

Supersymmetric Higgs boson with General Flavour Violation

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Outline

1. MSSM with General Flavour Violation
2. Impact of δ_{LR}^u on the Higgs boson mass
 - a) Dependence on A_t
 - b) Dependence on diagonal terms splitting
3. Experimental limits on δ_{LR}^u
4. Conclusions

MSSM with GFV

Minimal Flavour Violation \rightarrow **General** Flavour Violation

SCKM basis

$$Y_u^{\text{diag}} = V_R^u Y_u^T V_L^{u\dagger}$$

$$Y_{u,d}, (m_u^2)_{LR}, (m_q^2)_{LL}, (m_u^2)_{RR}$$

diagonal

CKM – the only source of FV

$$(m_q^2)_{LL} = V_L^d m_q^2 V_L^{d\dagger}$$

$$(m_u^2)_{RR} = V_R^u m_u^2 V_R^{u\dagger}$$

$$(m_u^2)_{LR} = \frac{v_2}{\sqrt{2}} V_R^u (T_u) V_L^{u\dagger}$$

- off-diagonal terms appears if **diagonal non-universal** (\sim mass splitting)
- non-zero arbitrary off-diagonal terms

MSSM with GFV

$$\mathcal{M}_{\tilde{u}}^2 = \tilde{m}^2 \left(\begin{array}{ccc|ccc} \alpha_2 & (\delta_{12}^u)_{LL} & (\delta_{13}^u)_{LL} & 0 & (\delta_{21}^u)_{LR} & (\delta_{31}^u)_{LR} \\ (\delta_{12}^u)_{LL} & \alpha_2 & (\delta_{23}^u)_{LL} & (\delta_{12}^u)_{LR} & 0 & (\delta_{32}^u)_{LR} \\ (\delta_{13}^u)_{LL} & (\delta_{23}^u)_{LL} & \alpha_3 + \frac{m_t^2}{\tilde{m}^2} & (\delta_{13}^u)_{LR} & (\delta_{23}^u)_{LR} & \frac{\langle v_2 \rangle \tilde{X}_t}{\sqrt{2}\tilde{m}^2} \\ \hline 0 & (\delta_{12}^u)_{LR} & (\delta_{13}^u)_{LR} & \alpha_2 & (\delta_{12}^u)_{RR} & (\delta_{13}^u)_{RR} \\ (\delta_{21}^u)_{LR} & 0 & (\delta_{23}^u)_{LR} & (\delta_{23}^u)_{RR} & \alpha_2 & (\delta_{23}^u)_{RR} \\ (\delta_{31}^u)_{LR} & (\delta_{32}^u)_{LR} & \frac{\langle v_2 \rangle \tilde{X}_t}{\sqrt{2}\tilde{m}^2} & (\delta_{13}^u)_{RR} & (\delta_{23}^u)_{RR} & \alpha_3 + \frac{m_t^2}{\tilde{m}^2} \end{array} \right)$$

Off-diagonal entries:

$$(\delta_{ij}^u)_{AB} = \frac{(m_u^2)_{AB}^{ij}}{\sqrt{(m_u^2)_{BB}^{ii} (m_u^2)_{AA}^{jj}}}$$

$$\tilde{X}_t = (T_u)_{33} - Y_t \mu \cot \beta$$

$$\left. \begin{array}{l} \tilde{m}_2 = \alpha_2 \tilde{m} \\ \tilde{m}_3 = \alpha_3 \tilde{m} \end{array} \right\} \text{Possible non-universality}$$

Higgs mass determination

$$m_h^2 = m_{h_{tree}}^2 + \Delta m_{h_{rad}}^2$$

1-loop radiative corrections:

Haber, Hempfling '93

1) Leading-logs resummed using RGEs

2) Non-log finite corrections due to squark mixing

$$\mathcal{M}_{\tilde{u}}^2 = \tilde{m}^2 \mathbb{I} + \mathcal{M}_T^2 + \mathcal{M}_F^2 \longrightarrow \text{F-term contribution } (\sim m_t^2)$$

Trilinear term contribution

$$(\Delta V_1)_{\text{finite}} = \frac{3}{64\pi^2} \frac{1}{\tilde{m}^2} \left[\text{tr}((\mathcal{M}_T^2)^2 \mathcal{M}_F^2) - \frac{1}{12\tilde{m}^2} \text{tr}(\mathcal{M}_T^2)^4 \right]$$

