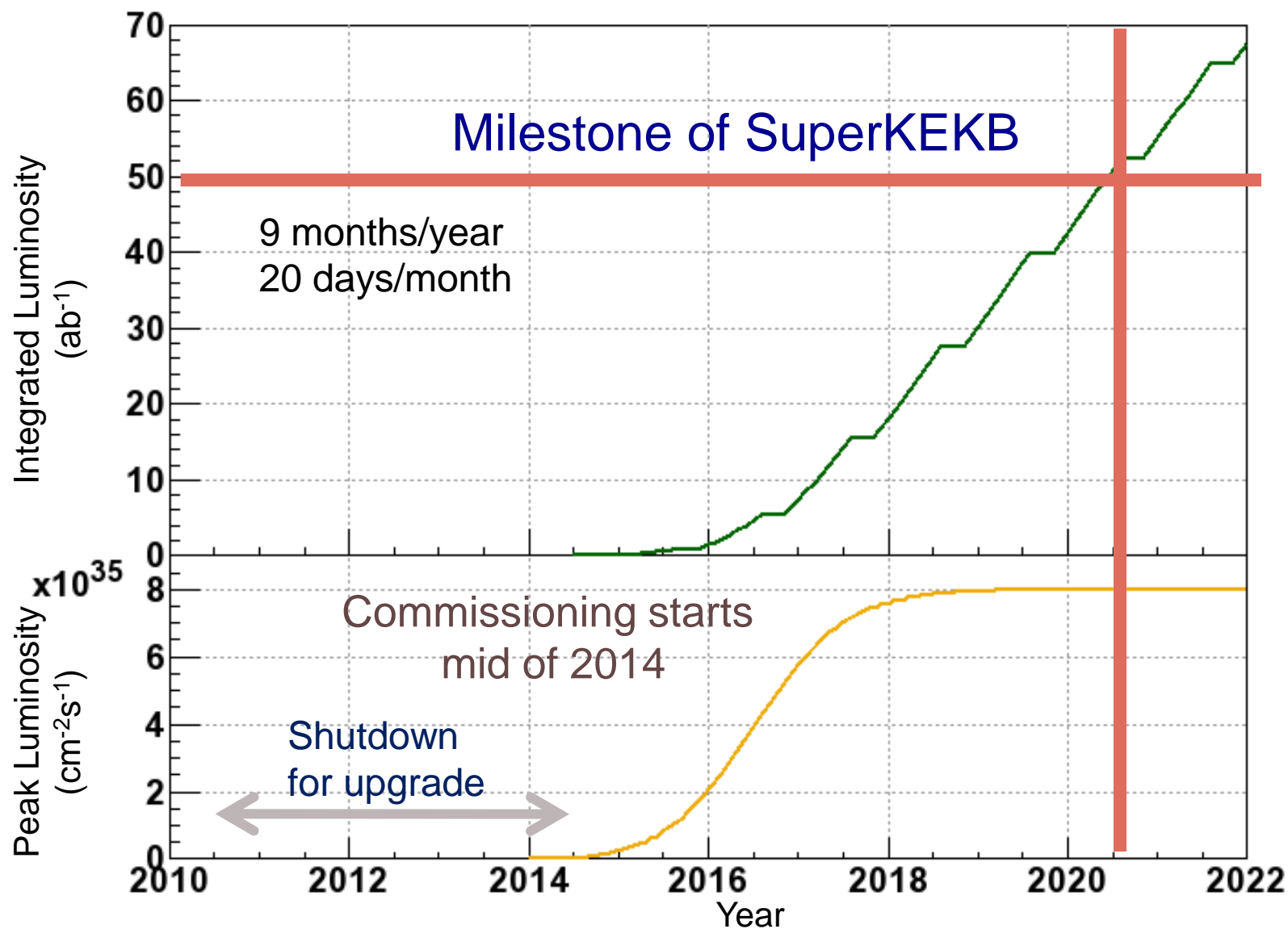
# Tau Lepton Factories

Group	Int. Luminosity $\text{fb}^{-1}$	$N_{\tau\tau}$ $10^6$
LEP(Z-peak)	0.34	0.33
CLEO(10.6 GeV)	13.8	12.6
Babar(10.6 GeV)	516	482
Belle(10.6 GeV)	1014	933
tau-c (4.2 GeV)	10	32,000
<b>BelleII/SuperKEKB</b>	<b>50,000</b>	<b>46,000</b>
<b>SuperB</b>	<b>75,000</b>	<b>69,000</b>

- ✓ Babar and Belle collected together about  $1.5 \text{ ab}^{-1}$
- ✓ Belle II/SuperB are planning to collect additional x50-75 times more data.
- ✓ At  $\Upsilon(4S)$   $\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.919 \text{ nb}$ , so B-factory is also a tau factory.

**Belle II/SuperB with  $50 \text{ ab}^{-1}$  will yield  $4.5 \times 10^{10} \tau^+\tau^-$  pairs.**

# Luminosity upgrade plan



We are planning to reach  $50 \text{ ab}^{-1}$  in 2020~2021.

# $\tau$ Lepton Physics

# Overview

Goal/Dream

Category

Physics

Important factors

New Physics

Absent in SM

- Lepton Flavor Violation
- Charged Lepton CPV
- $\tau$  EDM
- CPT violation

Luminosity



Background

Precision Measurement, search for deviation from SM

Particle ID ( $\pi/K$ )

- Lepton Universality  
 $m_t, \tau$  –lifetime,  $B_e, B_\mu, B_\pi, B_K$
- $(g-2)_\tau$

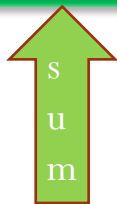
$\pi^0$

Hadrons

Inclusive Measurements

- (strange) Br, spectral functions  
 $\alpha_s, V_{us}, m_s, \langle qq \bar{q} \rangle$   
 $(g-2)_\mu^? / CVC$

Knowledge of decay angles



Spin-Spin corr.

Understand various pQCD and non-pQCD aspects of Hadrons from 1<sup>st</sup> principle.

Exclusive Measurements

Knowledge of  $\tau$  direction

$\tau$  is an ideal to study hadrons

String Theory helps us?  
AdS/CF

- Br, mass spectrums
- Form Factors(A, V, S)
- 2<sup>nd</sup> Class Current
- Resonances. Rare decays

Beam polarization

2010/9/17

# Note:

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I will discuss both subjects in a mixed form.

1. Subjects to be done mainly using Belle data.

Test of Lepton Universality

Br's, Hadron Spectral Functions.

.....

2. Subjects to be done using Belle data but also important in Belle II experiments.

Lepton Flavor Violation

CP Violation

CPT test,  $(g-2)_\tau$



# Lepton Flavor Violation (LFV)



- Charged lepton flavor violation is strongly suppressed in SM,

$$Br(\tau \rightarrow \ell \gamma) \propto \left( \frac{\Delta m_\nu^2}{m_w^2} \right)^2 \approx 10^{-49-54}$$

W.J. Marciano, A.I. Sanda (1977)

but a feature common to many possible extensions of the SM.

MSSM + seesaw, -- dipole as well as Higgs mediated.

Little Higgs, TeV scale  $v_R$ , 4<sup>th</sup> generation ...

( arxiv: 0801.1826 )



- Some of models predict rather high branching fraction comparable with current experimental sensitivity.
- Interesting interplay between  $\tau$  LFV and  $\mu \rightarrow e \gamma$  (MEG exp.) : complementary

