



# Domain Walls in Accidentally Symmetric Two Higgs Doublet Models

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# Introduction

- Motivation
  - Domain walls as cosmological probes
- The Two Higgs Doublet Model (2HDM)
  - Physical parameters
  - Possible discrete symmetries
- Kink Solutions
  - Variation with parameters
- Domain Wall Networks
  - Neutral vacum condition
  - Scaling dynamics
- Interaction of Kinks
  - An analytical approach

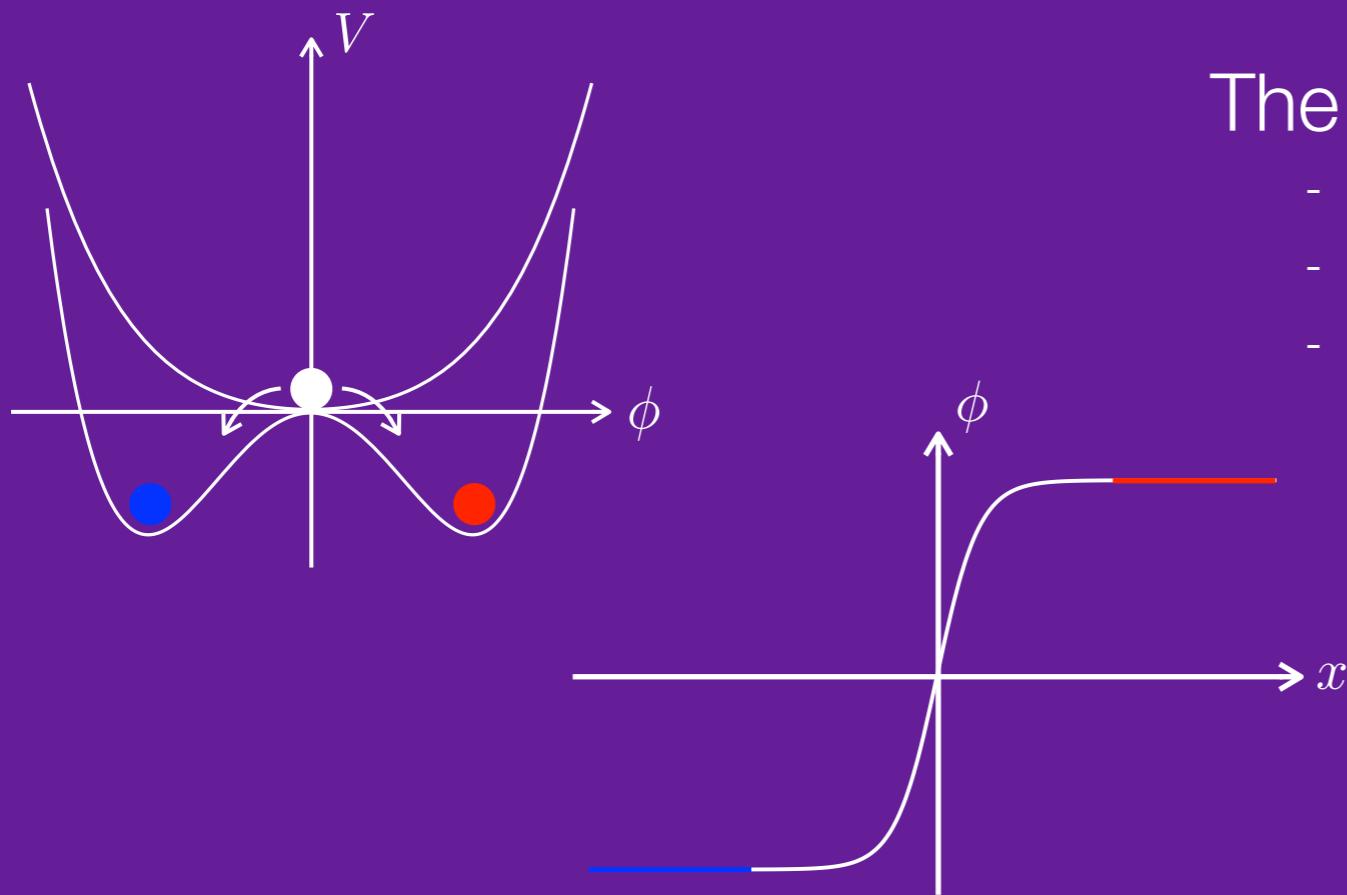


# Motivation

SM insufficient to describe observations in cosmology, e.g.

- Dark matter
- Baryon asymmetry
- Dark energy

2HDM is well-motivated but can also be topologically non-trivial



## The Domain Wall Problem

- Radiation and matter scale like  $t^{-2}$
- DWs scale like  $t^{-1}$
- DWs dominate Universe at late times



# The Two Higgs Doublet Model

$$\Phi_1 = \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_5 + i\phi_6 \\ \phi_7 + i\phi_8 \end{pmatrix}$$

$$\begin{aligned} V = & -\mu_1^2 \Phi_1^\dagger \Phi_1 - \mu_2^2 \Phi_2^\dagger \Phi_2 - (m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) + \lambda_1 (\Phi_1^\dagger \Phi_1)^2 \\ & + \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\ & + \left[ \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 (\Phi_1^\dagger \Phi_1)(\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + \text{h.c.} \right] \end{aligned}$$

3 accidental discrete symmetries:

Symmetry	$\mu_1^2$	$\mu_2^2$	$m_{12}^2$	$\lambda_1$	$\lambda_2$	$\lambda_3$	$\lambda_4$	$\lambda_5$	$\lambda_6$	$\lambda_7$
$Z_2$	-	-	0	-	-	-	-	Real	0	0
CP1	-	-	Real	-	-	-	-	Real	Real	Real
CP2	-	$\mu_1^2$	0	-	$\lambda_1$	-	-	-	-	$-\lambda_6$



# Physical 2HDM Parameters

$h, H$  CP-even scalars - mixing angle,  $\alpha$

$A$  CP-odd scalar - mixing angle,  $\beta$

$H^\pm$  Charged scalars

$$\left. \begin{array}{l} M_h = 125 \text{ GeV} \\ v_{\text{SM}} = 246 \text{ GeV} \end{array} \right\} \text{Fixed by experiment} \longrightarrow \hat{E} = \frac{M_h}{v_{\text{SM}}^2} E$$

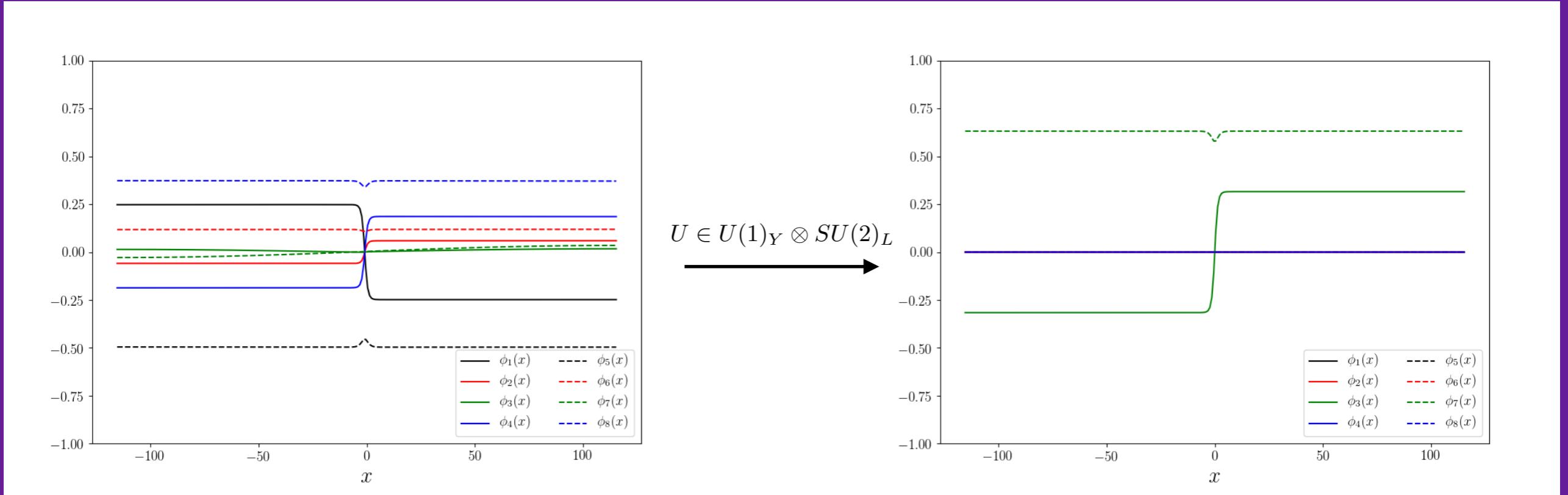
$\cos(\alpha - \beta) = 1$  SM alignment

5 physical parameters:  $M_H, M_A, M_{H^\pm}, \tan \beta, \cos(\alpha - \beta)$



# Kink Solutions

Minimum energy solutions via gradient flow



Field configuration interpolates  
between the VEVs,

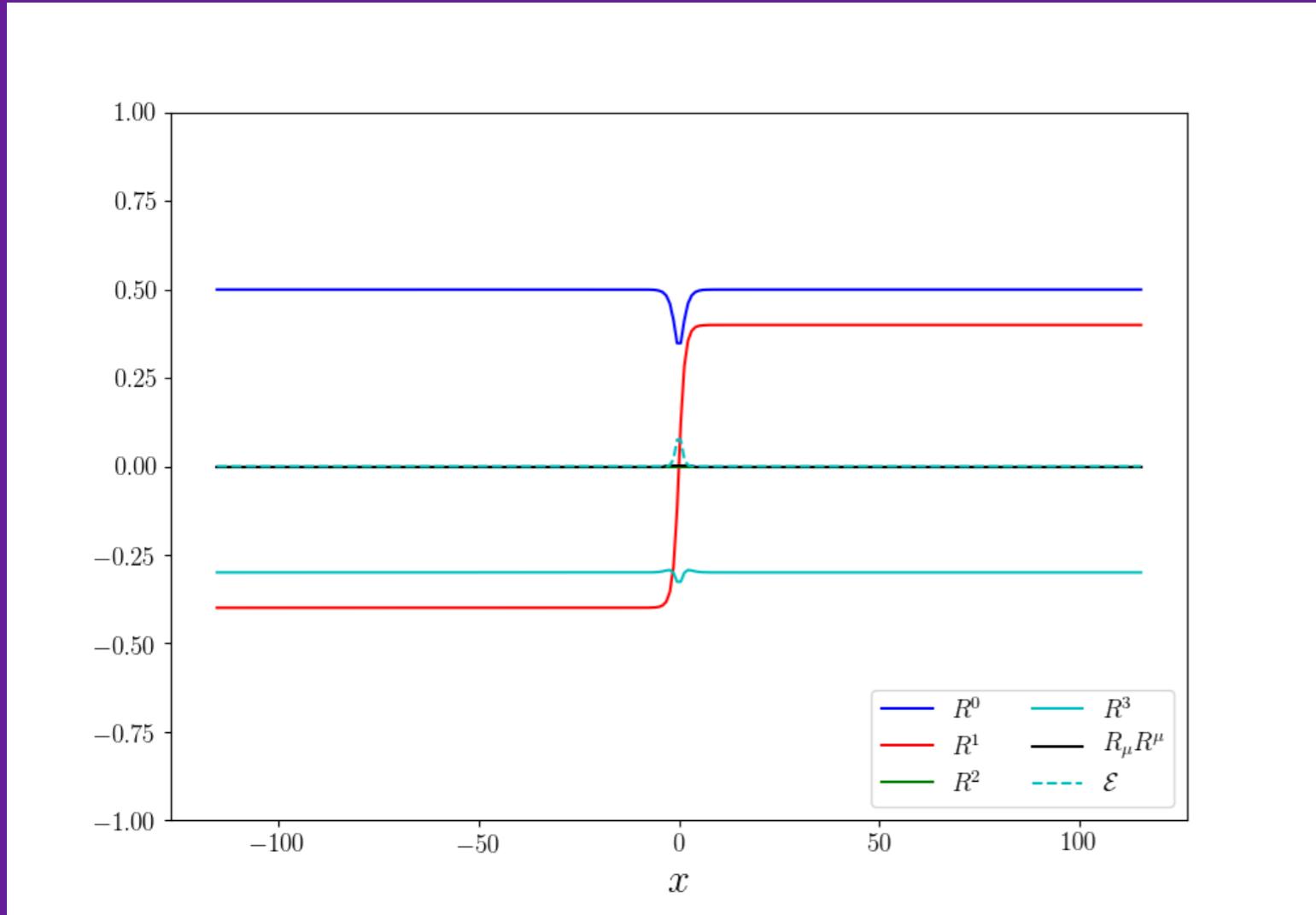
$$v_1 = v_{\text{SM}} \cos \beta$$

$$v_2 = v_{\text{SM}} \sin \beta$$

$$\Phi_1^0 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_1 \end{pmatrix}, \quad \Phi_2^0 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_2 \end{pmatrix}$$



# R-Space Profiles



Bilinear scalar field formalism:

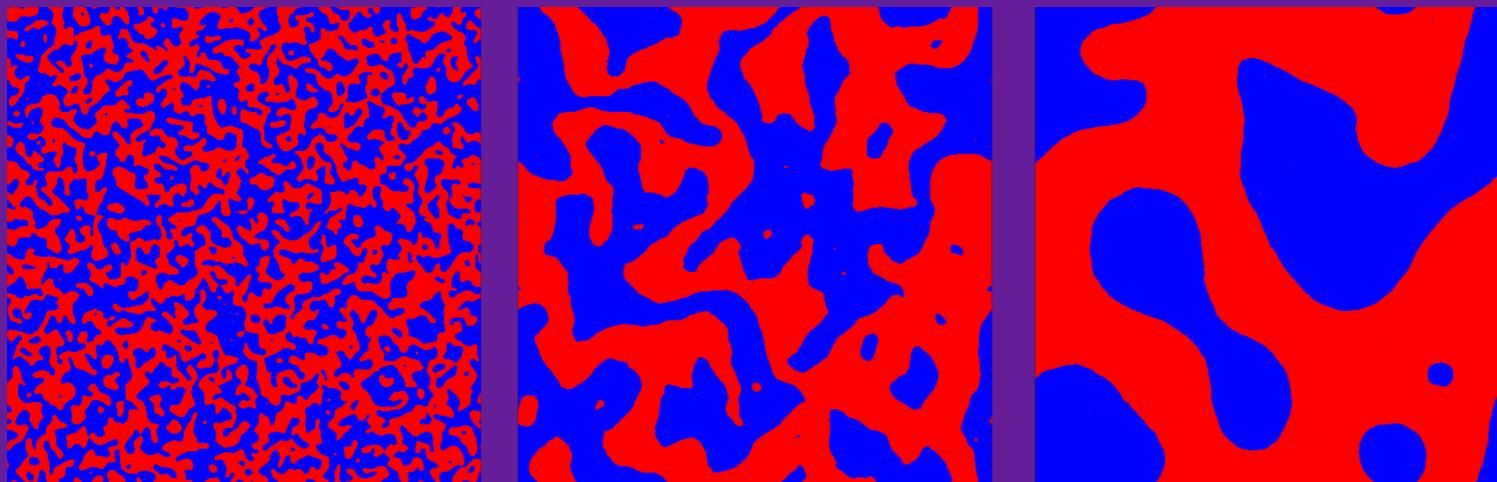
$$V = -\frac{1}{2}M_\mu R^\mu + \frac{1}{4}L_{\mu\nu}R^\mu R^\nu$$

