

# Rare Top-quark decays to Higgs boson in the MSSM

Athanasios Dedes

Department of Physics  
University of Ioannina, Greece

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# Outline

## Introduction

SUSY effects on  $t \rightarrow u h$

MSSM flavour sector

Operators

The calculation

Cancellations, Decoupling and Remnants

Enhanced Scenarios

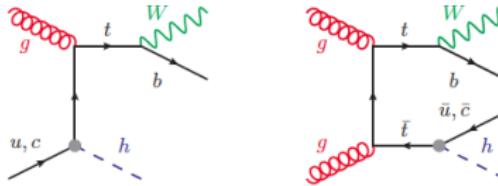
## Conclusions

# Introduction

- ▶ Last 20 years two elementary(?) particles discovered:  $t$  and  $h$
- ▶ Interesting to search for rare top decays

$$t \rightarrow u h , \quad \text{or} \quad t \rightarrow c h$$

- ▶ In SM :  $\mathcal{B}(t \rightarrow u(c) h)_{\text{SM}} \approx 4 \times 10^{-17(14)}$  because of GIM
- ▶ In MSSM : no GIM in sflavour  $\Rightarrow$  large ratios are expected
- ▶ LHC bound :  $\mathcal{B}(t \rightarrow u h) \leq 0.56\% *$   $\dagger$
- ▶ LHC projective reach (3000  $fb^{-1}$ , 14 TeV) :  $\gtrsim 2 \times 10^{-4} \ddagger$



\* CMS Collaboration, CMS-PAS-HIG-13-034.

$\dagger$  A. Greljo, J. F. Kamenik, and J. Kopp, arXiv:1404.1278 [hep-ph].

$\ddagger$  Top Quark Working Group, "Snowmass 2013," arXiv:1311.2028.

## Lagrangian and Branching Ratio for $t \rightarrow u h$

The relevant Lagrangian is

$$-\mathcal{L} \supset C_L^{(h)} \bar{u}_R t_L h + C_R^{(h)} \bar{u}_L t_R h + \text{H.c.},$$

Therefore, for  $m_{u(c)} = 0$  and  $\Gamma(t \rightarrow bW) = 1.39 \text{ GeV}$

$$\begin{aligned}\mathcal{B}(t \rightarrow u h) &= \frac{1}{1.39 \text{ GeV}} \frac{m_t}{32\pi} \left( |C_L^{(h)}|^2 + |C_R^{(h)}|^2 \right) \left( 1 - \frac{m_h^2}{m_t^2} \right)^2 \\ &\approx \frac{1}{4} \left( |C_L^{(h)}|^2 + |C_R^{(h)}|^2 \right)\end{aligned}$$

The current LHC bound provides us with a “tree level” bound:

$$|C_L|, |C_R| \lesssim 0.1$$

## Bibliography (SM)

-  G. Eilam, J. Hewett, and A. Soni,  
“Rare decays of the top quark in the standard and two Higgs doublet models,”  
*Phys.Rev.* **D44** (1991) 1473–1484; Erratum-*ibid.* **D59** (1999) 039901
-  B. Mele, S. Petrarca, and A. Soddu,  
“A New evaluation of the  $t \rightarrow cH$  decay width in the standard model,”  
*Phys.Lett.* **B435** (1998) 401–406, arXiv:hep-ph/9805498  
[hep-ph].

## Bibliography (MSSM)

-  J. Guasch and J. Sola,  
“FCNC top quark decays: A Door to SUSY physics in high luminosity colliders?,”  
*Nucl.Phys.* **B562** (1999) 3–28, arXiv:hep-ph/9906268 [hep-ph].
-  J. Cao, G. Eilam, M. Frank, K. Hikasa, G. Liu, *et al.*,  
“SUSY-induced FCNC top-quark processes at the large hadron collider,”  
*Phys.Rev.* **D75** (2007) 075021, arXiv:hep-ph/0702264 [hep-ph].
-  J. Cao, C. Han, L. Wu, J. M. Yang, and M. Zhang,  
“SUSY induced top quark FCNC decay  $t \rightarrow ch$  after Run I of LHC,”  
arXiv:1404.1241 [hep-ph].

## What is new in this work?



A. D., M. Paraskevas, J. Rosiek, K. Suxho, K. Tamvakis,  
Rare Top-quark Decays to Higgs boson in the MSSM revisited  
to appear soon

1. Includes NLO QCD Effects from SUSY-loops on chromomagnetic operator + running
2. Detailed analysis of cancellations
3. Effects from non-holomorphic SUSY breaking terms
4. Complete up-to-date constraints,  $\Delta M_D$ ,  $b \rightarrow s\gamma$ , ... e.t.c
5. All MSSM contributions are included into **SUSY\_FLAVOR**<sup>§</sup>

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<sup>§</sup>A. Crivellin, J. Rosiek, P. H. Chankowski, A. D., S. Jaeger and P. Tanedo,  
[arXiv:1203.5023 [hep-ph]].

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## MSSM flavour sector

$$\begin{aligned}\mathcal{L}_{\text{MSSM}} \supset & -\tilde{Q}_L^\dagger m_{Q_L}^2 \tilde{Q}_L - \tilde{U}_R^\dagger m_{U_R}^2 \tilde{U}_R - \tilde{D}_R^\dagger m_{D_R}^2 \tilde{D}_R \\ & + \left( H_2 \tilde{Q}_L A_u \tilde{U}_R + H_1 \tilde{Q}_L A_d \tilde{D}_R + \text{H.c.} \right) \\ & + \left( H_1^\dagger \tilde{Q}_L A'_u \tilde{U}_R + H_2^\dagger \tilde{Q}_L A'_d \tilde{D}_R + \text{H.c.} \right),\end{aligned}$$

$m_{Q_L}^2, m_{U_R}^2, m_{D_R}^2$  : soft SUSY breaking mass matrices

$A_u$  and  $A_d$  : soft SUSY breaking trilinear (mass) matrices ¶

$A'_u, A'_d$  : non-holomorphic soft SUSY breaking trilinear (mass matrices) || \*\*

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¶ M. Misiak, S. Pokorski and J. Rosiek, [hep-ph/9703442].

|| L. J. Hall and L. Randall, Phys. Rev. Lett. **65**, 2939 (1990).

\*\* F. Borzumati, G. R. Farrar, N. Polonsky and S. D. Thomas, Nucl. Phys. B **555**, 53 (1999) [hep-ph/9902443].

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# QCD Mixed Operators

$$O^{(h)} = \left( H^\dagger H \right) \bar{Q}_L^I u_R^J \tilde{H} + \text{H.c.}$$

$$O^{(g)} = g_s \bar{Q}_L^I \sigma^{\mu\nu} \lambda^A u_R^J \tilde{H} G_{\mu\nu}^A + \text{H.c.}$$

## Strategy

1. Full calculation of the relevant one-Particle-Irreducible (1PI) Feynman diagrams  $C_{L,R}^{(h)}$  at scale  $M_S$ , where  $M_S$  is the lightest coloured sparticle (usually gluino) mass.
2. Full calculation of the SUSY induced Wilson coefficient  $C_{L,R}^{(g)}$  associated with the dipole operator  $O^{(g)}$  that mix with strong (QCD) quantum corrections.
3. Use RGEs  $\dagger\dagger$  to run all operators down to  $m_t^{pole}$
4. Calculate  $\mathcal{B}(t \rightarrow u h)$

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$\dagger\dagger$ C. Zhang and F. Maltoni, arXiv:1305.7386

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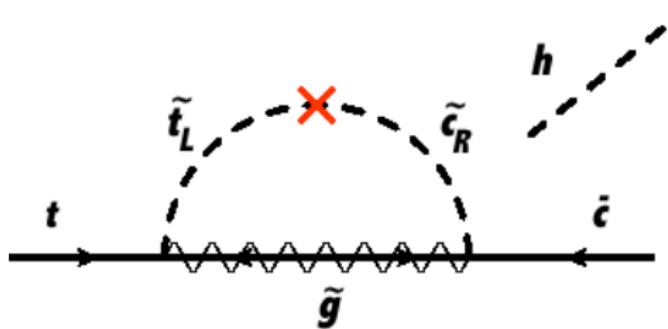
Conclusions

## The calculation

Assuming  $m_{u,c} \rightarrow 0$  the Wilson coefficient is e.g.,

$$C_L^{(h)} \approx \Delta F_L^{(h)} - \frac{1}{v} \left( \frac{\cos \alpha}{\sin \beta} \right) \Sigma_{mL}(0)$$

no  $\tan \beta$  enhancement



$$C_L^{(h)} \sim \left( \frac{\alpha_s}{4\pi} \right) \left( \frac{m_{\tilde{g}}}{M_S} \right) f(\delta_{LR}^{23}, \dots)$$

All particle corrections have been taken into account. However, the **gluino** diagram is the dominant source

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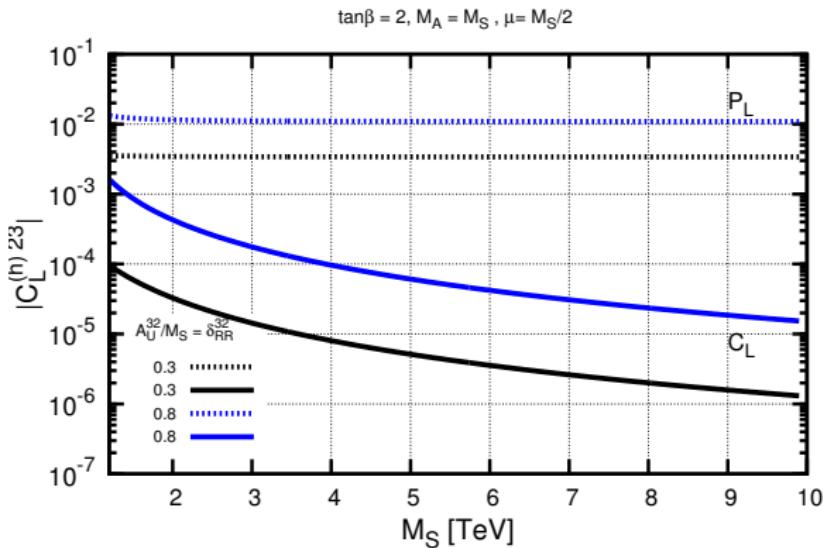
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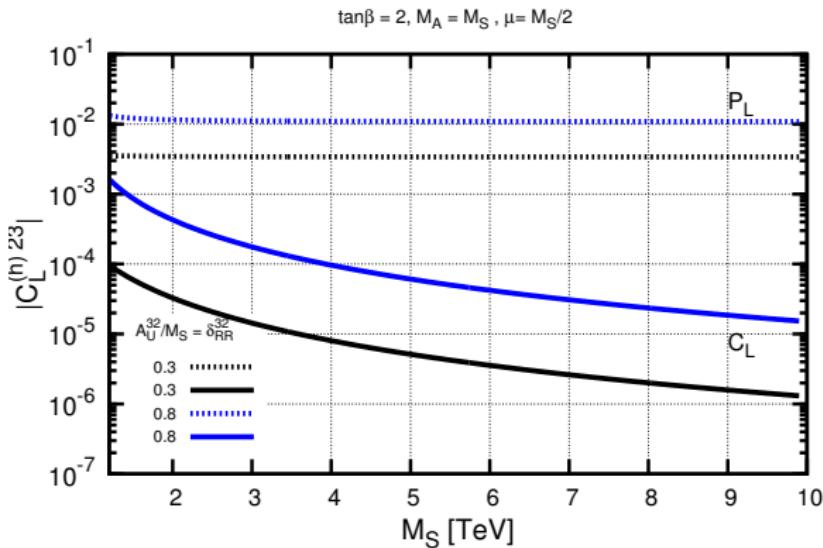
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# Cancellations and Decoupling



- ▶ Degenerate squark mass spectrum (in flavour space)
- ▶ Uniform mass scaling, ( $m_{\tilde{g}} = M_A = M_S$ )

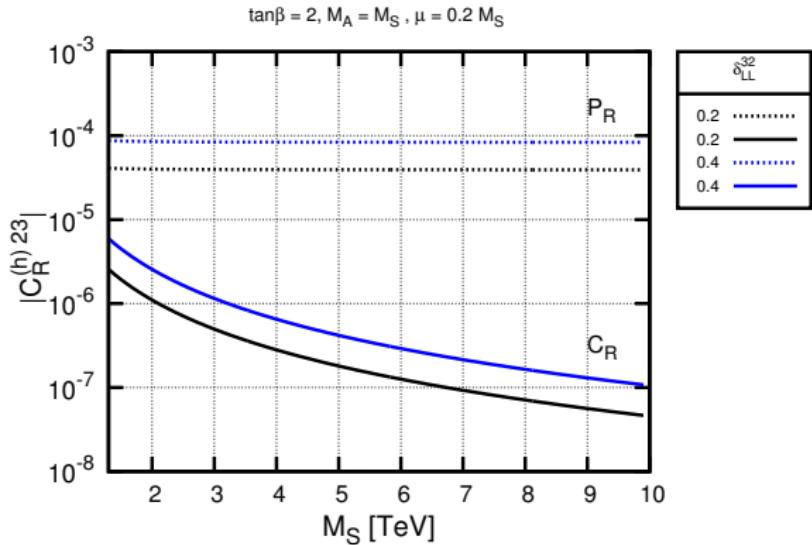
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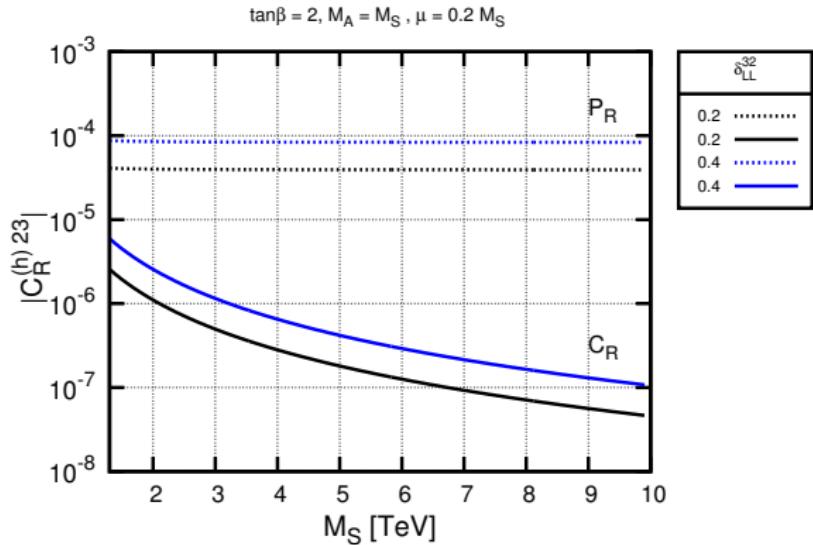
The decoupling works

## Cancellations and Decoupling (cont'd)



- ▶ Degenerate squark mass spectrum (in flavour space)
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- ▶ Degenerate squark mass spectrum (in flavour space)
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The decoupling works (despite claims in arXiv:1404.1241)

## Remnants for $\mathcal{B}(t \rightarrow u h)$

The remaining corrections are proportional to  $\frac{m_t^2}{M_S^2}$  or smaller.

Expansion of the 1-loop gluino contributions give for  $C_L^{(h)}$  terms:

$$\sim A_U'^{JI} \frac{\cos(\alpha - \beta)}{\sin \beta} \mathcal{O}\left(\frac{1}{M_S}\right) \quad \sim \hat{\delta}_{RR}^{JI} \left(\frac{\cos \alpha}{\sin \beta}\right) \mathcal{O}\left(\frac{m_t^2}{M_S^2}\right)$$

$$\sim \mu^* \hat{\delta}_{RR}^{JI} \frac{\cos(\alpha - \beta)}{\sin \beta} \mathcal{O}\left(\frac{1}{M_S}\right) \quad \sim \sum_{A=1}^3 \hat{\delta}_{RL}^{JA} \hat{\delta}_{LR}^{AI} \left(\frac{\cos \alpha}{\sin \beta}\right) \mathcal{O}(1)$$

$$\sim \hat{\delta}_{LR}^{JI} \left(\frac{\cos \alpha}{\sin \beta}\right) \mathcal{O}\left(\frac{m_t}{M_S}\right)$$

$$\sim \sum_{A=1}^3 \sum_{B=1}^3 \hat{\delta}_{LR}^{JA} \hat{\delta}_{RL}^{AB} \hat{\delta}_{LR}^{BI} \left(\frac{\cos \alpha}{\sin \beta}\right) \mathcal{O}\left(\frac{M_S}{m_t}\right)$$