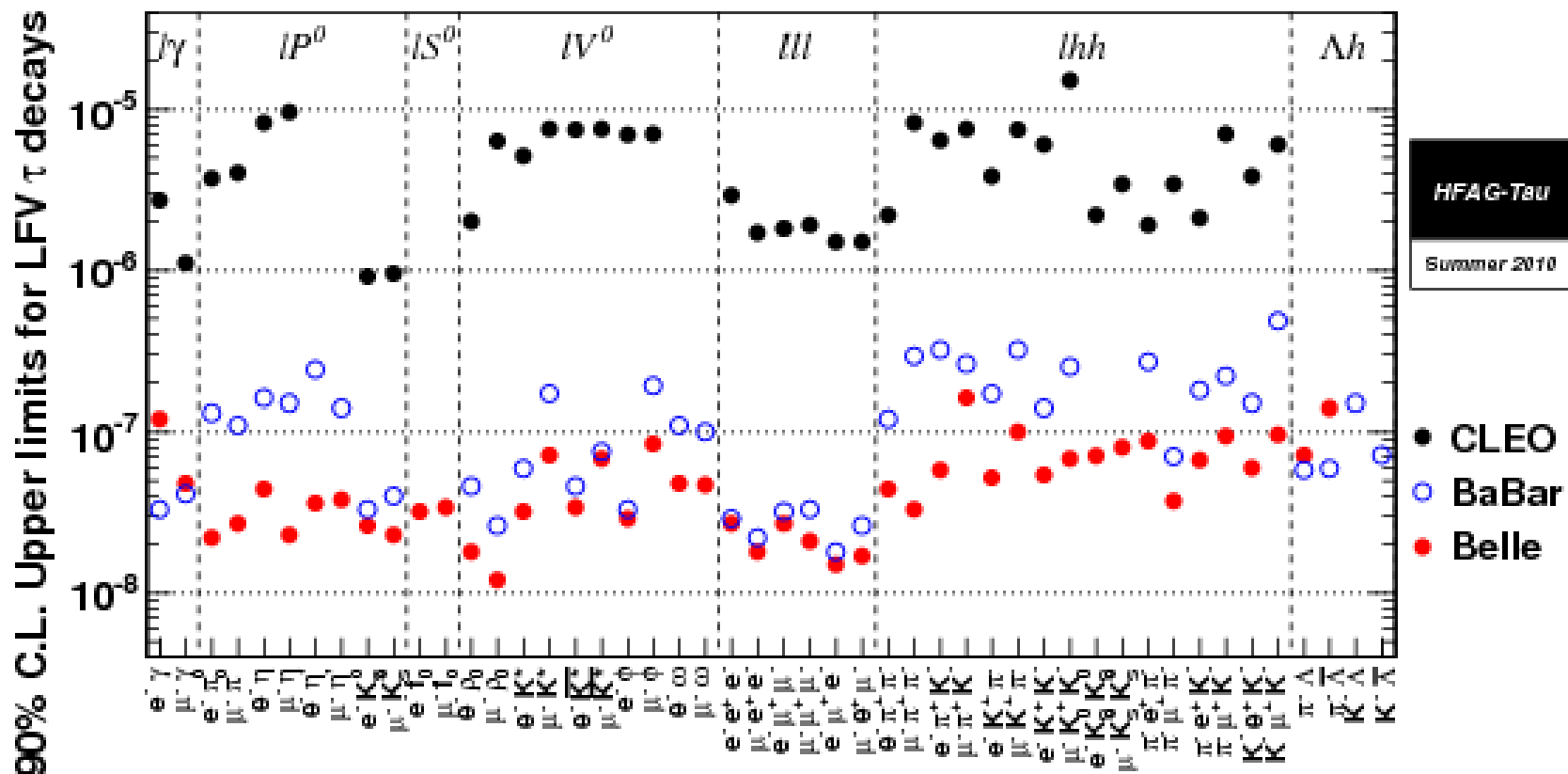
$\mu \rightarrow e \gamma$  : good sensitivity for MSSM + seesaw(dipole)

$\tau$  LFV : good sensitivity for Higgs mediated scenario

Many decay modes:

# LFV: Current Status

2010 Summer Status



- ✓ 49 LFV modes are studied.
- ✓ Our sensitivity reaches  $O(10^{-8})$

# LFV: Prospect at Belle II

## ■ Accessible Br. at $50 \text{ ab}^{-1}$

✓  $\tau \rightarrow \mu\gamma, e\gamma$       $3 \times 10^{-9}$  (limited BG)

✓  $\tau \rightarrow \mu\eta$       $2 \times 10^{-9}$

✓  $\tau \rightarrow 3l$  ( $\mu\mu\mu \dots$ )  $8 \times 10^{-10}$  (BG free)

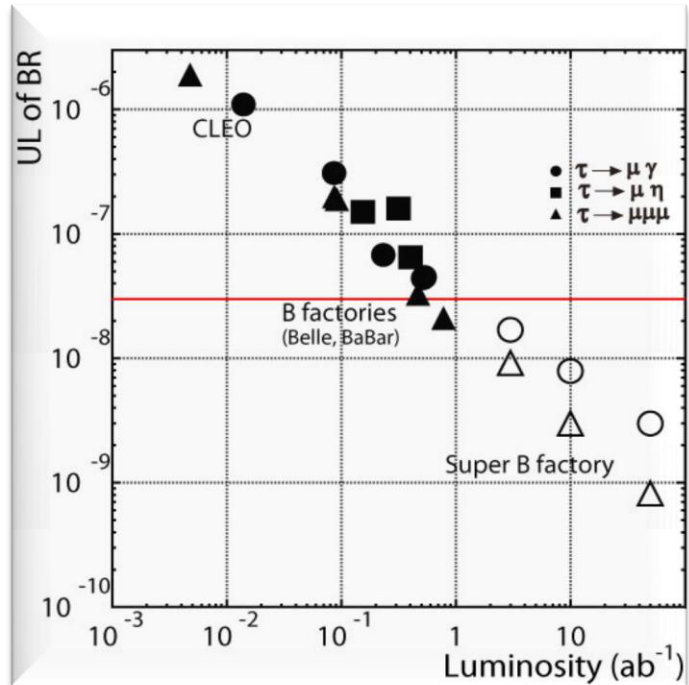
✓ Expectation is obtained assuming the current level of background and efficiency conservatively without assuming any improvement.

✓ Further improvements are expected by better detector performance and ...

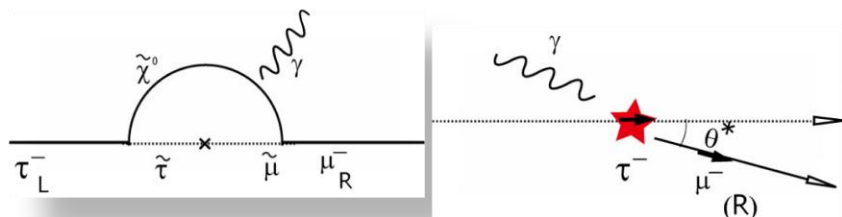
✓  $\tau \rightarrow \mu\gamma, e\gamma$ ;

Main BG is from the ISR photon +  $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\ell (\gamma)$

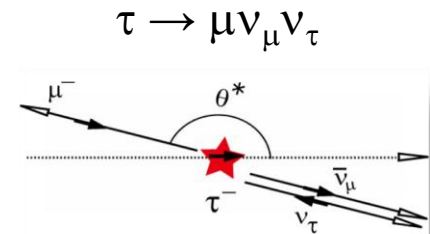
✓ Beam polarization or spin-correlation are expected to be useful to reduce these backgrounds. Chirality is changed (L $\leftrightarrow$ R) in  $\tau \rightarrow \mu\gamma$



Ref. arxiv:1002.5012



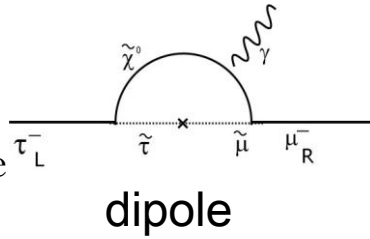
VS



# Belle II Sensitivity for some models

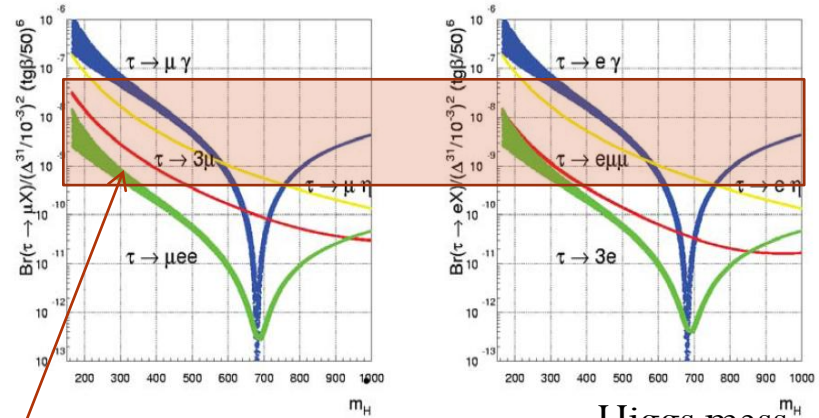
$\tau \rightarrow \mu \gamma$  vs.  $\mu \rightarrow e \gamma$

MSSM+seesaw, dipole diagrams are dominated.

