

Neutrino Oscillations Overview

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OUTLINE

1. Neutrino Masses and Mixing
2. Leptogenesis: Matter-Antimatter Asymmetry
3. Leptonic CP Violation
 - i) F.O.M. Insensitivity to θ_{13} & L (Osc. Length)
 - ii) Requirements ~300kton H₂O, 1-2MW protons,
Neutrino Wide Band Beam (WBB) $E_\nu \approx 0.5-5\text{GeV}$
4. “New Physics” search via ν_μ & $\bar{\nu}_\mu$ disappearance
5. Outlook

1. Neutrino Masses and Mixing

- 1969-90s Ray Davis Measures Solar ν_e Flux at Homestake Deep Underground Mine $\sim 1/3$ Expected!
Gallex, Sage, SuperK, SNO, Kamland (Reactor)
Interpretation: solar $\nu_e \rightarrow 1/3 \nu_e + 1/3 \nu_\mu + 1/3 \nu_\tau$ (roughly)
- 1980s IMB, Kamioka, measure atm. ν_μ flux, less than expected (Also observe supernova 1987a neutrinos!)
SuperK; K2K, MINOS (Accelerators)
Interpretation: atm. $\nu_\mu \rightarrow 1/2 \nu_\mu + 1/2 \nu_\tau$ (near maximal!)

Neutrino Oscillations Established \rightarrow Neutrino Masses & Mixing Measured (Great Progress!)

3 Generation Mixing Formalism & Status)

$$\begin{pmatrix} |\nu_e\rangle \\ |\nu_\mu\rangle \\ |\nu_\tau\rangle \end{pmatrix} = U \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix} \quad (1)$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$$c_{ij} = \cos \theta_{ij} \quad , \quad s_{ij} = \sin \theta_{ij}$$

$$J_{CP} \equiv \frac{1}{8} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \cos \theta_{13} \sin \delta. \quad (2)$$

Current Neutrino Mass & Mixing Parameters

- $\Delta m_{32}^2 = m_3^2 - m_2^2 = \pm 2.4(1) \times 10^{-3} \text{ eV}^2$ (atmospheric)
- $\Delta m_{21}^2 = m_2^2 - m_1^2 = +7.6(2) \times 10^{-5} \text{ eV}^2$ (solar)

(Very precise Minos & KamLAND Measurements)

$|\Delta m_{21}^2 / \Delta m_{32}^2 \approx 1/30| \rightarrow \text{CP Violation Exp Doable!}$

Hierarchy $m_3 > m_1 \& m_2$ (normal) or $m_3 < m_1 \& m_2$ (inverted)?

Large Mixing!

$$\theta_{23} \sim 45^\circ \quad \sin^2 2\theta_{23} = 1.0 \quad (\theta_{23} \text{ or } 90^\circ - \theta_{23}) \quad (\text{atm.})$$

$$\theta_{12} \sim 34^\circ \quad \sin^2 2\theta_{12} = 0.87(3) \quad (\text{solar})$$

$$\theta_{13} \leq 11^\circ \quad \sin^2 2\theta_{13} \leq 0.15 \quad (\text{How Small?})$$

$$0 \leq \delta \leq 360^\circ ?$$

$$J_{\text{CP}} \approx 0.11 \sin 2\theta_{13} \sin \delta \quad (\text{potentially large!})$$

What do we still need to learn?

- 1. **Value of θ_{13} ?** (Reactors: $\sin^2 2\theta_{13} \rightarrow 0.01$)
(Long Baseline $\nu_{\mu} \rightarrow \nu_e$ similar)
- 2. **Sgn Δm_{32}^2 ?** (Important for Neutrinoless $\beta\beta$ Decay)
- 3. **Value of δ ?, J_{CP} ?, CP Violation? (*Holy Grail*)**
- 4. **Precision Δm_{32}^2 , Δm_{21}^2 , θ_{23} , θ_{12}** (better than 1%!)
- 5. **“New Physics”** - Sterile ν , **Very Weak** Long Distance Physics (*The Dark World*)...

2. Leptogenesis: Matter-Antimatter Asymmetry

- More baryons than antibaryons in our Universe
- Leptogenesis Scenario:
 1. Heavy Majorana Neutrinos Created and Decay
 $N \rightarrow H^- e^+, H^0 \bar{\nu}$ (**L & CP VIOLATION**)
Leads to antilepton (excess)-lepton Asymmetry
 2. Electroweak Phase Transition (250GeV) (Baryogenesis)
't Hooft Mechanism **B-L Conserved (B&L Violated)**
antilepton excess \rightarrow baryon (quark) excess by 1 in 10^9

Is L Violated in Nature? (Neutrinoless $\beta\beta$ Decay)

Is there Leptonic CP Violation? (ν oscillations)

Indirect evidence for Leptogenesis (Best we can do.)

3. Leptonic CP Violation

$$P(\nu_\mu \rightarrow \nu_e) = P_I(\nu_\mu \rightarrow \nu_e) + P_{II}(\nu_\mu \rightarrow \nu_e) + P_{III}(\nu_\mu \rightarrow \nu_e) \\ + \text{matter} + \text{smaller terms}$$

$$\mathbf{P}_I(\nu_\mu \rightarrow \nu_e) = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E_\nu} \right)$$