Higgs mass with GFV

GFV effects in the Higgs sector also analyzed in:

- ◆ Heinemeyer, Hollik, Merz, Penaranda '04 - $(\delta_{LL})_{23}$
 - ◆ Cao, Eilam, Hikasa, Yang '06 – $(\delta_{LL})_{23}, (\delta_{RL})_{23}$, Higgs mass decrease
 - ◆ Arana-Catania, Heinemeyer, Herrero, Penaranda '12
 - ◆ Arana-Catania, Heinemeyer, Herrero '14
- } $(\delta_{LL})_{23}, (\delta_{RR})_{23}, (\delta_{RL})_{23}$,
possible enhancement observed

1-loop GFV structure implemented in:

FeynHiggs, Spheno, SoftSusy

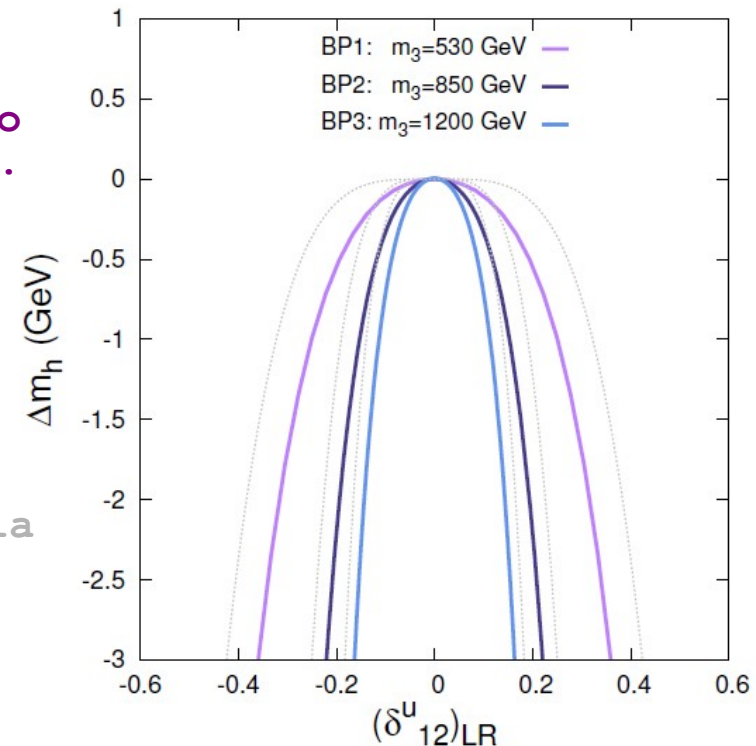
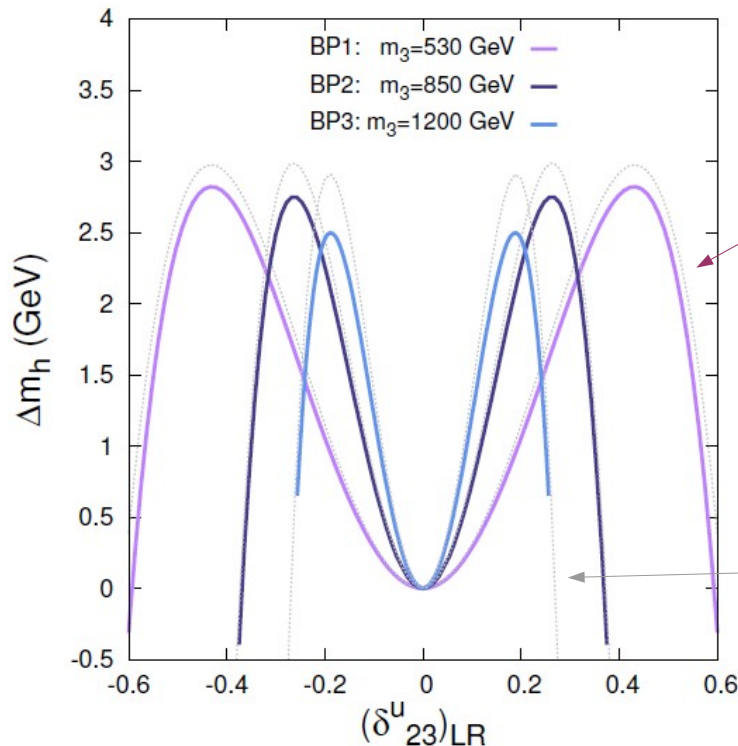
Universal masses, $A_t=0$

