

# Electroweak penguin decays to leptons at LHCb

SUSY 2014, Manchester

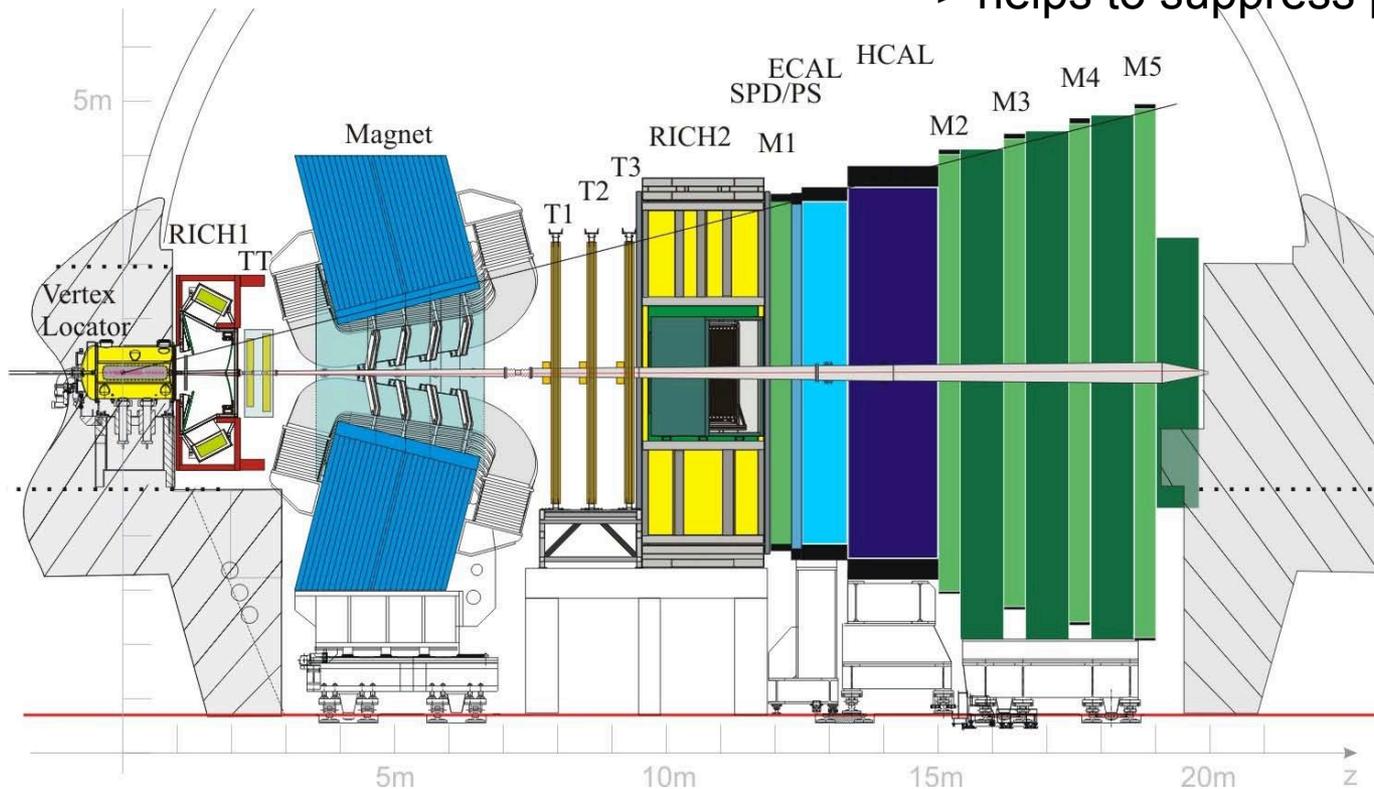
Christian Linn, CERN

on behalf of the LHCb Collaboration

## Forward spectrometer with acceptance optimized for b-hadrons: $2 < \eta < 5$

decay time resolution  $\sim 45$  fs  
 -> good separation of B vertices

excellent K -  $\pi$  separation  
 ( $\sim 95$  % for  $\sim 5$  %  $\pi \rightarrow K$  mis-id probability)  
 -> helps to suppress peaking background

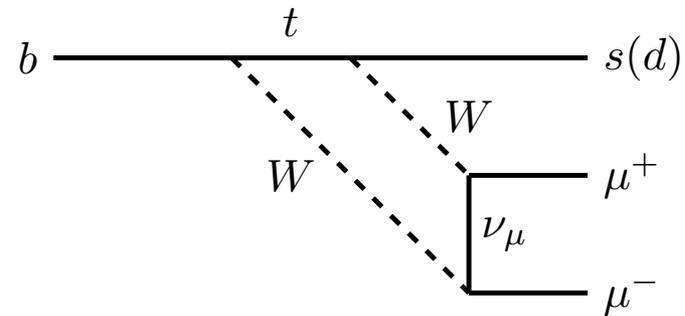
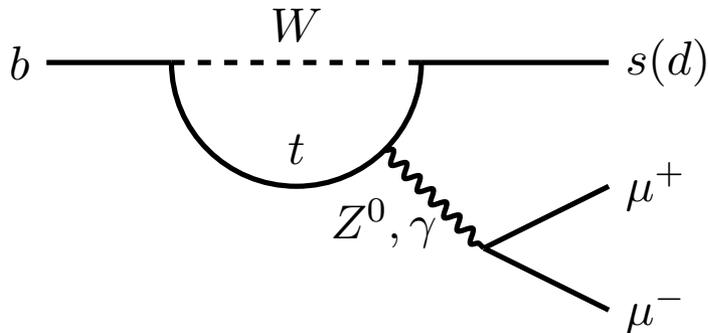


good momentum ( $\Delta p / p = 0.4 - 0.6$  %)  
 and mass resolution

excellent muon identification  
 ( $\sim 97$  % for 1-3 %  $\pi \rightarrow \mu$  mis-id probability)

+ very efficient trigger for di-muon channels  $\epsilon \approx 90$  %

FCNC as  $b \rightarrow sll$  transitions in the SM only possible via loop and box diagrams  
 -> highly suppressed / new particles can enter the loop and modify observables



$b \rightarrow sll$  decays can theoretically be described by effective hamiltonian:

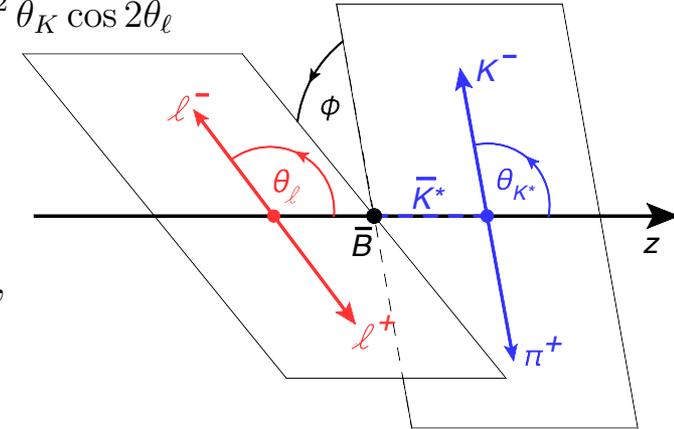
$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

- Operators  $\mathcal{O}_i$  depend on hadronic form factors (FF) of the decay  
 ( FF usually dominate theoretical uncertainties )
  
- Wilson coefficients  $C_i$  describe short distance effects – sensitive to NP contributions  
 -> **observables like branching fraction, CP asymmetries, angular distributions depend on  $C_i$**

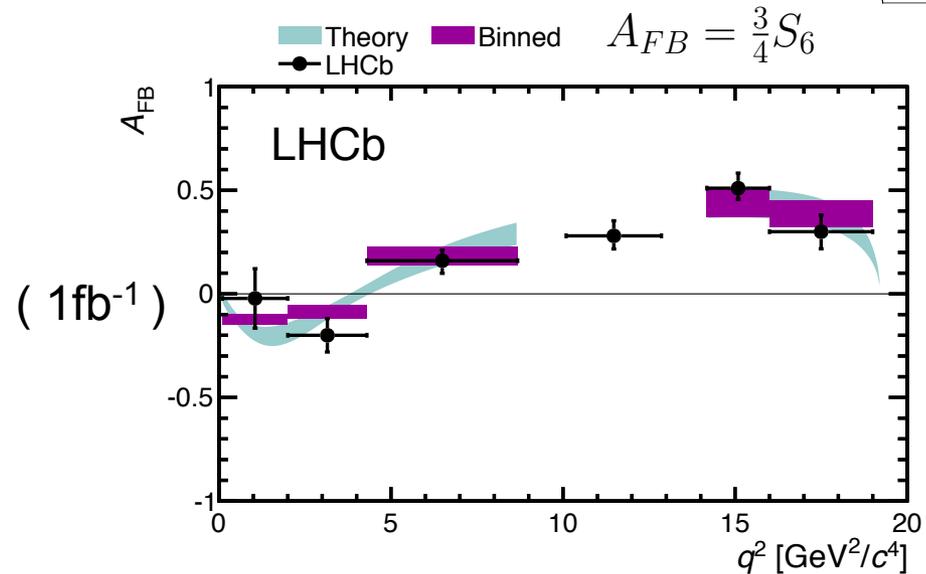
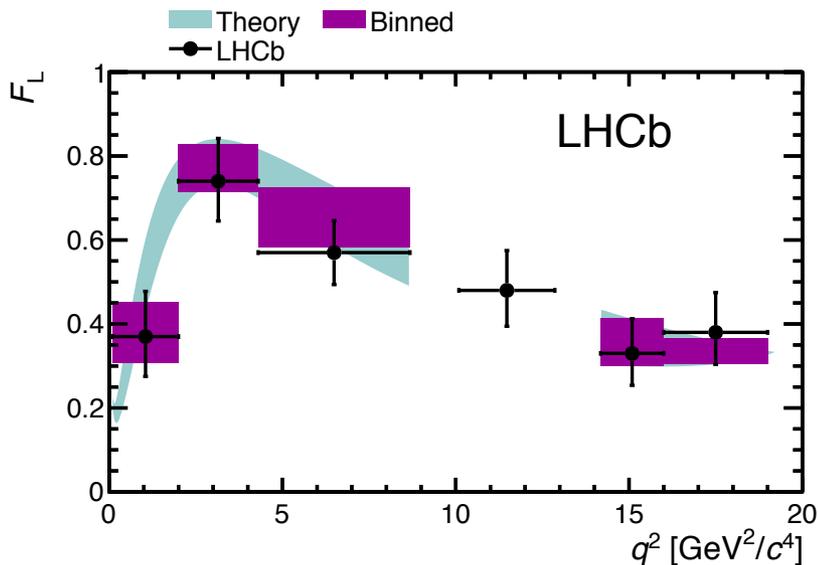
- Angular analysis of  $B^0 \rightarrow K^* \mu\mu$  (  $1\text{fb}^{-1}$  )  
JHEP 08 (2013) 131, Phys. Rev. Lett. 111 (2013) 191801  
  
and  $B^+ \rightarrow K^+ \mu\mu$ ,  $B^0 \rightarrow K_s^0 \mu\mu$  (  $3\text{fb}^{-1}$  )  
arXiv:1403.8045v2
- CP asymmetry of  $B^0 \rightarrow K^* \mu\mu$ ,  $B^+ \rightarrow K^+ \mu\mu$  (  $3\text{fb}^{-1}$  )  
LHCb-PAPER-2014-032, **PRELIMINARY**
- Branching fractions and isospin asymmetry of  $B \rightarrow K \mu\mu$  (  $3\text{fb}^{-1}$  )  
arXiv:1403.8044v3
- Ratio of branching fractions  $B^+ \rightarrow K^+ \mu\mu$  and  $B^+ \rightarrow K^+ ee$  (  $3\text{fb}^{-1}$  )  
arXiv:1406.6482v1
- Branching fractions of  $B^+ \rightarrow hhh \mu\mu$  (  $3\text{fb}^{-1}$  )  
LHCb-PAPER-2014-030, **PRELIMINARY**

$B^0 \rightarrow K^* \mu \mu$  described by three angles ( $\theta_K, \theta_\ell, \Phi$ ) and di-muon mass squared,  $q^2$ :

$$\frac{1}{d\Gamma/dq^2 d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right. \\ \left. + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right],$$



Observables extracted from 4d fit – in bins of  $q^2$

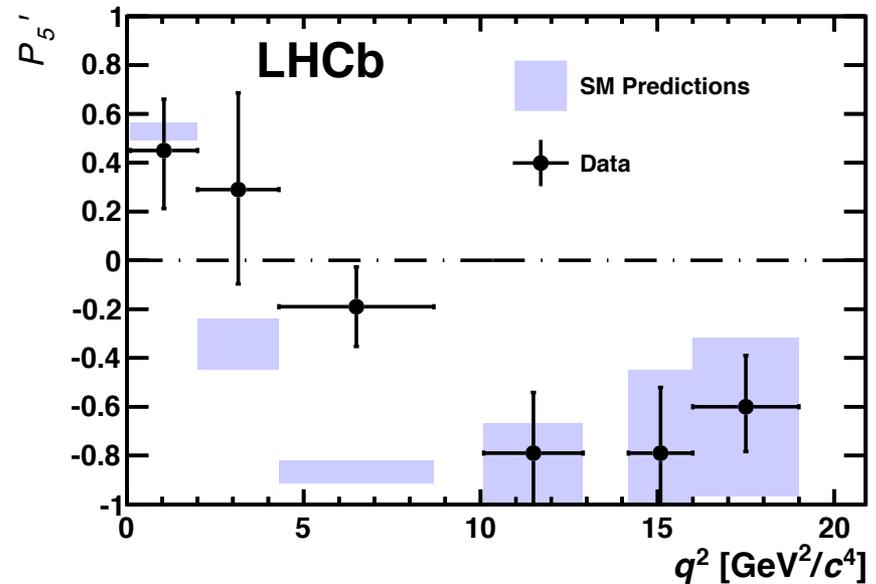
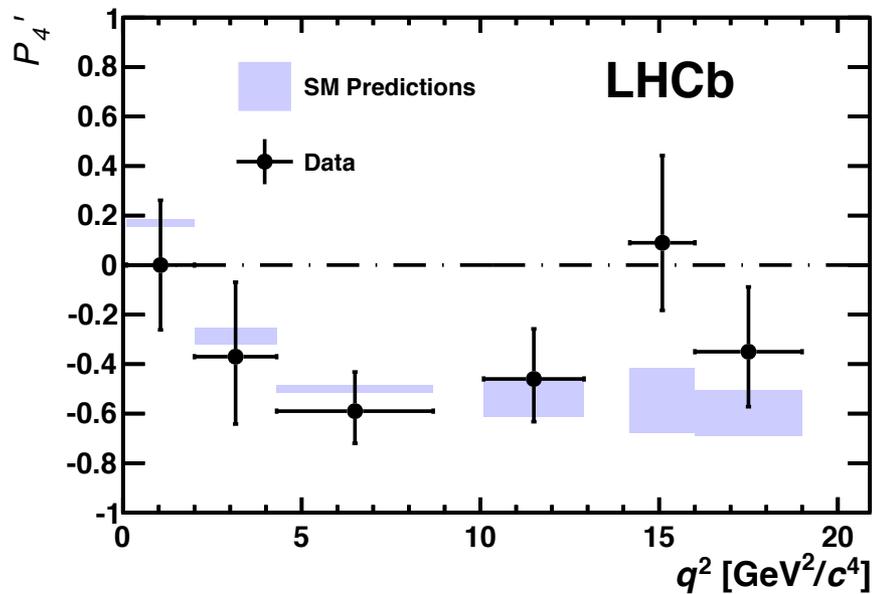