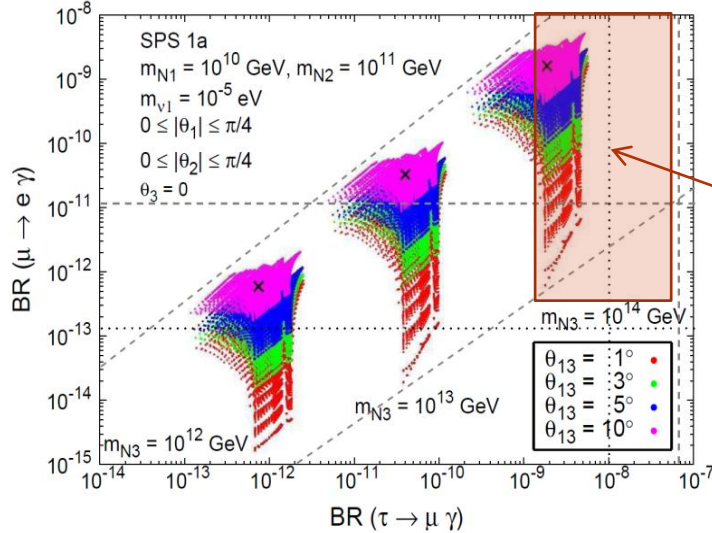


$\tau \rightarrow 3\mu$   $\tau \rightarrow \mu\eta$  Higgs mediated

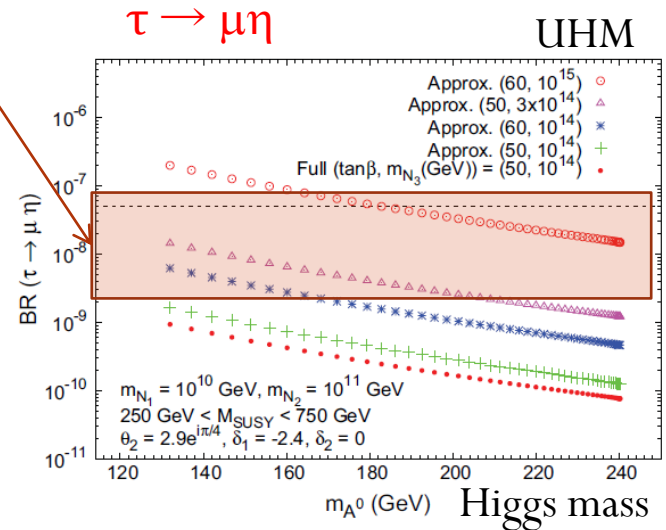
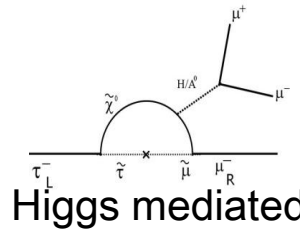
Paradisi., 0602 (2006) 050



Region covered by Belle II experiments



S. Antusch et al., JHEP 11, 090 (2006).



MSSM + seesaw + light Higgs

M. Herrero et al. arxiv:0903.5151

✓ If Higgs mass is light (130- 400 GeV), where Higgs mediated diagrams play an important role. Belle II has a good sensitivity for that scenario.

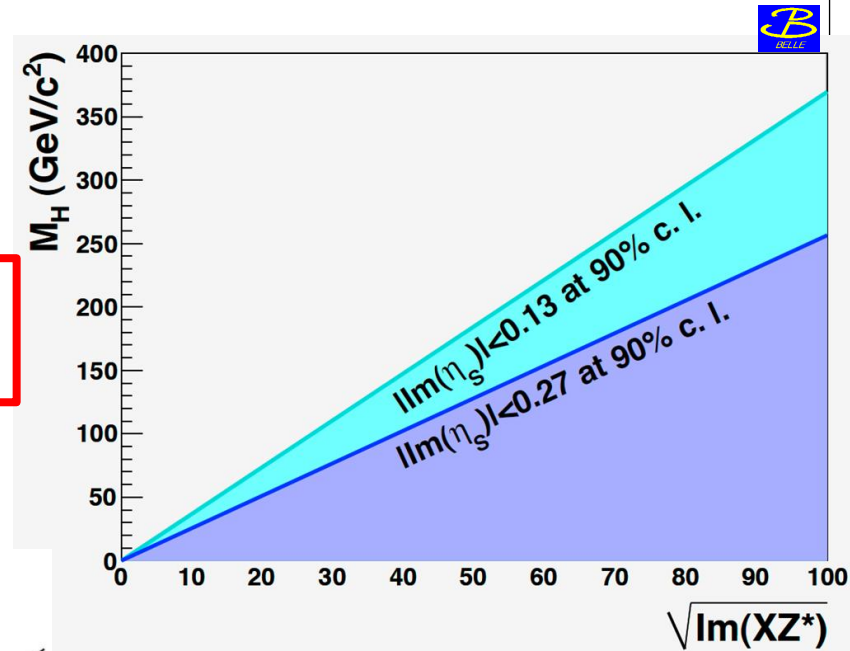
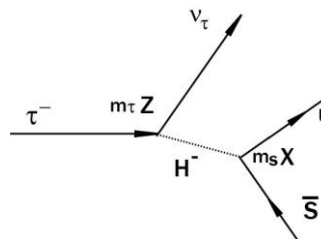
# CP violation in $\tau$ decays



- CP violation in charged leptons is absent in SM but it is possible in some models beyond the SM such as **multi-Higgs-doublet -model (3HDM)**.
- Belle reports the results for search for CPV in  $\tau^- \rightarrow K_S \pi^- \nu_\tau$  with 700 fb<sup>-1</sup> data (M. Bischofberger).
- Obtained U.L. of CP asymmetry is
  - $-0.005 < A_{cp} < 0.008$
  - $|\text{Im}(\eta_S)| < 0.13-0.27$  at 90% C.L.
- Limit for New Physics scenario 3HDM

$$\text{Im}(\eta_S) = -\frac{m_\tau M_N}{M_H^2} \cdot \text{Im}(XZ^*) \quad \text{with} \quad M_N = 1 \text{ GeV}/c^2$$

- ✓  $M_H$ : mass of the lightest charged Higgs
- ✓  $X, Z$ : complex coupling constants:



# Prospect for CPV at Belle II

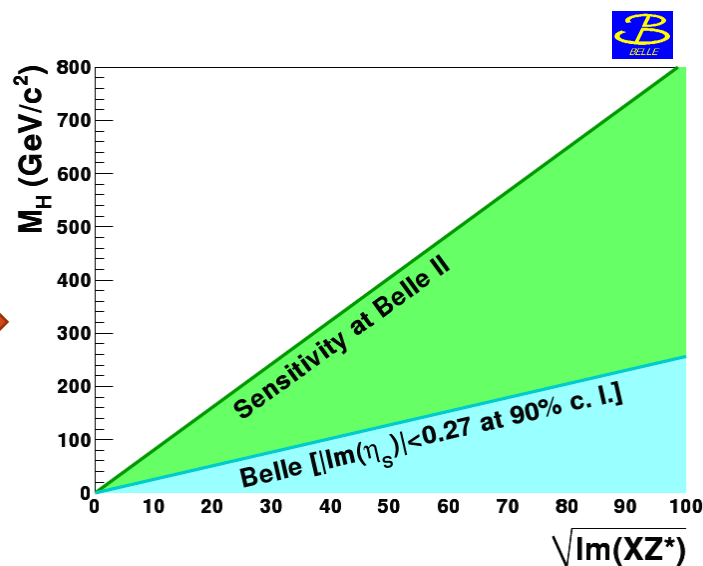
- ✓ Bias from detector charge asymmetry,  $\gamma$ -Z int. effects are small  $O(10^{-3})$ .
- ✓ Systematic is determined by the stat. error of control sample, then it can be improved if statistic is increased.



- 10 times improvement is expected at Belle II ( $50 \text{ ab}^{-1}$ ).

The accessible region for NP searches increases twice.

- Direct extraction of S-wave amplitude using decay angular distribution is needed.
- Interesting possibility for CPV searches in other decay modes  
 $\rho\pi$ .  $K\pi\pi$  ....

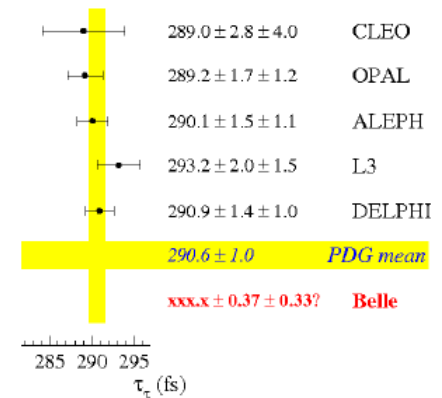


# Lepton Universality

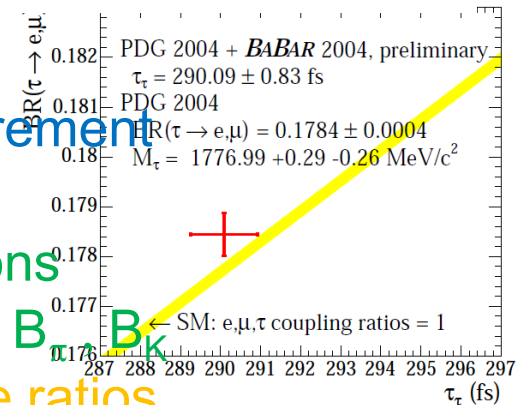


- Precise tests of the Lepton Universality is good place to look for BSM.
- There are various relations between fundamental observables  $m_\tau, \tau_\tau, B_{e\tau}, B_{\mu\tau}, B_{\pi\tau}, B_{K\tau}$

$$\tau_\tau = \tau_\mu \left( \frac{g_\mu}{g_\tau} \right)^2 \left( \frac{m_\mu}{m_\tau} \right)^5 Br(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) \frac{f(m_e^2/m_\mu^2) F_W^\mu F_{rad}^\mu}{f(m_e^2/m_\tau^2) F_W^\tau F_{rad}^\tau}$$



- ✓ Need a precision of 0.1-0.2%
- ✓ Belle measures  $m_\tau$ , and can provide a precise measurement of tau lifetime  $\tau_\tau$ , soon
- ✓ We are planning to measure leptonic branching fractions  $B_{\mu\tau}, B_{e\tau}$  as well as a single hadron branching fractions  $B_{\pi\tau}, B_{K\tau}$
- ✓ A high accuracy measurements will be possible for the ratios  $B_{\mu\tau}/B_{e\tau}, B_{\pi\tau}/B_{e\tau}, B_{K\tau}/B_{e\tau}$ .



