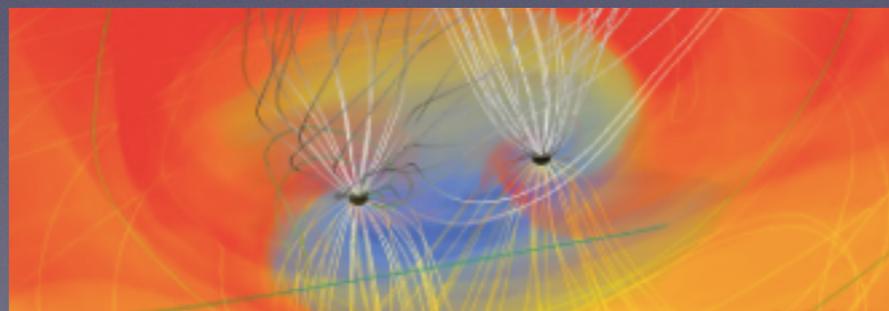


*Sterile Neutrinos*  
*with*  
*Altered Dispersion Relations*  
*as an Explanation for*  
*MiniBooNE, LSND, Gallium and*  
*Reactor Anomalies*

- HEINRICH PÄS -

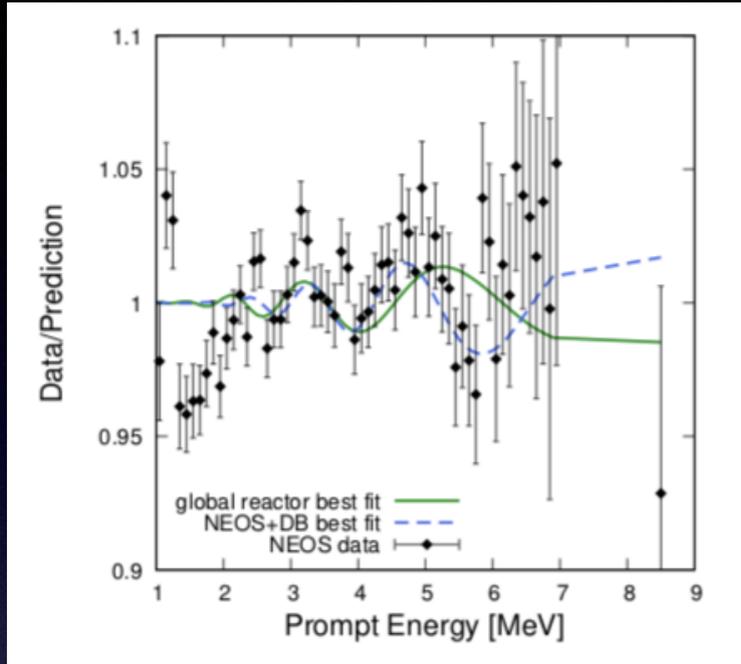
tu dortmund



PASCOS 2019  
XXV International Symposium

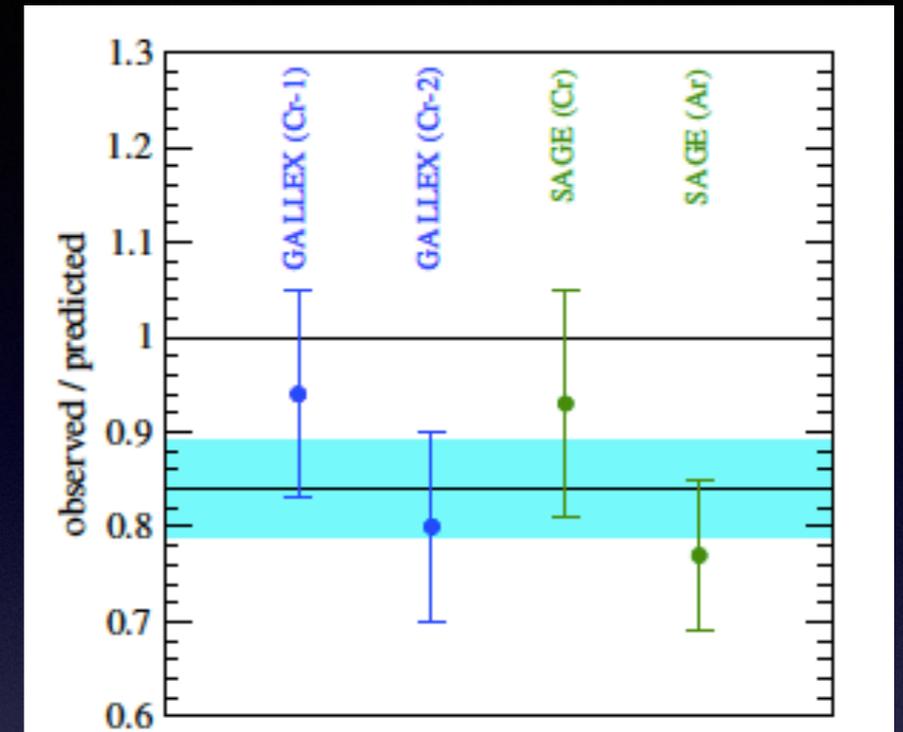
# Sterile Neutrinos?

Reactor Anomaly

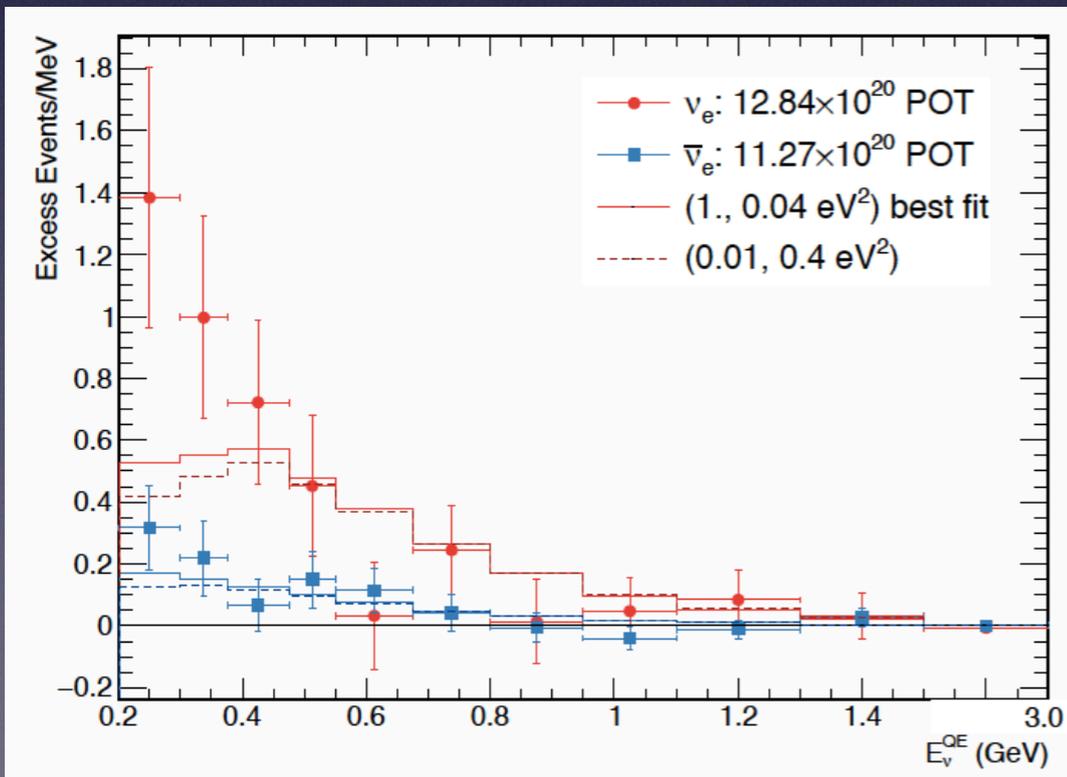


All pointing towards a 1 eV sterile neutrino!