Zero-crossing point of  $A_{FB}$  in SM largely free from form-factor uncertainties:

$$q_0^2 = 4.9 \pm 0.9 \text{ GeV}^2/c^4 \rightarrow \text{consistent with SM predictions ( 3.9 – 4.4 GeV}^2/c^4 \text{ )}$$

Form-factor independent observables:  $P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$

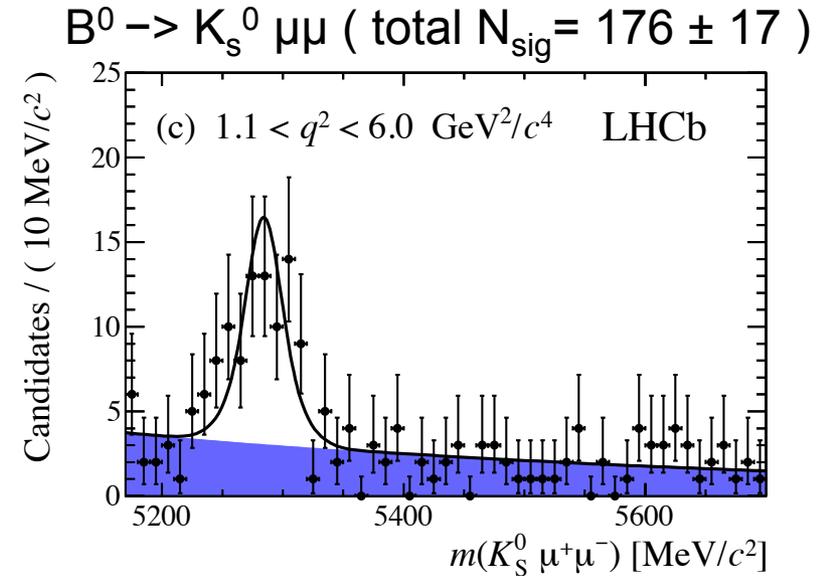
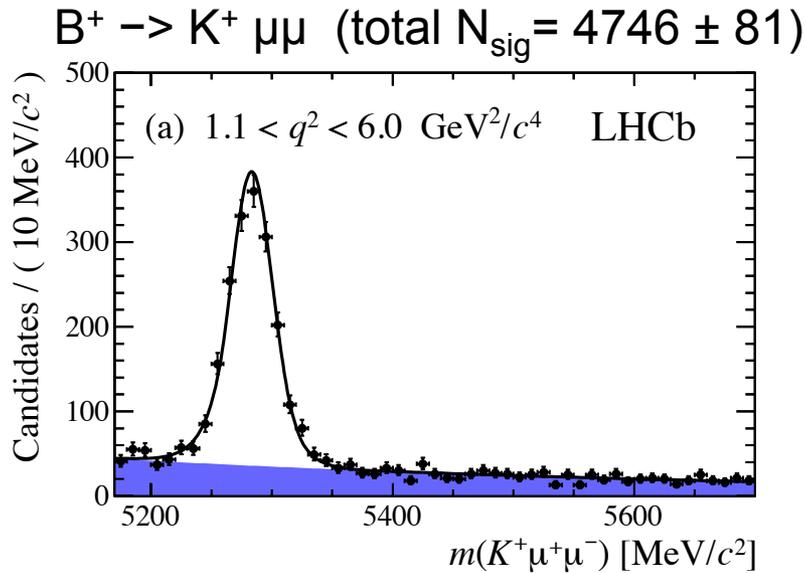
Observables extracted separately from different fits to dataset:



- In general good agreement with SM expectation, discrepancy for  $P'_5$  in 3<sup>rd</sup>  $q^2$  bin
- P-value for observed deviation is 0.02% (  $3.7\sigma$  )

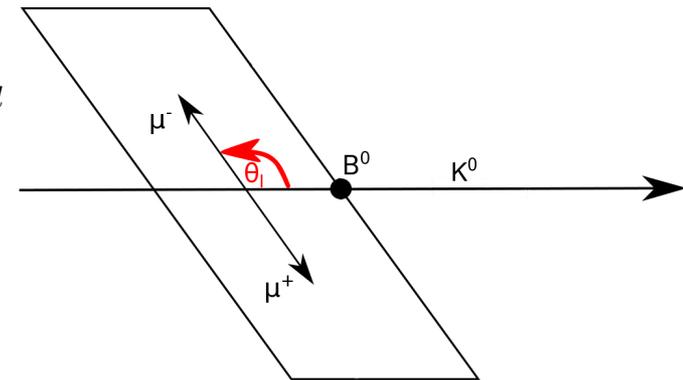
possible reasons: smaller Wilson coefficient  $C_9$  with respect to SM

## Angular analysis of



$$B^+ \rightarrow K^+ \mu\mu: \quad \frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_l} = \frac{3}{4} (1 - F_H) (1 - \cos^2 \theta_l) + \frac{1}{2} F_H + A_{\text{FB}} \cos \theta_l$$

$$B^0 \rightarrow K_s^0 \mu\mu: \quad \frac{1}{\Gamma} \frac{d\Gamma}{d |\cos \theta_l|} = \frac{3}{2} (1 - F_H) (1 - |\cos \theta_l|^2) + F_H$$



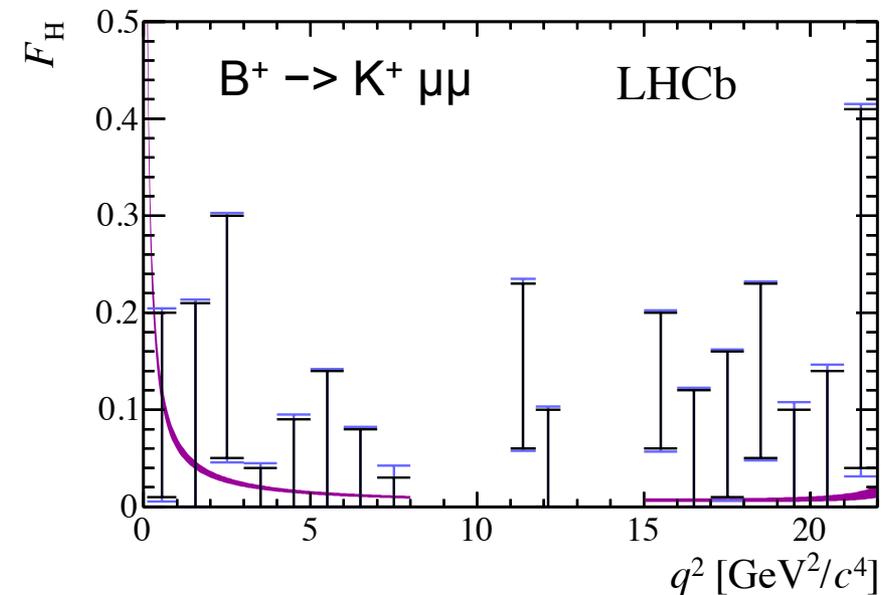
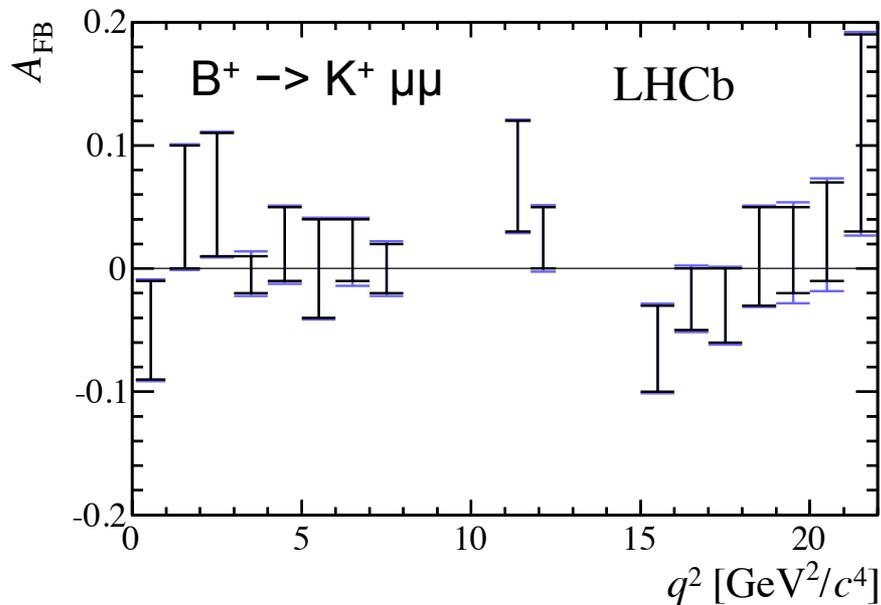
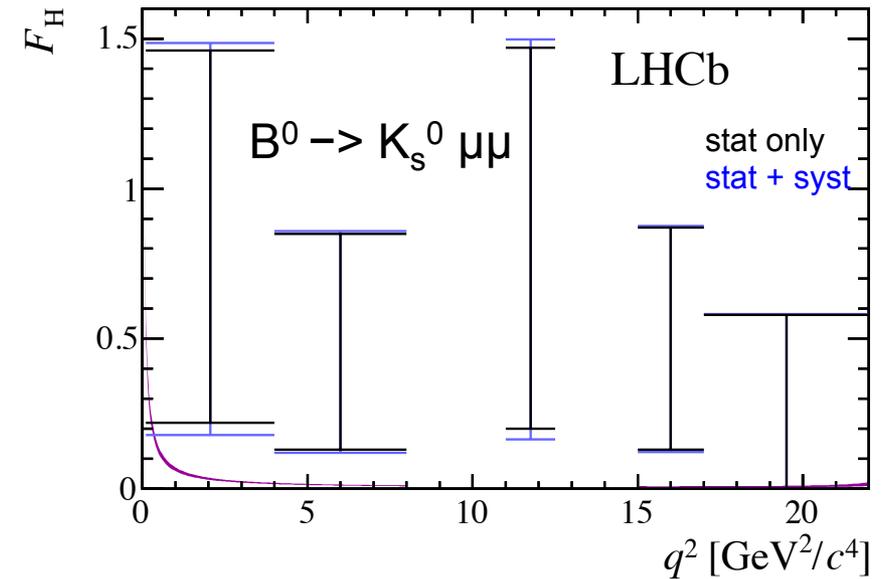
$A_{\text{FB}}$ : forward backward asymmetry of di-muon system  $\rightarrow$  zero in SM

$F_H$ : fractional contribution of (pseudo)scalar + tensor amplitudes  $\rightarrow$  small in SM

Parameters extracted from 2d fit ( mass – angle )

➤ in bins of  $q^2$

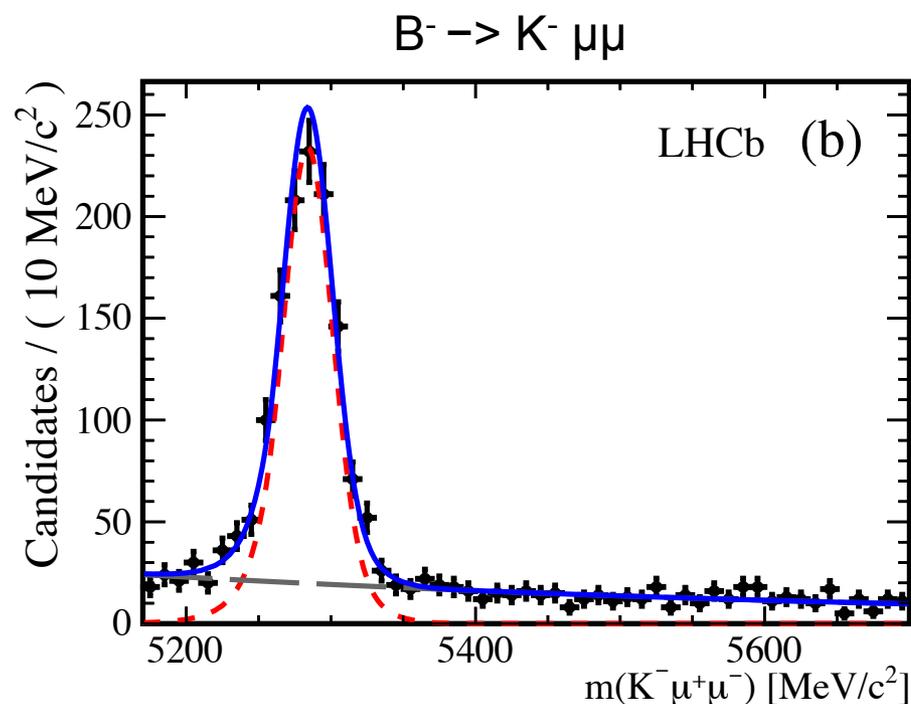
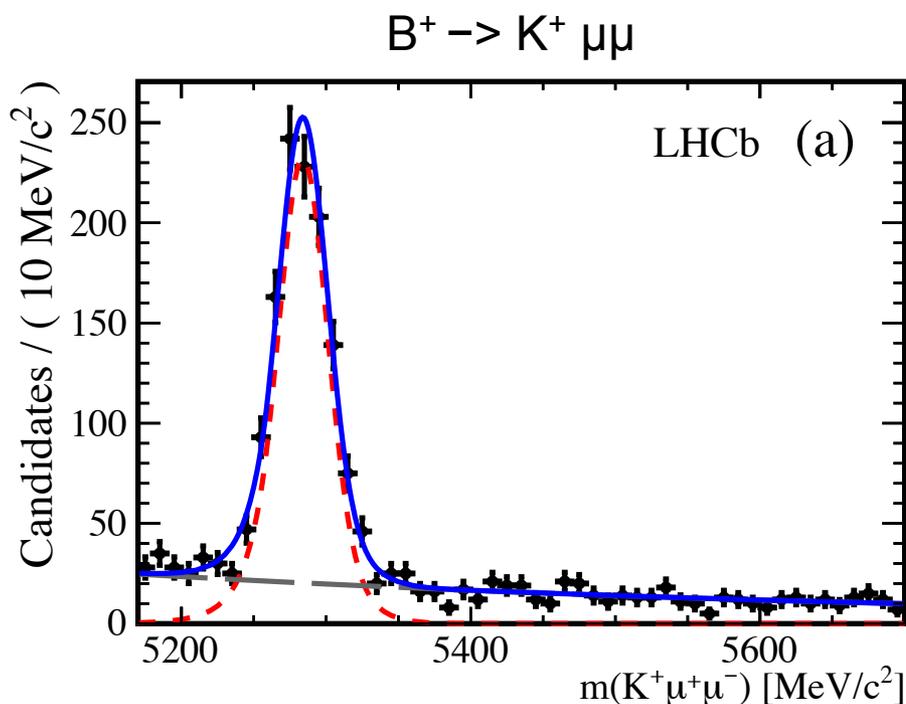
-> most precise to date + consistent with SM