# Hadronic Decays

- Inclusive measurements

$$\alpha_s, V_{us}, m_s, \langle qq \rangle ..$$

- Exclusive Measurements

Br, mass spectrum, Spectral Function,  
Form Factors

To get Inclusive quantities, we need  
many exclusive measurements.

2010/9/17



# Cabibbo suppressed decays



- ▣ Cabibbo suppressed (strange)  $\tau$  decays are important for the determination of  $V_{us}$ ,  $m_s$  plus non-p-QCD parameters at low- $Q^2$
- ▣ Status of  $V_{us}$  is nicely summarized by Sobie/Swagato
- ▣ There is a systematic difference between the one determined by Kaon decays and one using  $\tau$  inclusive decays.
- ▣  $V_{us}$  determination using Inclusive  $\tau$  strange decays is the cleanest theoretically.



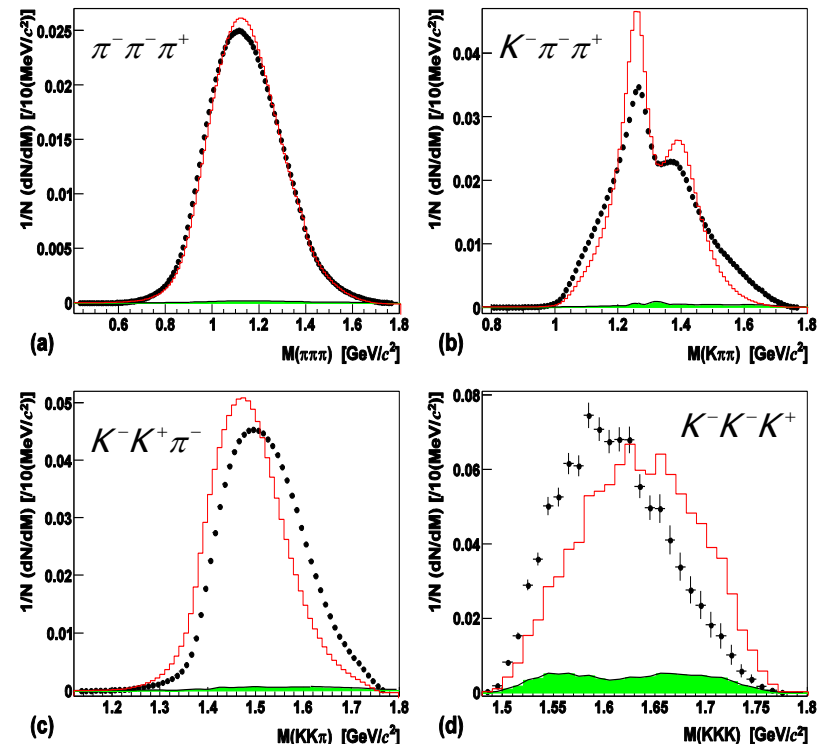
✓ -We will need measurements of **Br** of all strange decays also need **Spectral Functions** for theoretical consistency check. (Maltman Tau08).

Recently, Belle provides precise unfolded mass spectrum for 2 strange decay modes;  $\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau$ ,  $K^- K^+ K^- \nu_\tau$  and 2 non-strange decays  $\pi^- \pi^+ \pi^- \nu_\tau$ ,  $K^- K^+ \pi^- \nu_\tau$

• Green band is the systematic errors, including dependence of the resonance model for efficiency determination. Red histogram TAUOLA

• The mass spectrum with Kaon does not agree with TAUOLA.

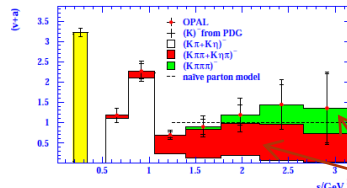
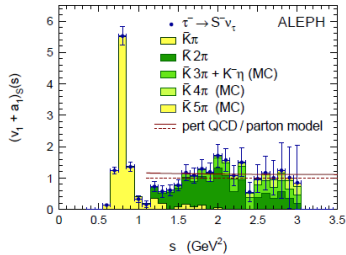
Published in PRD 81, 113007 (2010)



# Strange spectral function








■ Should be compared with the previous LEP exp.

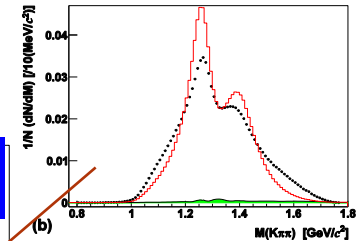
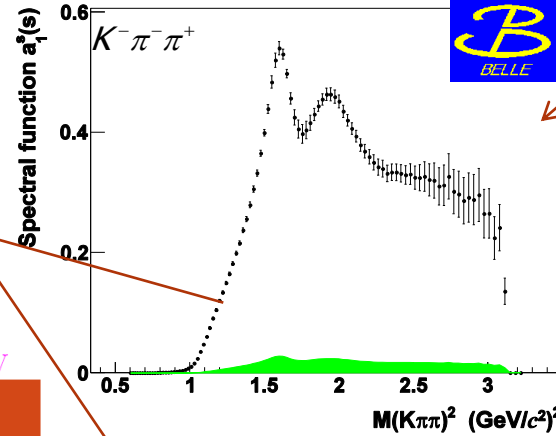
Strange spectral function



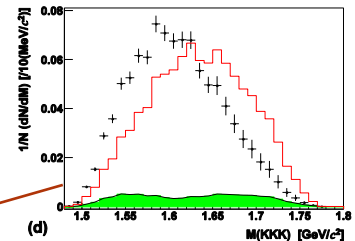
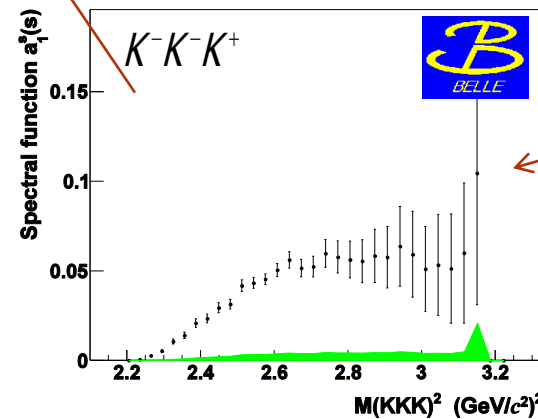
ALEPH:  $|V_{us}| = 0.2204 \pm 0.0028_{\text{exp}} \pm 0.0003_{\text{th}} \pm 0.0001_{m_s}$

J.Prades from OPAL data:  $|V_{us}| = 0.2219 \pm 0.0034$ ,  $m_s = (81 \pm 20)$  MeV