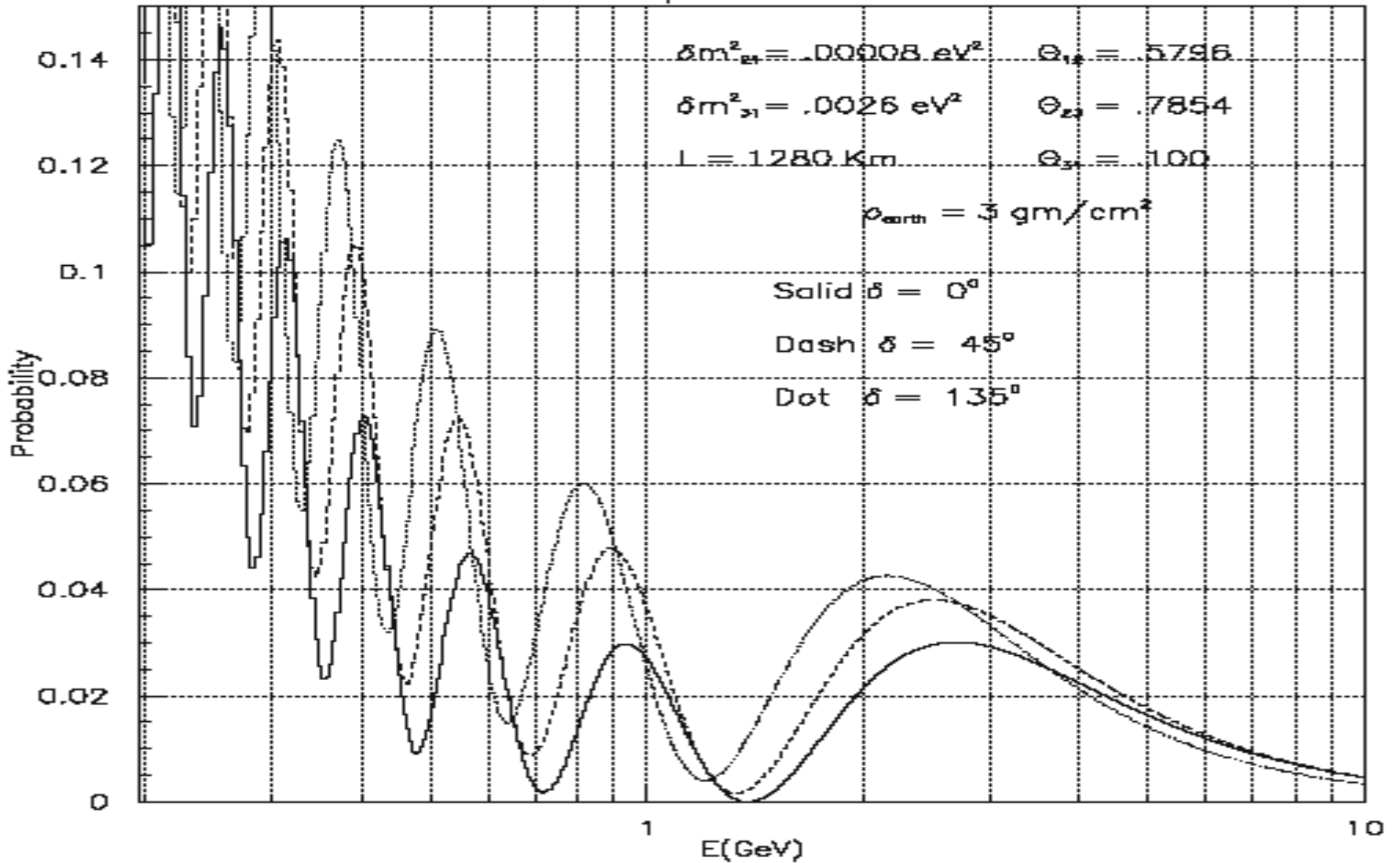
$$\mathbf{P}_{II}(\nu_\mu \rightarrow \nu_e) = \frac{1}{2} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \cos \theta_{13} \\ \sin \left(\frac{\Delta m_{21}^2 L}{2E_\nu} \right) \times \left[\sin \delta \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E_\nu} \right) \right. \\ \left. + \cos \delta \sin \left(\frac{\Delta m_{31}^2 L}{4E_\nu} \right) \cos \left(\frac{\Delta m_{31}^2 L}{4E_\nu} \right) \right]$$

$$\mathbf{P}_{III}(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta_{12} \cos^2 \theta_{13} \cos^2 \theta_{23} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E_\nu} \right)$$

For antineutrinos, $\delta \rightarrow -\delta$ and opposite matter effect.

FNAL

$$\nu_\mu \rightarrow \nu_\tau$$



CP Violation Asymmetry

$$A_{CP} \equiv \frac{P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}{P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \quad (3)$$

To leading order in Δm_{21}^2 ($\sin^2 2\theta_{13}$ is not too small):

$$A_{CP} \simeq \frac{\cos \theta_{23} \sin 2\theta_{12} \sin \delta}{\sin \theta_{23} \sin \theta_{13}} \left(\frac{\Delta m_{21}^2 L}{4E_\nu} \right) + \text{matter effects} \quad (4)$$

$$F.O.M. = \left(\frac{\delta A_{CP}}{A_{CP}} \right)^{-2} = \frac{A_{CP}^2 N}{1 - A_{CP}^2} \quad (5)$$

N is the total number of $\nu_\mu \rightarrow \nu_e + \bar{\nu}_\mu \rightarrow \bar{\nu}_e$ events. Since N falls (roughly) as $\sin^2 \theta_{13}$ and $A_{CP}^2 \sim 1/\sin^2 \theta_{13}$, to a first approximation the F.O.M. is independent of $\sin \theta_{13}$. Similarly, given E_ν the neutrino flux and consequently N falls as $1/L^2$ but that is canceled by L^2 in A_{CP}^2 .

i) CP Violation Insensitivities

- To a very good approx., our statistical ability to determine δ or A_{cp} is independent of $\sin^2 2\theta_{13}$ (down to ~ 0.003) and the detector distance L (for long distance).

