

Updated Constraints on the Higgs Singlet Extension of the SM

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based on

G.M. Pruna, TR (PRD 88 (2013) 115012)

D. Lopez-Val, TR (arXiv:1406.1043)

TR, T. Stefaniak, work in progress

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Higgs Singlet extension (aka The Higgs portal)

The model

- Singlet extension:
simplest extension of the SM Higgs sector
- add an **additional scalar**, singlet under SM gauge groups
(further reduction of terms: impose additional symmetries)

⇒ potential (H doublet, χ real singlet)

$$\mathbf{V} = -\mathbf{m}^2 \mathbf{H}^\dagger \mathbf{H} - \mu^2 \chi^2 + \lambda_1 (\mathbf{H}^\dagger \mathbf{H})^2 + \lambda_2 \chi^4 + \lambda_3 \mathbf{H}^\dagger \mathbf{H} \chi^2,$$

- **collider phenomenology studied by many authors:** Schabinger, Wells; Patt, Wilzcek; Barger ea; Bhattacharyya ea; Bock ea; Fox ea; Englert ea; Batell ea; Bertolini/ McCullough; ...
- our approach: **minimal:** no hidden sector interactions
- equally: **Singlet acquires VeV**

Singlet extension: free parameters in the potential

$$\text{VeVs: } H \equiv \begin{pmatrix} 0 \\ \frac{\tilde{h}+v}{\sqrt{2}} \end{pmatrix}, \quad \chi \equiv \frac{h'+x}{\sqrt{2}}.$$

- potential: 5 free parameters: 3 couplings, 2 VeVs

$$\lambda_1, \lambda_2, \lambda_3, v, x$$

- rewrite as

$$\mathbf{m}_h, \mathbf{m}_H, \sin \alpha, \mathbf{v}, \tan \beta$$

- fixed, free

$$\sin \alpha: \text{ mixing angle, } \tan \beta = \frac{v}{x}$$

- physical states ($m_h < m_H$):

$$\begin{pmatrix} \mathbf{h} \\ \mathbf{H} \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \tilde{h} \\ h' \end{pmatrix},$$

Phenomenology (in the following: focus on $m_h \sim 126$ GeV)

- SM-like couplings of **light/ heavy** Higgs:
rescaled by $\sin \alpha, \cos \alpha$
- in addition: **new physics channel:** $H \rightarrow hh$

$$\Gamma_{\text{tot}}(H) = \sin^2 \alpha \Gamma_{\text{SM}}(H) + \Gamma_{H \rightarrow hh},$$

- **SM like decays** parametrized by

$$\kappa \equiv \frac{\sigma_{\text{BSM}} \times \text{BR}_{\text{BSM}}}{\sigma_{\text{SM}} \times \text{BR}_{\text{SM}}} = \frac{\sin^4 \alpha \Gamma_{\text{tot,SM}}}{\Gamma_{\text{tot}}}$$

- **new physics channel** parametrized by

$$\kappa' \equiv \frac{\sigma_{\text{BSM}} \times \text{BR}_{H \rightarrow hh}}{\sigma_{\text{SM}}} = \frac{\sin^2 \alpha \Gamma_{H \rightarrow hh}}{\Gamma_{\text{tot}}}$$

Theoretical and experimental constraints on the model

our studies: $m_{h,H} = 125.7 \text{ GeV}, 0 \text{ GeV} \leq m_{H,h} \leq 1 \text{ TeV}$

we considered

- ① limits from **perturbative unitarity**
- ② limits from EW precision observables through S, T, U
- ③ **perturbativity** of the couplings (up to certain scales*)
- ④ **vacuum stability and minimum condition** (up to certain scales*)
- ⑤ **collider limits** using HiggsBounds
- ⑥ measurement of **light Higgs signal rates** using HiggsSignals
(debatable: minimization up to arbitrary scales, \Rightarrow perturbative unitarity to arbitrary high scales [these are common procedures though in the SM case])

(*): only for $m_h = 125.7 \text{ GeV}$

Results

- strongest constraints:**

- $m_H \gtrsim 800 \text{ GeV}$: **perturbativity of couplings**
- $m_H \in [200; 800] \text{ GeV}$: **m_W @ NLO**
- $m_H \in [130; 200] \text{ GeV}$: **experimental searches**
- $m_h \lesssim 120 \text{ GeV}$: **SM-like Higgs coupling rates (+ LEP)**