$$\Delta m_h^2((\delta_{23}^u)_{LR}) = \frac{3}{4\pi^2} \left[\tilde{m}^2 (\delta_{23}^u)_{LR}^2 \left(\frac{1}{2} Y_t^2 \sin^2 \beta - \frac{\tilde{m}^2 (\delta_{23}^u)_{LR}^2}{6v^2} \right) \right] \rightarrow \text{The same for } \delta_{13}^u$$

$$\Delta m_h^2((\delta_{12}^u)_{LR}) = -\frac{3}{24\pi^2 v^2} \tilde{m}^4 (\delta_{12}^u)_{LR}^4$$

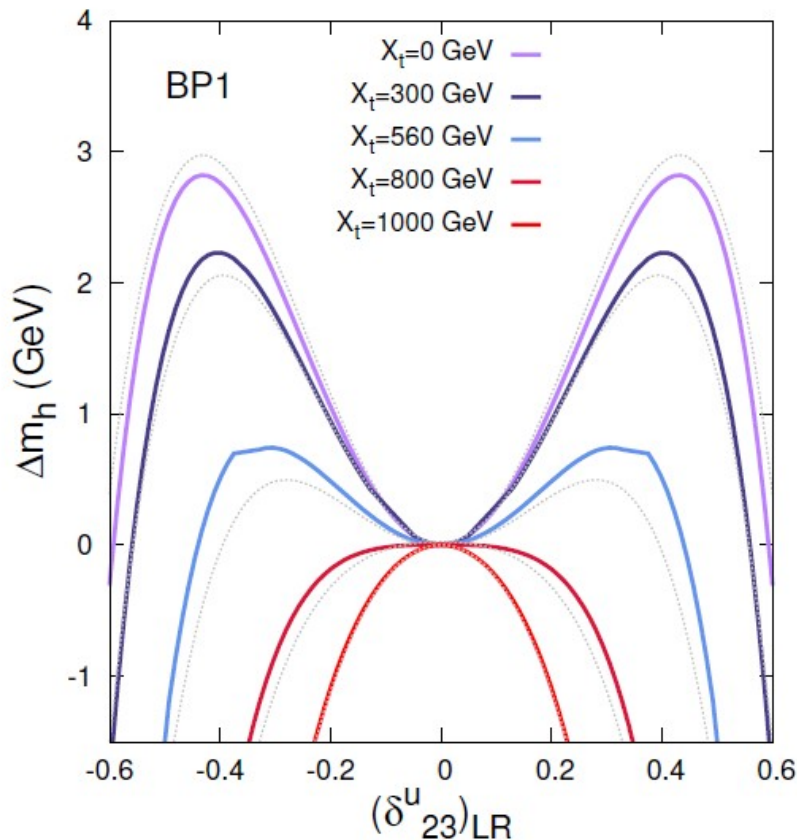
	M_1	M_2	M_3	$A_{t,b,\tau}$	μ	m_A	$\tan \beta$	$m_{\tilde{L},\tilde{e}}$	$m_{\tilde{Q}_{1,2},\tilde{u}_{1,2},\tilde{d}}$	$m_{\tilde{Q}_{3},\tilde{u}_3}$
BP1	126	233	670	0	242	1860	20	5950	560	530
BP2	126	233	670	0	362	1712	30	1455	945	850
BP3	126	233	670	0	462	1512	30	2500	1300	1200

A_t - like shape



Universal masses, $A_t \neq 0$

$$\Delta m_h^2 = \frac{3}{4\pi^2} \tilde{m}^2 \left[Y_t^2 \sin^2 \beta \left((\delta_{33}^u)^2 + \frac{1}{2} (\delta_{23}^u)_{LR}^2 \right) - \frac{\tilde{m}^2}{6v^2} \left((\delta_{33}^u)^4 + (\delta_{23}^u)_{LR}^4 + 2(\delta_{33}^u)^2 (\delta_{23}^u)_{LR}^2 \right) \right]$$