CP asymmetries of  $B^+ \rightarrow K^+ \mu \mu$  and  $B^0 \rightarrow K^* \mu \mu$

$$\mathcal{A}_{\text{CP}} = \frac{\Gamma(\bar{B} \rightarrow \bar{K}^{(*)} \mu^+ \mu^-) - \Gamma(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\Gamma(\bar{B} \rightarrow \bar{K}^{(*)} \mu^+ \mu^-) + \Gamma(B \rightarrow K^{(*)} \mu^+ \mu^-)}$$

➤ SM prediction is  $O(10^{-3})$ , JHEP 01 (2009) 019

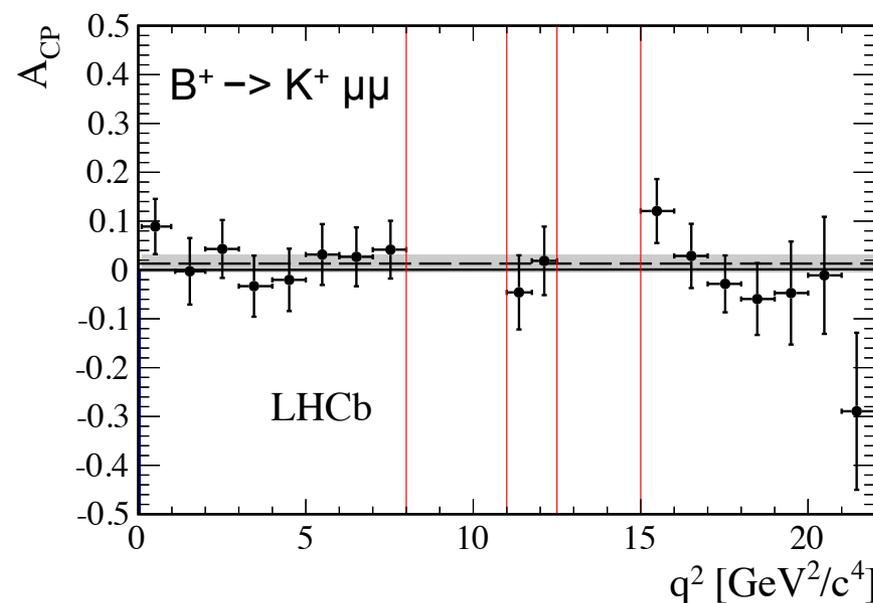
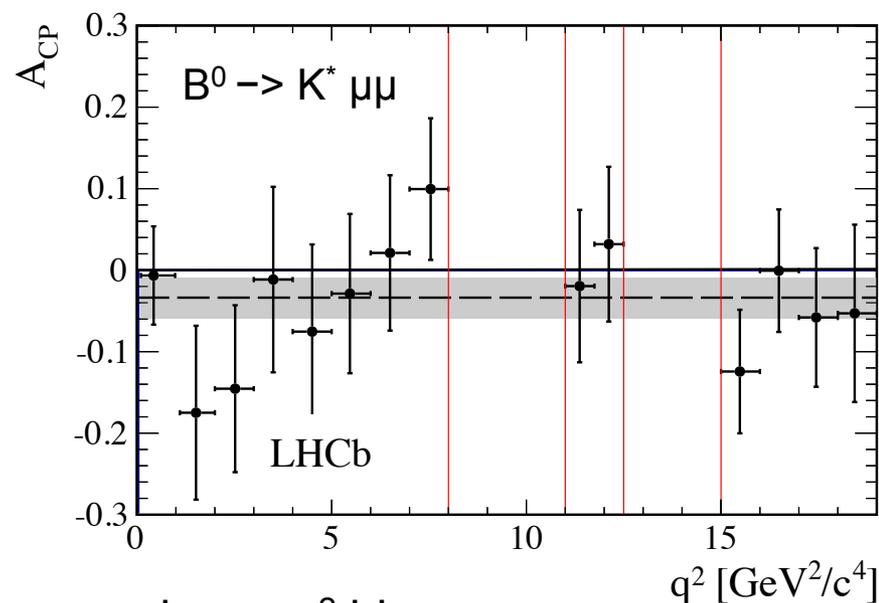


Yields give raw asymmetry  $A_{\text{RAW}} \rightarrow$  contaminated by production and detection asymmetries

$$A_{\text{CP}}(B \rightarrow K^{(*)} \mu^+ \mu^-) = \mathcal{A}_{\text{RAW}}(B \rightarrow K^{(*)} \mu^+ \mu^-) - \mathcal{A}_{\text{RAW}}(B \rightarrow J/\Psi K^{(*)})$$

$A_{\text{CP}}(B \rightarrow J/\Psi K^{(*)})$  assumed to be zero

difference removes production and detection efficiencies



averaged over  $q^2$  bins:

$$A_{\text{CP}}(B^* \rightarrow K^* \mu^+ \mu^-) = -0.035 \pm 0.024(\text{stat}) \pm 0.003(\text{syst})$$

$$A_{\text{CP}}(B^0 \rightarrow K^0 \mu^+ \mu^-) = 0.012 \pm 0.017(\text{stat}) \pm 0.001(\text{syst})$$

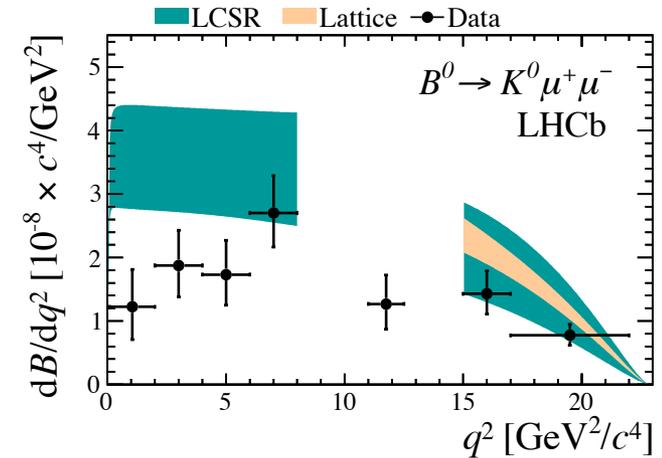
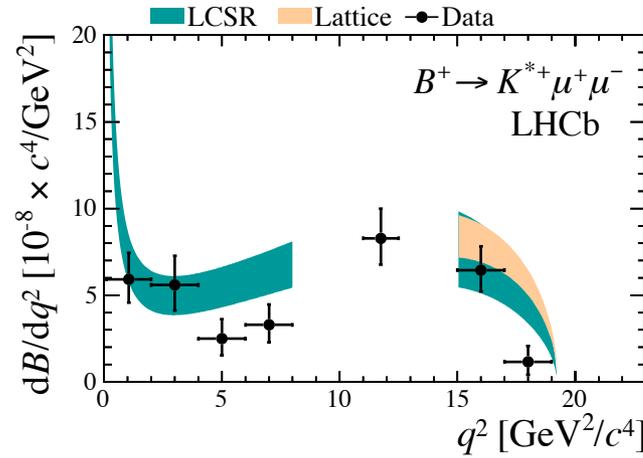
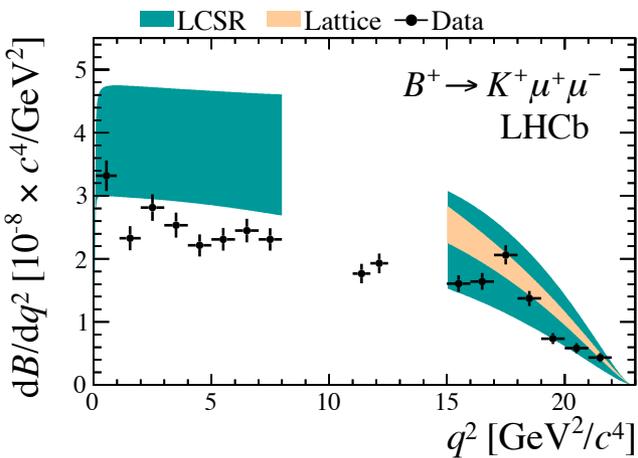
$\rightarrow$  consistent with SM prediction

- Branching fraction measurement for  $B^0 \rightarrow K^0 \mu \mu$ ,  $B^+ \rightarrow K^+ \mu \mu$  and  $B^+ \rightarrow K^{*+} \mu \mu$   
(  $B^0 \rightarrow K^{*0} \mu \mu$  to be updated soon with detailed study of s-wave contribution )

- Full Run-2 dataset (  $3\text{fb}^{-1}$  )

- normalized to resonant  $B \rightarrow J/\Psi K$  channels

Decay mode	Signal yield
$B^+ \rightarrow K^+ \mu^+ \mu^-$	$4746 \pm 81$
$B^0 \rightarrow K_s^0 \mu^+ \mu^-$	$176 \pm 17$
$B^+ \rightarrow K^{*+} (\rightarrow K_s^0 \pi^+) \mu^+ \mu^-$	$162 \pm 16$
$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$	$2361 \pm 56$



extrapolated to full  $q^2$  range:

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.29 \pm 0.07(\text{stat}) \pm 0.21(\text{syst})) \cdot 10^{-7}$$

$$\mathcal{B}(B^0 \rightarrow K^0 \mu^+ \mu^-) = (3.27 \pm 0.34(\text{stat}) \pm 0.17(\text{syst})) \cdot 10^{-7}$$

$$\mathcal{B}(B^+ \rightarrow K^{*+} \mu^+ \mu^-) = (39.24 \pm 0.93(\text{stat}) \pm 0.67(\text{syst})) \cdot 10^{-7}$$

main systematic uncertainty:  $B \rightarrow J/\Psi K$  branching fraction

- > more precise than world average
- > consistent with predictions but favors lower values

- Isospin asymmetry is determined from measured branching fractions:

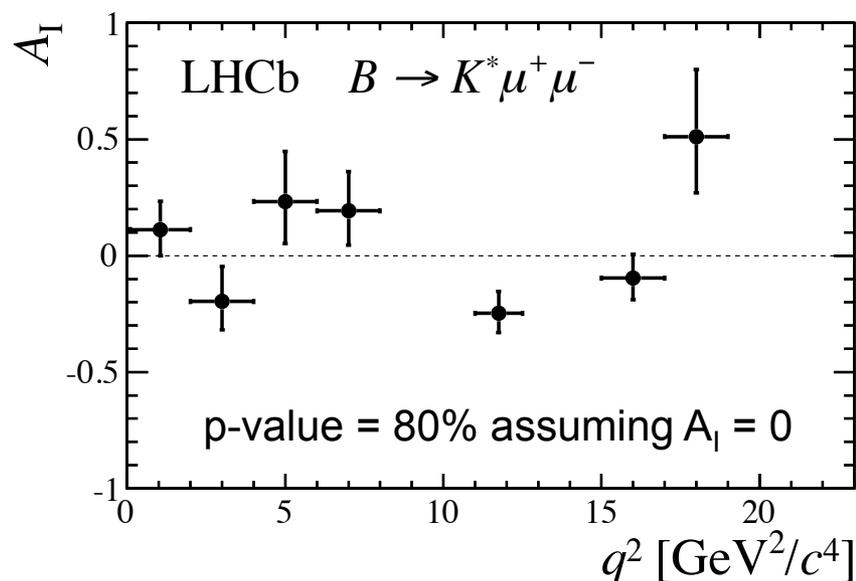
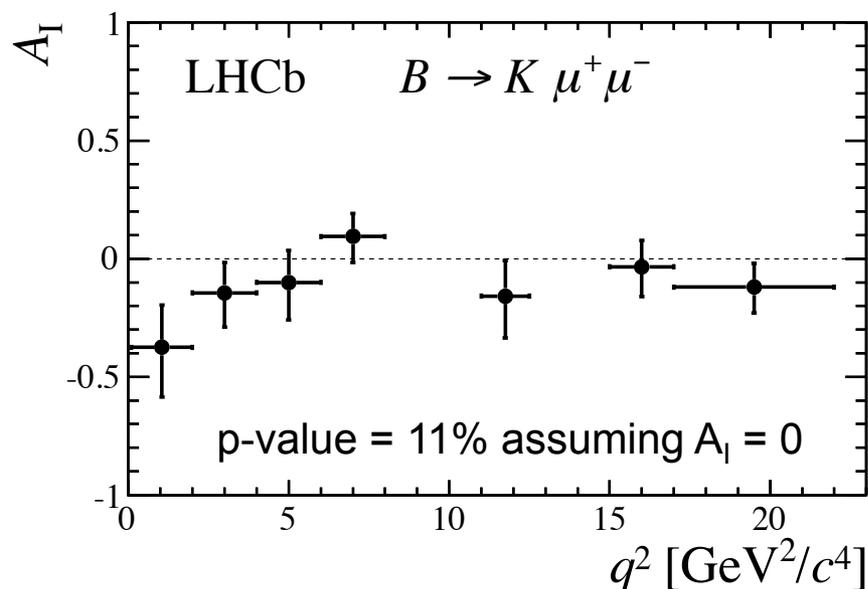
$$A_I = \frac{\mathcal{B}(B^0 \rightarrow K^{(*)0} \mu^+ \mu^-) - (\tau_0/\tau_+) \mathcal{B}(B^+ \rightarrow K^{(*)+} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{(*)0} \mu^+ \mu^-) + (\tau_0/\tau_+) \mathcal{B}(B^+ \rightarrow K^{(*)+} \mu^+ \mu^-)}$$