$\Rightarrow \kappa \leq 0.25$ for all masses considered here

$$\Gamma_{\text{tot}} \lesssim 0.02 m_H$$

\Rightarrow **Highly (??) suppressed, narrow(er) heavy scalars** \Leftarrow

\Rightarrow **new (easier ?) strategies needed wrt searches for SM-like Higgs bosons in this mass range** \Leftarrow

\Rightarrow **(partially) already correctly treated in experimental searches (variation of Γ by hand...)** \Leftarrow

Comments on constraints (1) - Perturbativity issues

Perturbative unitarity:

- tests combined system of all (relevant) $2 \rightarrow 2$ scattering amplitudes for $s \rightarrow \infty$
- makes sure that the largest eigenvalue for the "0"-mode partial wave of the diagonalized system ≤ 0.5
- "crude" check that unitarity is not violated
(in the end: all "beaten" by perturbativity of running couplings)

Perturbativity of couplings

- make sure that no coupling $\geq 4\pi$ ("typical" loop prefactor^{-0.5})
- at ew scale: perturbative unitarity stronger

Comments on constraints (2) - running couplings and vacuum

Vacuum stability and perturbativity of couplings at arbitrary scales

- clear: vacuum should be stable for large scales
 - unclear: do we need ew-like breaking everywhere ?
perturbativity ?
- ⇒ check at relative low scale (cf next slide)
- ⇒ bottom line: small mixings excluded from stability for larger scales (for $m_H \leq 1 \text{ TeV}$!! for the model-builders...)
- arbitrary large m_H can cure this !! cf Lebedev; Elias-Miro ea.
Out of collider range though ($\sim 10^8 \text{ GeV}$)
 - perturbativity of couplings severely restricts parameter space, even for low scales

RGE running in more detail

Question: at which scale did we require perturbativity ?

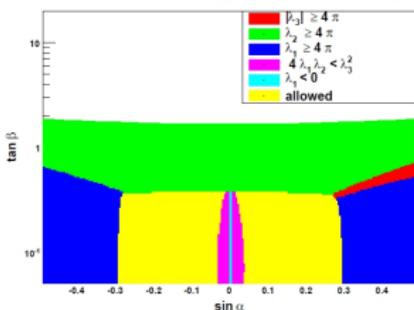
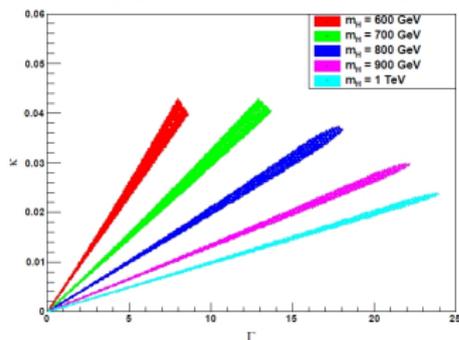
Answer: "just above" the SM breakdown

(other answers equally valid...)

- RGEs for this model **well-known** (cf eg Schabinger, Wells)
- **decoupling** ($\lambda_3 = 0$): **recover SM** case
- in our setup: $\mu_{\text{SM,break}} \sim 6.3 \times 10^{10} \text{ GeV}$
(remark: just simple NLO running)
- **we took:** $\mu_R \sim 1.2 \times 10^{11} \text{ GeV}$
(higher scales \iff stronger constraints)
- **obvious:** for $m_H = 125.7 \text{ GeV}$, **breakdown "immediate"**
when going to $\mu_{\text{run}} > v$

\Rightarrow disregard constraints from running in this case

Limits for $m_H \geq 600 \text{ GeV}$

Effects of perturbativity and vacuum stability, $t=37$ Limits in $\sin \alpha$, $\tan \beta$ plane, $m_H = 600 \text{ GeV}$ including all boundsallowed scale factor and total width, $t=37$ limits on κ , Γ plane from all constraints

for $\sin \alpha \leq 0.23$: only λ_2 **running important**

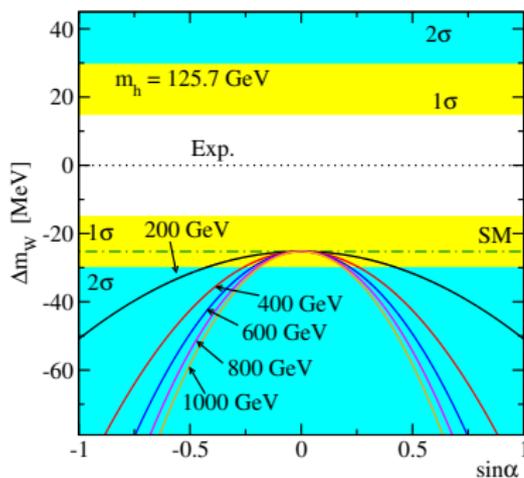
(sideremark: here, 1σ constraint on mixing from μ ; relaxed and improved in newer work, just as an example here)

NLO corrections to m_W (D. Lopez-Val, TR, arXiv:1406.1043)

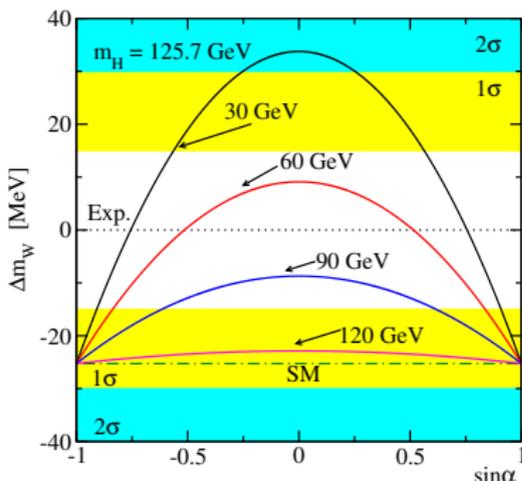
- idea: **replace** electroweak tests using S, T, U by m_W
(includes calculation of $\Delta\rho, \dots$)
- **setup renormalization for Higgs and Gauge boson masses**
- EW gauge and matter sector: on-shell scheme
- Higgs sector: **several choices, currently a mixture of onshell/
 \overline{MS}**
(in this case: $\delta\lambda$ only enter at 2-loop \implies not relevant here)
- **first step on the road to full renormalization**

NLO corrections to m_W (D. Lopez-Val, TR, arXiv:1406.1043)

Contribution to m_W for different Higgs masses



$m_h = 125.7$ GeV

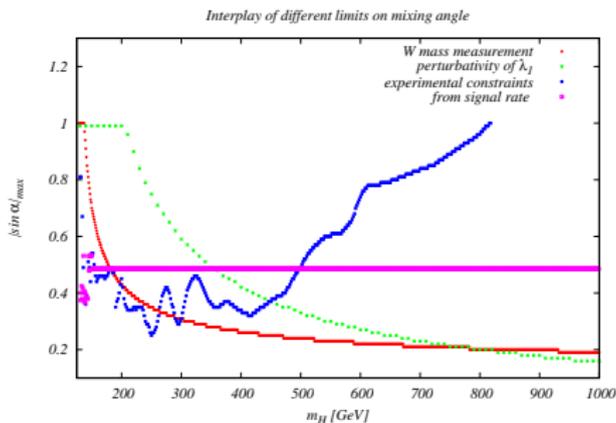


$m_H = 125.7$ GeV

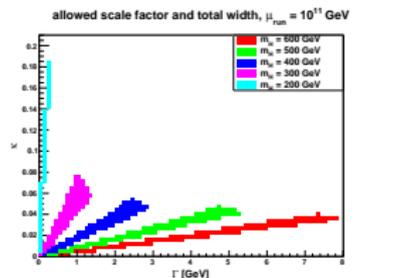
\Rightarrow low m_h bring m_W^{NLO} close to m_W^{exp} \Leftarrow

Combined limits on $|\sin \alpha|$

(D. Lopez-Val, TR, arXiv:1406.1043, and TR, T. Stefaniak, to appear)



several bounds on $|\sin \alpha|$



limits on κ , Γ plane from all constraints

m_W , perturbativity, LHC direct searches, Higgs Signal strength

Limits in numbers; high mass scenario

m_H [GeV]	$ \sin \alpha $	source upper limit	$(\tan \beta)_{\max}$
1000	[0.020; 0.16]	λ_1 perturbativity	0.21
800	[0.028; 0.20]	m_W at NLO / λ_1 perturbativity	0.26
600	[0.038; 0.22]	m_W at NLO	0.36
400	[0.057; 0.26]	m_W at NLO	0.54
200	[0.092; 0.43]	m_W at NLO	1.08
180	[0.10; 0.44]	126 GeV signal strength	1.20
160	[0.12; 0.44]	126 GeV signal strength	1.34
140	[0.17; 0.36]	$h \rightarrow \ell^+ \ell^- \ell^+ \ell^-$	1.54

- $\sin \alpha_{\min}$ always from **vacuum stability**
- $\tan \beta_{\max}$ always from **perturbativity of λ_2**

Results from generic scans and predictions for LHC 14

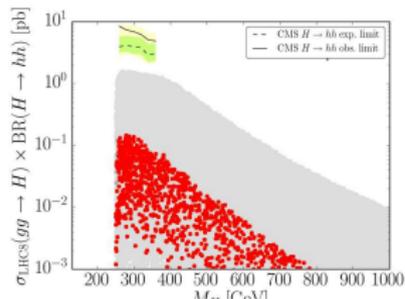
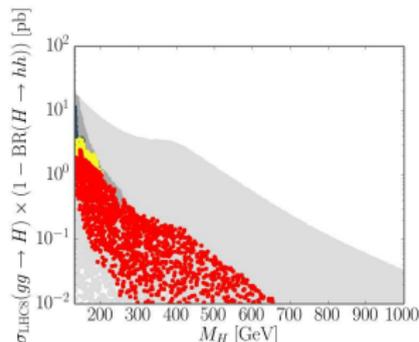
(TR, T. Stefaniak, in preparation)

1 σ , 2 σ , allowed

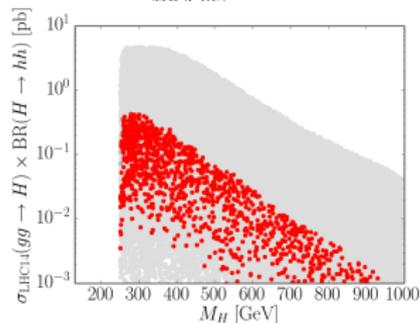
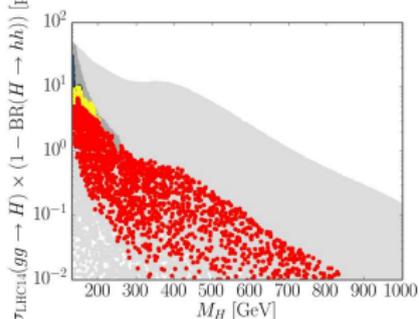
SM like decays

BSM decay to hh

limits



pred.



Could we have seen them ??

all numbers below: $\sqrt{S_{\text{hadr}}} = 8\text{TeV}$, $\int \mathcal{L} = 23\text{fb}^{-1}$

m_H [GeV]	κ_{max}	#gg \sim	κ'_{max}	#gg \sim
200	0.18	3×10^4	0	0
300	0.076	6×10^3	0.038	3×10^3
400	0.053	4×10^3	0.021	1×10^3
500	0.047	1×10^3	0.015	440
600	0.039	470	0.012	140
700	0.035	180	0.010	50
800	0.033	80	0.009	20
900	0.027	40	0.007	10
1000	0.021	15	0.005	4

[for specific final state, multiply with SM-like BR (LO approx)]
**for $m_H \lesssim 600\text{ GeV}$, may could already have been produced
 which are not excluded by current searches !!**

What about the “inverse” scenario, ie. $m_H = 125.7 \text{ GeV}$

mainly ruled out by LEP and/ or χ^2 fit from HiggsSignals
 however, *still* large number produced due to large $\sigma_{gg \rightarrow h}$

$m_h [\text{GeV}]$	$ \sin \alpha _{\text{min, exp}}$	$ \sin \alpha _{\text{min, } 2\sigma}$	$(\tan \beta)_{\text{max}}$	$\#gg \sim$
110	0.82	0.89	9.2	10^5
100	0.86	--	10.1	10^5
90	0.91	--	11.2	10^5
80	0.98	--	12.6	10^4
70	0.99	--	14.4	10^4
60	0.98	$\gtrsim 0.99$	16.8	10^4
50	0.99	$\gtrsim 0.99$	20.2	10^4
40	0.99	$\gtrsim 0.99$	25.2	10^4

Table: Upper limit on $\tan \beta$ from perturbative unitarity. (— means no additional constraint)

(side remark: for $m_h \gtrsim 60 \text{ GeV}$, $\tan \beta$ irrelevant for collider observables)

Summary

- Singlet extension: **simplest extension of the SM Higgs sector**, easily identified with one of the benchmark scenarios of the HHXWG (cf. also YR3, Snowmass report)
- constraints on **maximal mixing** from m_W at **NLO** ($m_H \in [200 \text{ GeV}; 800 \text{ GeV}]$), **experimental searches and fits** ($m_{H,h} \leq 200 \text{ GeV}$) and/ or **running couplings** ($m_H \geq 800 \text{ GeV}$)
- **quite narrow widths wrt SM-like Higgses** in this mass range \Rightarrow **better theoretical handle**
- quite large suppression from current experimental/ theoretical constraints

!!! still, large numbers could have been produced already !!!

\Rightarrow STAY TUNED \Leftarrow

Appendix

Coupling and mass relations

$$m_h^2 = \lambda_1 v^2 + \lambda_2 x^2 - \sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}, \quad (1)$$

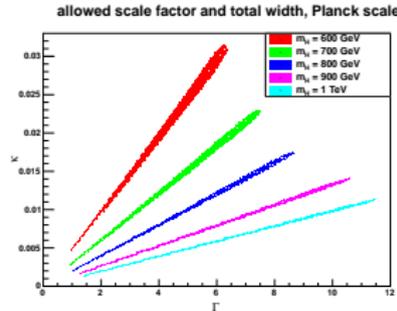
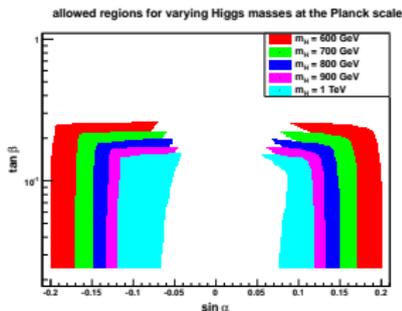
$$m_H^2 = \lambda_1 v^2 + \lambda_2 x^2 + \sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}, \quad (2)$$

$$\sin 2\alpha = \frac{\lambda_3 x v}{\sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}}, \quad (3)$$

$$\cos 2\alpha = \frac{\lambda_2 x^2 - \lambda_1 v^2}{\sqrt{(\lambda_1 v^2 - \lambda_2 x^2)^2 + (\lambda_3 x v)^2}}. \quad (4)$$

Limits at Planck scale

assume that the model is valid up to $\mu_{\text{run}} \sim 10^{19}$ GeV
(not always well motivated)



- naturally: **parameter space more restricted**
- translates to $\kappa \lesssim 0.03$ for $m_H = 600$ GeV (25% decrease)
- now: μ no longer relevant, only constraint from perturbativity of λ_1, λ_2

Tools which can do it ?? (incomplete list)

("it" = LO, NLO, ...)

- LO: **any tool talking to FeynRules** (in principle)/ **LanHep** (in practice)
- implemented and run: **CompHep** (M. Pruna), **Sherpa** (\pm) (would need some modification, T. Figy), privately modified codes (??)
- NLO: (mb) a modified version of **aMC@NLO** (R. Frederix) ?? (production only; might be important for VBF)
- new tool in the MadGraph environment (Artoisenet ea, 06/13): QCD-part of NLO
- complete higher orders: would need to be implemented in respective tools (I am not aware of any at the moment)

One more word about $H \rightarrow hh$

- all above: **focuses on SM-like decays**
- **viable alternative:** search for

$$H \rightarrow hh \rightarrow \dots$$

- **widely discussed in the literature**
(for recent work, cf Gouzevitch, Oliveira, Rojo, Rosenfeld, Salam, Sanz; Cooper, Konstantinidis, Lambourne, Wardrope; ...)
 - **HOWEVER** in our scan, **WW always dominant**
- ⇒ **would go for this first**
(but mb more than 1 group is interested...)