mode	Br	Spectral func.
K		-
Kπ	 	 (no. e-matrix)
Kππ	 	
Kπππ+Kη	 (Kη)	
K4π		
KKK	 	



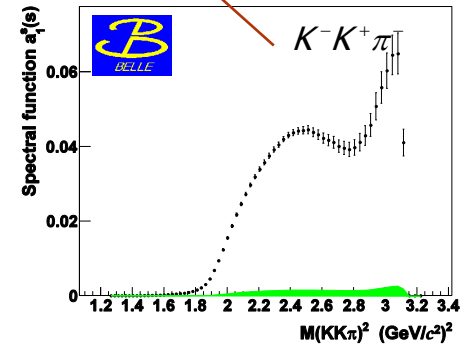
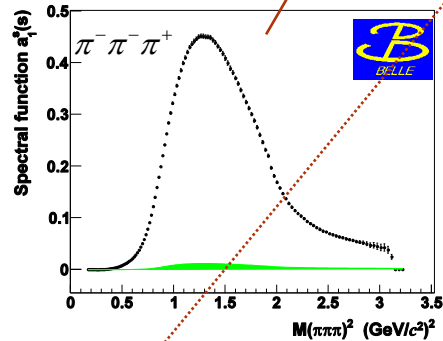
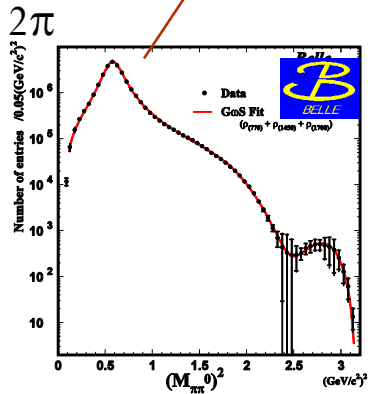
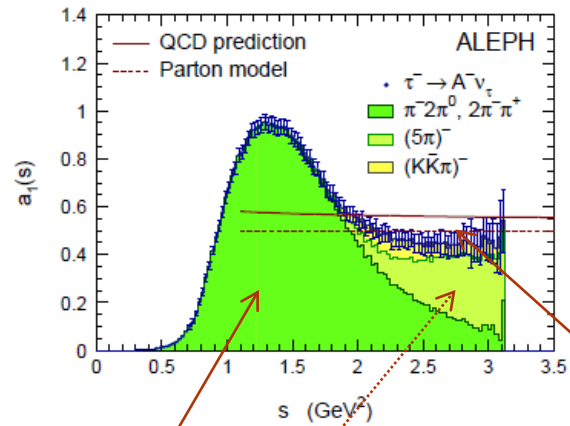
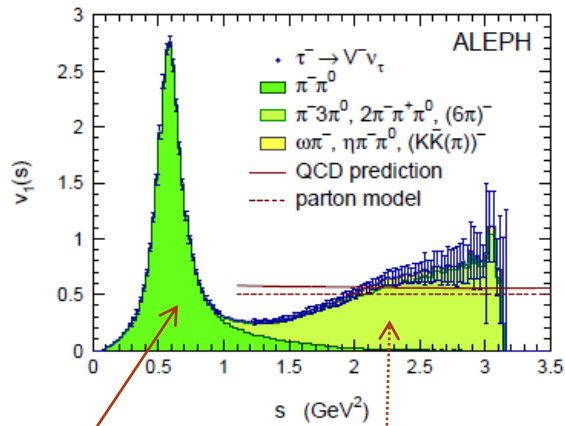
PRD 81, 113007 (2010).



We can provide mass spectrums and their error matrix. Please contact us if it is needed.

Needed to measure missing parts.

# Belle also contribution for Non-strange spectral functions



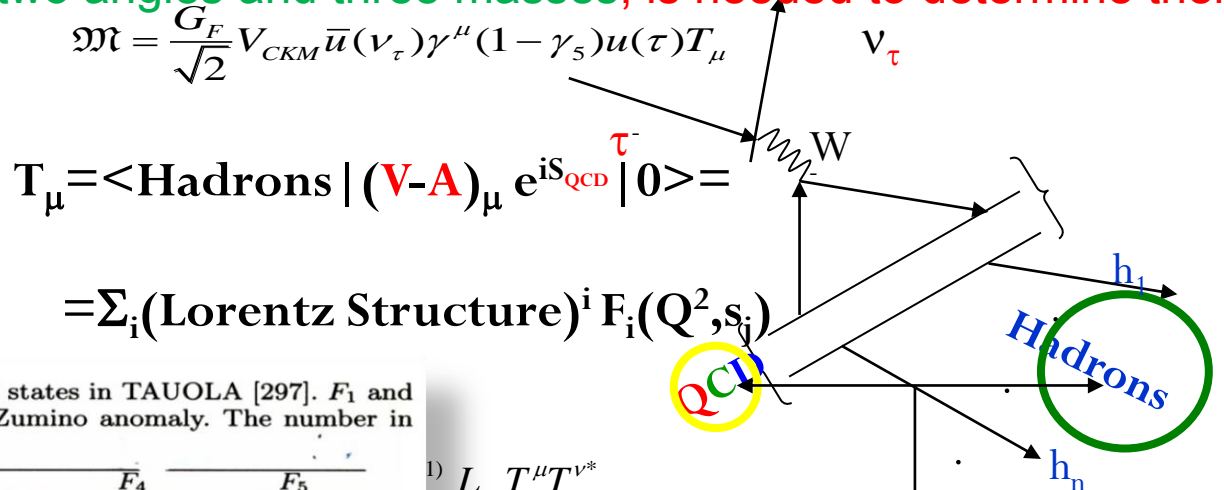
Missing are  $\tau \rightarrow 4\pi\nu, \omega\pi\nu, 5\pi\nu, \eta\pi\nu$  .....

High static data are important at high mass region, where p-QCD plays an important role.

# Prospect for Form Factor Measurements

- ✓ Form Factors include all information of hadron system.
- ✓ Multi-dimensional analysis, two angles and three masses, is needed to determine them.

✓ Determination of FF is one of the ultimate goal of B factory experiments.



$$\mathfrak{M} = \frac{G_F}{\sqrt{2}} V_{CKM} \bar{u}(v_\tau) \gamma^\mu (1 - \gamma_5) u(\tau) T_\mu$$

$$T_\mu = \langle \text{Hadrons} | (\mathbf{V}-\mathbf{A})_\mu e^{iS_{\text{QCD}}} | 0 \rangle =$$

$$= \sum_i (\text{Lorentz Structure})^i F_i(Q^2, s_j)$$

**Table 2.6.** Form factors of the three-meson final states in TAUOLA [297].  $F_1$  and  $F_2$  axial-vector,  $F_4$  pseudoscalar, and  $F_5$  Wess-Zumino anomaly. The number in the left column is the internal ID of the channel

Mode	$F_1$	$F_2$	$F_4$	$F_5$
5 $\tau \rightarrow 3 \pi \nu_\tau$	$a_1 \rightarrow \rho \pi$ $\rho \rightarrow \pi \pi$	$a_1 \rightarrow \pi \rho$ $\rho \rightarrow \pi \pi$	$\pi'(\text{1300})$ optional	-
14 $\tau \rightarrow K^+ K^- \pi^\pm \nu_\tau$	$a_1 \rightarrow K^* K$ $K^* \rightarrow K \pi$	$a_1 \rightarrow \pi \rho$ $\rho \rightarrow K K$	-	$\rho \rightarrow K^* K$ $K^* \rightarrow K \pi$
15 $\tau \rightarrow K^0 K^0 \pi^\pm \nu_\tau$	$a_1 \rightarrow K^* K$ $K^* \rightarrow K \pi$	$a_1 \rightarrow \pi \rho$ $\rho \rightarrow K K$	-	$\rho \rightarrow K^* K$ $K^* \rightarrow K \pi$
16 $\tau \rightarrow K^\pm K^0 \pi^0 \nu_\tau$	-	$a_1 \rightarrow \pi \rho$ $\rho \rightarrow K K$	-	-
17 $\tau \rightarrow K^\pm \pi^0 \pi^0 \nu_\tau$	$K_1 \rightarrow K^* \pi$ $K^* \rightarrow K \pi$	$K_1 \rightarrow \pi K^*$ $K^* \rightarrow K \pi$	-	-
18 $\tau \rightarrow K^\pm \pi^+ \pi^- \nu_\tau$	$K_1 \rightarrow K \rho$ $\rho \rightarrow \pi \pi$	$K_1 \rightarrow \pi K^*$ $K^* \rightarrow K \pi$	-	$K^* \rightarrow \rho K$ $\rho \rightarrow \pi \pi$
19 $\tau \rightarrow K^0 \pi^\pm \pi^0 \nu_\tau$	-	$K_1 \rightarrow K \rho$ $\rho \rightarrow \pi \pi$	-	$K^* \rightarrow \rho K$ $\rho \rightarrow \pi \pi$
20 $\tau \rightarrow \eta \pi^\pm \pi^0 \nu_\tau$	-	-	-	$\rho \rightarrow \rho \eta$ $\rho \rightarrow \pi \pi$

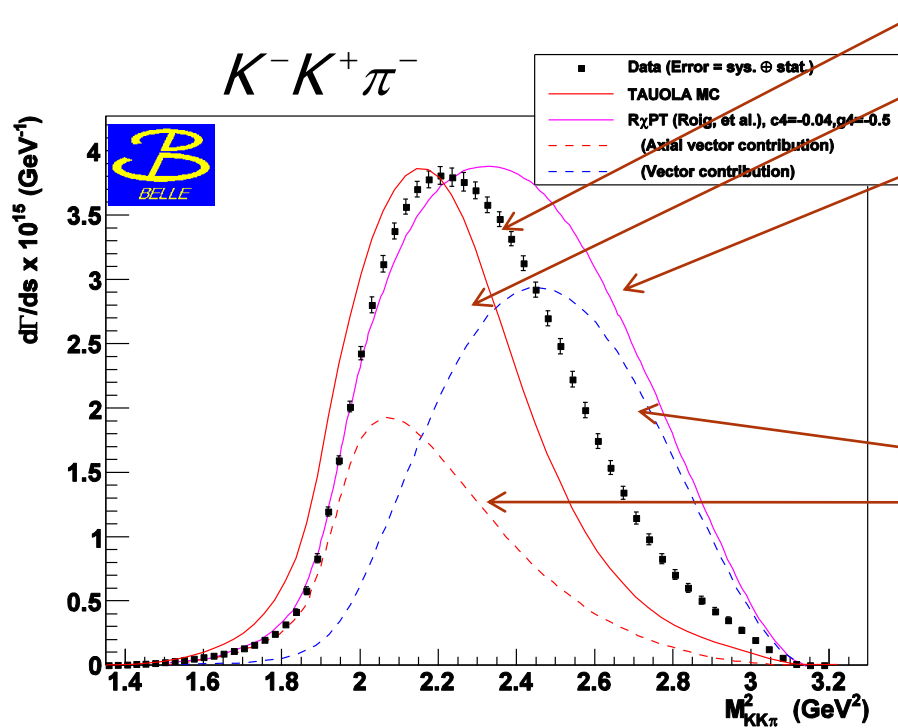
$$1) L_{\mu\nu} T^{\mu} T^{\nu*}$$

P. Roig at Tau08

Scalar and Vector parts are poorly known.