Gallium Anomaly

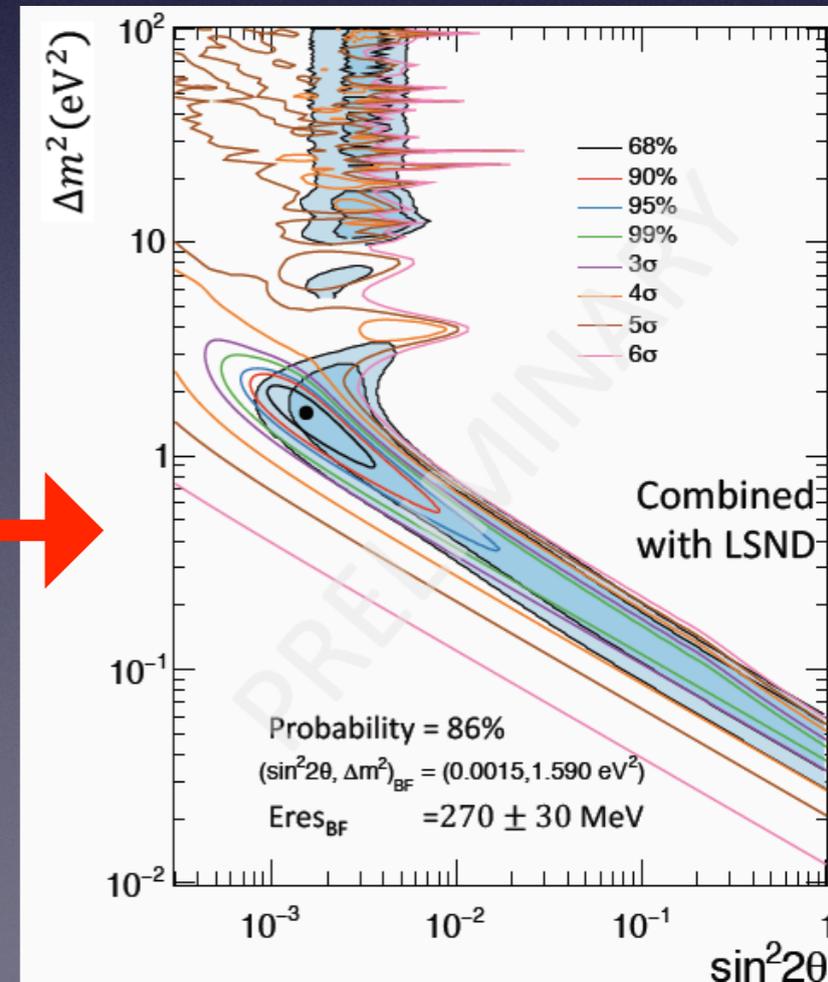


## LSND/MiniBooNE Anomaly



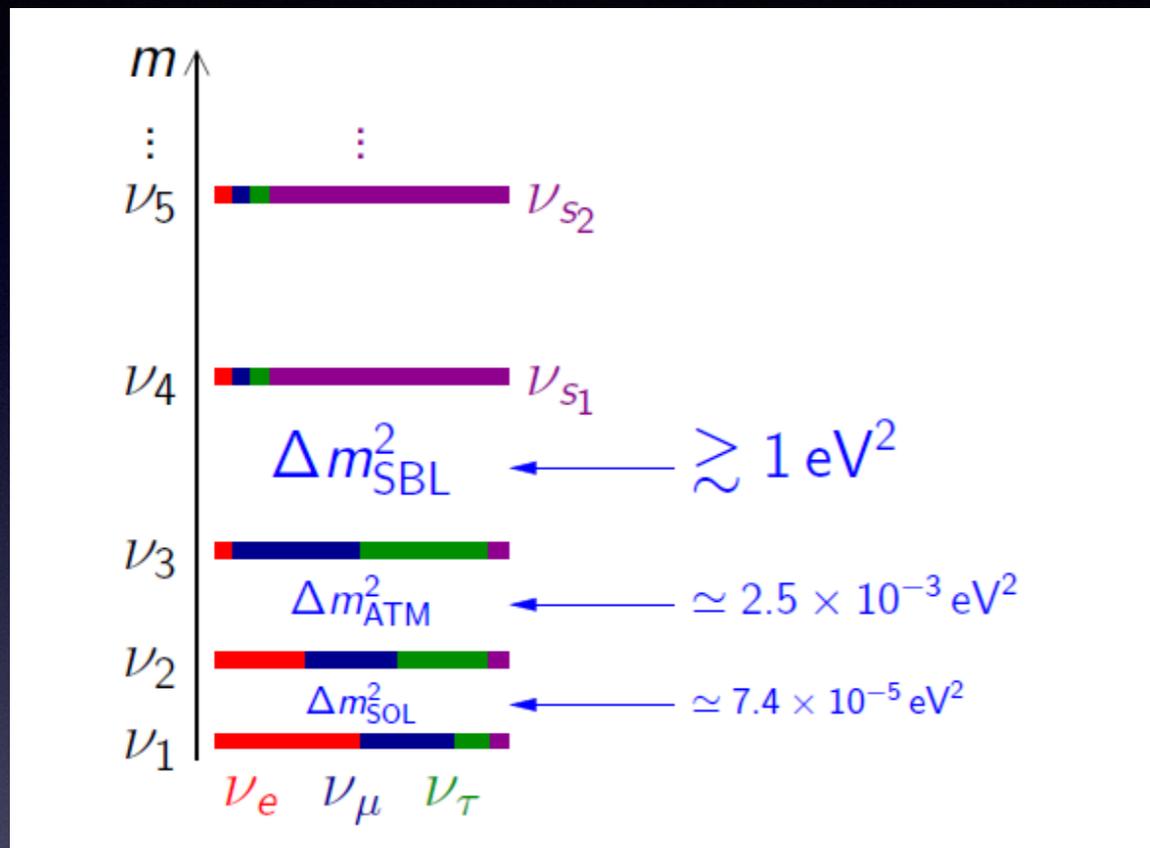
“MSW-like resonance model”

En-Chuan Huang, Talk at Neutrino2018



# Sterile Neutrinos?

→ Add a sterile neutrino with  $\Delta m^2 \sim 1 \text{ eV}^2$



*Conrad/Shaevitz*

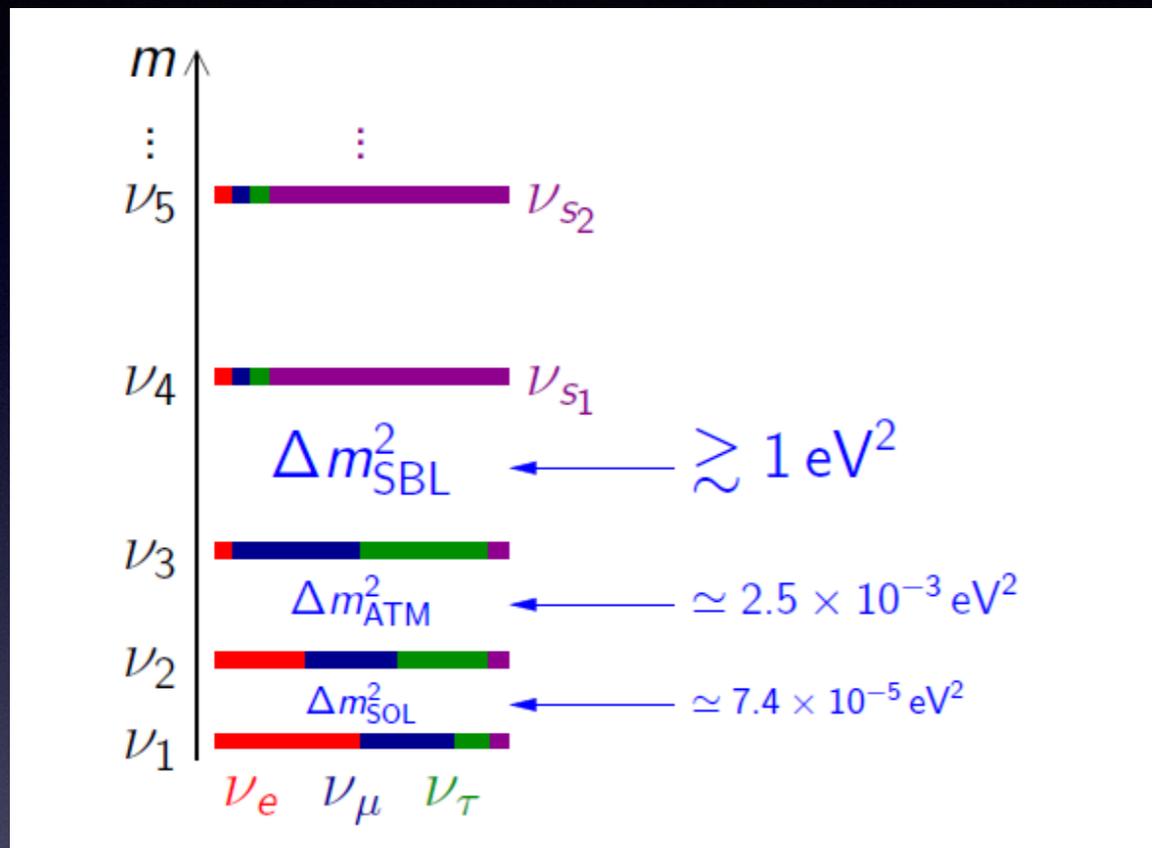
To explain LSND/MiniBooNE:

$\nu_s$  -mixing with both  $\nu_e$  and  $\nu_\mu$ :

$$\begin{aligned} \sin^2 2\theta_{\mu e} &= 4 |U_{\mu 4}|^2 |U_{e 4}|^2 = \frac{1}{4} (\sin^2 2\theta_{\mu\mu} + 4 |U_{\mu\mu}|^4) (\sin^2 2\theta_{ee} + 4 |U_{ee}|^4) \\ &\simeq \frac{1}{4} \sin^2 2\theta_{\mu\mu} \sin^2 2\theta_{ee}, \end{aligned}$$

# Sterile Neutrinos?

→ Add a sterile neutrino with  $\Delta m^2 \sim 1 \text{ eV}^2$



constrained by  $\nu_\mu$  disappearance

constrained by  $\nu_e$  disappearance

To explain LSND/MiniBooNE:  
 $\nu_s$  -mixing with both  $\nu_e$  and  $\nu_\mu$ :

*Giunti, Zavanin, 2015*

$$\sin^2 2\theta_{\mu e} = 4 |U_{\mu 4}|^2 |U_{e 4}|^2 = \frac{1}{4} (\sin^2 2\theta_{\mu\mu} + 4 |U_{\mu\mu}|^4) (\sin^2 2\theta_{ee} + 4 |U_{ee}|^4)$$

$$\approx \frac{1}{4} \sin^2 2\theta_{\mu\mu} \sin^2 2\theta_{ee},$$

## A 4th sterile neutrino ?

Sterile neutrinos can have a very different origin than the SM neutrinos (e.g. superpartners of dilaton, radion or other moduli fields, mirror world fermions, etc...)

There is **NO** compelling reason to believe that a sterile neutrino should behave just as the SM neutrinos

# Sterile neutrino Altered Dispersion Relations

Evidence for light sterile  $\nu$  is **partly conflicting!**

- ▶ May be **wrong!**
- ▶ May hint towards deviations from the usual oscillation mechanism!
- ▶ Sterile neutrinos as **messengers of exciting new physics?**

Attractive candidate: **Altered dispersion relations**

$$E = p + m^2/2E + \text{new terms}$$

→ novel energy dependence!

*HP, Pakvasa, Weiler 2005*

# Altered dispersion relations: vanilla type

Evolution equation in flavor space:

$$i \frac{d}{dt} \begin{pmatrix} \nu_a(t) \\ \nu_s(t) \end{pmatrix} = H_F \begin{pmatrix} \nu_a(t) \\ \nu_s(t) \end{pmatrix}$$

Hamiltonian in the presence of bulk shortcuts:

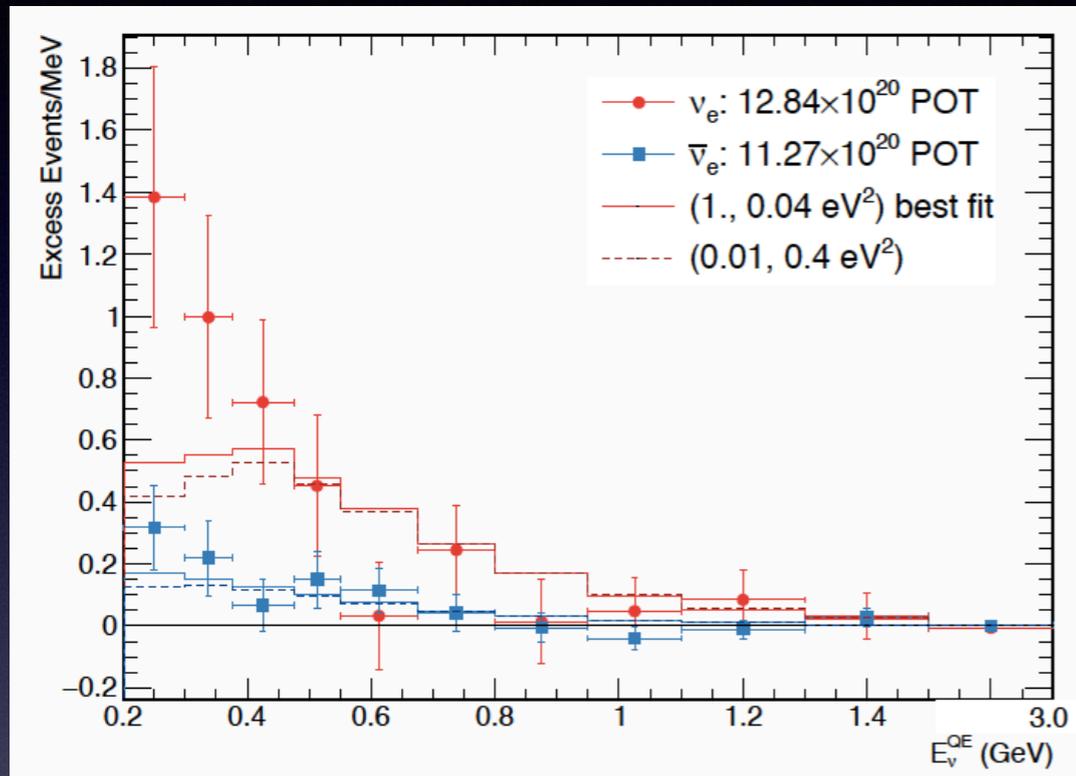
$$H_F = + \frac{\delta m^2}{4E} \begin{pmatrix} \cos 2\theta & -\sin 2\theta \\ -\sin 2\theta & -\cos 2\theta \end{pmatrix} + E \frac{\epsilon}{2} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$

$\Rightarrow$  A Resonance exists at  $E_{\text{res}} = \sqrt{\frac{\delta m^2 \cos 2\theta}{2\epsilon}}$

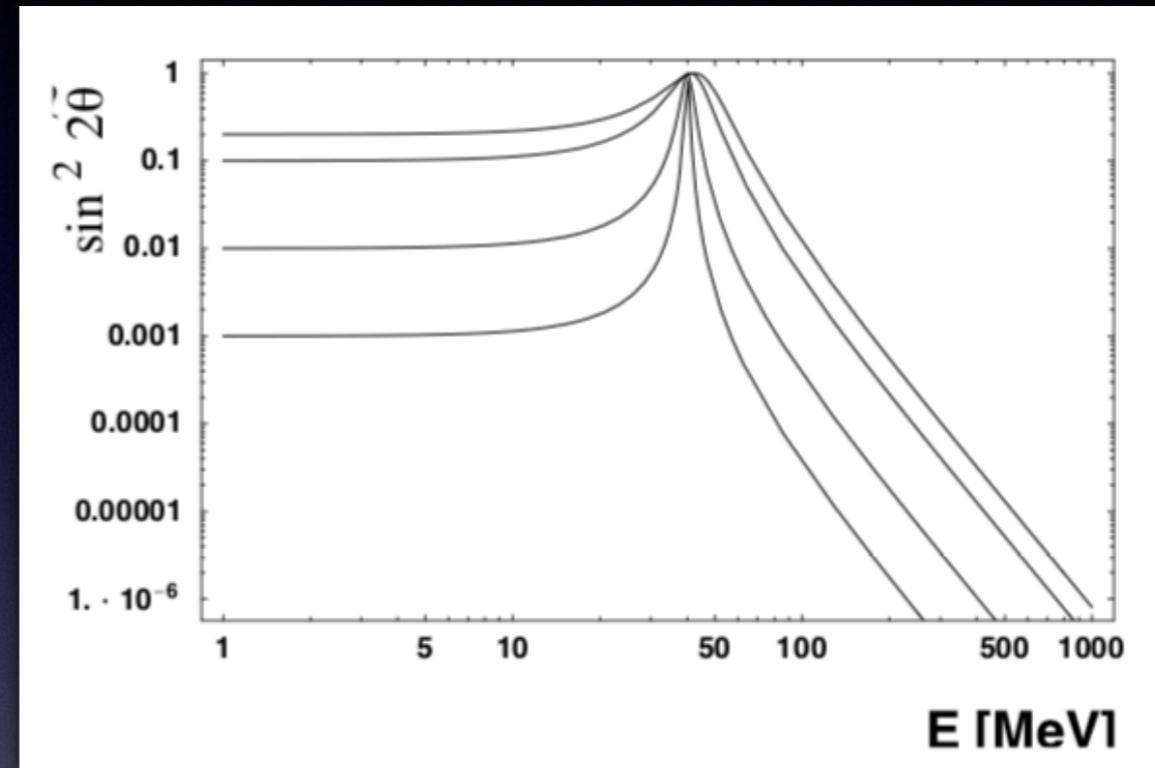
$\rightarrow$  choose  $E_{\text{res}} = 30\text{-}400 \text{ MeV} \leftrightarrow \epsilon \simeq 10^{-18} - 10^{-16}$

(Päs, Pakvasa, Weiler, 2005)

# Altered dispersion relations: vanilla type



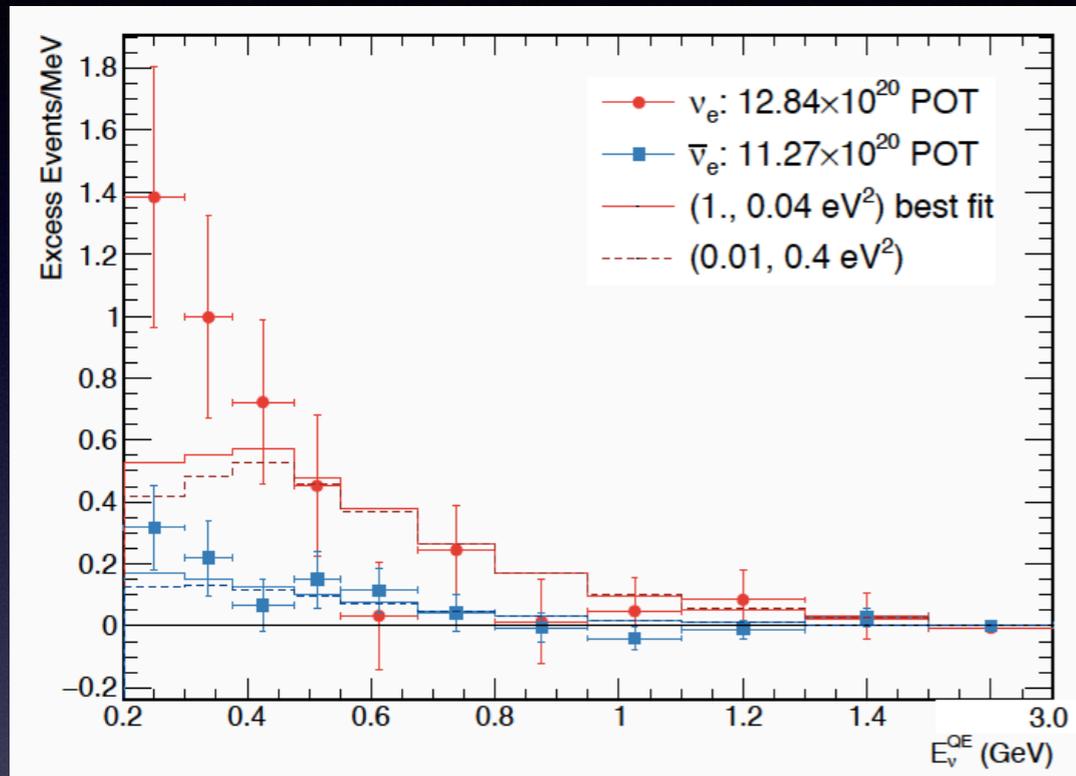
*MiniBooNE 2018*



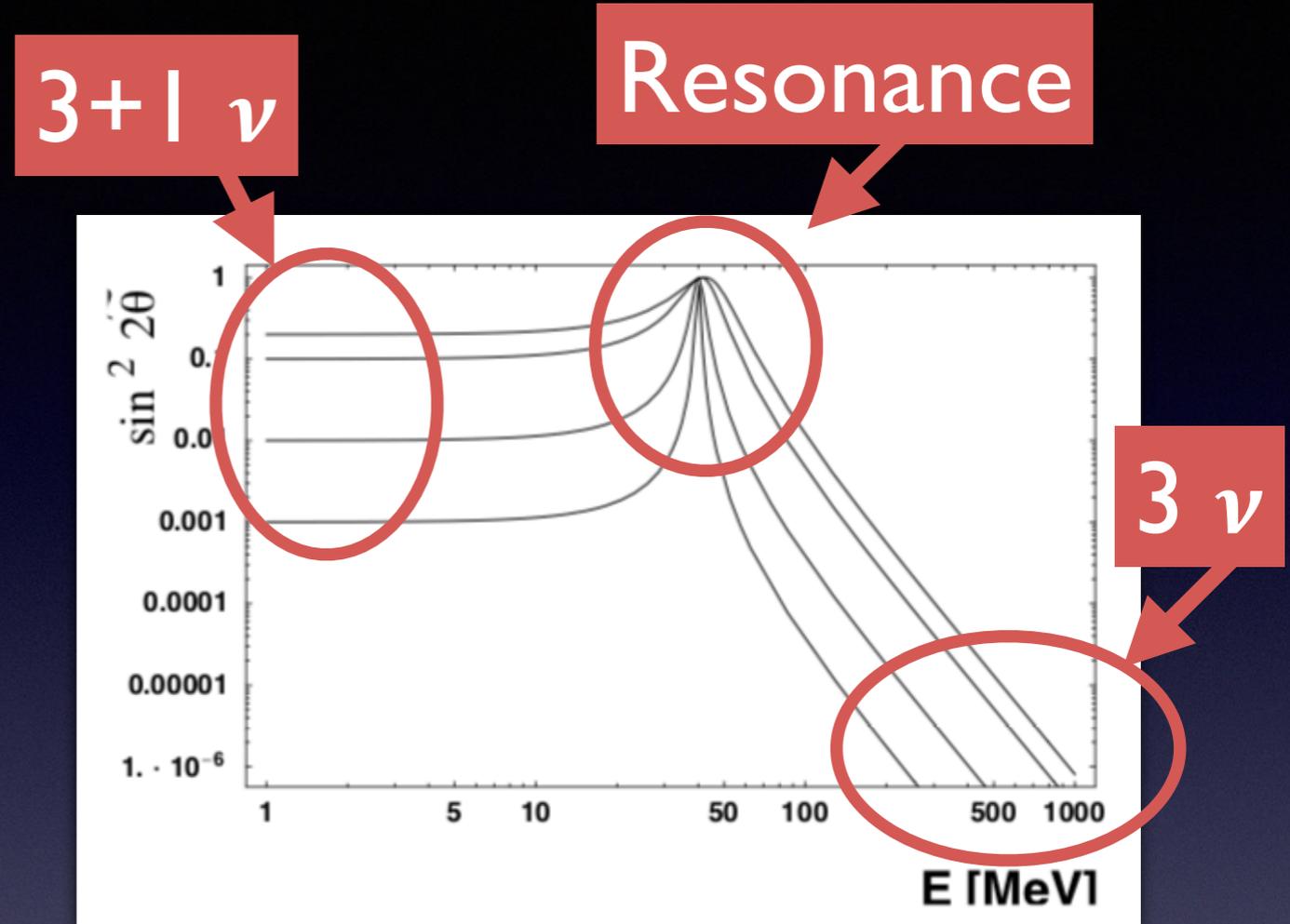
*HP, Pakvasa, Weiler 2005*

→ resonance-like features!

# Altered dispersion relations: vanilla type



*MiniBooNE 2018*



*HP, Pakvasa, Weiler 2005*

→ resonance-like features!

*[P. Huber, 2007]*

# Altered dispersion relations: vanilla type

*“A nice model -  
but unfortunately it doesn't work”*

*P. Huber*

# Altered dispersion relations with 3+1 neutrinos

$$\lambda_{4/3} \equiv \lambda_{\pm} = \frac{\Delta}{4E} \left( 1 - \cos 2\theta_{34} \left( \frac{E}{E_R} \right)^2 \pm \sqrt{\sin^2 2\theta_{34} + \cos^2 2\theta_{34} \left[ 1 - \left( \frac{E}{E_R} \right)^2 \right]^2} \right)$$

▶ 2 mass eigenstates with **large effective** masses!

▶ Large  $\Delta m^2$ 's

*[Marfatia, HP, Pakvasa, Weiler, 2012]*

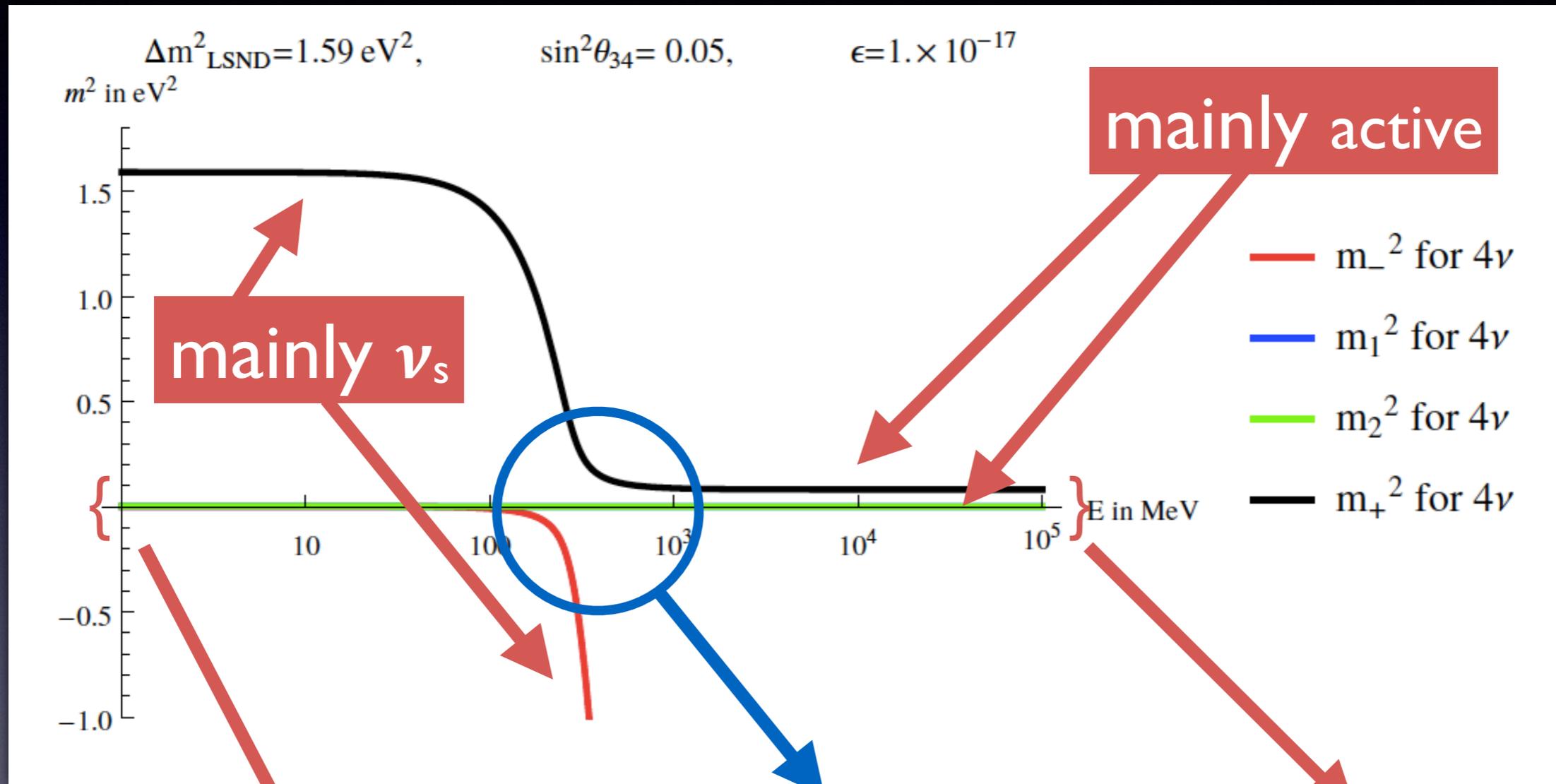
▶ Fast oscillations:

$$P(\nu_a \rightarrow \nu_b) = 4 V_{a3}^2 V_{b3}^2 \times \begin{cases} -\sin^2 \left( \frac{L(\lambda_+ - \lambda_-)}{2} \right) & \sin^2 \tilde{\theta} \cos^2 \tilde{\theta} \\ +\sin^2 \left( \frac{L\lambda_+}{2} \right) & \sin^2 \tilde{\theta} \\ +\sin^2 \left( \frac{L\lambda_-}{2} \right) & \cos^2 \tilde{\theta}. \end{cases}$$