$$\tilde{X}_t = (T_u)_{33} - Y_t \mu \cot \beta$$

Negative mixed term

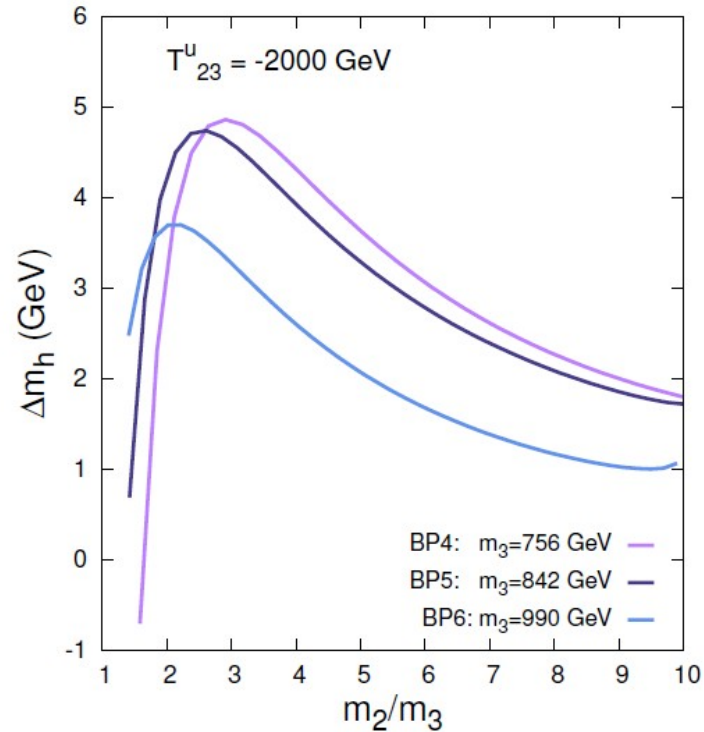
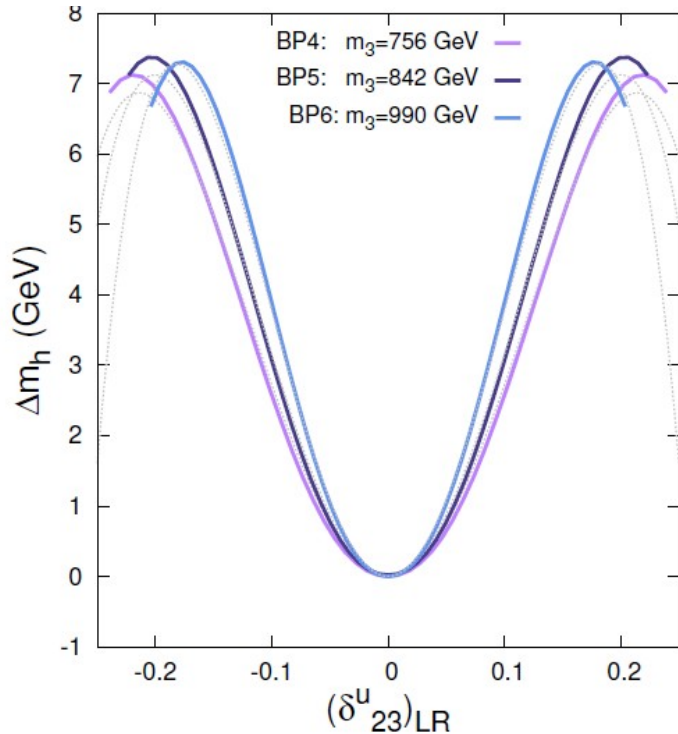
Standard A_t contribution

Hierarchical masses, $A_t=0$

$$\Delta m_h^2((\delta_{23}^u)_{LR}) = \frac{3}{4\pi^2} \left\{ (\delta_{23}^u)_{LR}^2 \frac{\tilde{m}_2^2 \tilde{m}_3^2}{\tilde{m}_2^2 - \tilde{m}_3^2} \left[\frac{1}{2} Y_t^2 \sin^2 \beta \ln \left(\frac{\tilde{m}_2^2}{\tilde{m}_3^2} \right) + (\delta_{23}^u)_{LR}^2 \frac{\tilde{m}_2^2 \tilde{m}_3^2}{v^2 (\tilde{m}_2^2 - \tilde{m}_3^2)} \left(2 - \frac{\tilde{m}_2^2 + \tilde{m}_3^2}{\tilde{m}_2^2 - \tilde{m}_3^2} \ln \left(\frac{\tilde{m}_2^2}{\tilde{m}_3^2} \right) \right) \right] \right\}$$