# A comparison with $R_{\chi T}$ prediction

Exclusive hadron spectrum is useful for a test of theoretical models in resonance region.



Plots: Belle unfolded spectrum

Red line : TAUOLA MC

Purple line: A prediction based on  $\chi RT$  by G. Dumm, Pich, Portoles, P. Roig (Tau08)

No good agreement indicates need for further tuning /study of the Theory

Vector

Axial Vector

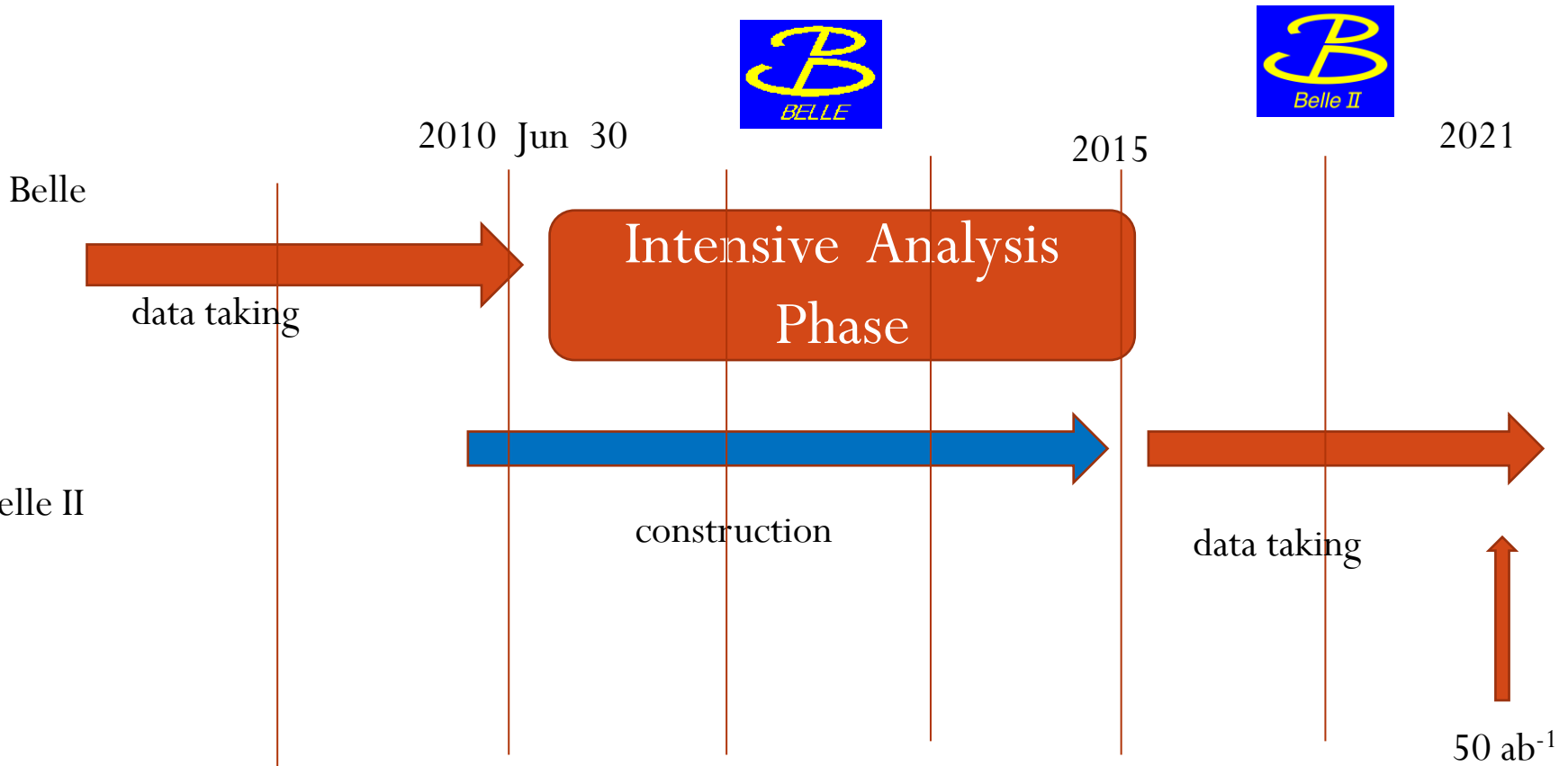
In order separate Axial Vector and Vector (Wess-Zumino) terms, need to analyze decay angle distribution.

PRD 81 ,113007 (2010).

# Summary

- Huge  $\tau$  data ( $1\text{ab}^{-1}$ ) from both B-factory experiments are great source of the information of SM and Beyond SM physics.
- Many physics items still not explored yet.
- Yet, additional 50-100 times data are expected in the BelleII/SuperB exp. in the next decades.
  - ✓ Probe  $\tau$  LFV to  $O(10^{-9})$ - $O(10^{-10})$
  - ✓ Probe  $\tau$  CPV to  $O(10^{-4})$  w/o beam polarization.
  - ✓ More sensitive check on Lepton universality,  $(g-2)_\tau$  □
  - ✓ Improved understanding of Hadrons. Bernabeu, arxiv: 0707.2496
    - Through measurements of Br, Spectral Functions and Form Factors for various  $\tau$  decay modes.

# Analysis Plan: Belle and Belle II



We still have many things can/should be done using Belle data, and have a great future at Belle II.

**Stay tuned.**

2010/9/17

# Backup Slide

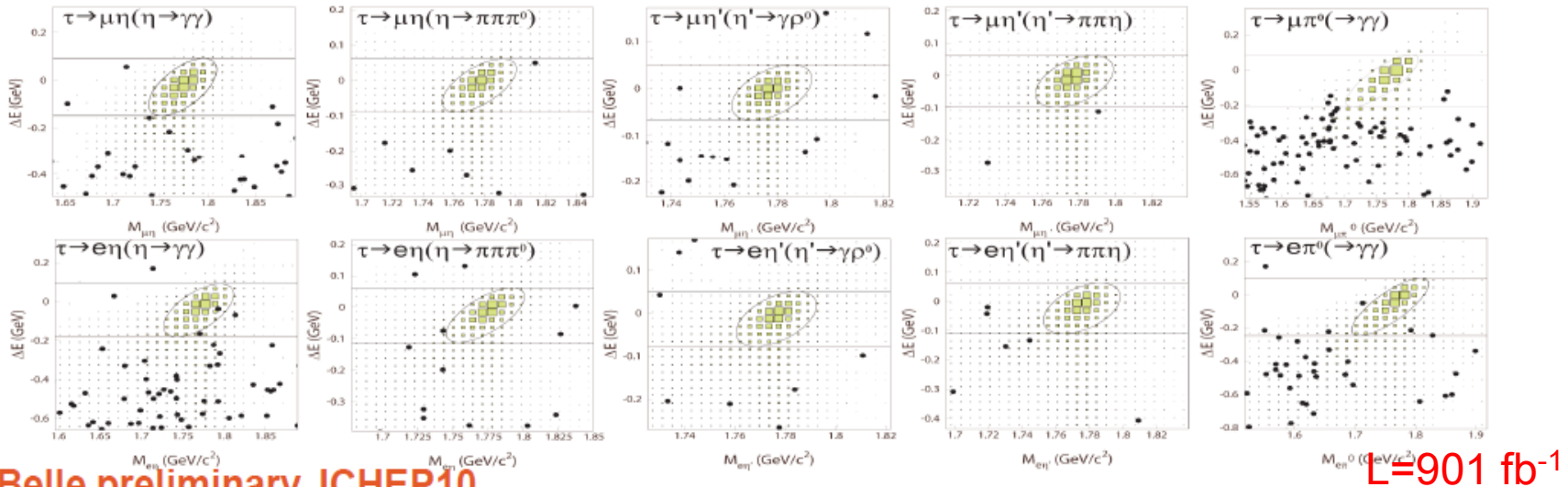
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Backup