▶ Sterile neutrino Lorentz violation **excluded by atmospheric  $\nu$  L/E !!!**

*[P. Huber, 2007]*

# Altered dispersion relations with 3+1 neutrinos



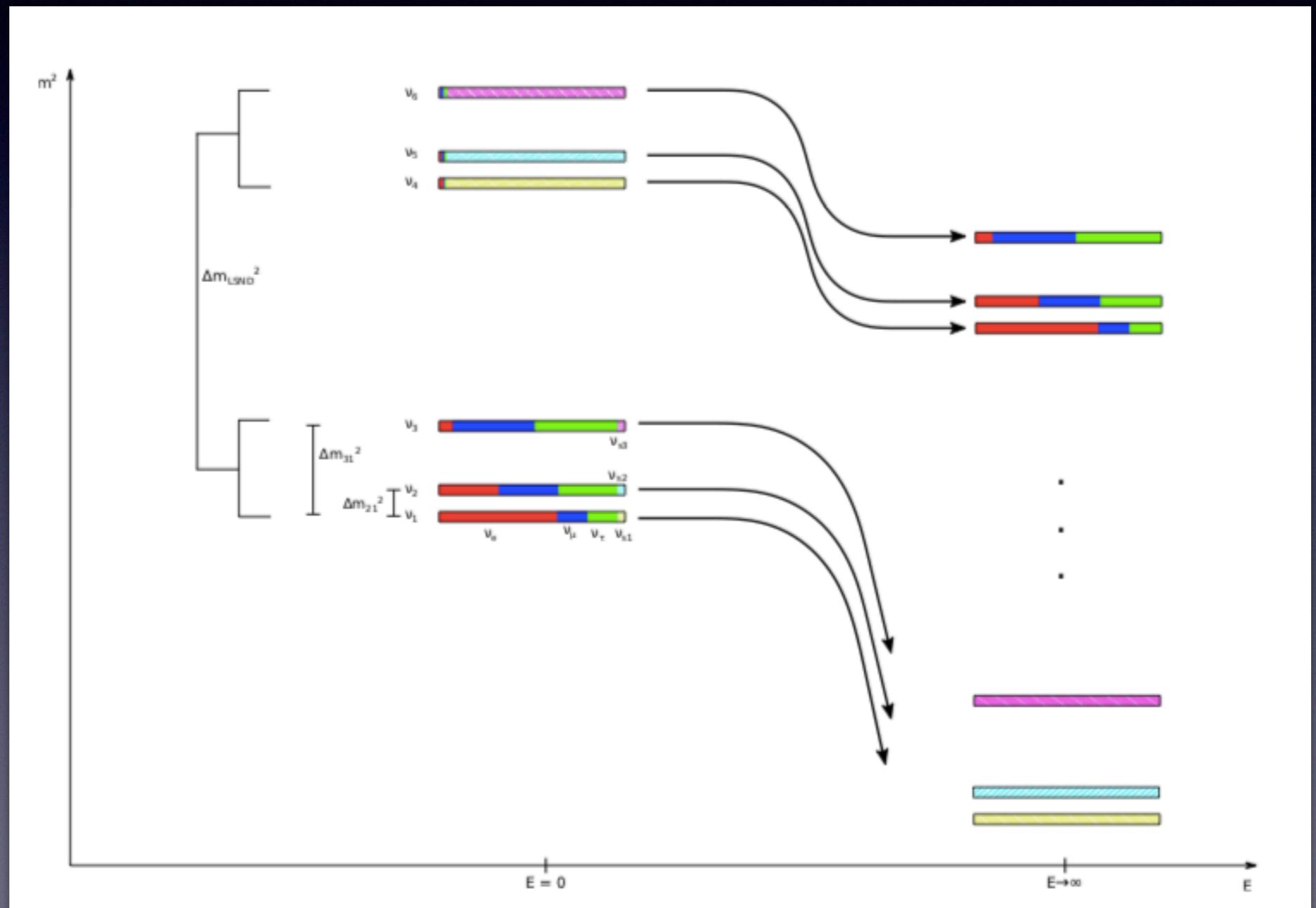
small  $\Delta m^2$

flavor swap  
level crossing gap

large  $\Delta m^2$

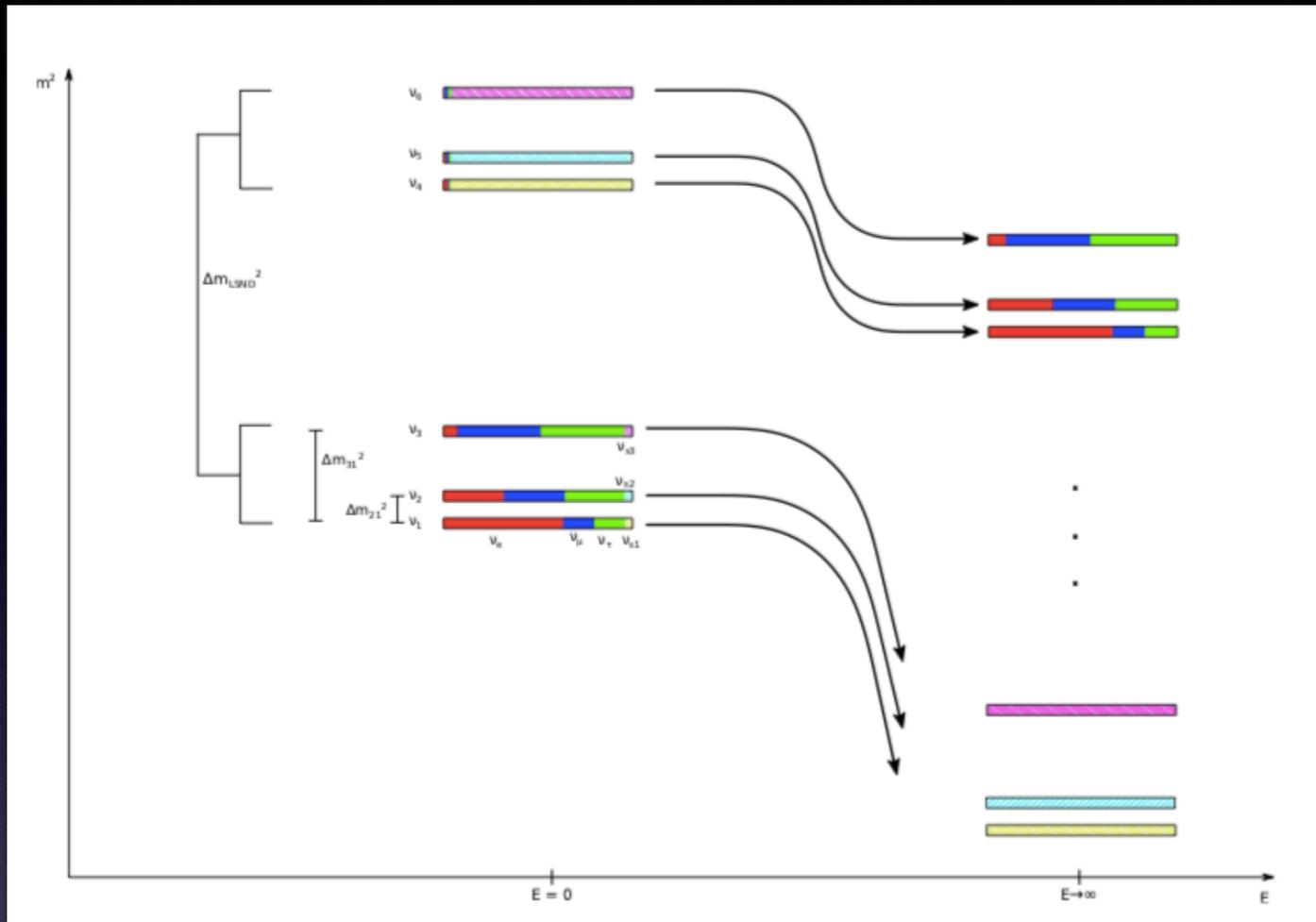
# Solution ?

→ Promote the model to 3+3



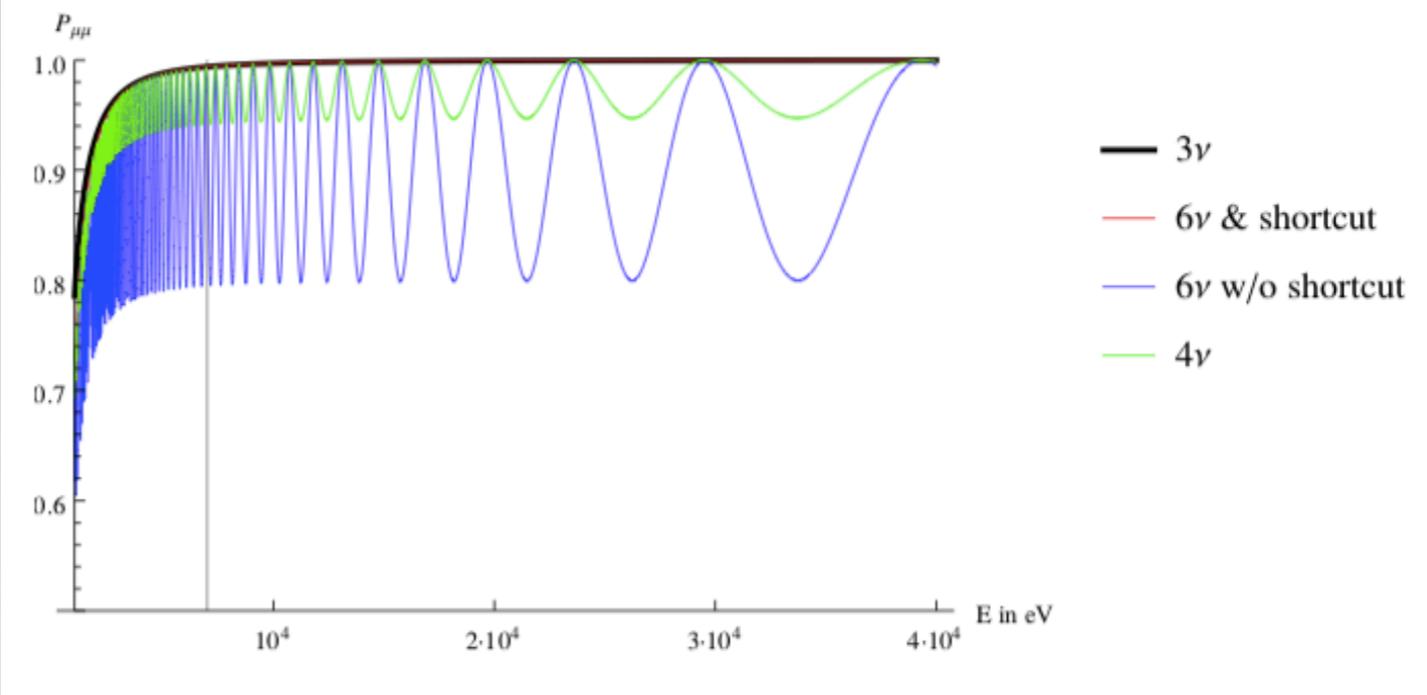
*Döring, HP, Sicking, Weiler, arXiv:1808.07460*

# Sterile Neutrinos?



In a 3+3 model with democratic mixing the sterile neutrino decouples completely at high energies

Probabilities @ MINOS FarDetector  
 $\Delta m^2_{\text{LSND}} = 1.59 \text{ eV}^2$ ,  $\sin^2 \theta = 0.0528$ ,  
 $\epsilon = 5 \cdot 10^{-17}$ ,  $\kappa = \xi = 100 = 5 \cdot 10^{-17}$ ,  $L = 735 \text{ km}$



*Döring, HP, Sickling,  
 Weiler,  
 arXiv:1808.07460*

# Altered dispersion relations with 3+3 neutrinos

Necessary: Different resonance energies for 3 sterile neutrinos to avoid unitarity cancellation!

$$V_{\text{eff}} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \varepsilon E & 0 & 0 \\ 0 & 0 & 0 & 0 & \kappa \cdot \varepsilon E & 0 \\ 0 & 0 & 0 & 0 & 0 & \xi \cdot \varepsilon E \end{pmatrix}.$$

*Döring, HP,  
Sicking, Weiler,  
arXiv:  
1808.07460*

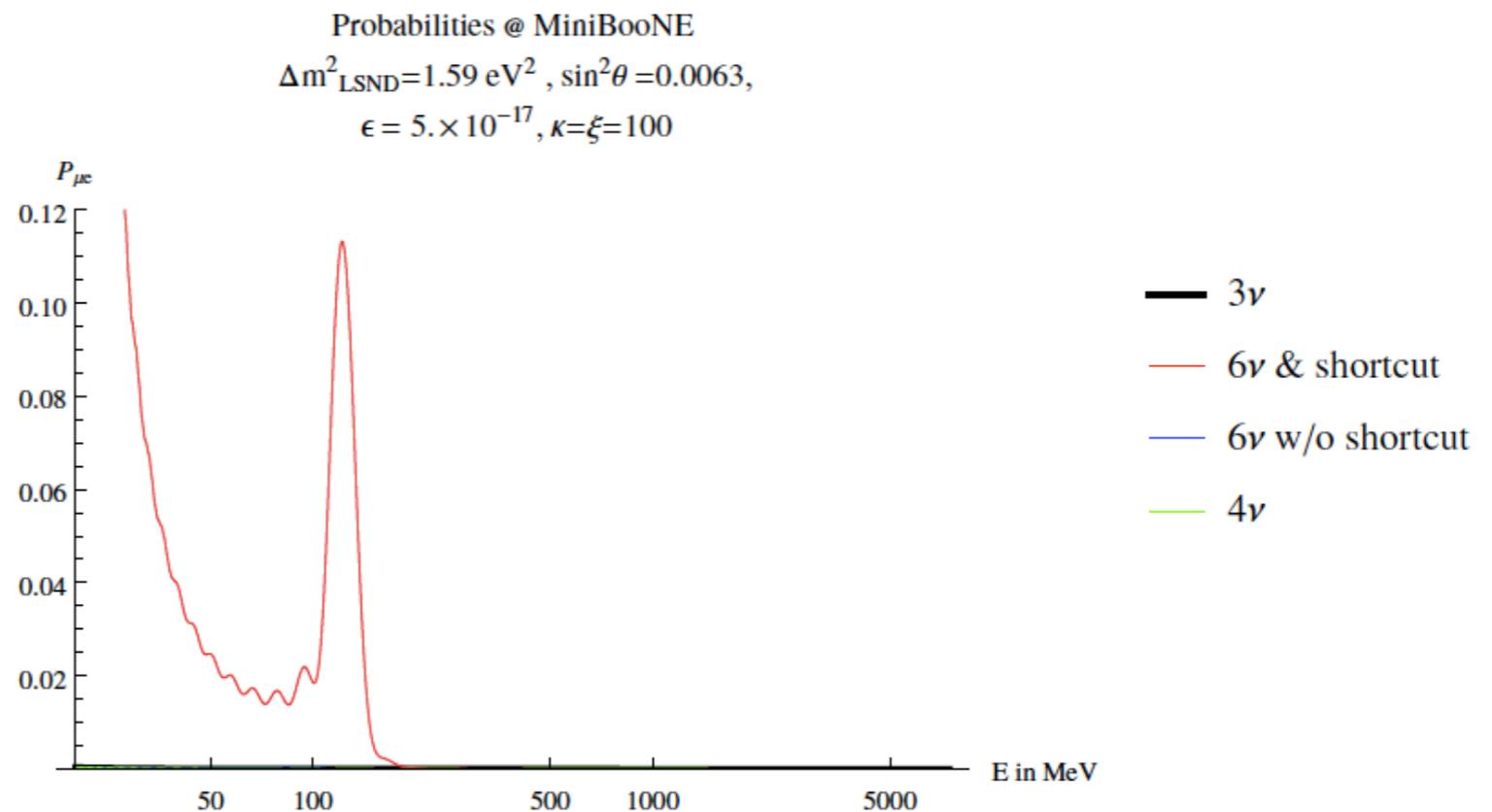
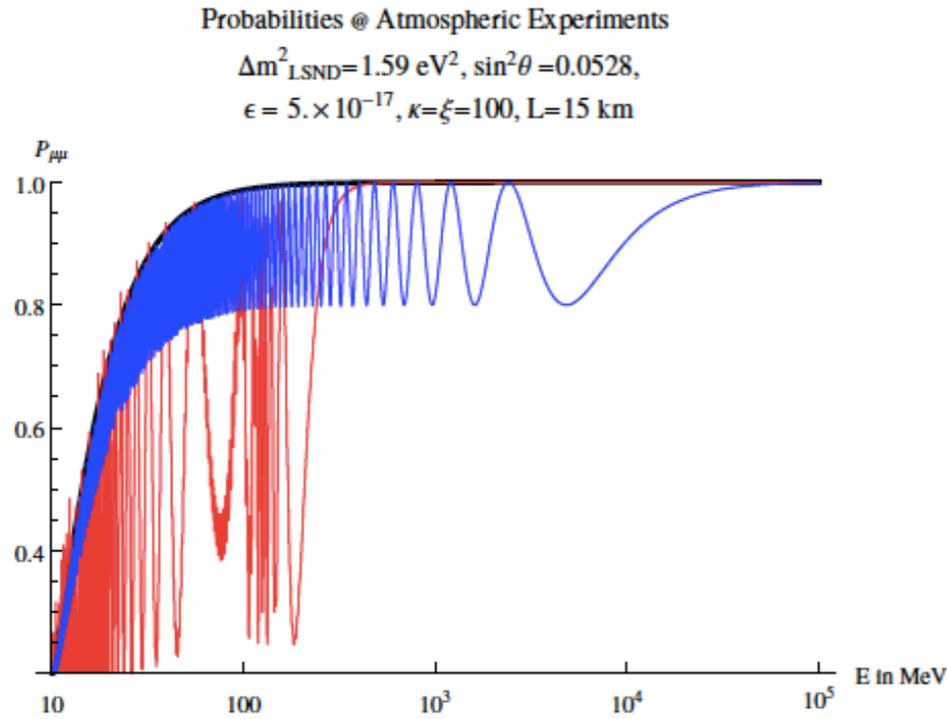
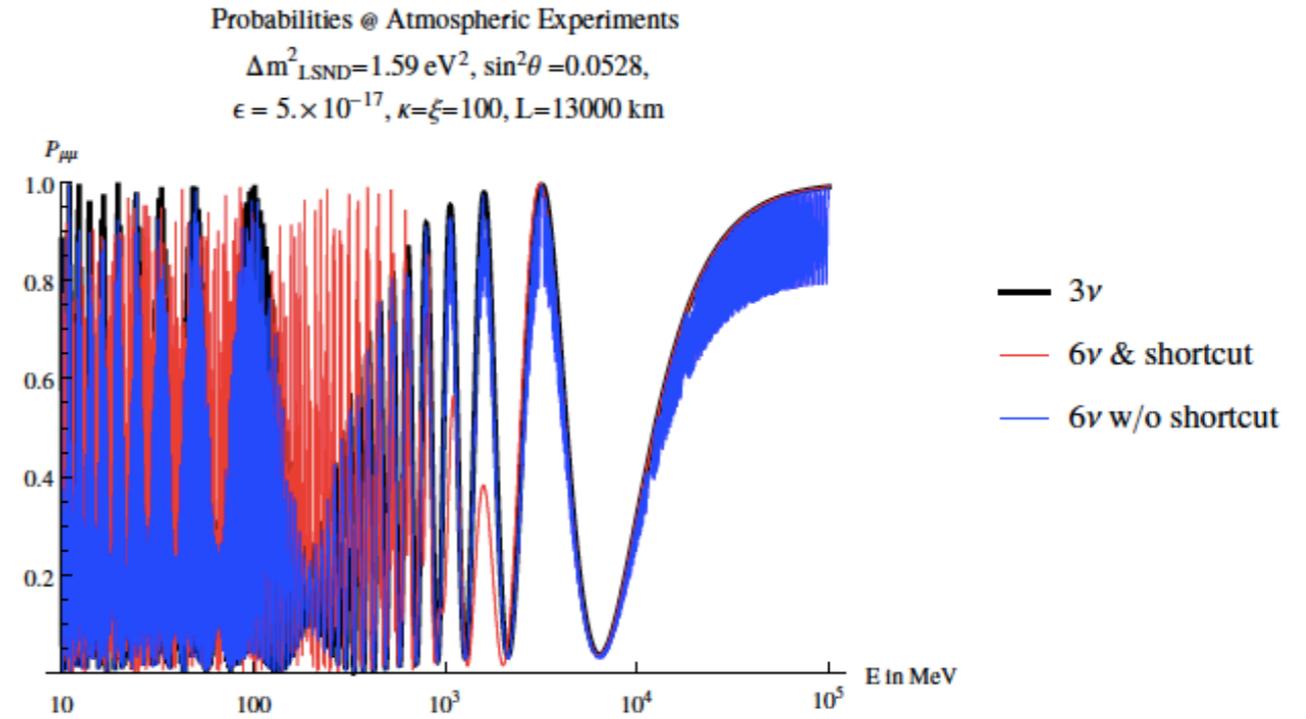


Figure: Probabilities  $P$  at MiniBooNE in the  $\nu_\mu \rightarrow \nu_e$  channel.