ii) CP Violation Requirements

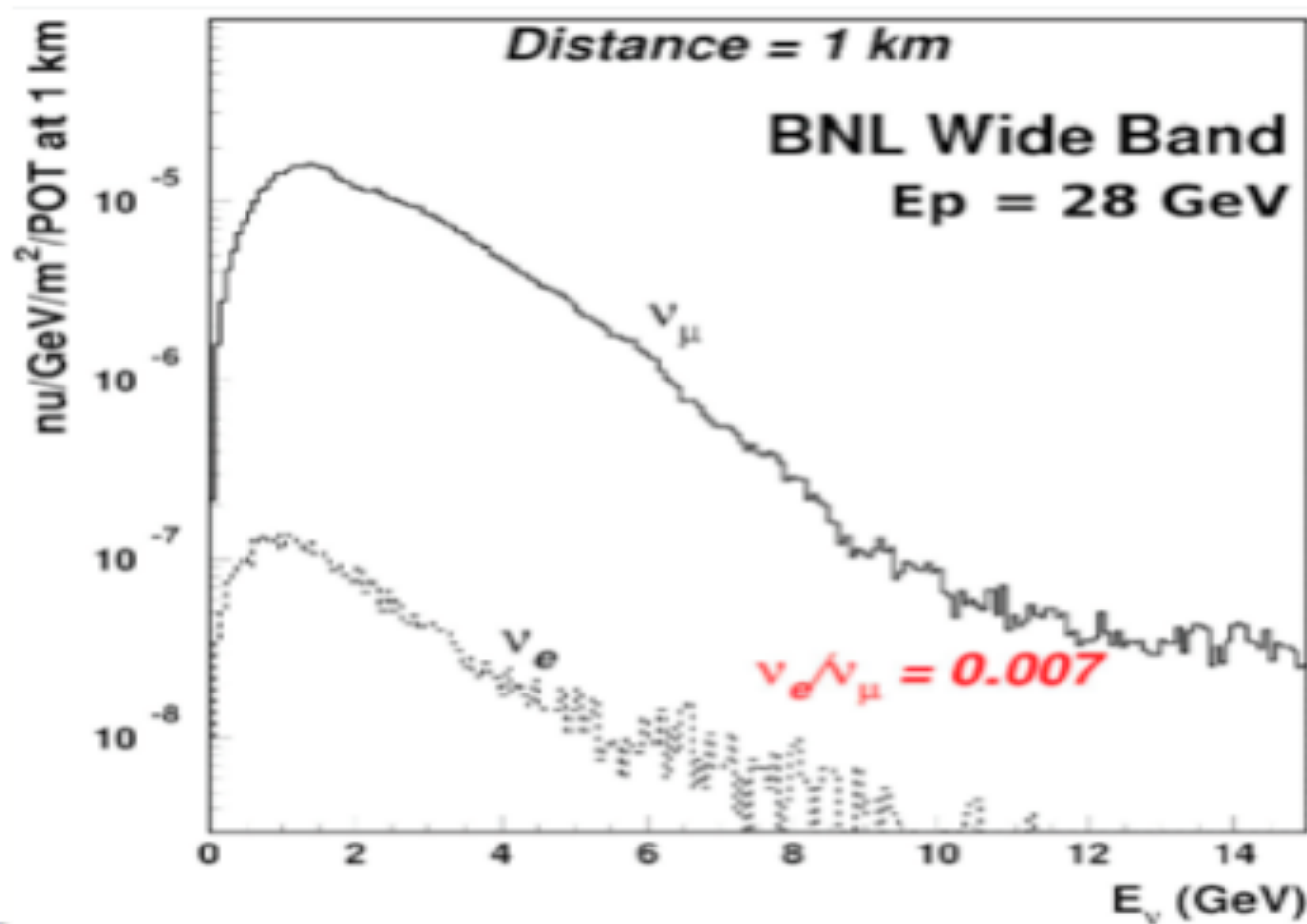
- Pick any reasonable θ_{13} (eg $\sin^2 2\theta_{13}=0.04$)
- What does it take to measure δ to $\pm 15^\circ$ in about 5×10^7 sec?

Answer (Approx.): [300kton Water Cerenkov Detector](#)