# Search for decays

$$\tau^- \rightarrow l^- P^0 (\pi^0, \eta, \eta')$$



Belle preliminary, ICHEP10

$\tau \rightarrow$	Eff.	$N_{BG}^{exp}$	UL( $\times 10^{-8}$ )	$\tau \rightarrow$	Eff.	$N_{BG}^{exp}$	UL( $\times 10^{-8}$ )
$\mu\eta(\rightarrow\gamma\gamma)$	8.2%	$0.63 \pm 0.37$	3.6	$\mu\eta'(\rightarrow\pi\pi\eta)$	8.1%	$0.00 + 0.16 - 0.00$	10.0
$\mu\eta(\rightarrow\pi\pi\pi^0)$	6.9%	$0.23 \pm 0.23$	8.6	$\mu\eta'(\rightarrow\rho^0\gamma)$	6.2%	$0.59 \pm 0.41$	6.6
$\mu\eta(\text{comb.})$			<b>2.3</b>	$\mu\eta'(\text{comb.})$			<b>3.8</b>
$e\eta(\rightarrow\gamma\gamma)$	7.0%	$0.66 \pm 0.38$	8.2	$e\eta'(\rightarrow\pi\pi\eta)$	7.3%	$0.63 \pm 0.45$	9.4
$e\eta(\rightarrow\pi\pi\pi^0)$	6.3%	$0.69 \pm 0.40$	8.1	$e\eta'(\rightarrow\rho^0\gamma)$	7.5%	$0.29 \pm 0.29$	6.8
$e\eta(\text{comb.})$			<b>4.4</b>	$e\eta'(\text{comb.})$			<b>3.6</b>
$\mu\pi^0(\rightarrow\gamma\gamma)$	4.2%	$0.64 \pm 0.32$	<b>2.7</b>	$e\pi^0(\rightarrow\gamma\gamma)$	4.7%	$0.89 \pm 0.40$	<b>2.2</b>

- ✓ Current muon anomalous magnetic moment shows 3  $\sigma$  difference between data and theory,

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} \approx (3 \pm 1) \times 10^{-9}$$

- ✓ Natural scaling of the NP effects on the lepton magnetic dipole moments is

$$\frac{\Delta a_\tau}{\Delta a_\mu} \propto \frac{m_\tau^2}{m_\mu^2} = 290$$

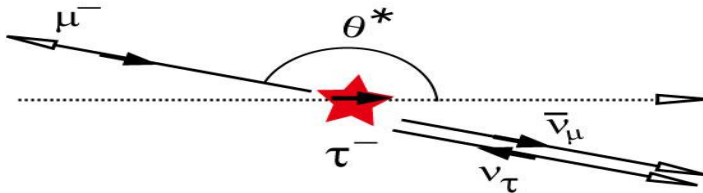
- ✓ If we interpret the present muon discrepancy as NP effects, we expect  $\Delta a_\tau \approx 10^{-6}$   
In the special SUSY scenario even  $\Delta a_\tau \approx 10^{-5}$  is expected.
- ✓ At Belle II/Super B, we will be able to measure in the similar level of accuracy,  
Bernabeu, arxiv: 0707.2496

Need to study.

- reliability of measurement with or w/o beam pol.
- how to know the tau direction.
- How beam pol. is useful ?

# Background suppression using $\tau$ spin

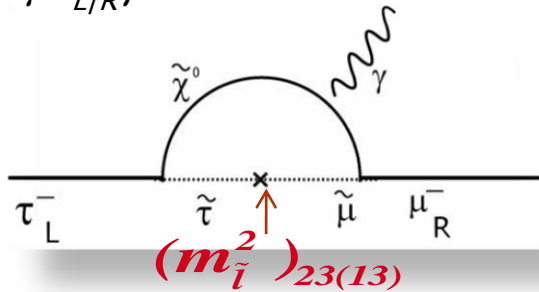
$$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$$



✓ Since muon is mostly left handed, the direction of muon is preferentially against the  $\tau$  spin

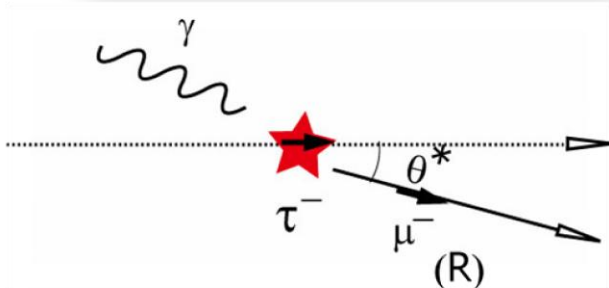
$$\frac{d\Gamma}{dx^* d\cos\theta^*} \propto x^{*2} \left[ \left( \frac{1}{2} - \frac{1}{3} x^* \right) + h_\tau \cos\theta^* \left( \frac{1}{6} - \frac{1}{3} x^* \right) \right], x^* = \frac{E_\mu^*}{E_\mu^{\max}}$$

$$\tau^-_{R/L} \rightarrow \mu^-_{L/R} \gamma$$



✓ Chi rarity is changed (L $\rightarrow$ R, R $\rightarrow$ L) in the  $\tau^- \rightarrow \mu^- \gamma$  decay.

✓ Photon polarization is perpendicular to the photon direction.

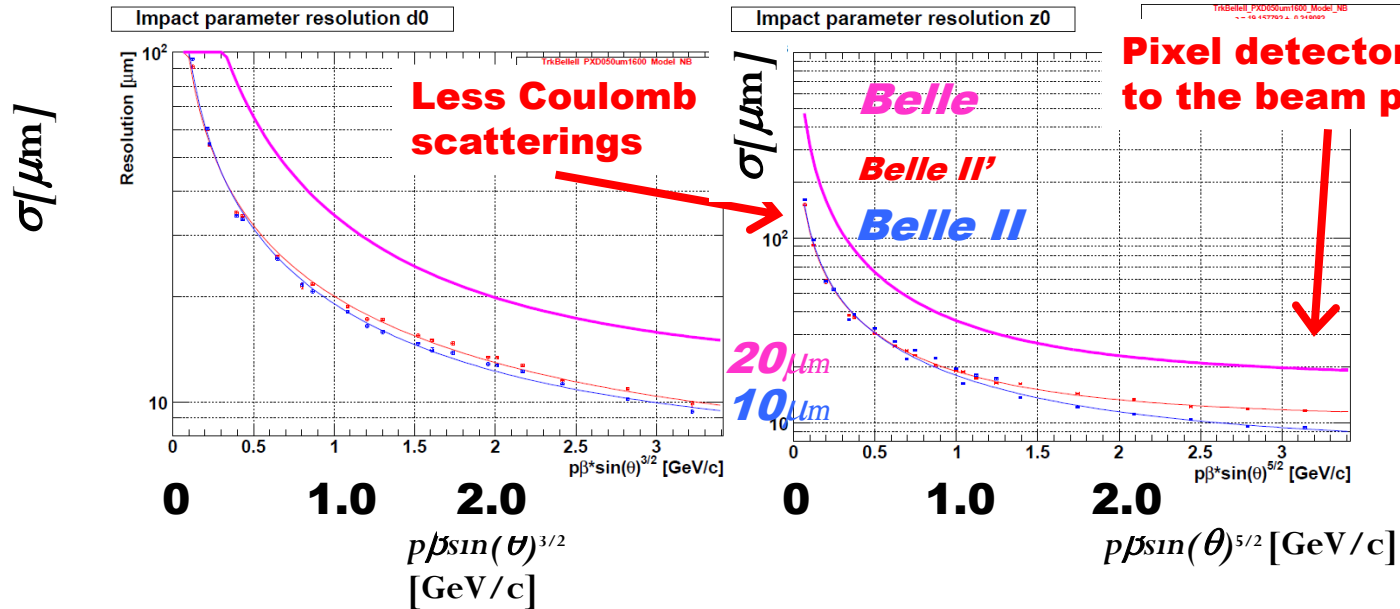


✓ The direction of muon is preferentially parallel to the  $\tau$  spin

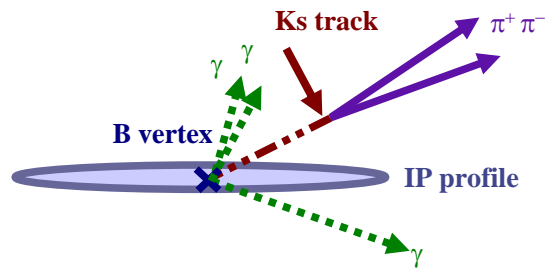
# Expected performance

$$\sigma = a + \frac{b}{p\beta \sin^v \theta}$$

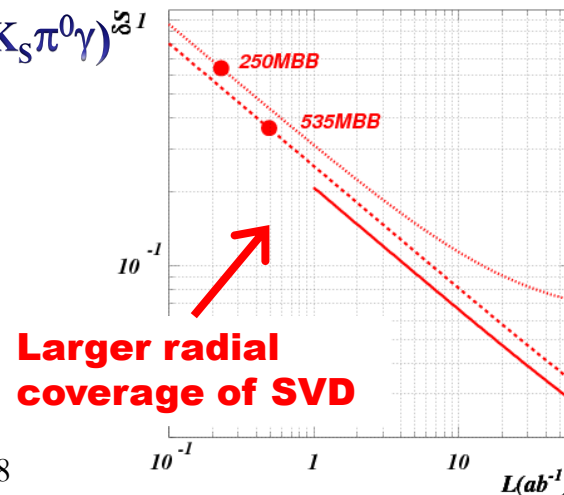
Significant improvement in IP resolution!



Significant improvement in  $\delta S(K_S \pi^0 \gamma)^{\text{SVD}}$

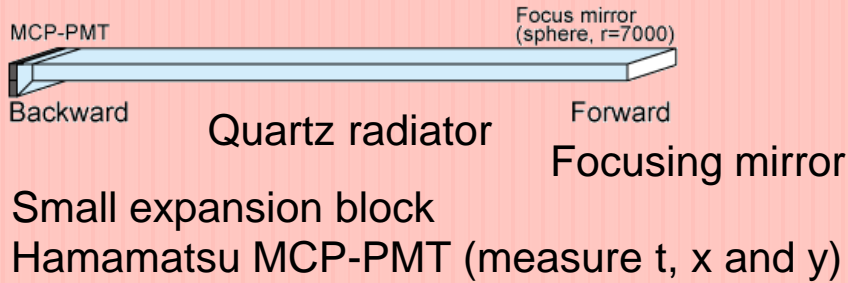


B decay point reconstruction with  $K_S$  trajectory

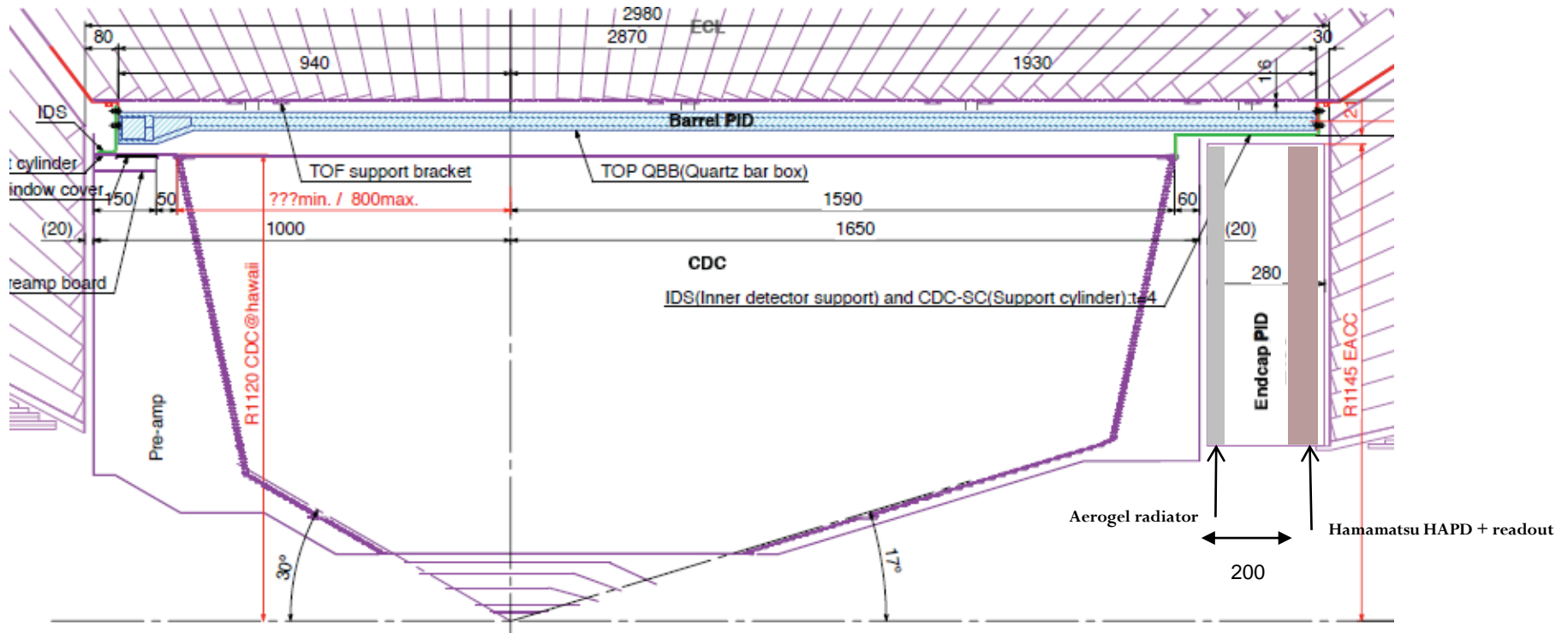
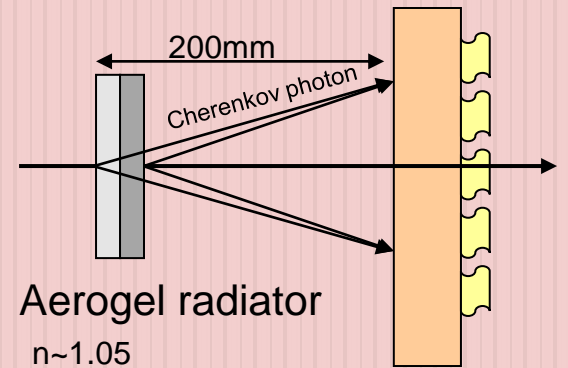


# Particle Identification Devices

Barrel PID: Time of Propagation Counter (TOP)



End cap PID: Aerogel RICH (ARICH)



# CP violation in $\tau$ decays.



- CP violation in charged leptons are absent in SM but it is possible some models beyond the SM such as **multi-Higgs-doublet -model (3HDM)**.
- Belle reports the results for search for CPV in  $\tau^- \rightarrow K_S \pi^- \nu_\tau$  with 700 fb<sup>-1</sup> data (M. Bischofberger).

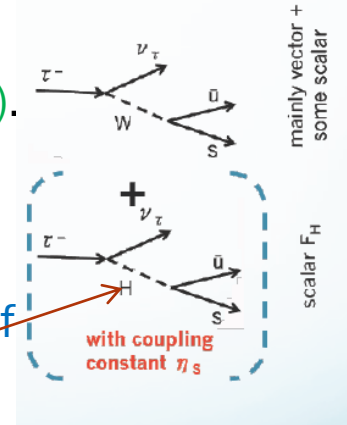
To see CPV effects, they use “modified” CP asymmetry parameter  $A_{cp}$  def

$$A_{cp} \equiv \frac{1}{\Gamma'} \int \cos \beta \cos \psi \left[ \frac{d\Gamma(\tau^-)}{dQ^2 d \cos \beta \cos \psi} - \frac{d\Gamma(\tau^+)}{dQ^2 d \cos \beta \cos \psi} \right] dQ^2 d \cos \beta d \cos \theta$$

$$\propto \text{Im}(FF_s^*) \text{Im}(\eta_s)$$

$$\Gamma' \equiv \int \frac{d\Gamma(\tau^-)}{dQ^2 d \cos \beta \cos \psi} dQ^2 d \cos \beta d \cos \theta$$

$\eta_s$

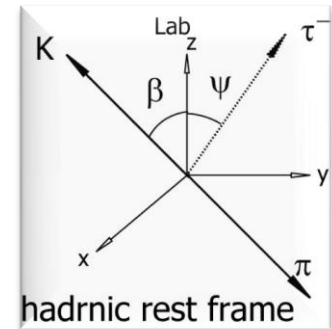


Note:

✓ The CP asymmetry is measured with angular weights. This  $A_{cp}$  has a similar sensitivity with an optimum observable used by CLEO but does not depend on the S-wave amplitude which is not well known.

✓ The observable  $A_{cp}$  is proportional to  $\text{Im}(FF_s) \text{Im}(\eta_s)$ , where F is dominant P-wave,  $F_s$  is the S-wave amp. And  $\eta_s$  is a CP violating coupling constant in NP model.

✓ Our definition of  $\eta_s$  is the same as the one defined in the original paper, J.H. Kuhn and E. Mirkes, Phys. Lett. B398 (1997) 407-414 but with different scale.



$$\left( \frac{\eta_s}{m_N} \right)_{ours} = \left( \frac{\eta_s}{m_d - m_s} \right)_{Kuhn}$$

2010/9/17