$$R^\mu = \begin{pmatrix} \Phi_1^\dagger \Phi_1 + \Phi_2^\dagger \Phi_2 \\ \Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1 \\ -i [\Phi_1^\dagger \Phi_2 - \Phi_2^\dagger \Phi_1] \\ \Phi_1^\dagger \Phi_1 - \Phi_2^\dagger \Phi_2 \end{pmatrix}$$

Neutral vacuum condition:  $R^\mu R_\mu = 0$

# Domain Wall Networks

→ time



Time evolution of  $Z_2$  2HDM domains

Numerically solve EoMs for  
2HDM

$$\partial_\mu \partial^\mu \Phi_i + \frac{\partial V}{\partial \Phi_i^\dagger} = 0$$

Walls/condensates form  
in  $R^\mu$

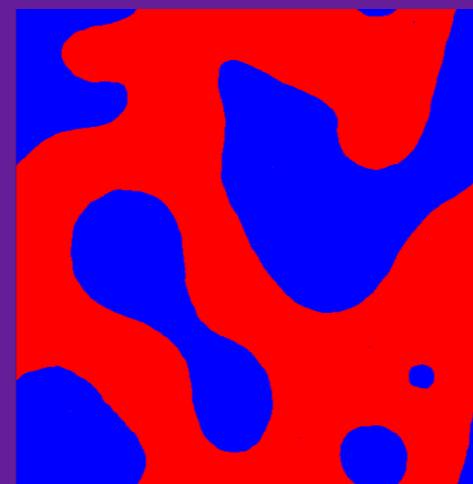
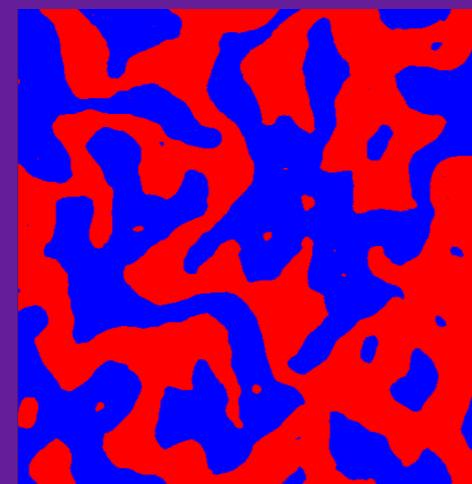
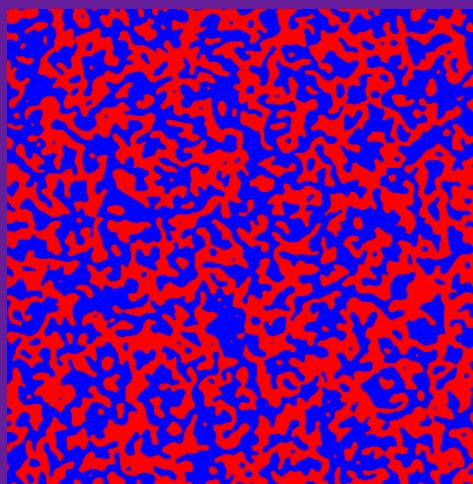
- Walls in  $R^1$  in  $Z_2$  and CP2
- Walls in  $R^2$  in CP1

$$R^\mu = \begin{pmatrix} \Phi_1^\dagger \Phi_1 + \Phi_2^\dagger \Phi_2 \\ \Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1 \\ -i [\Phi_1^\dagger \Phi_2 - \Phi_2^\dagger \Phi_1] \\ \Phi_1^\dagger \Phi_1 - \Phi_2^\dagger \Phi_2 \end{pmatrix}$$



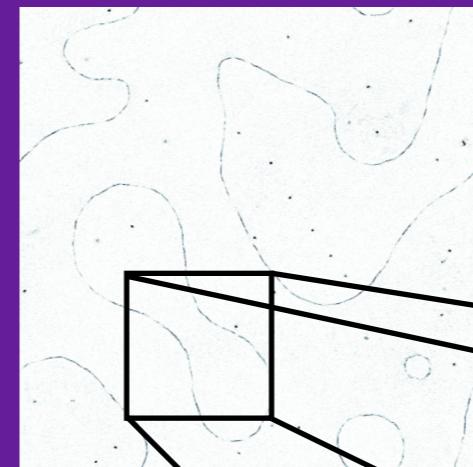
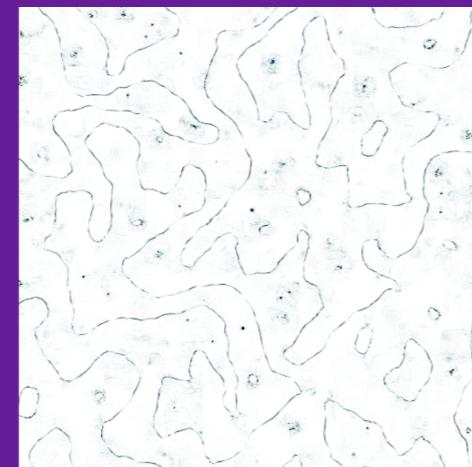
# Neutral Vacuum Condition

→ time



Neutral vacuum condition violated locally

Dynamical feature of simulations

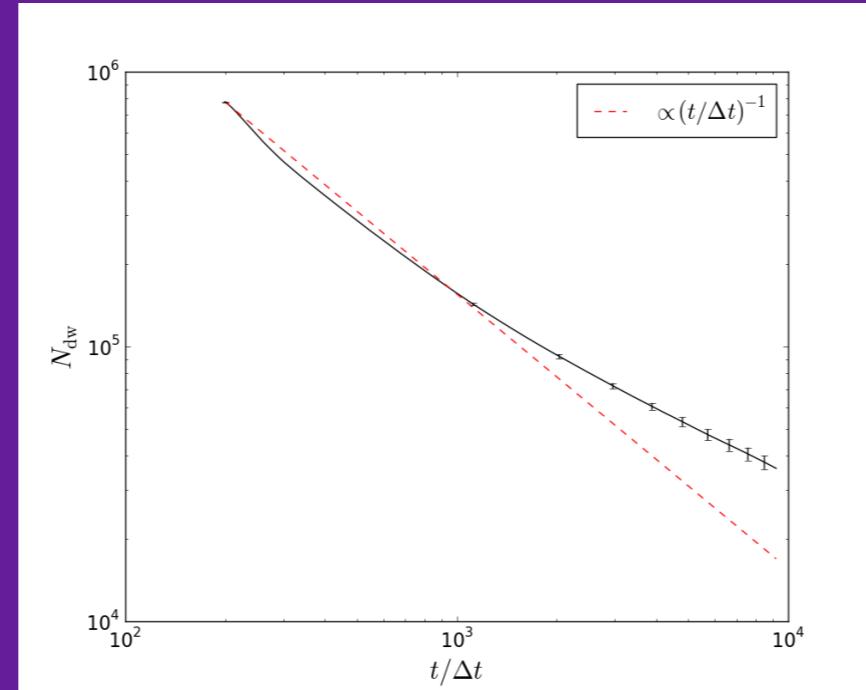


Not seen in kink solutions

$R_\mu R^\mu \neq 0$  on the walls

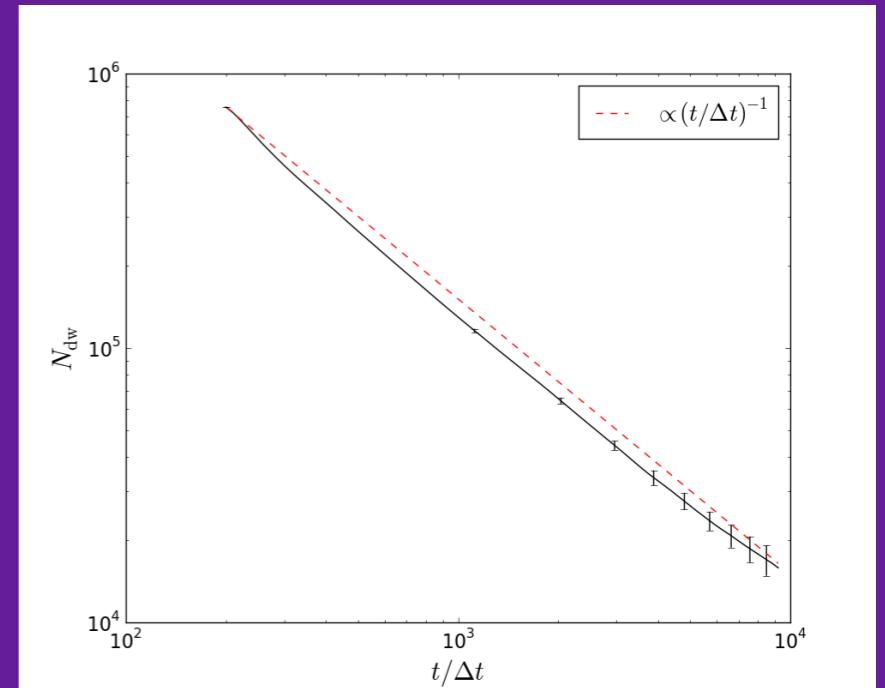
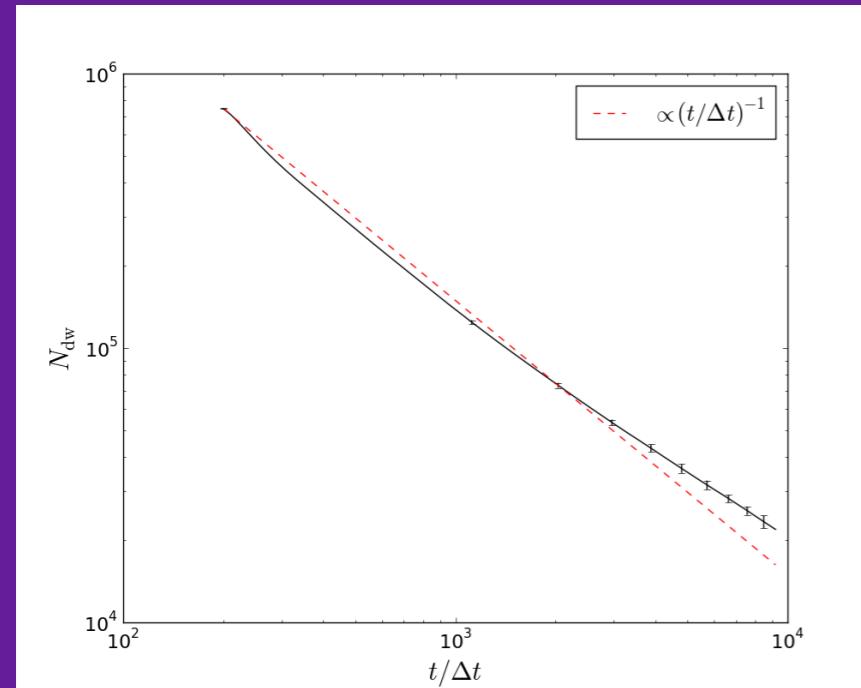
# Network Scaling

Radiation era



Matter era

Minkowski

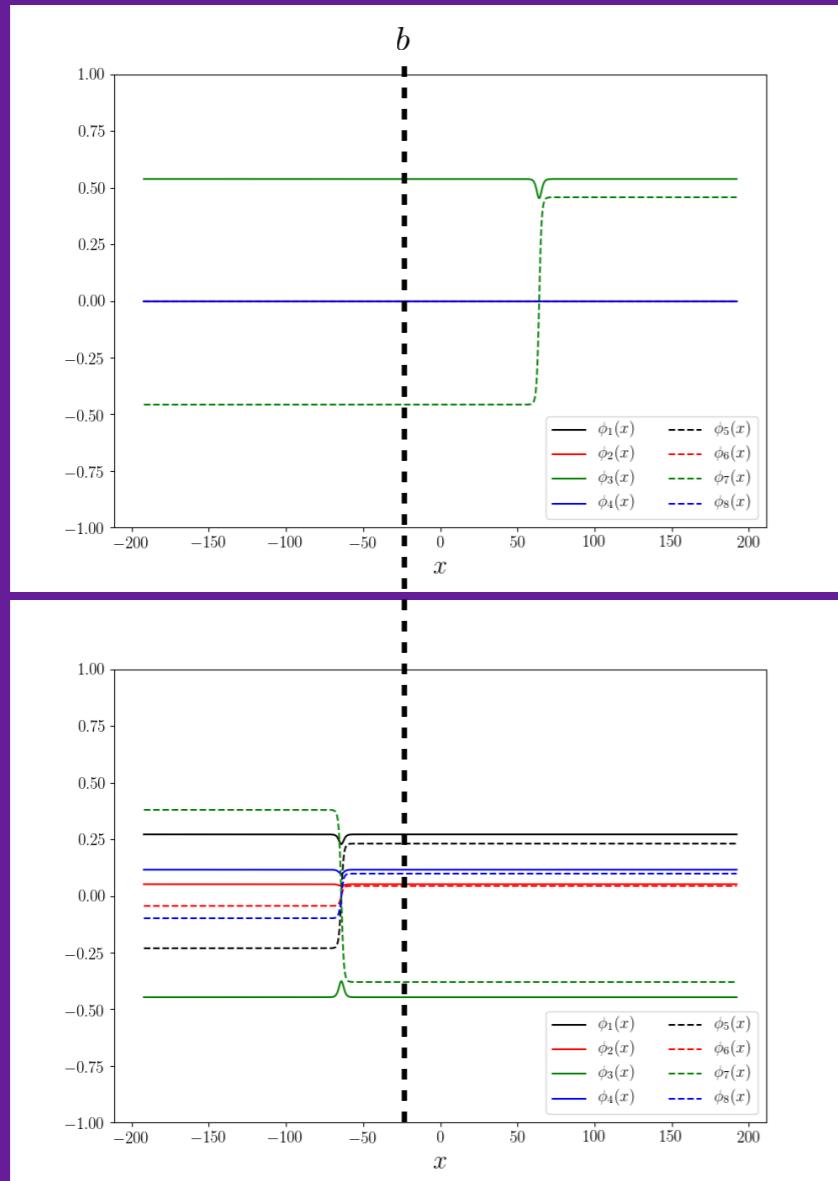


# Kink Interaction Energy

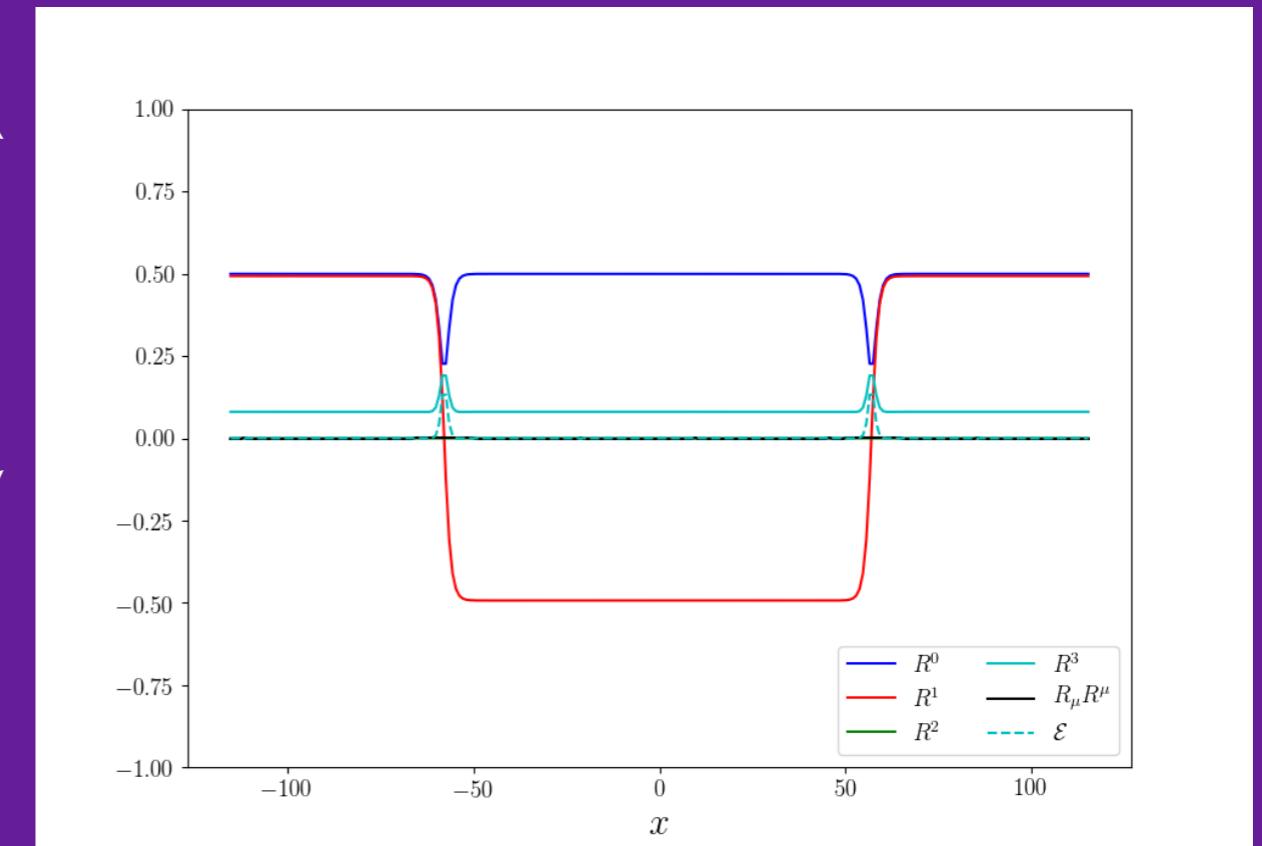
$$\Phi_1(x) = \hat{\Phi}_1(x-a) + U \left[ \hat{\Phi}_1(x+a) - \Phi_1^0 \right]$$

$$\Phi_2(x) = \hat{\Phi}_2(x-a) - U \left[ \hat{\Phi}_2(x+a) - \Phi_2^0 \right]$$

$$U = e^{i\theta} \begin{pmatrix} \bar{A} & B \\ -\bar{B} & A \end{pmatrix}$$



$$F = \left[ -\Phi_1^{\dagger'} \Phi_1' - \Phi_2^{\dagger'} \Phi_2' + V(\Phi_1, \Phi_2) \right]_b^\infty$$



# Kink Interaction Energy

$$\begin{aligned}\Phi_1(x) &= \hat{\Phi}_1(x-a) + U \left[ \hat{\Phi}_1(x+a) - \Phi_1^0 \right] \\ \Phi_2(x) &= \hat{\Phi}_2(x-a) - U \left[ \hat{\Phi}_2(x+a) - \Phi_2^0 \right]\end{aligned}$$

$$U = e^{i\theta} \begin{pmatrix} \bar{A} & B \\ -\bar{B} & A \end{pmatrix}$$

$$F = \left[ -\Phi_1^{\dagger'} \Phi_1' - \Phi_2^{\dagger'} \Phi_2' + V(\Phi_1, \Phi_2) \right]_b^\infty$$

Well-separated kinks:  $-a \ll b \ll a$

Linearize in  $\hat{\Phi}_i(x+a)$ :

$$F = \frac{dE_{\text{int}}}{dR} = -(e^{i\theta} A + e^{-i\theta} \bar{A}) (\rho^2 \mu^2 e^{-\mu R} + \sigma^2 \nu^2 e^{-\nu R})$$

$$E_{\text{int}} = (e^{i\theta} A + e^{-i\theta} \bar{A}) (\rho^2 \mu e^{-\mu R} + \sigma^2 \nu e^{-\nu R})$$

Kink separation,  $R = 2a$



# Summary and Outlook

- 2HDM can admit topological defects
  - 3 accidental symmetries produce DWs
  - Domain wall problem
- Kink Solutions
  - Energy of kinks sets DW domination time
  - Physical parametrisation needed for CP1/2
- Domain Wall Networks
  - Dynamical features not found in kinks
  - Non-standard scaling of DWs
  - Local violation of neutral vacuum condition
- Interaction of Kinks
  - Falls exponentially with kink separation
  - Kinks in different fields can attract/repel



# Thanks for listening.



# Gauge Fields

$$\partial_\mu F^{\mu\nu,a} + g \varepsilon^{abc} W_\mu^b F^{\mu\nu,c} = -\frac{ig}{2} \left( \Phi_i^\dagger \sigma^a D^\nu \Phi_i - (D^\nu \Phi_i)^\dagger \sigma^a \Phi_i \right)$$

$$\partial_\mu f^{\mu\nu} = -\frac{ig'}{2} Y \left( \Phi_i^\dagger D^\nu \Phi_i - (D^\nu \Phi_i)^\dagger \Phi_i \right)$$

$$f_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu$$

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g \varepsilon^{abc} W_\mu^b W_\nu^c$$

$$D_\mu = \partial_\mu - \frac{ig}{2} \sigma^a W_\mu^a - \frac{ig'}{2} Y B_\mu$$



# U(1) Charge?

$$\Phi_1^0 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_1 \end{pmatrix}$$

$$\Phi_i = U \Phi_i^0$$

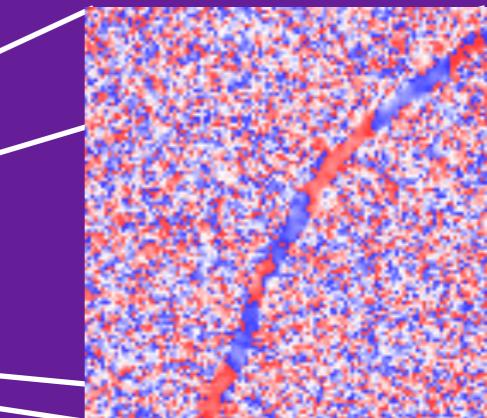
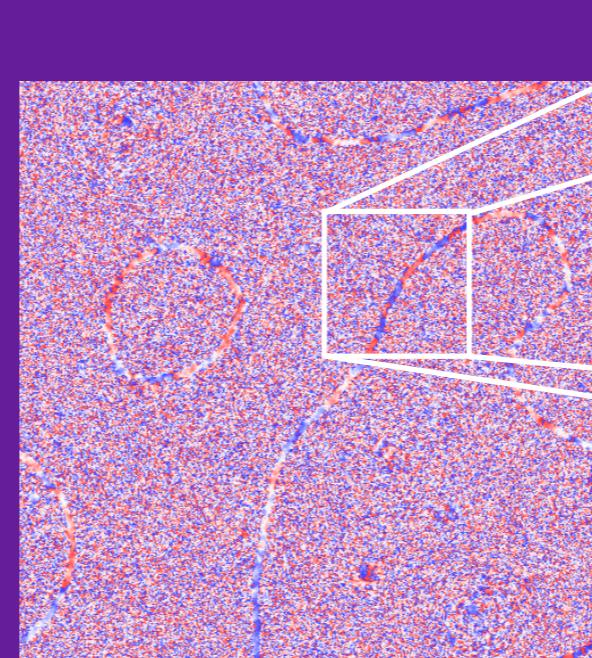
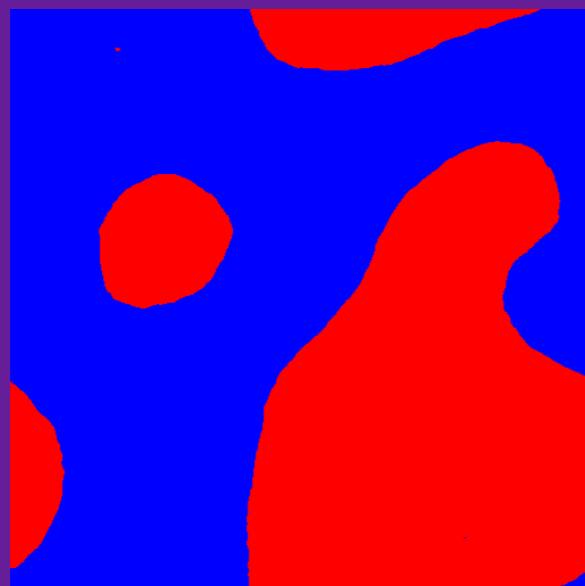
$$R^\mu \rightarrow R^A, \ A = 0, 1, \dots, 5$$

$$\Phi_2^0 = \frac{1}{\sqrt{2}} \begin{pmatrix} v_+ \\ v_2 e^{i\xi} \end{pmatrix}$$

$$U = e^{i\theta} \begin{pmatrix} \bar{A} & B \\ -\bar{B} & A \end{pmatrix}$$

$$R^4 = \Phi_1^T i\sigma^2 \Phi_2 - \Phi_2^\dagger i\sigma^2 \Phi_1^*$$

$$R^5 = -i \left( \Phi_1^T i\sigma^2 \Phi_2 + \Phi_2^\dagger i\sigma^2 \Phi_1^* \right)$$



$\theta$  winds around the wall