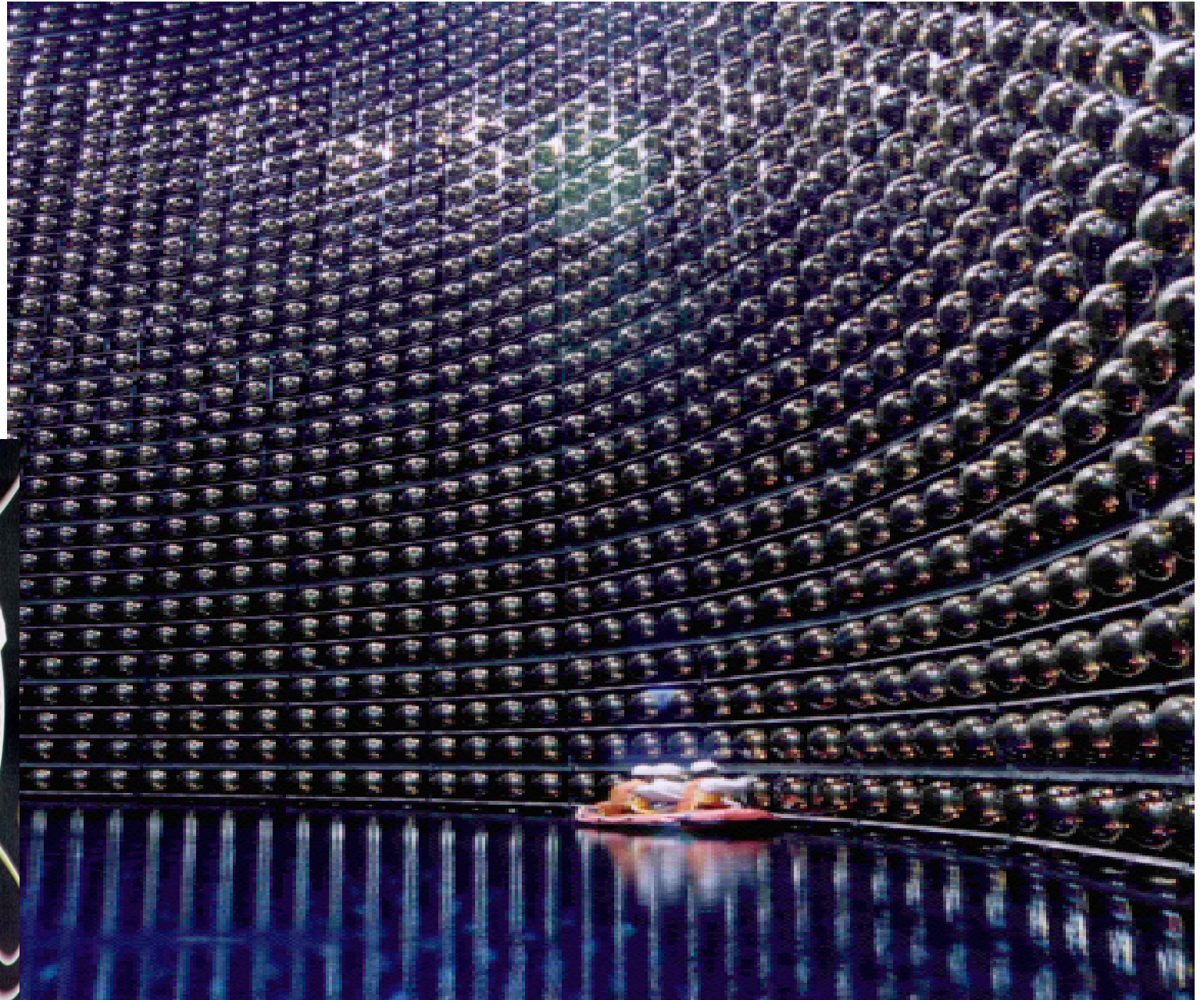
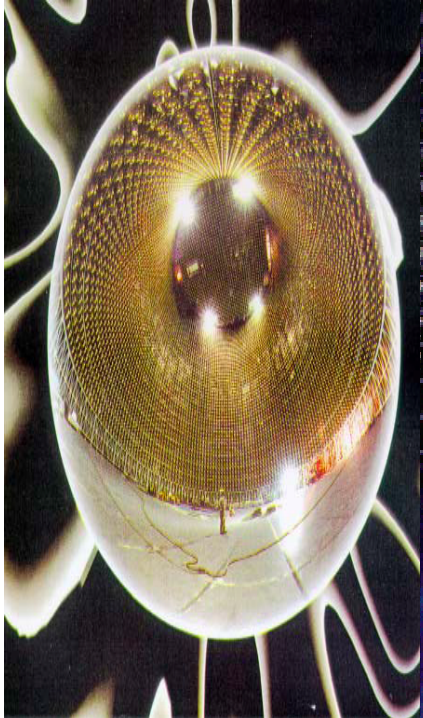
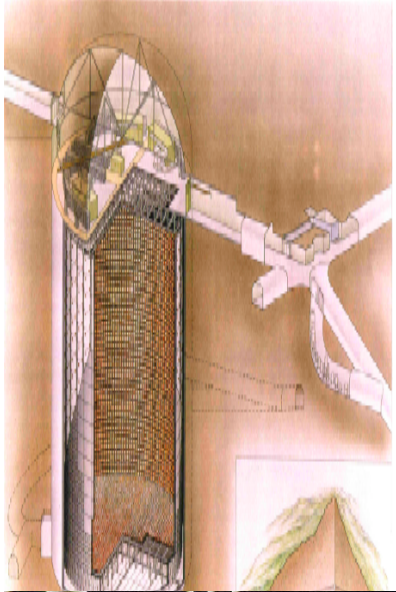
Approx 20% Acceptance,
50 kton LArgon 90% Acceptance
or Hybrid combination

+ [Traditional Horn Focused \$\nu\$ WBB](#) powered by
[1-2MW proton accelerator](#) (egs. Project X at FNAL)