- SM prediction is O(1%) below J/Ψ resonance, even smaller above

JHEP 01 (2003) 074, JHEP 02 (2013) 010, Phys. Rev D88 (2013) 094004

- previous measurements from Babar, Belle, LHCb (1fb<sup>-1</sup>)

Phys. Rev. D86 (2012) 032012, Phys. Rev. Lett. 103 (2009) 171801, JHEP 07 (2012) 133



supersedes previous LHCb result ( quoted  $4.4\sigma$  difference to zero )

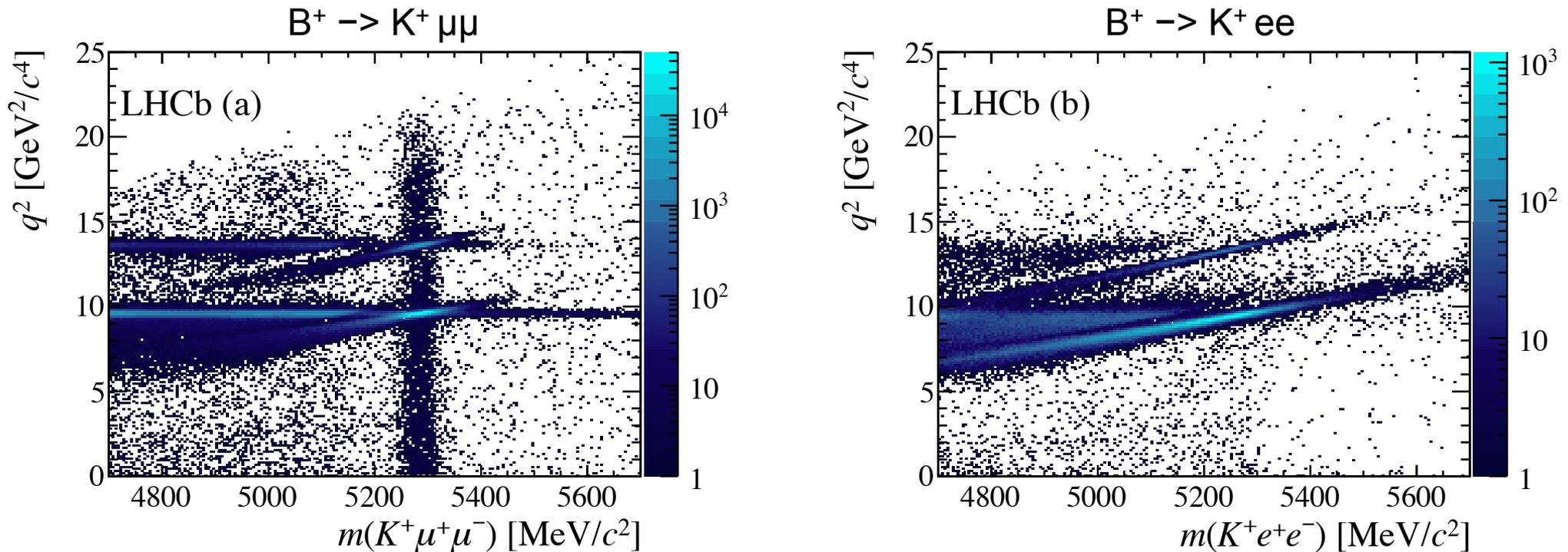
->inclusion of 2012 dataset, updated reconstruction and selection, changes in test statistics

Ratio of branching fractions of  $B^+ \rightarrow K^+ \mu\mu$  and  $B^+ \rightarrow K^+ ee$ :

$$R_K = \frac{\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\Gamma(B^+ \rightarrow K^+ e^+ e^-)}$$

- Lepton universality in SM  $\rightarrow R_K$  predicted to be 1 in SM within  $O(10^{-3})$   
JHEP 12 (2007) 040, Phys. Rev. Lett. 111 (2013) 162002

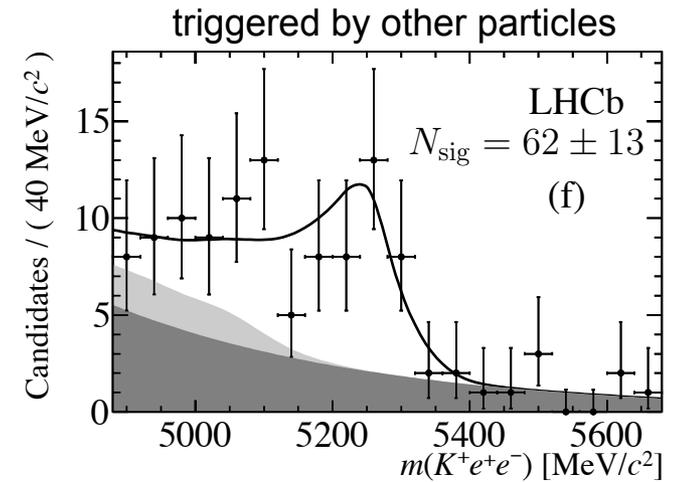
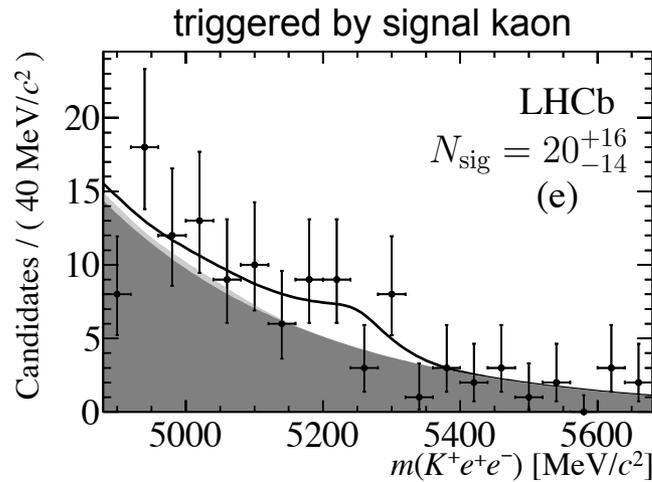
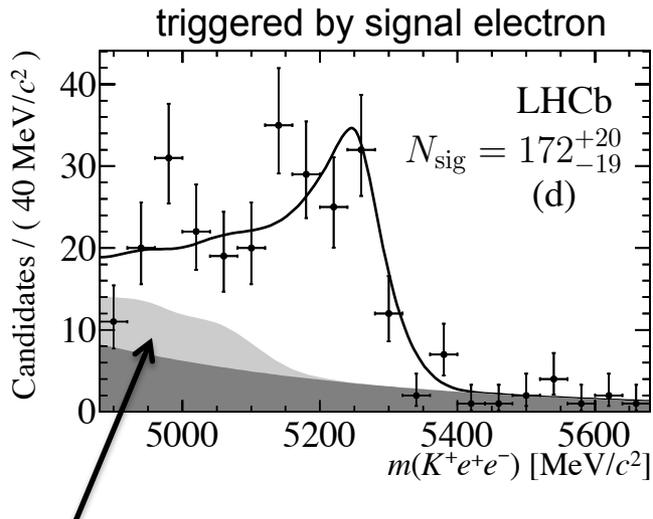
- First measurement of LHCb, uses full  $3\text{fb}^{-1}$  dataset - in  $1 < q^2 < 6 \text{ GeV}^2/c^4$



- $R_K$  measured as ratio of relative branching fractions between  $B^+ \rightarrow K^+ \mu\mu$  and  $B^+ \rightarrow J/\Psi K^+ \mu\mu$   
 $\rightarrow$  cancellation of systematic uncertainties

$B^+ \rightarrow K^+ ee$  mass shape affected by

- number of bremsstrahlung photons, transverse momentum of electron and occupancy
- > sample divided in three trigger categories /  $B^+ \rightarrow J/\psi K^+$  to investigate shape dependence

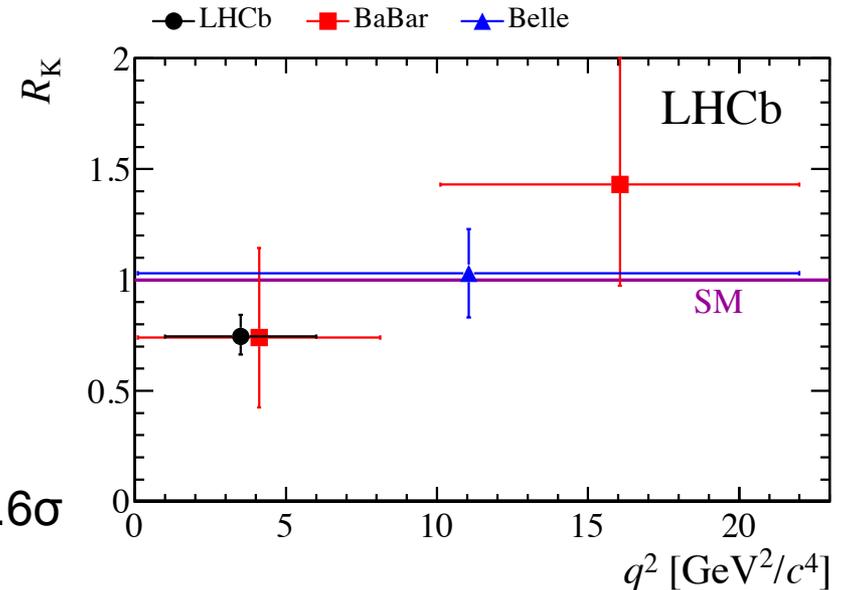


partially reconstructed background: mainly  $B^0 \rightarrow K^* ee$

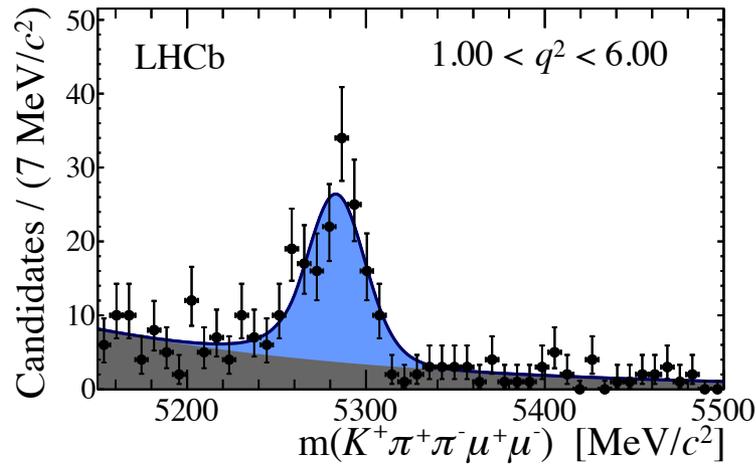
Combined result:

$$R_K = 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$$

-> most precise to date, compatible with SM within  $2.6\sigma$

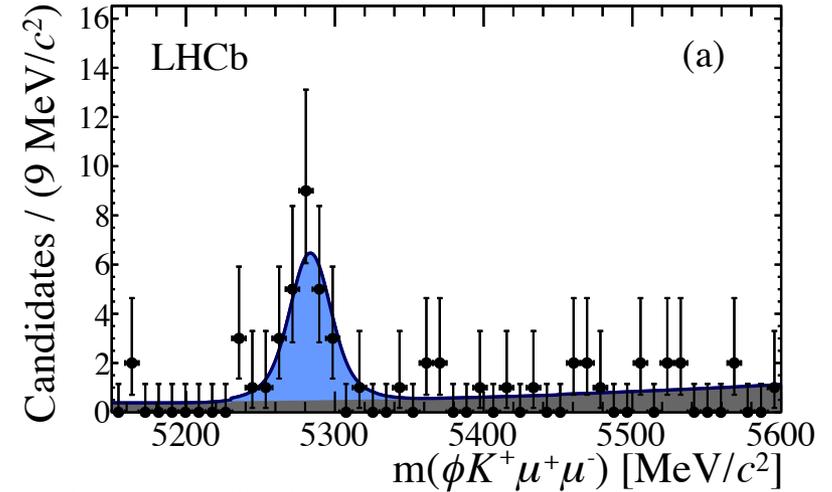


$B^+ \rightarrow K^+ \pi^+ \pi^- \mu^+ \mu^-$   $N_{\text{sig}} = 367_{-23}^{+23}$