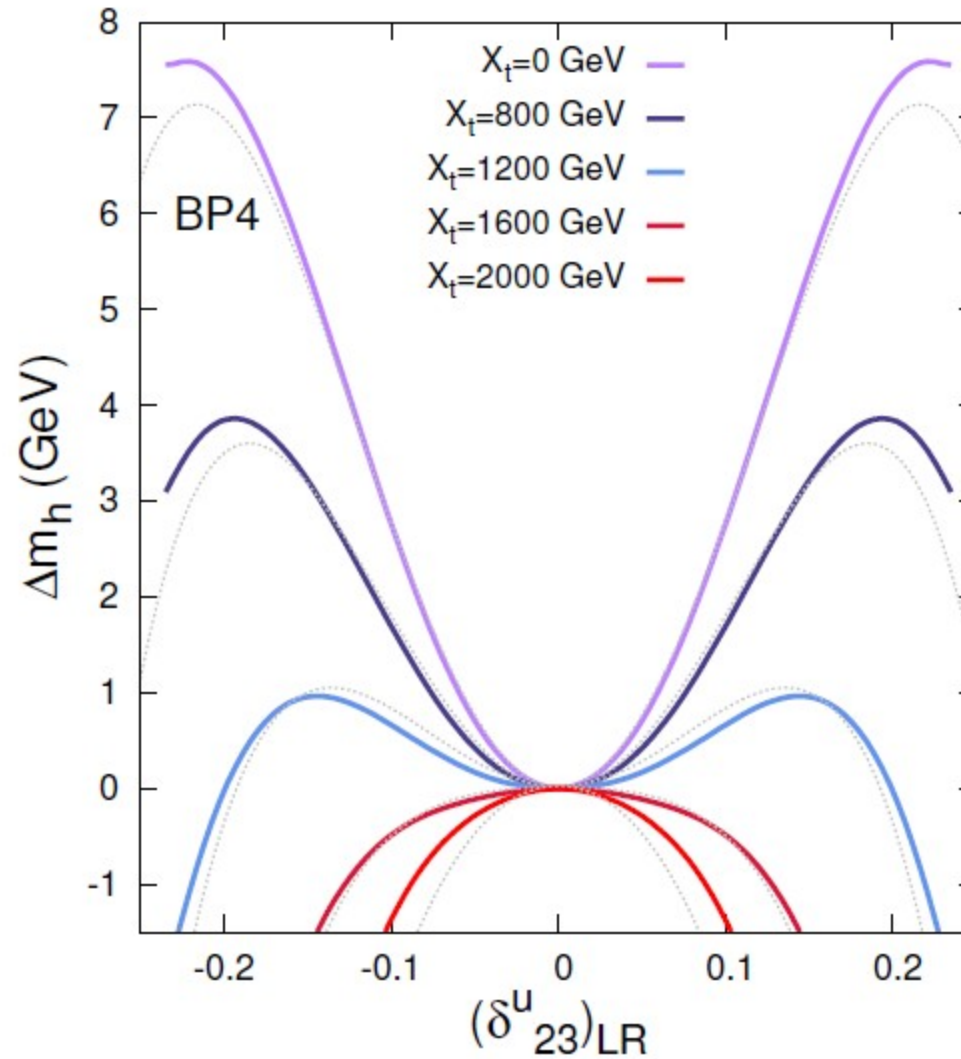
Haber, Hempfling '93
for stop mixing

	M_1	M_2	M_3	$A_{t,b,\tau}$	μ	m_A	$\tan \beta$	$m_{\tilde{L},\tilde{e}}$	$m_{\tilde{Q}_{1,2},\tilde{u}_{1,2},\tilde{d}}$	$m_{\tilde{Q}_3,\tilde{u}_3}$
BP4	300	160	1600	0	236	1665	39	3000	5000	756
BP5	300	160	1600	0	189	1310	49	3000	5000	842
BP6	300	160	1600	0	236	1410	49	3000	5000	990



maximum at
 $m_2/m_3 \sim 2 - 4$

Hierarchical masses, $A_t \neq 0$



Hierarchical masses, $A_t=0$, $2\delta_{LR}$

$$\left. \begin{aligned} (\delta_{23}^u)_{LR} &= (\delta_{32}^u)_{LR} \\ (\delta_{13}^u)_{LR} &= (\delta_{31}^u)_{LR} \\ (\delta_{23}^u)_{LR} &= (\delta_{31}^u)_{LR} \\ (\delta_{32}^u)_{LR} &= (\delta_{13}^u)_{LR} \end{aligned} \right\}$$

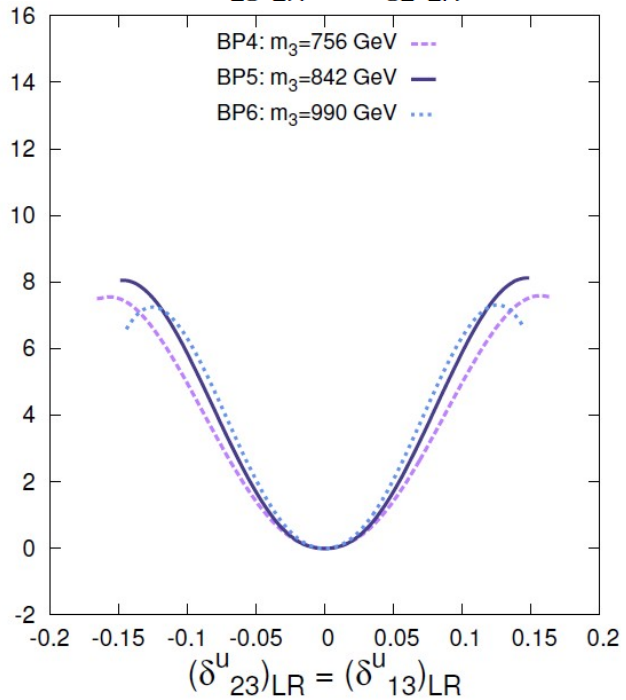
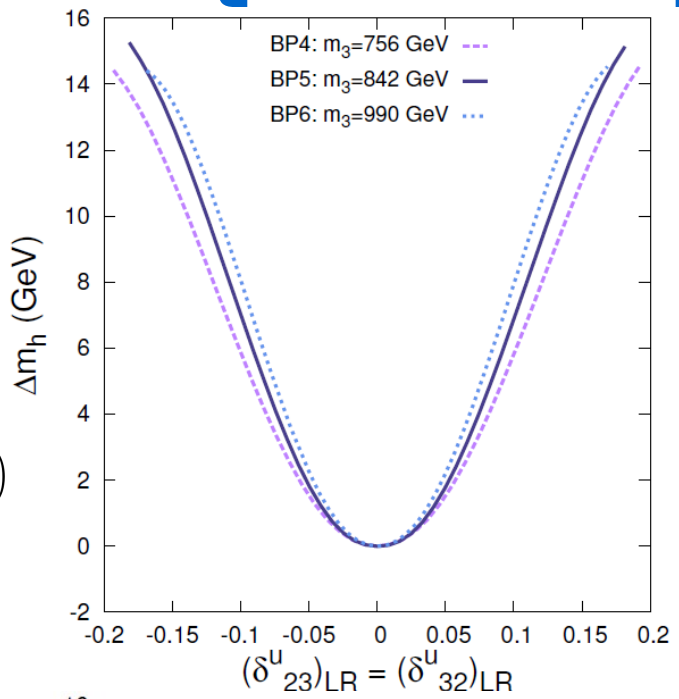
Contributions add up

$$\Delta m_h^2 = \frac{3}{4\pi^2} \tilde{m}^2 \left[Y_t^2 \sin^2 \beta \frac{1}{2} \left((\delta_{32}^u)^2 + (\delta_{23}^u)_{LR}^2 \right) - \frac{\tilde{m}^2}{6v^2} \left((\delta_{32}^u)^4 + (\delta_{23}^u)_{LR}^4 \right) \right]$$

No "mixing" term

$$\left. \begin{aligned} (\delta_{23}^u)_{LR} &= (\delta_{13}^u)_{LR} \\ (\delta_{32}^u)_{LR} &= (\delta_{31}^u)_{LR} \end{aligned} \right\}$$

$$\Delta m_h^2 = \frac{3}{4\pi^2} \tilde{m}^2 \left[Y_t^2 \sin^2 \beta \frac{1}{2} \left((\delta_{13}^u)^2 + (\delta_{23}^u)_{LR}^2 \right) - 2 \frac{\tilde{m}^2}{6v^2} \left((\delta_{13}^u)^4 + (\delta_{23}^u)_{LR}^4 \right) \right]$$



Limits on deltas - FCNC

B - physics:

Gabbiani et al '96, Misiak et al '97, Arana-Catania et al '12, '14

$$BR(B_s \rightarrow \mu^+ \mu^-) = 2.9 \pm 0.76 \times 10^{-9}$$

$$BR(B_d \rightarrow \mu^+ \mu^-) < 7.4 \times 10^{-10}$$

$$BR(B_s \rightarrow X_s \gamma) = 3.43 \pm 0.3 \times 10^{-4}$$

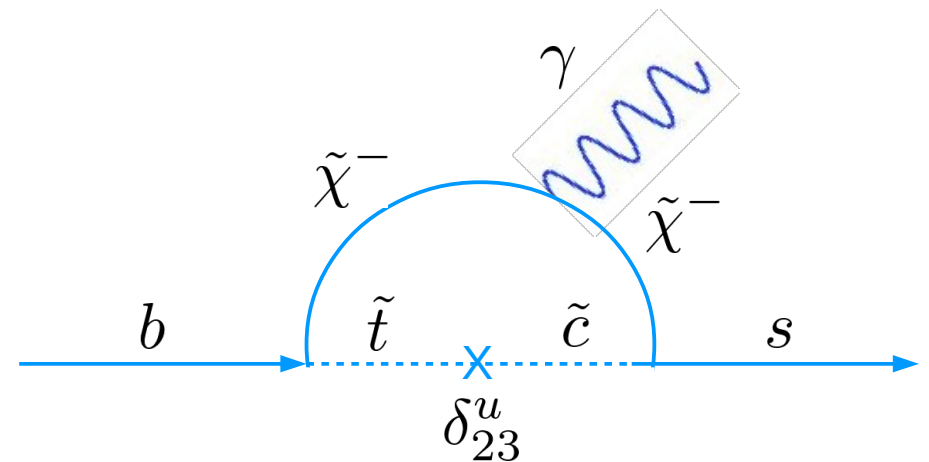
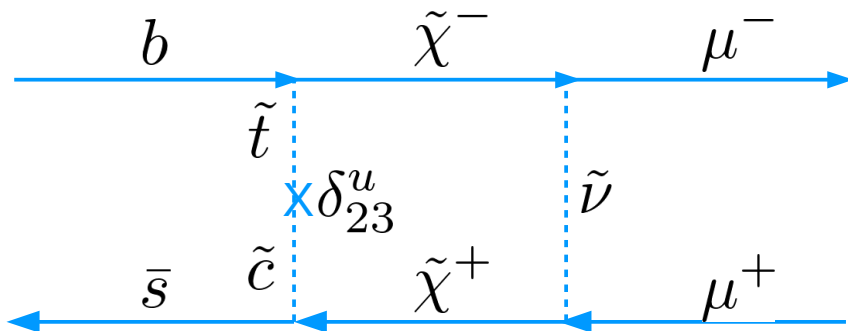
$$\Delta M_{B_s} = 1.166 \pm 0.168 \times 10^{-11} \text{ GeV}$$

$$(\delta_{23}^u)_{LR}$$

$$(\delta_{32}^u)_{LR}$$

$$(\delta_{13}^u)_{LR}$$

$$(\delta_{31}^u)_{LR}$$



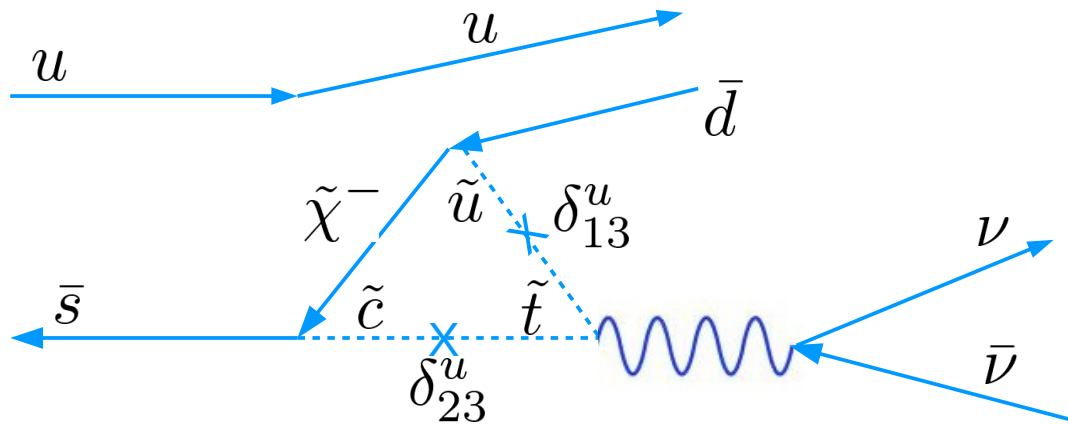
Limits on deltas - FCNC

K - decays:

$$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.73 \pm 1.15 \times 10^{-10}$$

$$(\delta_{23}^u)_{LR}$$

$$(\delta_{13}^u)_{LR}$$



Colangelo et al '98,
Altmannshofer et al '09,
Behring et al '12,

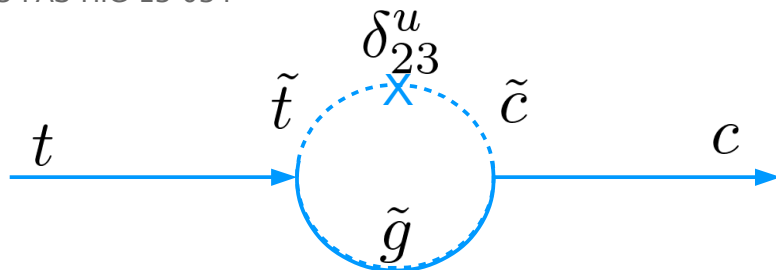
Rare top decays:

$$BR(t \rightarrow hc) < 5.6 \times 10^{-3}$$

$$(\delta_{23}^u)_{LR}$$

$$(\delta_{32}^u)_{LR}$$

CMS-PAS-HIG-13-034



In MSSM:

Guasch et al '99, Cao et al '06

$$BR(t \rightarrow hc)_{\text{MSSM}} \simeq 6 \times 10^{-5}$$

Limits on deltas - FCNC

	M_1	M_2	M_3	$A_{t,b,\tau}$	μ	m_A	$\tan \beta$	$m_{\tilde{L},\tilde{e}}$	$m_{\tilde{Q}_{1,2},\tilde{u}_{1,2},\tilde{d}}$	$m_{\tilde{Q}_{3},\tilde{u}_3}$
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	M_1	M_2	M_3	$A_{t,b,\tau}$	μ	m_A	$\tan \beta$	$m_{\tilde{L},\tilde{e}}$	$m_{\tilde{Q}_{1,2},\tilde{u}_{1,2},\tilde{d}}$	$m_{\tilde{Q}_{3},\tilde{u}_3}$
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SUSY FLAVOR v2 (Crivellin, Rosiek, Chankowski, Dedes, Jaeger '12)

	BP1	BP2	BP3	BP4	BP5	BP6	FCNC process
$(\delta_{23}^u)_{LR}$	$[-0.87 : 0.55]$	—	—	—	—	—	$b \rightarrow s\gamma$
$(\delta_{32}^u)_{LR}$	$[-0.2 : 0.52]$	—	—	$[-0.15 : 0.3]$	$[-0.16 : 0.19]$	$[-0.2 : -]$	$b \rightarrow s\gamma (B_s \rightarrow \mu^+\mu^-)$
$(\delta_{13}^u)_{LR}$	—	—	—	—	—	—	—
$(\delta_{31}^u)_{LR}$	$[-0.45 : 0.55]$	—	—	—	—	—	$K^+ \rightarrow \pi^+\nu\bar{\nu}$

max. Higgs ~0.4

~0.2

~0.2

~0.2

- FCNC constraining only for light spectra
- Limits compatible with Higgs mass enhancement

Conclusions

- The Higgs boson mass can be significantly enhanced by non-zero $(\delta^u_{23})_{LR}$, $(\delta^u_{32})_{LR}$, $(\delta^u_{13})_{LR}$, $(\delta^u_{31})_{LR}$
- The effect is mitigated by the presence of non-zero stop mixing term
- The effect is enhanced by the splitting of the diagonal entries
- The size of deltas is mildly constraint by the FCNC