Horn Focused Neutrino Beam



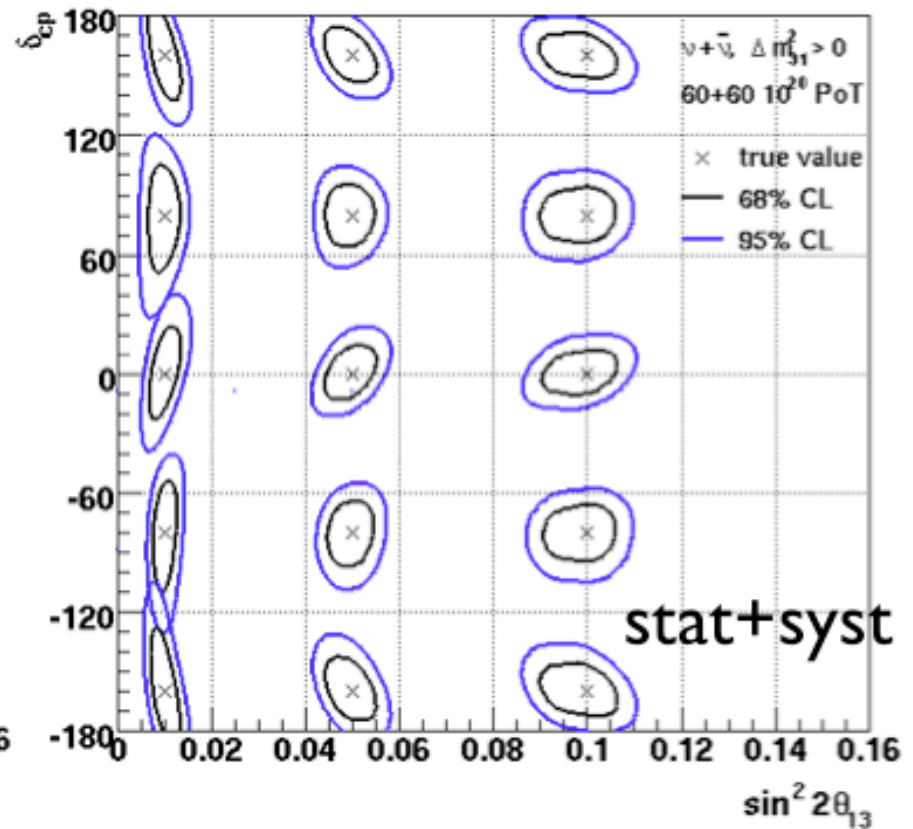
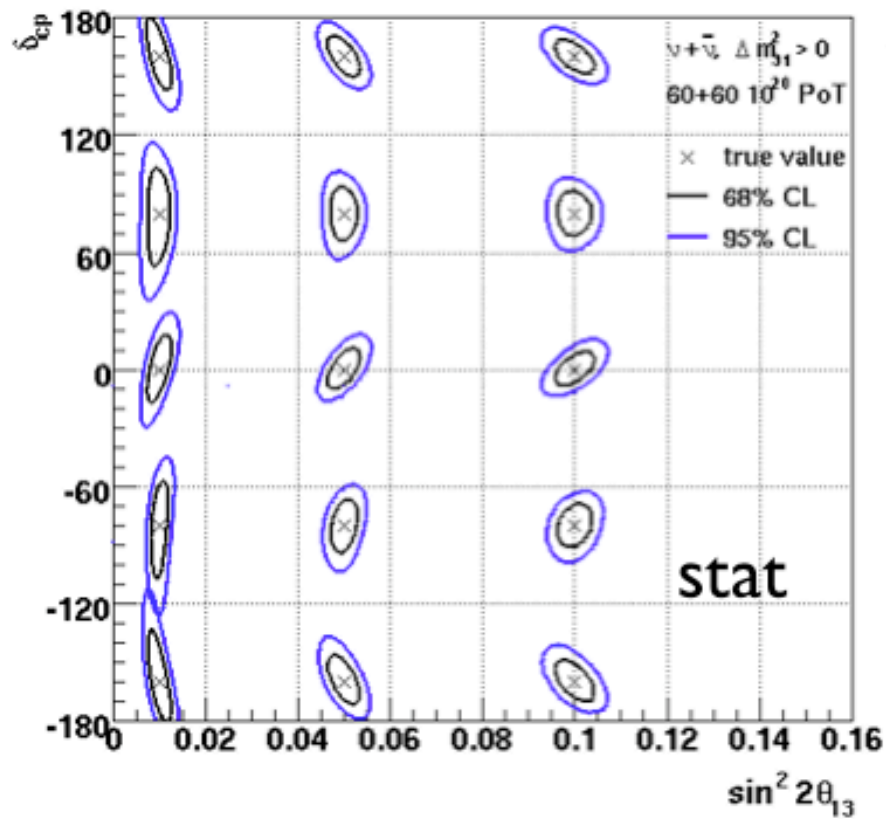
SUPER KAMIOKANDE



CP Phase Insensitivity to θ_{13} Value

WCC 1300 km 300kT

(-95% CL -68% CL)



4. “New Physics” search via ν_μ & $\bar{\nu}_\mu$ disappearance

Disappearance at MINOS $\nu_\mu \rightarrow \nu_\mu$ & $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ show differences?

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{32} \sin^2(\Delta m_{32}^2 L / 4E_\nu)$$

$$\begin{array}{ll} \nu_\mu \rightarrow \nu_\mu: & \Delta m_{32}^2 = 2.35(11) \times 10^{-3} \text{eV}^2 \quad \sin^2 2\theta_{32} \sim 1 (>0.91) \\ \bar{\nu}_\mu \rightarrow \bar{\nu}_\mu: & \Delta m_{32}^2 = 3.36(45) \times 10^{-3} \text{eV}^2, \quad \sin^2 2\theta_{32} = 0.86(11) \end{array}$$

2 σ difference? 30%?

(Collaboration does not claim discrepancy!)

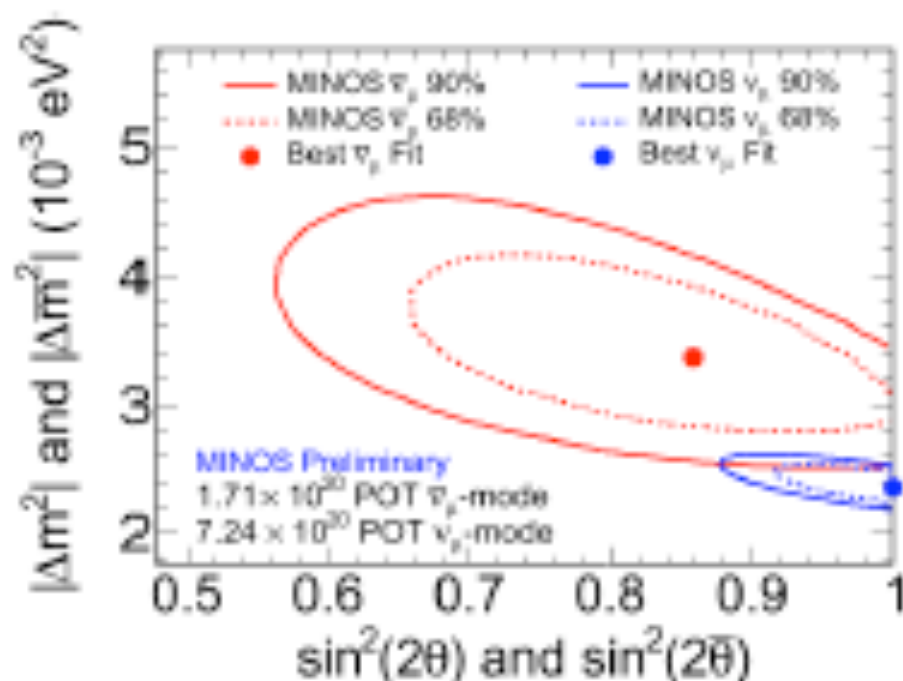
But good motivation to examine “New Physics” effects in neutrino oscillation experiments, since in the future one might expect better than 1% measurements!

Anticipate Surprises!

 $\bar{\nu}_\mu$

oscillation parameters

UCL



➤ Contours include the effects of systematic uncertainties

ν_μ Disappearance

Neutrino Running

- Total exposure: 2500 kT.MW.(10^7).sec
- 195000 CC evts/6yrs: 2MW-FNAL, 100kT-HS
- Use only clean single muon events.

Measurements

- 1% determination of Δm_{32}^2
- 1% determination of $\sin^2 2\theta_{23}$
- Most likely systematics limited.

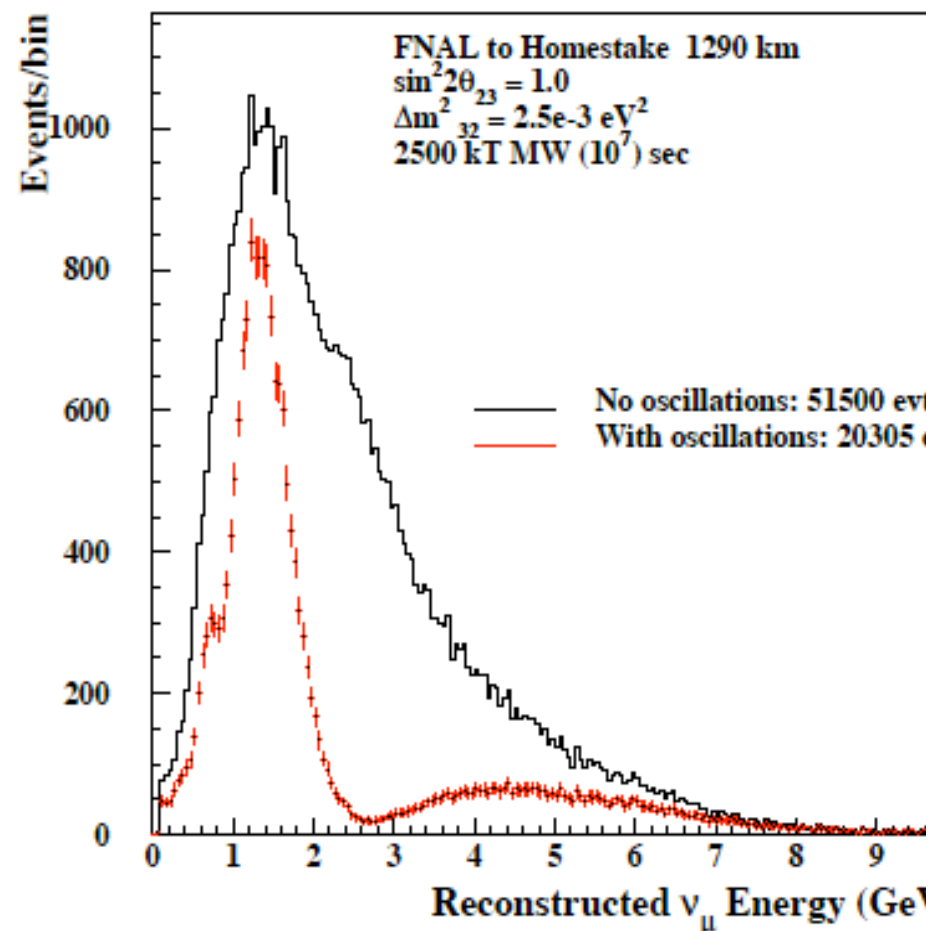
$\bar{\nu}$ running

- Need twice the exposure for similar size data set.
- very precise CPT test possible.

Very easy to get this effect

Does not need extensive pattern recognition. Can enhance the second minimum by background subtraction

ν_μ disappearance



Δm^2_{32} and $\sin^2 2\theta_{32}$ can be measured in long baselines as functions of E_ν (also obtained from atmospheric ν).

$$\nu_\mu \rightarrow \nu_\mu \text{ \& \ } \bar{\nu}_\mu \rightarrow \bar{\nu}_\mu \text{ **Comparison**}$$

Usually phrased as a test of CPT (true in vacuum)

Apparent CPT violation \rightarrow “New Physics” in ν interactions
(in matter)

$$\varepsilon \sqrt{2} G_F \bar{\nu} \gamma_\mu \nu' \bar{f} \gamma^\mu f, \quad f=e, u, d$$

Potential changes sign $\nu_\mu \rightarrow \bar{\nu}_\mu$

Sterile Neutrinos? etc

“General bounds on non-standard neutrino interactions” by
 Biggio, Blennow and Fernandez-Martinez (2009)

Using solar and atmospheric oscillation data in $\nu_e \nu_\mu \nu_\tau$ space

	ν_e	ν_μ	ν_τ		From Solar and Atmospheric
$ \varepsilon <$	2.5	0.21	1.7	ν_e	
	0.21	0.046	0.21	ν_μ	
	1.7	0.21	9.0	ν_τ	

(Bounds being updated-Take with a grain of salt)

ε represents the size of the “New Physics” potential relative to
 MSW potential (Weak Strength $\sqrt{2}G_F \bar{\nu}_e \gamma_\mu \nu_e \bar{e} \gamma^\mu e$)

Some Interesting Recent $\varepsilon \neq 0$ Examples

Engelhardt, Nelson and Walsh: sterile neutrinos & gauge B-L
new long distance physics
weakly coupled

Heeck and Rodejohann: gauge $L_\mu - L_\tau$ (violate e- μ - τ universality)
very long range interaction, $m_\nu < 10^{-18} \text{eV}$!

Earlier: Joshipura & Mohanty Gauged $L_e - L_\mu$, $L_e - L_\tau$, $L_\mu - L_\tau$
Fifth Force: $\alpha' \approx 10^{-52}$!

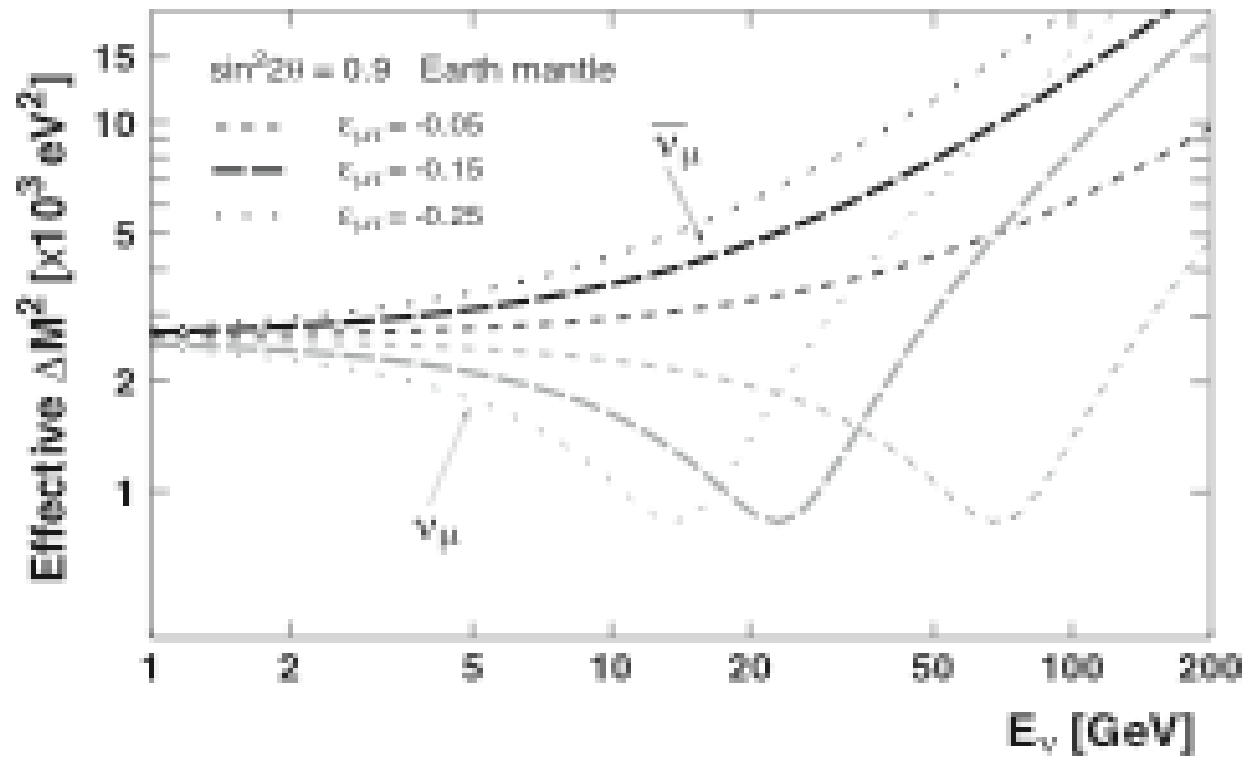
Mann et al.: New $\nu_\mu \rightarrow \nu_\tau$ Interaction $\varepsilon_{\mu\tau} \sim -0.1$ (see figure, some
generic features)

Either $O(\alpha/\Lambda^2)$ Λ large or $O(\alpha'/m^2)$ α' and m small (long distance)
Effective potential changes sign for $\nu_\mu \rightarrow \bar{\nu}_\mu$

All lead to different ν_μ and $\bar{\nu}_\mu$ oscillations (in matter)

E_ν Dependence of Oscillation Parameters

From Mann, Cherdack, Musial and Kafka
(Example)



$\nu_\mu \rightarrow \nu_\mu$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ disappearance

- $$\frac{d}{dt} \begin{pmatrix} |\nu_\mu(t)| \\ |\nu_\tau(t)| \end{pmatrix} = \begin{pmatrix} \Delta m_{32}^2 s^2 / 2p_\nu & \Delta m_{32}^2 sc / 2p_\nu \\ \Delta m_{32}^2 sc / 2p_\nu & \Delta m_{32}^2 c^2 / 2p_\nu - p_\nu(n_{\nu\tau} - n_{\nu\mu}) \end{pmatrix} \begin{pmatrix} |\nu_\mu(t)| \\ |\nu_\tau(t)| \end{pmatrix}$$

$$s = \sin\theta_\nu \quad c = \cos\theta_\nu$$

Could also be off diagonal matter effects, eg Mann et al

$$L_\nu = 2(2p_\nu / \Delta m_{32}^2) \sim 1000(E_\nu / 1\text{GeV})\text{km}$$

$$L_0 = 2\pi / p_\nu(n_{\nu\tau} - n_{\nu\mu}) \sim 5000/\varepsilon\text{km} \quad \text{Refraction index length}$$

$$y = L_\nu / L_0 \sim E_\nu \varepsilon / 5\text{GeV} \quad (\text{Big Effects For } y \sim O(1))$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_m \sin^2(\pi x / L_m) \text{ disappearance}$$

(Suggests studies at high energies & long distances)

$E_\nu > 5\text{GeV}/\varepsilon$ Atmospheric & Very Long Baseline

$$\sin^2 2\theta_m = \sin^2 2\theta_v / (1 \pm 2y \cos 2\theta_v + y^2) \quad \mathbf{y = L_v / L_0 \sim E_v \epsilon / 5 \text{ GeV}}$$

$$L_m = L_v / (1 \pm 2y \cos 2\theta_v + y^2)^{1/2} \quad \text{for } 3 \text{ gm/cm}^3$$

$$\Delta m_{32}^2(\text{matter}) = \Delta m_{32}^2 (1 \pm 2y \cos 2\theta_v + y^2)^{1/2}$$

for $y \gg 1$ oscillations highly suppressed $L_m \sim L_0$

for $y \ll 1$ matter effects very small

Resonance $y = \cos 2\theta_v \rightarrow \theta_m = 45^\circ$, minimum $\Delta m_{32}^2(\text{matter}) = \Delta m_{32}^2 \sin 2\theta_v$

No resonance for maximal vacuum mixing $\theta_v = 45^\circ$ (our world)

No Δm_{32}^2 difference in ν_μ vs $\bar{\nu}_\mu$ for $\theta_v = 45^\circ$ (but depends on E_ν)

Note high E_ν more sensitive to matter!

Anticipate possible differences in ν_μ and $\bar{\nu}_\mu$ effective energy dependent mixing angles and Δm_{32}^2 in matter

Future experiments will measure those parameters with very high precision! Atmospheric as well as Long Baseline ν_μ and $\bar{\nu}_\mu$ disappearance will be very powerful probes of non standard (long and short distance) neutrino interactions!

Note, $\nu_\mu \rightarrow \nu_\tau$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau$ appearance potentially very interesting

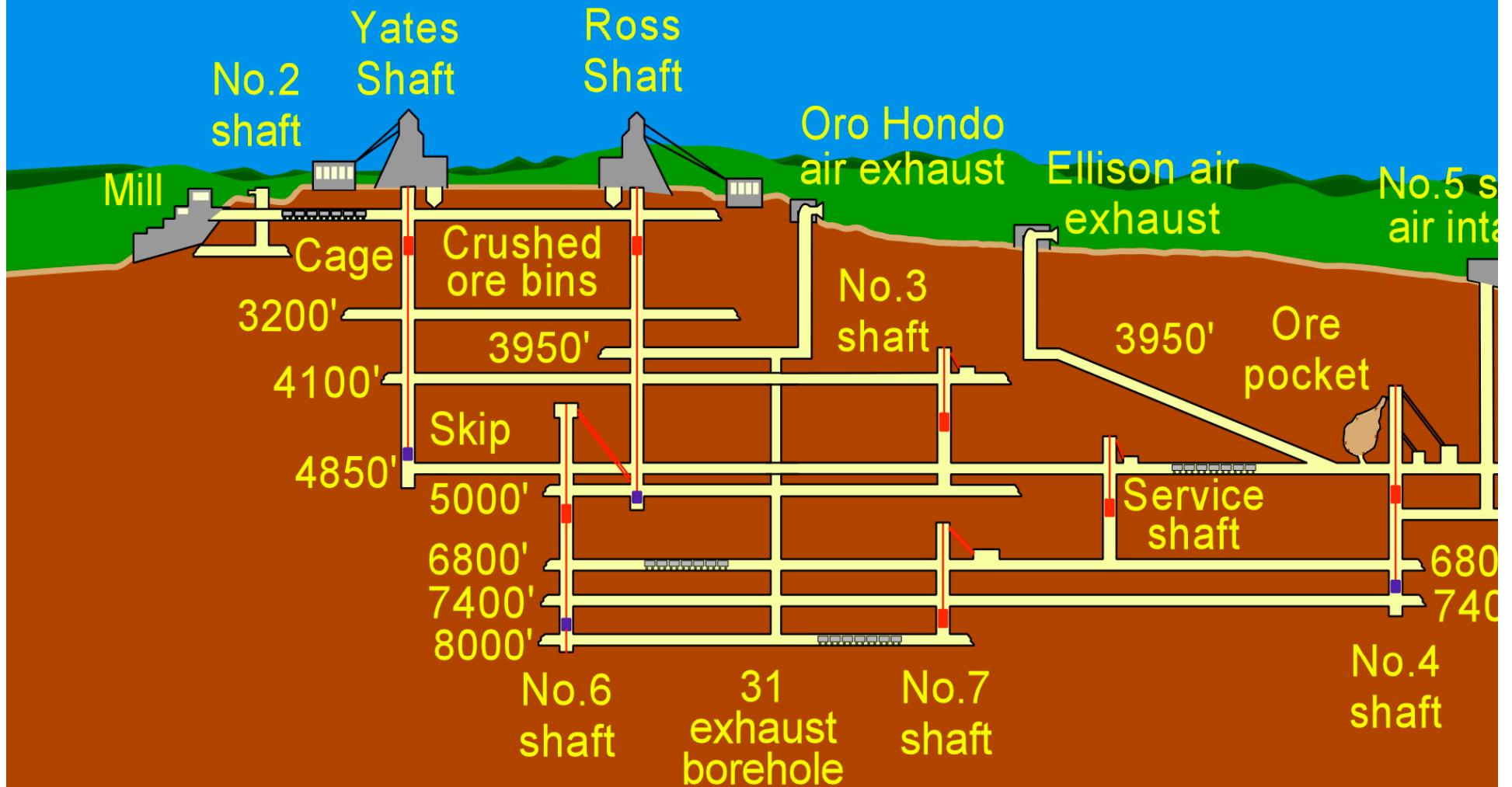
Moral: Neutrino ν_μ and $\bar{\nu}_\mu$ Osc in Matter provides a potentially powerful probe of (weakly coupled) light and heavy “New Physics”. Particularly light $\epsilon \sim \alpha'/G_F m^2$

(Does not depend sensitively on $\sin^2 2\theta_{13}$ value!)

5. Outlook

- Neutrino exps will advance: θ_{13} Mass Hierarchy, ν CP Violation
... via LBNE Requires Big Detector: 300kton H₂O or equivalent
2MW Accelerator wide band neutrino beam
 - Also
 - Atmospheric & Solar ν
 - 100,000 supernova ν events (if in our galaxy)!
 - Observe relic supernova ν (universe history)!
 - **“New Physics”**: sterile ν , extra dim. dark energy...
 - Proton decay, n - \bar{n} osc.,...magnetic monopoles
- The potential for major discoveries & surprises is great!**

General Homestake Mine Development





Fermilab Activities

- What does Fermilab do after the LHC starts?
- (Great Hope - ILC e^+e^- Collider ($\mu^+\mu^-$ Collider?))

In the meantime? New Working Group Report

Project X Option- 2MW 8GeV proton linac (ILC R&D)
8GeV fixed target program (eg. $\mu N \rightarrow e N \dots$)

+ Main Injector 30-120GeV (also at 2MW)

2MW at 50GeV provides nice neutrino beam for

FNAL-Homestake (Cost ?) Total Project \approx \$1-2 Billion

Doable! Must Do!

(START AS SOON AS POSSIBLE!)