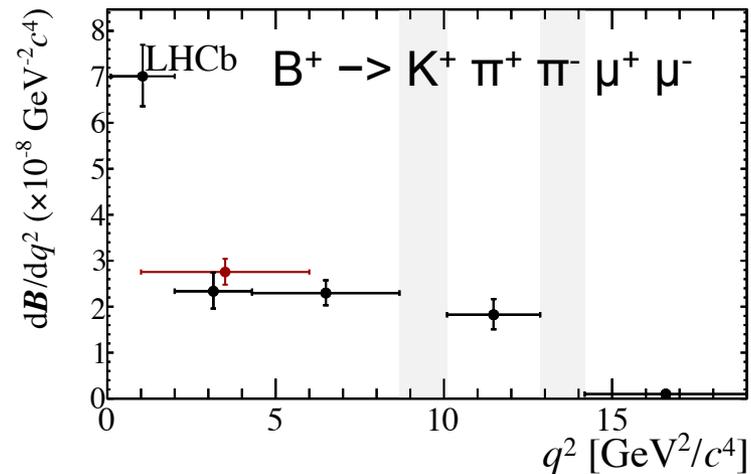
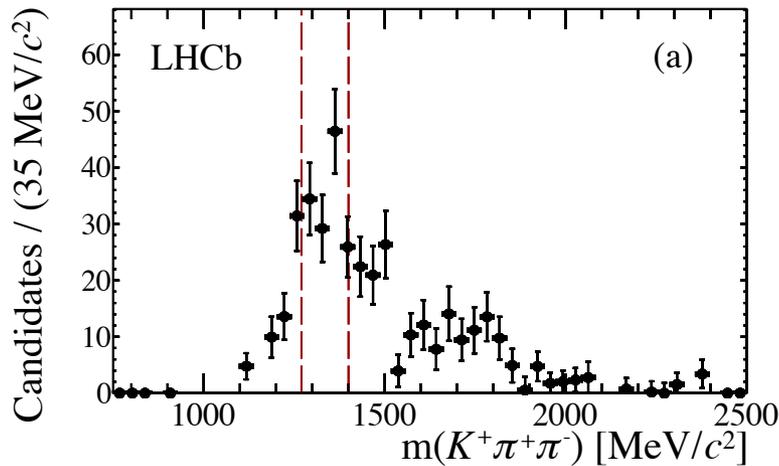


unknown resonance structure  
largest contribution from  $B^+ \rightarrow K_1^+(1270) \mu^+ \mu^-$   
Phys. Rev. D83 (2011) 032005

$B^+ \rightarrow \phi K^+ \mu^+ \mu^-$   $N_{\text{sig}} = 25.2_{-5.3}^{+6.0}$



$$\mathcal{B}(B^+ \rightarrow \phi K^+ \mu^+ \mu^-) = (8.22_{-1.67}^{+1.88}(\text{stat}) \pm 0.35(\text{syst}) \pm 2.47(\text{norm})) \cdot 10^{-8}$$



$$\mathcal{B}(B^+ \rightarrow K^+ \pi^+ \pi^- \mu^+ \mu^-) = (4.36_{-0.27}^{+0.29}(\text{stat}) \pm 0.20(\text{syst}) \pm 0.18(\text{norm})) \cdot 10^{-7}$$

**Electroweak penguins are an excellent way for indirect NP searches**

**LHCb is a unique ground to study these decays:**

- **a lot of different EW penguin decays have been investigated**
- **plenty of interesting results ( not all presented today )**  
**angular observables, CP asymmetries, branching fractions, ...**

**-> In general good agreement with SM, but some small tensions:**

**branching fractions, arXiv:1403.8044v3,**

**$P_5'$  of  $B^0 \rightarrow K^* \mu\mu$ , Phys. Rev. Lett. 111 (2013) 191801**

**More to come...**

**- Angular analysis of  $B^0 \rightarrow K^* \mu\mu$  with  $3\text{fb}^{-1}$**

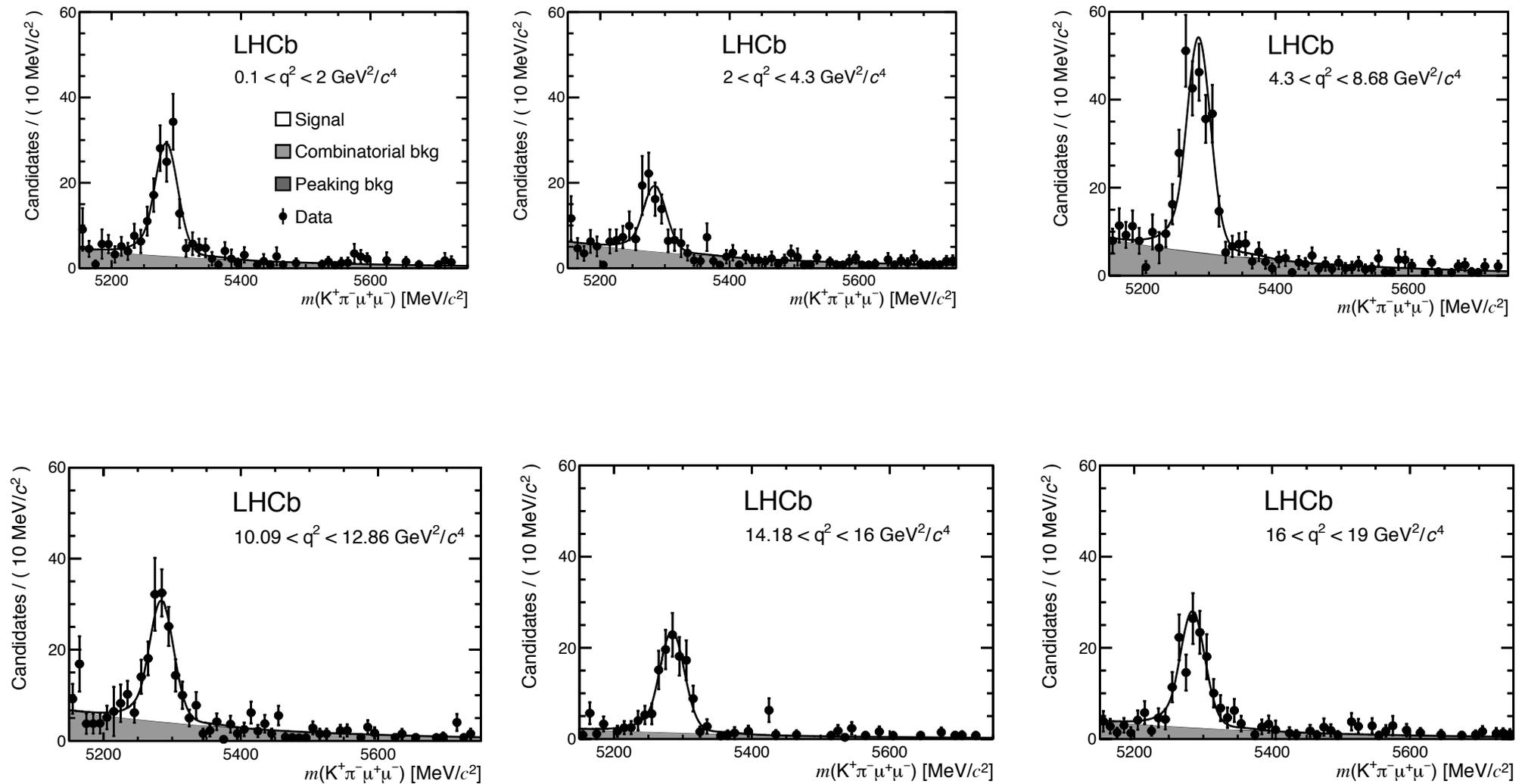
**- ...**

Stay tuned...  
penguins are always  
good for surprises!



# Backup

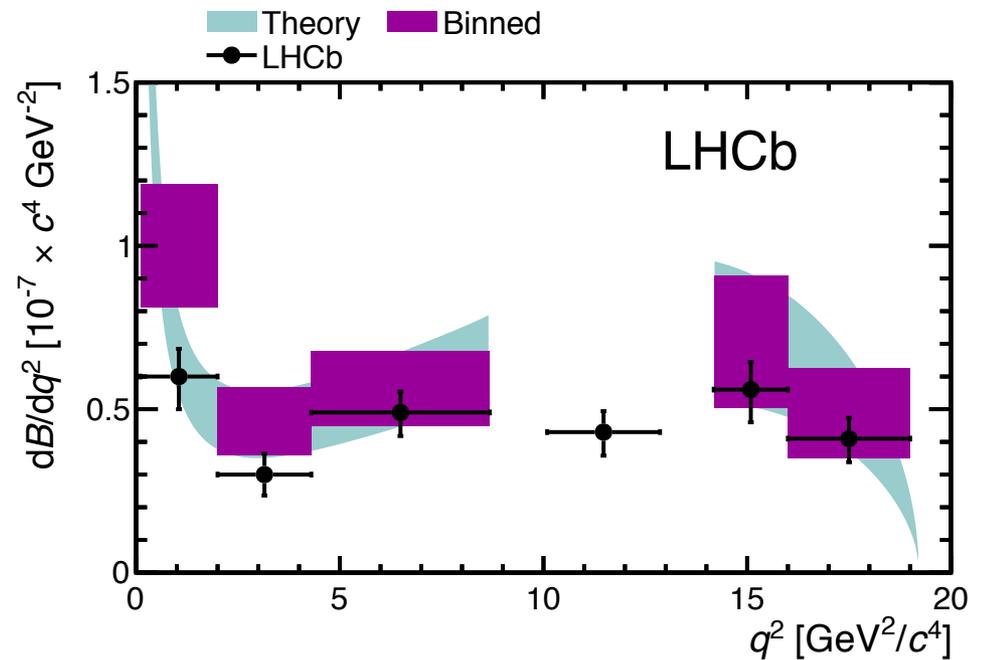
## Invariant mass distributions in bins of $q^2$



Differential branching fraction:

$$\frac{d\mathcal{B}}{dq^2} = \frac{1}{q_{\max}^2 - q_{\min}^2} \frac{N_{\text{sig}}}{N_{K^*0 J/\psi}} \frac{\varepsilon_{K^*0 J/\psi}}{\varepsilon_{K^*0 \mu^+ \mu^-}} \times \mathcal{B}(B^0 \rightarrow K^*0 J/\psi) \times \mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-)$$

$q^2$ (GeV <sup>2</sup> /c <sup>4</sup> )	$N_{\text{sig}}$	$d\mathcal{B}/dq^2$ (10 <sup>-7</sup> GeV <sup>-2</sup> c <sup>4</sup> )
0.10 – 2.00	140 ± 13	0.60 ± 0.06 ± 0.05 ± 0.04 <sup>+0.00</sup> <sub>-0.05</sub>
2.00 – 4.30	73 ± 11	0.30 ± 0.03 ± 0.03 ± 0.02 <sup>+0.00</sup> <sub>-0.02</sub>
4.30 – 8.68	271 ± 19	0.49 ± 0.04 ± 0.04 ± 0.03 <sup>+0.00</sup> <sub>-0.04</sub>
10.09 – 12.86	168 ± 15	0.43 ± 0.04 ± 0.04 ± 0.03 <sup>+0.00</sup> <sub>-0.03</sub>
14.18 – 16.00	115 ± 12	0.56 ± 0.06 ± 0.04 ± 0.04 <sup>+0.00</sup> <sub>-0.05</sub>
16.00 – 19.00	116 ± 13	0.41 ± 0.04 ± 0.04 ± 0.03 <sup>+0.00</sup> <sub>-0.03</sub>
1.00 – 6.00	197 ± 17	0.34 ± 0.03 ± 0.04 ± 0.02 <sup>+0.00</sup> <sub>-0.03</sub>



Folding of angular distributions: 
$$\hat{\phi} = \begin{cases} \phi + \pi & \text{if } \phi < 0 \\ \phi & \text{otherwise} \end{cases}$$

Differential decay rate with reduced number of observables:

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\hat{\phi}} = \frac{9}{16\pi} \left[ F_L \cos^2 \theta_K + \frac{3}{4}(1 - F_L)(1 - \cos^2 \theta_K) - F_L \cos^2 \theta_K (2 \cos^2 \theta_\ell - 1) + \frac{1}{4}(1 - F_L)(1 - \cos^2 \theta_K)(2 \cos^2 \theta_\ell - 1) + S_3(1 - \cos^2 \theta_K)(1 - \cos^2 \theta_\ell) \cos 2\hat{\phi} + \frac{4}{3}A_{\text{FB}}(1 - \cos^2 \theta_K) \cos \theta_\ell + A_9(1 - \cos^2 \theta_K)(1 - \cos^2 \theta_\ell) \sin 2\hat{\phi} \right].$$

Constraints of observables to keep decay rate positive in allowed phase space:

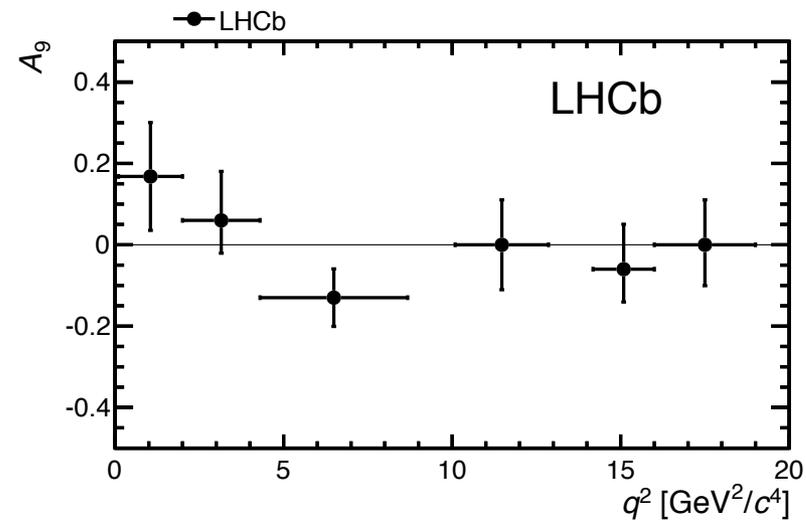
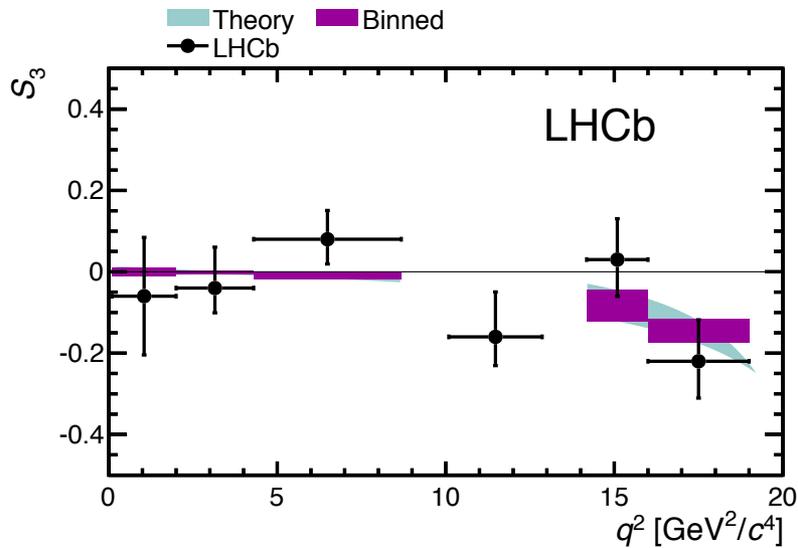
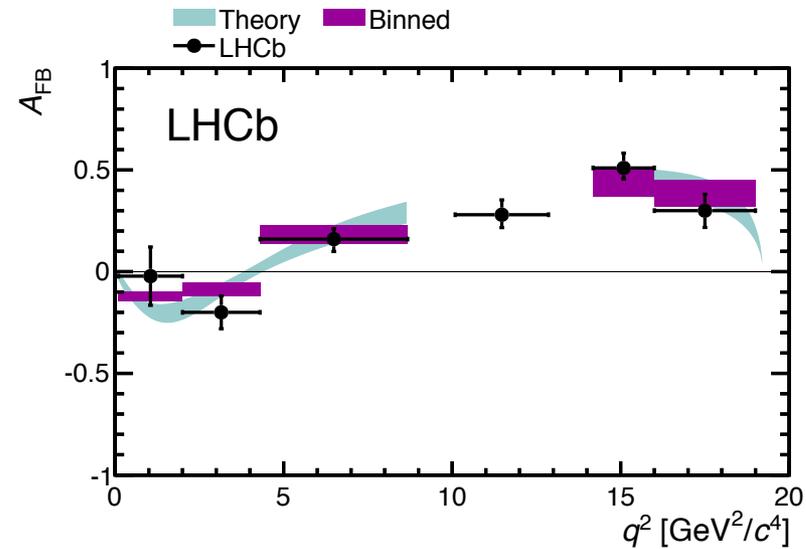
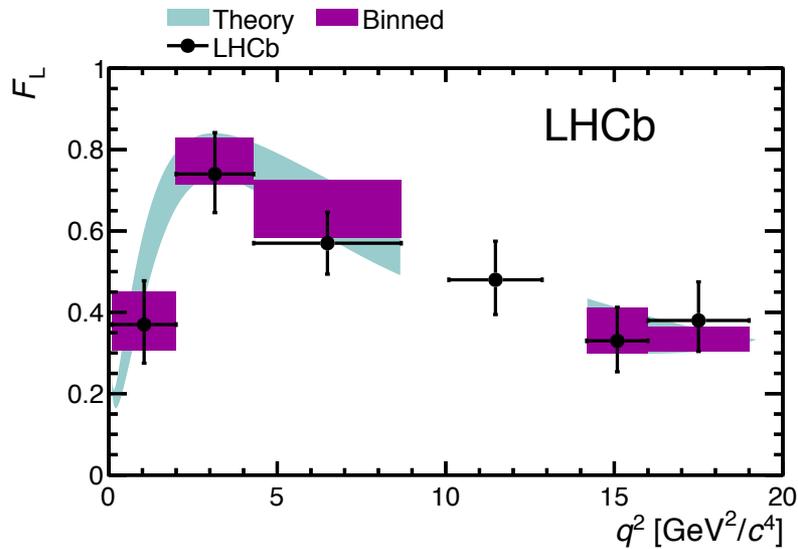
$$|A_{\text{FB}}| \leq \frac{3}{4}(1 - F_L), \quad |A_9| \leq \frac{1}{2}(1 - F_L) \quad \text{and} \quad |S_3| \leq \frac{1}{2}(1 - F_L)$$

Results of  
angular analysis:

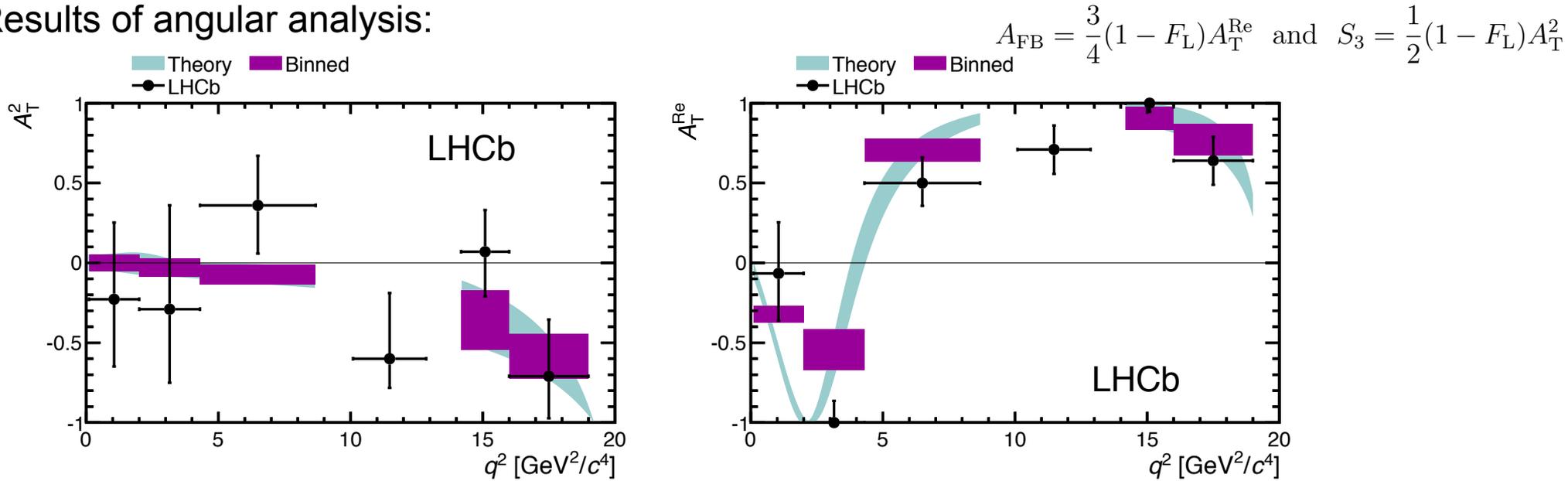
$q^2$ (GeV <sup>2</sup> /c <sup>4</sup> )	$F_L$	$A_{FB}$	$S_3$	$S_9$
0.10 – 2.00 (uncorrected)	$0.37^{+0.10+0.04}_{-0.09-0.03}$	$-0.02^{+0.12+0.01}_{-0.12-0.01}$	$-0.04^{+0.10+0.01}_{-0.10-0.01}$	$0.05^{+0.10+0.01}_{-0.09-0.01}$
0.10 – 2.00 (corrected)	$0.37^{+0.10+0.04}_{-0.09-0.03}$	$-0.02^{+0.13+0.01}_{-0.13-0.01}$	$-0.05^{+0.12+0.01}_{-0.12-0.01}$	$0.06^{+0.12+0.01}_{-0.12-0.01}$
2.00 – 4.30	$0.74^{+0.10+0.02}_{-0.09-0.03}$	$-0.20^{+0.08+0.01}_{-0.08-0.01}$	$-0.04^{+0.10+0.01}_{-0.06-0.01}$	$-0.03^{+0.11+0.01}_{-0.04-0.01}$
4.30 – 8.68	$0.57^{+0.07+0.03}_{-0.07-0.03}$	$0.16^{+0.06+0.01}_{-0.05-0.01}$	$0.08^{+0.07+0.01}_{-0.06-0.01}$	$0.01^{+0.07+0.01}_{-0.08-0.01}$
10.09 – 12.86	$0.48^{+0.08+0.03}_{-0.09-0.03}$	$0.28^{+0.07+0.02}_{-0.06-0.02}$	$-0.16^{+0.11+0.01}_{-0.07-0.01}$	$-0.01^{+0.10+0.01}_{-0.11-0.01}$
14.18 – 16.00	$0.33^{+0.08+0.02}_{-0.07-0.03}$	$0.51^{+0.07+0.02}_{-0.05-0.02}$	$0.03^{+0.09+0.01}_{-0.10-0.01}$	$0.00^{+0.09+0.01}_{-0.08-0.01}$
16.00 – 19.00	$0.38^{+0.09+0.03}_{-0.07-0.03}$	$0.30^{+0.08+0.01}_{-0.08-0.02}$	$-0.22^{+0.10+0.02}_{-0.09-0.01}$	$0.06^{+0.11+0.01}_{-0.10-0.01}$
1.00 – 6.00	$0.65^{+0.08+0.03}_{-0.07-0.03}$	$-0.17^{+0.06+0.01}_{-0.06-0.01}$	$0.03^{+0.07+0.01}_{-0.07-0.01}$	$0.07^{+0.09+0.01}_{-0.08-0.01}$

$q^2$ (GeV <sup>2</sup> /c <sup>4</sup> )	$A_9$	$A_T^2$	$A_T^{\text{Re}}$	p-value
0.10 – 2.00 (uncorrected)	$0.12^{+0.09+0.01}_{-0.09-0.01}$	$-0.14^{+0.34+0.02}_{-0.30-0.02}$	$-0.04^{+0.26+0.02}_{-0.24-0.01}$	0.18
0.10 – 2.00 (corrected)	$0.14^{+0.11+0.01}_{-0.11-0.01}$	$-0.19^{+0.40+0.02}_{-0.35-0.02}$	$-0.06^{+0.29+0.02}_{-0.27-0.01}$	–
2.00 – 4.30	$0.06^{+0.12+0.01}_{-0.08-0.01}$	$-0.29^{+0.65+0.02}_{-0.46-0.03}$	$-1.00^{+0.13+0.04}_{-0.00-0.00}$	0.57
4.30 – 8.68	$-0.13^{+0.07+0.01}_{-0.07-0.01}$	$0.36^{+0.30+0.03}_{-0.31-0.03}$	$0.50^{+0.16+0.01}_{-0.14-0.03}$	0.71
10.09 – 12.86	$0.00^{+0.11+0.01}_{-0.11-0.01}$	$-0.60^{+0.42+0.05}_{-0.27-0.02}$	$0.71^{+0.15+0.01}_{-0.15-0.03}$	–
14.18 – 16.00	$-0.06^{+0.11+0.01}_{-0.08-0.01}$	$0.07^{+0.26+0.02}_{-0.28-0.02}$	$1.00^{+0.00+0.00}_{-0.05-0.02}$	0.38
16.00 – 19.00	$0.00^{+0.11+0.01}_{-0.10-0.01}$	$-0.71^{+0.35+0.06}_{-0.26-0.04}$	$0.64^{+0.15+0.01}_{-0.15-0.02}$	0.28
1.00 – 6.00	$0.03^{+0.08+0.01}_{-0.08-0.01}$	$0.15^{+0.39+0.03}_{-0.41-0.03}$	$-0.66^{+0.24+0.04}_{-0.22-0.01}$	0.72

## Results of angular analysis:



## Results of angular analysis:

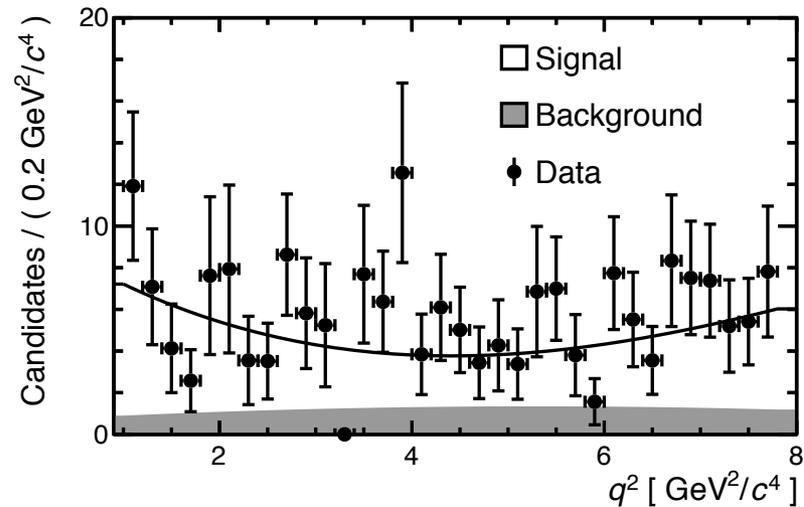
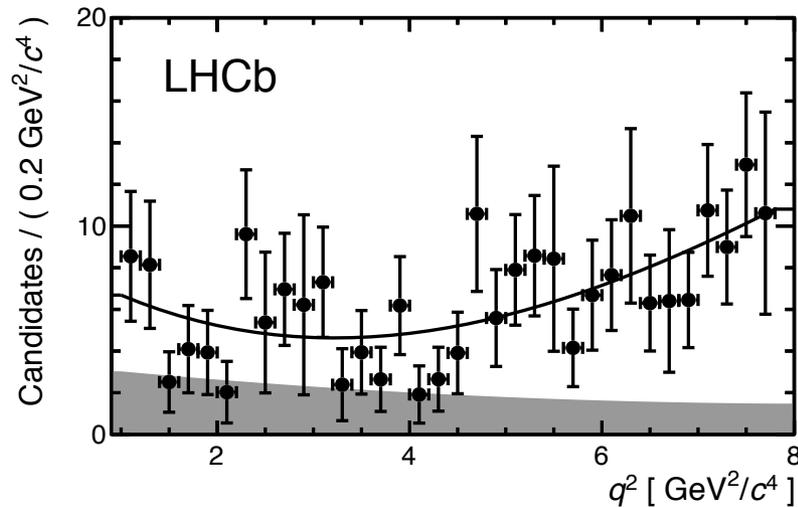


## Systematic uncertainties:

Source	$A_{FB}$	$F_L$	$S_3$	$S_9$	$A_9$	$A_T^2$	$A_T^{\text{Re}}$
Acceptance model	0.02	0.03	0.01	< 0.01	< 0.01	0.02	0.01
Mass model	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
$B^0 \rightarrow \bar{B}^0$ mis-id	< 0.01	< 0.01	< 0.01	< 0.01	0.01	< 0.01	< 0.01
Data-simulation diff.	0.01	0.03	0.01	< 0.01	< 0.01	0.03	0.01
Kinematic reweighting	< 0.01	0.01	< 0.01	< 0.01	< 0.01	0.01	< 0.01
Peaking backgrounds	0.01	0.01	0.01	0.01	0.01	0.01	0.01
S-wave	0.01	0.01	0.02	0.01	< 0.01	0.05	0.04
$B^0$ - $\bar{B}^0$ asymmetries	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01