Guide to search for enhanced effects in  $\mathcal{B}(t \rightarrow u h)$

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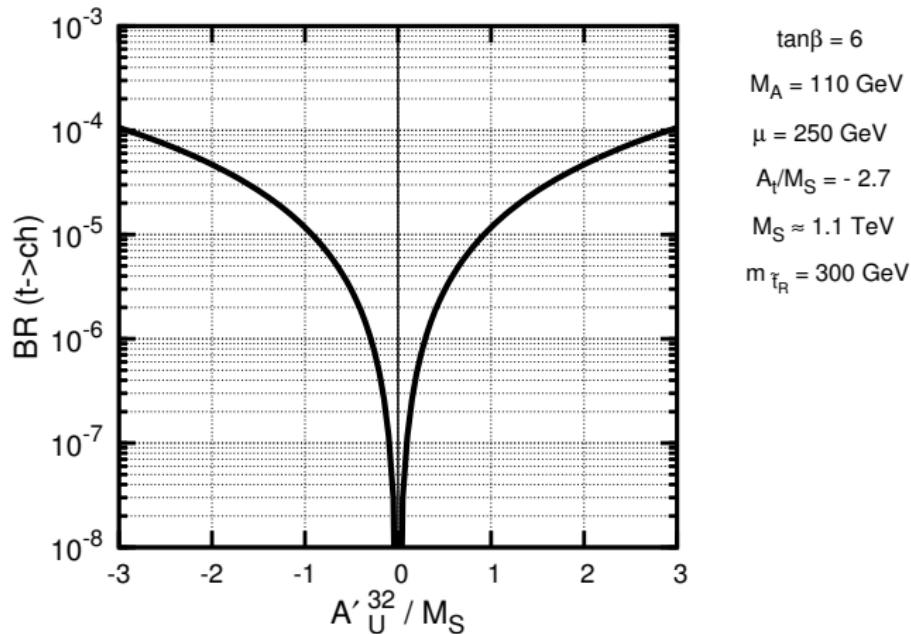
Cancellations, Decoupling and Remnants

**Enhanced Scenarios**

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## Enhanced Scenarios

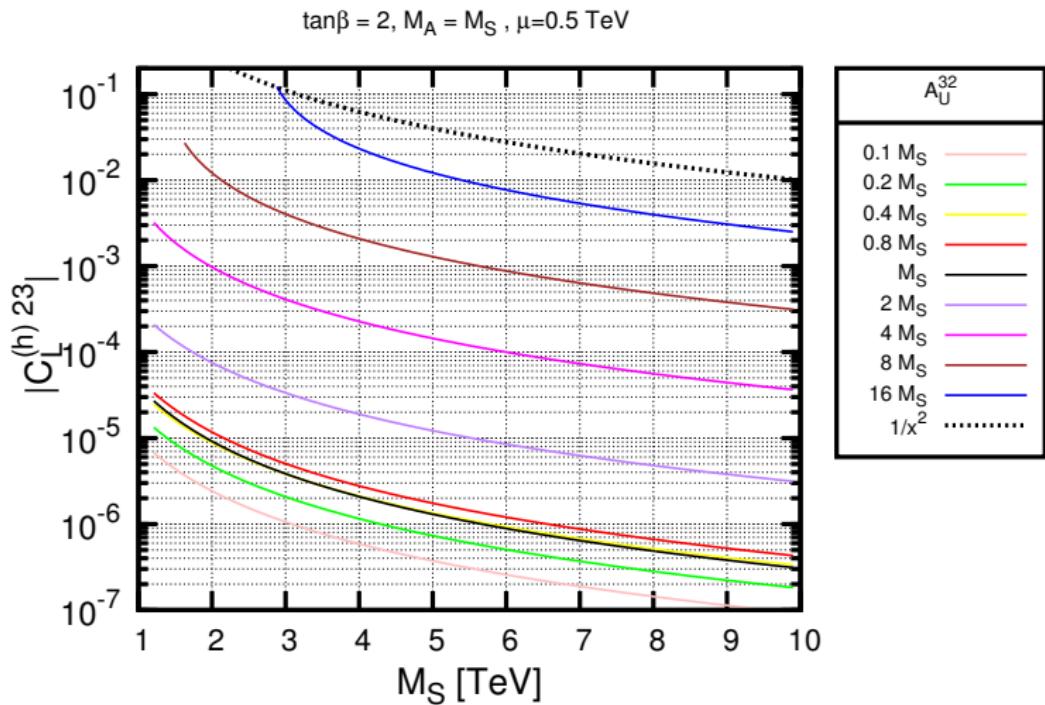
1. Observed Higgs is  $H$  and non-holomorphic coupling  $A'_U{}^{32}$



\* challenged by LHC charged Higgs searches (ATLAS-CONF-2013-090) \*

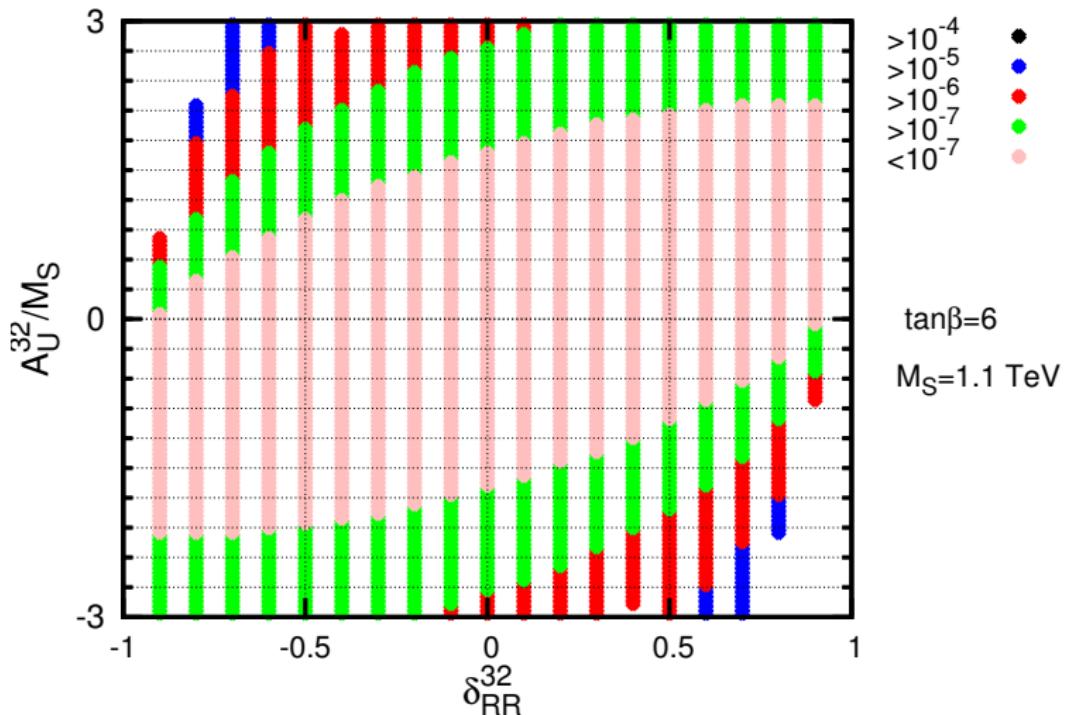
# Enhanced Scenarios

## 2. Enhancement through $\delta_{\text{LR}}^{32} \propto A_U^{32}/M_S > 1$



## Enhanced Scenarios

### 3. Combination of couplings, $\delta_{\text{LR}}^{32}$ , $\delta_{\text{RR}}^{32}$



## Conclusions

- ▶ We have studied rare and flavour changing top decays to Higgs boson in MSSM
- ▶ The relevant flavour changing squark mass insertions are mostly unconstrained
- ▶ However, large cancellations between diagrams do take place, and effects are proportional to  $m_t^2/M_S^2$  at best
- ▶ Classified all dominant contributions
- ▶  $\mathcal{B}(t \rightarrow c h)$  may become visible at LHC if the Higgs boson we see is the heavy Higgs ( $H$ ) and the non-holomorphic term,  $A_U'^{32}$ , is of order  $M_S$
- ▶ For all other points with  $\delta_{LR}^{32} \gtrsim O(1)$  or  $\delta_{RR}^{32} \sim O(1)$  we obtain  $\mathcal{B}(t \rightarrow c h) \lesssim 10^{-4}$  consistent with constraints

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Thank you!