# sub-GeV Super-K data?

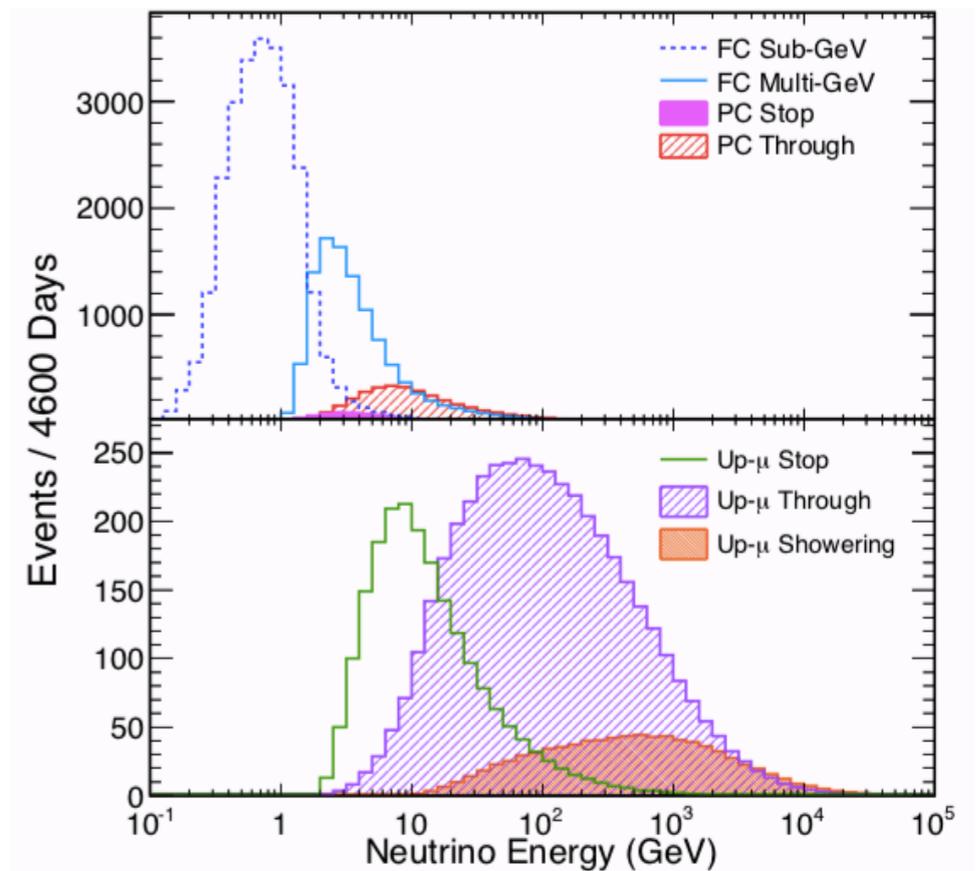


(a) Downward going neutrinos



(b) Upward going neutrinos

*Döring, HP, Sickling, Weiler,  
arXiv:1808.07460*



# Model Building ?

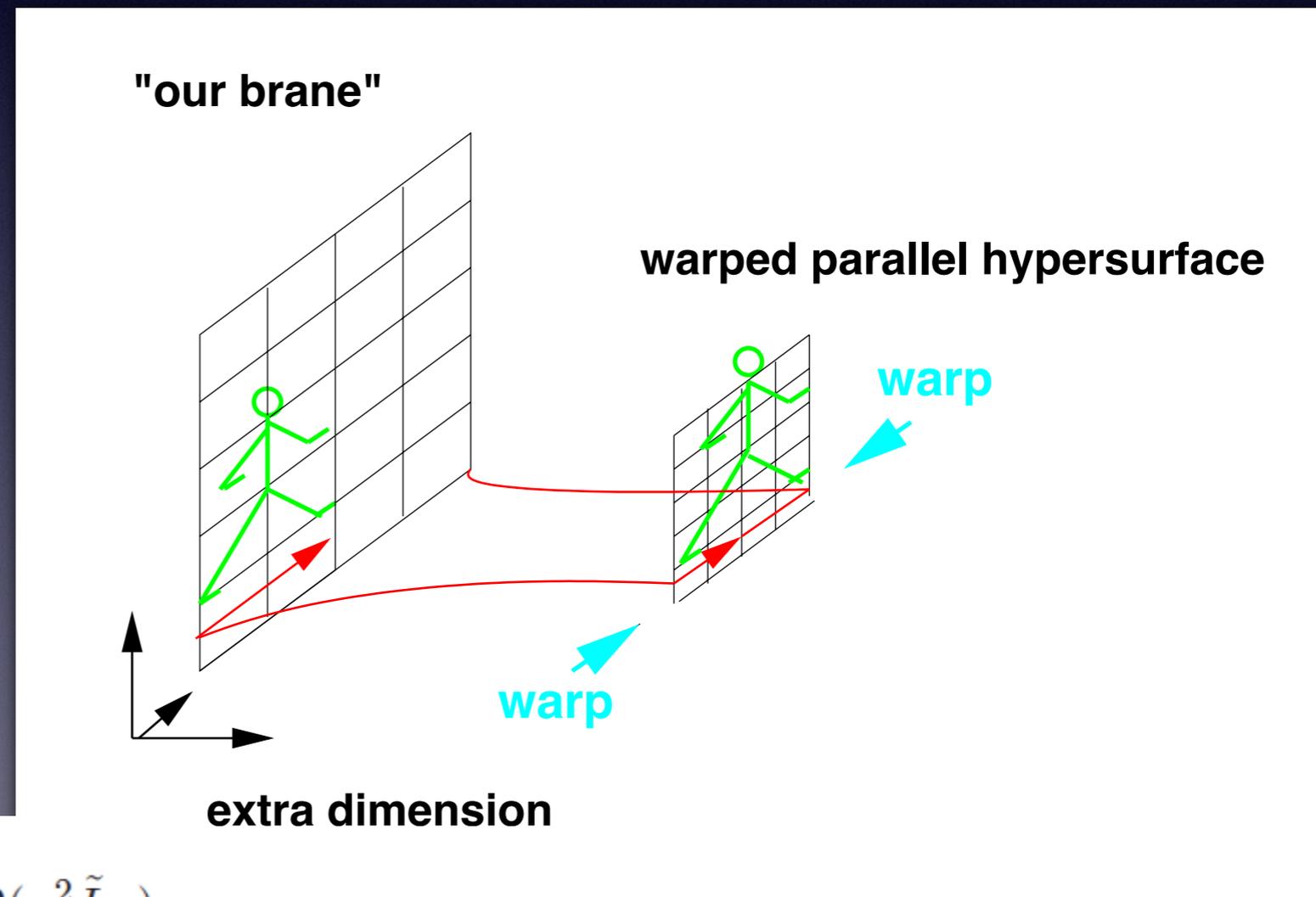
Consider an asymmetrically warped extra dimension  
with a sterile neutrino in the bulk

$$ds^2 = dt^2 - e^{-2k|u|} dx^2 - du^2$$

*Chung, Freese, 1999, 2000*  
*Csaki, Erlich, Grojean, 2001*

- ▶ Shrinks space parallel to the brane
- ▶ Allows for shortcuts in the extra dimension!

*[Döring, HP,  
arXiv:1808.07734*



$$p_{x/\xi} \approx E - \frac{\kappa^2}{2E} - \frac{E^2}{2E} \tilde{I}_{00} + \mathcal{O}(\tilde{I}_{00}^2) + \mathcal{O}(\kappa^2 \tilde{I}_{00})$$

# Summary

- ▶ Chances are high that MiniBooNE and other anomalies due to backgrounds or systematics
- ▶ Partially in conflict with other bounds
- ▶ But keep in mind: “1 eV<sup>2</sup> miracle”
- ▶ ADR  $\nu$  oscillations: energy dependence & resonant conversion
- ▶ ADR 3+3  $\nu$  model seems to explain all data !
- ▶ 4D EFT limit of  $\nu$  mass models in asymmetrically warped extra dimensions
- ▶ Potential to alleviate cosmological bounds