Determination of zero-crossing point:

$$A_{\text{FB}}(q^2) = \frac{P_{\text{F}}(q^2) - P_{\text{B}}(q^2)}{P_{\text{F}}(q^2) + P_{\text{B}}(q^2)}$$



Transformation of angular distributions:

$$P'_4, S_4: \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \phi \rightarrow \pi - \phi & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_5, S_5: \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_6, S_7: \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_8, S_8: \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_K \rightarrow \pi - \theta_K & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2. \end{cases}$$

$q^2$ [ GeV <sup>2</sup> /c <sup>4</sup> ]	$P'_4$	$P'_5$	$P'_6$	$P'_8$
0.10 – 2.00	$0.00^{+0.26}_{-0.26} \pm 0.03$	$0.45^{+0.19}_{-0.22} \pm 0.09$	$-0.24^{+0.19}_{-0.22} \pm 0.05$	$-0.06^{+0.28}_{-0.28} \pm 0.02$
2.00 – 4.30	$-0.37^{+0.29}_{-0.26} \pm 0.08$	$0.29^{+0.39}_{-0.38} \pm 0.07$	$0.15^{+0.36}_{-0.38} \pm 0.05$	$-0.15^{+0.29}_{-0.28} \pm 0.07$
4.30 – 8.68	$-0.59^{+0.15}_{-0.12} \pm 0.05$	$-0.19^{+0.16}_{-0.16} \pm 0.03$	$-0.04^{+0.15}_{-0.15} \pm 0.05$	$0.29^{+0.17}_{-0.19} \pm 0.03$
10.09 – 12.90	$-0.46^{+0.20}_{-0.17} \pm 0.03$	$-0.79^{+0.16}_{-0.19} \pm 0.19$	$-0.31^{+0.23}_{-0.22} \pm 0.05$	$-0.06^{+0.23}_{-0.22} \pm 0.02$
14.18 – 16.00	$0.09^{+0.35}_{-0.27} \pm 0.04$	$-0.79^{+0.20}_{-0.13} \pm 0.18$	$-0.18^{+0.25}_{-0.24} \pm 0.03$	$-0.20^{+0.30}_{-0.25} \pm 0.03$
16.00 – 19.00	$-0.35^{+0.26}_{-0.22} \pm 0.03$	$-0.60^{+0.19}_{-0.16} \pm 0.09$	$0.31^{+0.38}_{-0.37} \pm 0.10$	$0.06^{+0.26}_{-0.27} \pm 0.03$
1.00 – 6.00	$-0.29^{+0.18}_{-0.16} \pm 0.03$	$0.21^{+0.20}_{-0.21} \pm 0.03$	$-0.18^{+0.21}_{-0.21} \pm 0.03$	$0.23^{+0.18}_{-0.19} \pm 0.02$

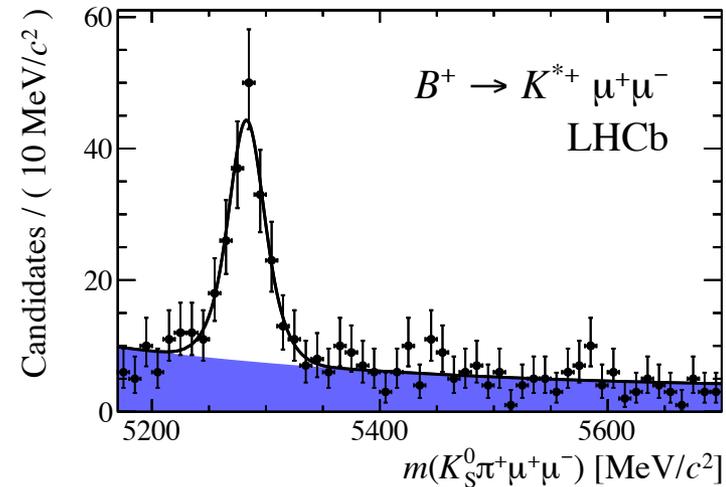
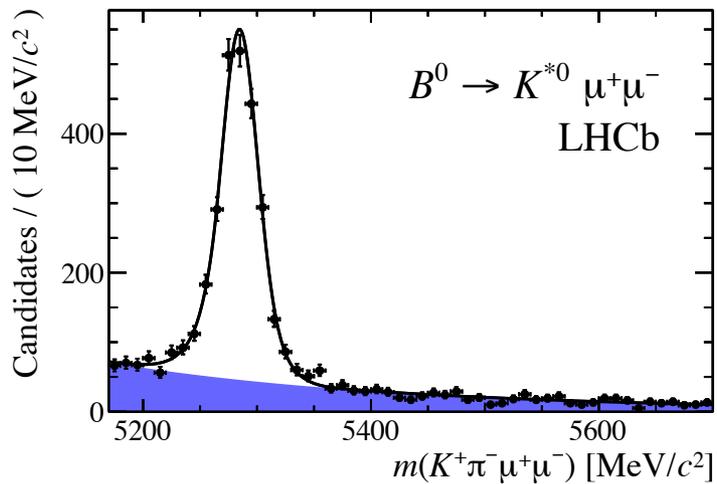
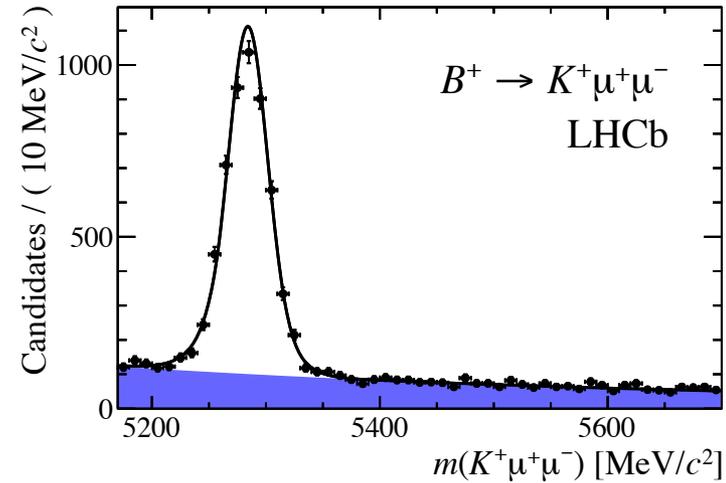
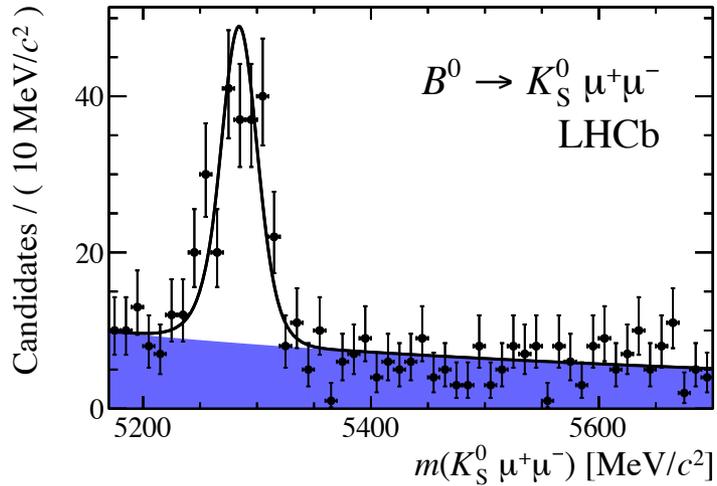
$q^2$ [ GeV <sup>2</sup> /c <sup>4</sup> ]	$S_4$	$S_5$	$S_7$	$S_8$
0.10 – 2.00	$0.00^{+0.12}_{-0.12} \pm 0.03$	$0.22^{+0.09}_{-0.10} \pm 0.04$	$-0.11^{+0.11}_{-0.11} \pm 0.03$	$-0.03^{+0.13}_{-0.12} \pm 0.01$
2.00 – 4.30	$-0.14^{+0.13}_{-0.12} \pm 0.03$	$0.11^{+0.14}_{-0.13} \pm 0.03$	$0.06^{+0.15}_{-0.15} \pm 0.02$	$-0.06^{+0.12}_{-0.12} \pm 0.02$
4.30 – 8.68	$-0.29^{+0.06}_{-0.06} \pm 0.02$	$-0.09^{+0.08}_{-0.08} \pm 0.01$	$-0.02^{+0.07}_{-0.08} \pm 0.04$	$0.15^{+0.08}_{-0.08} \pm 0.01$
10.09 – 12.90	$-0.23^{+0.09}_{-0.08} \pm 0.02$	$-0.40^{+0.08}_{-0.10} \pm 0.10$	$-0.16^{+0.11}_{-0.12} \pm 0.03$	$-0.03^{+0.10}_{-0.10} \pm 0.01$
14.18 – 16.00	$0.04^{+0.14}_{-0.08} \pm 0.01$	$-0.38^{+0.10}_{-0.09} \pm 0.09$	$-0.09^{+0.13}_{-0.14} \pm 0.01$	$-0.10^{+0.13}_{-0.12} \pm 0.02$
16.00 – 19.00	$-0.17^{+0.11}_{-0.09} \pm 0.01$	$-0.29^{+0.09}_{-0.08} \pm 0.04$	$0.15^{+0.16}_{-0.15} \pm 0.03$	$0.03^{+0.12}_{-0.12} \pm 0.02$

## Results for $B^0 \rightarrow K^* \mu \mu$

$q^2$ bin [ $\text{GeV}^2/c^4$ ]	yield	$\mathcal{A}_{CP}$	stat. error	syst. error
0.10–0.98	$304 \pm 18$	$-0.007$	0.060	0.006
1.10–2.00	$105 \pm 11$	$-0.175$	0.106	0.009
2.00–3.00	$120 \pm 13$	$-0.145$	0.102	0.008
3.00–4.00	$101 \pm 12$	$-0.012$	0.113	0.014
4.00–5.00	$120 \pm 13$	$-0.075$	0.106	0.012
5.00–6.00	$143 \pm 13$	$-0.029$	0.097	0.009
6.00–7.00	$144 \pm 14$	$0.021$	0.095	0.008
7.00–8.00	$177 \pm 15$	$0.100$	0.087	0.006
11.0–11.8	$144 \pm 14$	$-0.020$	0.093	0.007
11.8–12.5	$147 \pm 14$	$0.032$	0.093	0.022
15.0–16.0	$205 \pm 16$	$-0.124$	0.075	0.009
16.0–17.0	$216 \pm 16$	$-0.001$	0.074	0.010
17.0–18.0	$169 \pm 14$	$-0.058$	0.085	0.009
18.0–19.0	$105 \pm 11$	$-0.053$	0.108	0.016
0.10–19.0	$2190 \pm 52$	$-0.034$	0.024	0.003

## Results for $B^+ \rightarrow K^+ \mu \mu$

$q^2$ bin [ GeV <sup>2</sup> /c <sup>4</sup> ]	yield	$\mathcal{A}_{CP}$	stat. error	syst. error
0.10–0.98	387±22	0.089	0.057	0.001
1.10–2.00	277±19	−0.003	0.068	0.002
2.00–3.00	367±22	0.043	0.059	0.001
3.00–4.00	334±21	−0.033	0.063	0.001
4.00–5.00	307±20	−0.020	0.064	0.001
5.00–6.00	332±21	0.032	0.062	0.002
6.00–7.00	355±22	0.027	0.060	0.001
7.00–8.00	371±22	0.042	0.059	0.002
11.0–11.8	232±18	−0.046	0.076	0.002
11.8–12.5	247±17	0.019	0.070	0.002
15.0–16.0	287±19	0.121	0.065	0.004
16.0–17.0	287±19	0.029	0.066	0.001
17.0–18.0	349±21	−0.029	0.058	0.001
18.0–19.0	222±17	−0.060	0.074	0.003
19.0–20.0	121±13	−0.047	0.105	0.003
20.0–21.0	95±12	−0.011	0.120	0.003
21.0–22.0	50±8	−0.289	0.161	0.004
0.10–22.0	4630±78	0.013	0.017	0.001



Branching fraction:

$$\frac{d\mathcal{B}}{dq^2} = \frac{N(B \rightarrow K^{(*)} \mu^+ \mu^-)}{N(B \rightarrow J/\psi K^{(*)})} \cdot \frac{\varepsilon(B \rightarrow J/\psi K^{(*)})}{\varepsilon(B \rightarrow K^{(*)} \mu^+ \mu^-)} \cdot \frac{\mathcal{B}(B \rightarrow J/\psi K^{(*)}) \mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-)}{(q_{\max}^2 - q_{\min}^2)}$$

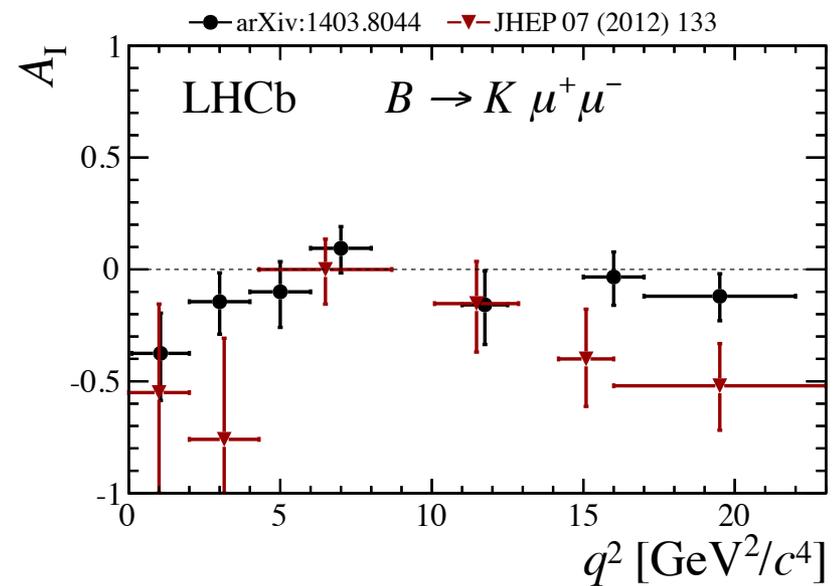
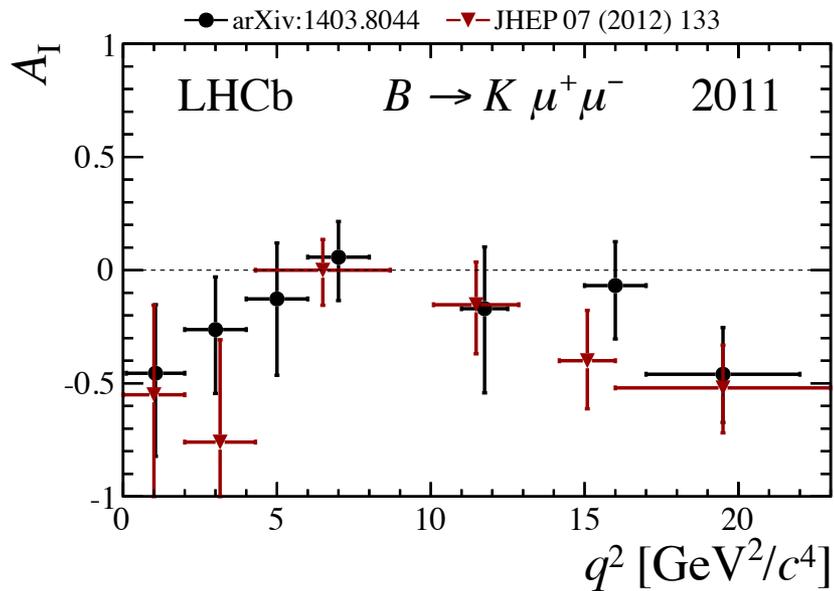
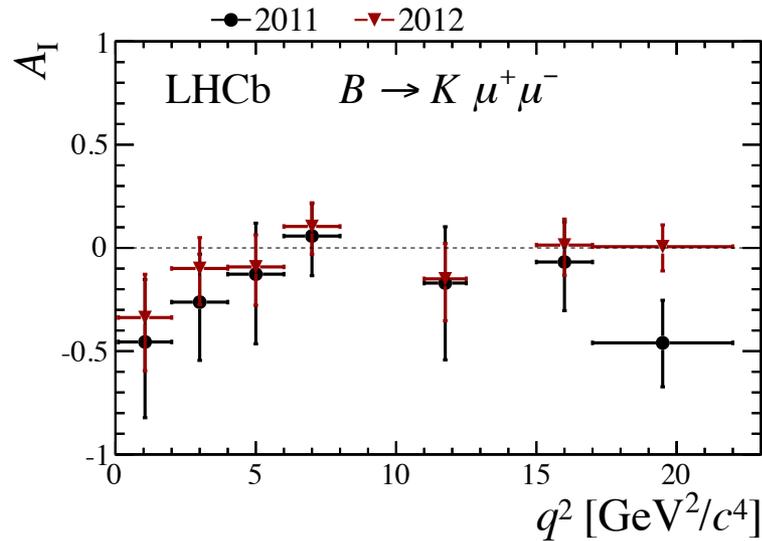
Branching fraction of normalization channels:

$$\begin{aligned} \mathcal{B}(B^+ \rightarrow J/\psi K^+) &= (0.998 \pm 0.014 \pm 0.040) \times 10^{-3}, \\ \mathcal{B}(B^0 \rightarrow J/\psi K^0) &= (0.928 \pm 0.013 \pm 0.037) \times 10^{-3}, \\ \mathcal{B}(B^+ \rightarrow J/\psi K^{*+}) &= (1.431 \pm 0.027 \pm 0.090) \times 10^{-3}, \\ \mathcal{B}(B^0 \rightarrow J/\psi K^{*0}) &= (1.331 \pm 0.025 \pm 0.084) \times 10^{-3}, \end{aligned}$$

Systematic uncertainties:

Source	Branching fraction	Isospin asymmetry
$B \rightarrow J/\psi K^{(*)}$ branching fractions	4% – 6%	–
Physics model	1% – 2%	1% – 2%
Simulation mis-modelling	1% – 3%	1% – 3%

Isospin asymmetry comparison 2011 and 2012 data set:





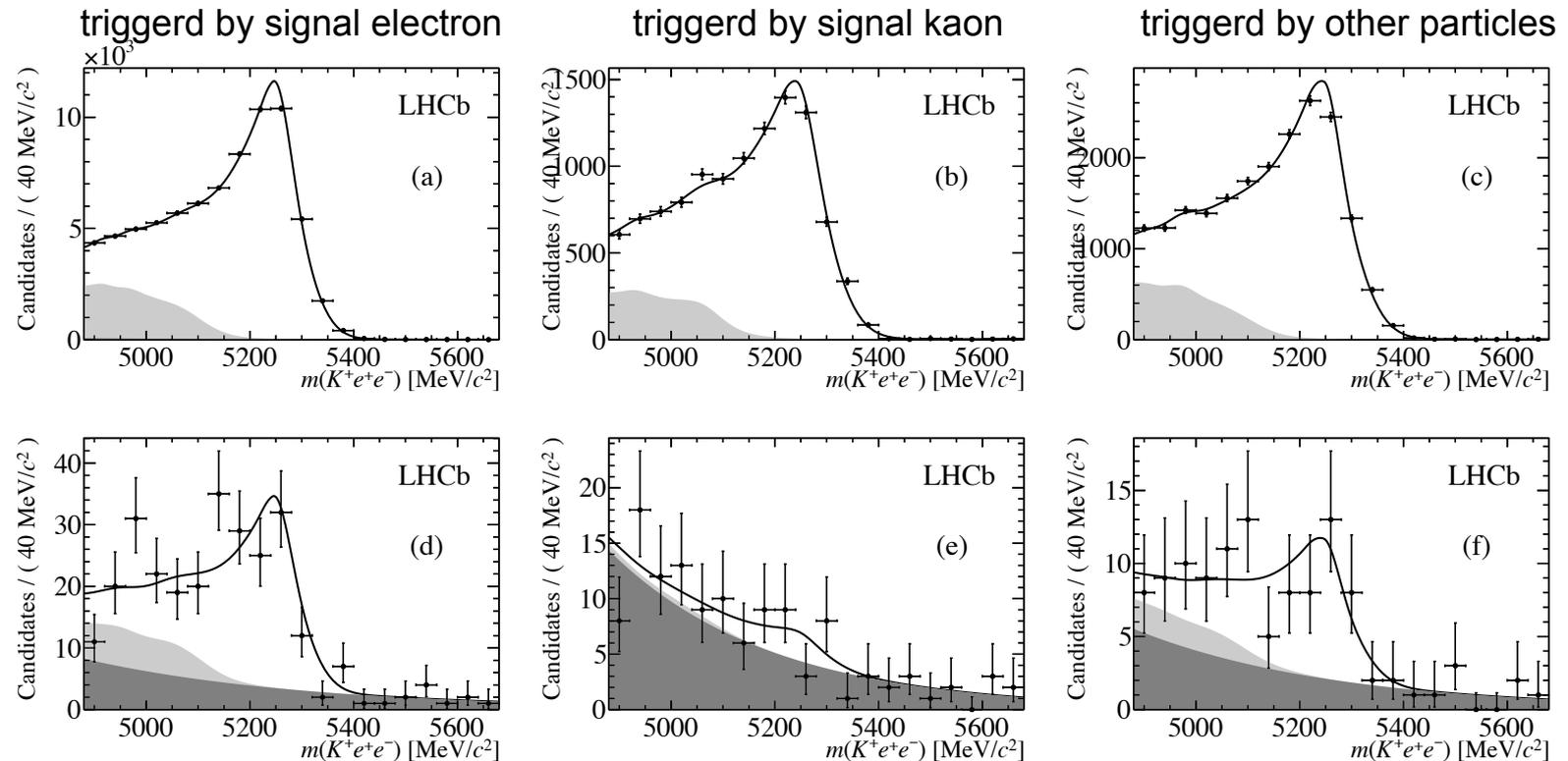
Definition of  $R_K$ :

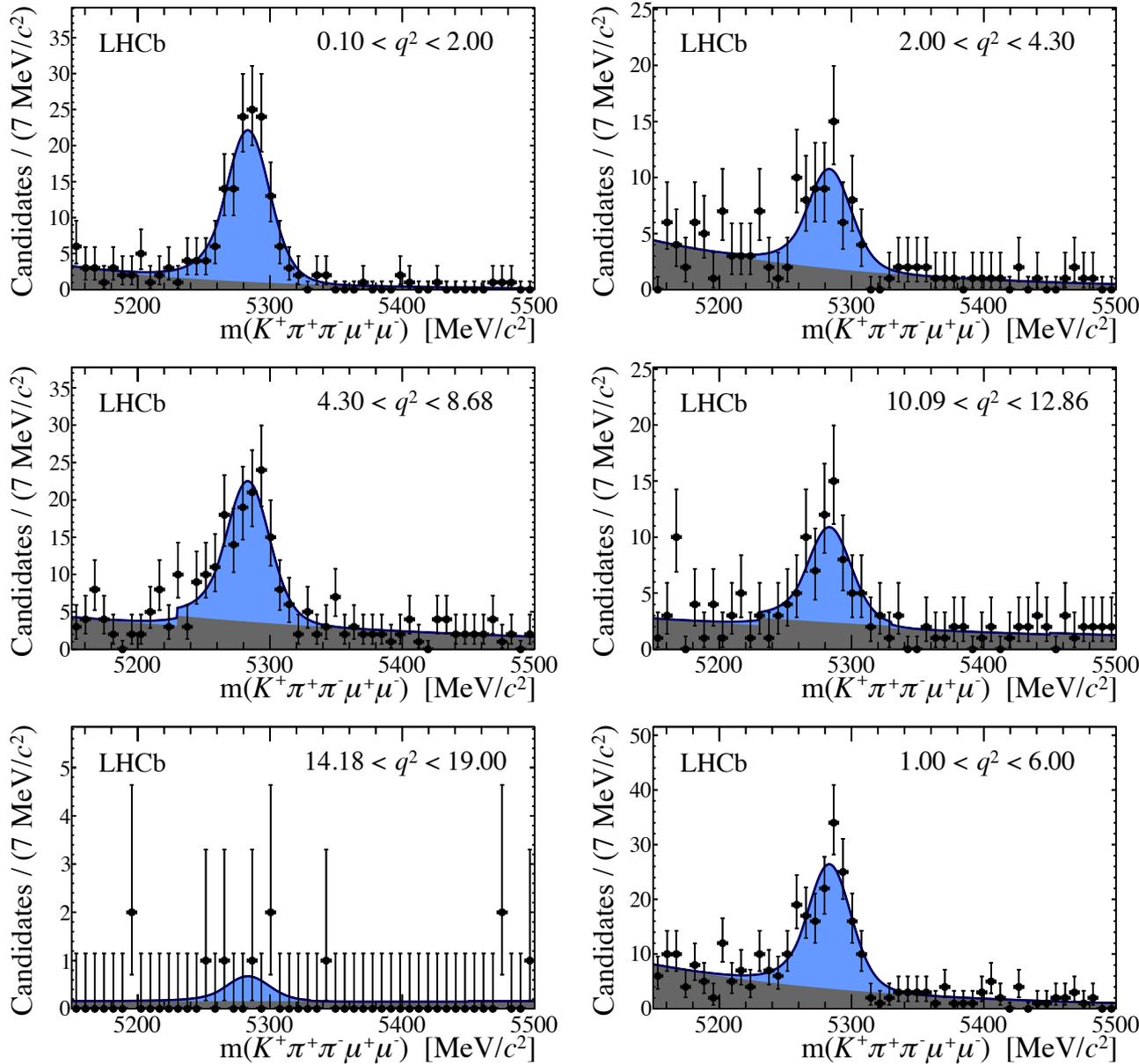
$$R_K = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ e^+ e^-]}{dq^2} dq^2}$$

$$R_K = \left( \frac{\mathcal{N}_{K^+ \mu^+ \mu^-}}{\mathcal{N}_{K^+ e^+ e^-}} \right) \left( \frac{\mathcal{N}_{J/\psi(e^+ e^-) K^+}}{\mathcal{N}_{J/\psi(\mu^+ \mu^-) K^+}} \right) \left( \frac{\epsilon_{K^+ e^+ e^-}}{\epsilon_{K^+ \mu^+ \mu^-}} \right) \left( \frac{\epsilon_{J/\psi(\mu^+ \mu^-) K^+}}{\epsilon_{J/\psi(e^+ e^-) K^+}} \right)$$

Mass fits of

$B^+ \rightarrow J/\Psi (ee) K^+$



Invariant mass fits of  $B^+ \rightarrow K^+ \pi^+ \pi^- \mu^+ \mu^-$  in bins of  $q^2$ 


## Results branching fraction:

$q^2$ bin [ $\text{GeV}^2/c^4$ ]	$N_{\text{sig}}$	$\frac{dB}{dq^2} [\times 10^{-8} \text{GeV}^{-2}c^4]$
[ 0.10, 2.00]	$134.1^{+12.9}_{-12.3}$	$7.01^{+0.69}_{-0.65} \pm 0.47$
[ 2.00, 4.30]	$56.5^{+9.7}_{-9.1}$	$2.34^{+0.41}_{-0.38} \pm 0.15$
[ 4.30, 8.68]	$119.9^{+14.6}_{-13.7}$	$2.30^{+0.28}_{-0.26} \pm 0.20$
[10.09, 12.86]	$54.0^{+10.1}_{-9.4}$	$1.83^{+0.34}_{-0.32} \pm 0.17$
[14.18, 19.00]	$3.3^{+2.8}_{-2.1}$	$0.10^{+0.08}_{-0.06} \pm 0.01$
[ 1.00, 6.00]	$144.8^{+14.9}_{-14.3}$	$2.75^{+0.29}_{-0.28} \pm 0.16$

Reconstructed  $K^+ \pi^+ \pi^-$  mass of  $B^+ \rightarrow K^+ \pi^+ \pi^- \mu^+ \mu^-$  signal decays:

